The Oxygen Paradigm—Quantitative Impact of High Concentrations of Dissolved Oxygen on Kinetics and Large-Scale Production of Arthrospira platensis

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Abstract: The cultivation of Arthrospira platensis in tubular photobioreactors (tPBRs) presents a promising approach for the commercial production of nutraceuticals and food products as it can achieve high productivity and effective process control. In closed photobioreactors, however, high amounts of photosynthetically produced oxygen can accumulate. So far, there has been a wide range of discussion on how dissolved oxygen concentrations (DOCs) affect bioprocess kinetics, and the subject has mainly been assessed empirically. In this study, we used photorespirometry to quantify the impact of DOCs on the growth kinetics and phycocyanin content of the widely cultivated cyanobacterium A. platensis. The photorespirometric routine revealed that the illumination intensity and cell dry weight concentration are important interconnected process parameters behind the impact that DOCs have on the bioprocess kinetics. Unfavorable process conditions such as low biomass concentrations or high illumination intensities yielded significant growth inhibition and reduced the phycocyanin content of A. platensis by up to 35%. In order to predict the biomass productivity of the large-scale cultivation of A. platensis in tPBRs, a simple process model was extended to include photoautotrophic oxygen production and accumulation in the tPBR to evaluate the performance of two configurations of a 5000 L tPBR.

Keywords: photorespirometry; Arthrospira platensis; tubular photobioreactor; dissolved oxygen; process modeling

1. Introduction

Around 3000–4000 metric tons per annum of Arthrospira platensis (also known as Spirulina) biomass is produced commercially worldwide by companies such as Earthrise Nutritional (Irvine, CA, USA) and the Siam Algae Company (Bangkok, Thailand) [1]. This underlines the rising interest in A. platensis in the food [1,2] and feed [3,4] industry for its high nutritive value, such as a high protein content of 43–65% (w/w), and a balanced profile of essential amino acids [2]. Besides the food sector, biomass from A. platensis is also commercially valued as a dietary supplement [1,2,5] since an intake of dried A. platensis has been proven to reduce blood cholesterol levels and improve patients’ lipid profiles [6,7]. Recent studies have further attributed anti-inflammatory, immunostimulatory, antioxidant, cancer-inhibiting [8,9] and antiviral [10] properties to cyanobacterial biomass and metabolites [11,12] such as phycocyanin (8–13% w/w of dry biomass [13]) and carotenoids (0.15–0.2% w/w of dry biomass [14]). As an example, Zeaxanthin is believed to reduce the risk of age-related macular degeneration [15,16]. A. platensis further contains lipids that are of medical interest (6–13% [17]), such as polyunsaturated γ-linolenic acid, known...
among other things for its anti-inflammatory properties and beneficial impact on the risk of coronary heart disease [18,19].

Basically, phototrophic microorganisms are cultivated in open or closed photobioreactors. Tubular photobioreactors (tPBRs) are common in industrial cultivation [20], since high volumetric biomass productivity and good process control can be achieved with a reduced risk of contamination compared to open cultivation systems [20,21]. However, a lower gas transfer efficiency in closed tubes is among the disadvantages of tPBR systems, resulting in photoautotrophically produced oxygen accumulation and the formation of oxygen gradients alongside the closed tPBRs [20,22]. Weissman et al. [23] showed that tPBRs can exhibit volumetric rates of oxygen evolution that are up to 25 times higher compared to open pond systems (20 cm depth). As an example, at the maximum photosynthesis rate of *Chlorella* sp., oxygen accumulation in tPBRs (tube diameter: 1 cm) can account for as much as 8–10 mgO₂ L⁻¹ min⁻¹, resulting in an increase in the dissolved oxygen concentration (DOC) of 100 mg L⁻¹ (assuming a tube length of 100 m) without any gas exchange [23]. Torzillo et al. observed a DOC rate of 2–3 mgO₂ L⁻¹ min⁻¹ for outdoor cultivations of *A. platensis* (tPBR, tube diameter: 5 cm), resulting in a maximum DOC of 70–80 mgO₂ L⁻¹ [24,25]. This oxygen accumulation capacity indicates the high risk of the formation of spatial DOC gradients along the tube axis and the need to manage the gas-liquid mass transfer in tPBRs [25,26]. Kazbar et al. [26] compared the mass transfer parameter $k_La$ and the maximum DOC attainable with several PBR systems and concluded that oxygen accumulation may result in the inhibition of growth rates of phototrophic microorganisms, especially in PBRs with $k_La$ values smaller than 7 h⁻¹. Only a few studies have examined the $k_La$ of tPBRs, which revealed oxygen mass transfer parameters in the range of 3–7 h⁻¹ [27,28]. Integrated airlift systems and advanced degassing units [28–31] are known to improve oxygen mass transfer in tPBRs to prevent oxygen accumulation [26,28]. However, high gas-flow rates and the pumping of the liquid phase may induce shear stress to the cells accompanied by considerable energy costs [32,33].

Mathematical models have been developed to predict the accumulation of oxygen in tPBRs considering the impact on the growth kinetics of microalgae. Rubio et al. [27] introduced a model for estimating DOC profiles in tPBRs that took into consideration oxygen mass transfer characteristics. However, the authors assumed the microalgal oxygen production rate to be average and did not take into account the impacts of dynamic changing illumination intensity or the DOC on the microalgal growth rate [27]. In contrast, Trentin et al. [34] developed a comprehensive model for *C. protothecoides* to predict biomass productivity in a tPBR taking into consideration various impact factors such as the DOC and illumination intensity. Although the oxygen mass transfer characteristics of the liquid phase were neglected, their model can predict how several environmental factors and design modifications to the tPBR affect the biomass productivity. To specifically describe the impact of DOCs on photoautotrophic growth, Costache et al. [35] have proposed a kinetic model based on product inhibition, describing the exponential decline in the oxygen production rate ($OPR$) at an increasing DOC for *S. almeriensis*. The model takes into account the competitive inhibition of RuBisCO’s carboxylase function by oxygen (photorespiration), which occurs increasingly at high DOCs [35]. Sforza et al. [36] investigated the extent of inhibition on the photosynthetic activity of the microalgae *C. protothecoides* at high DOCs and varying illumination intensities and biomass concentrations, indicating that the $OPR$ at rising DOC levels differs in experiments under varying process conditions.

This study aims to quantify the impact of high DOCs on the growth kinetics and cellular phycoceyanin content of *A. platensis* PCC7345 using a lab-scale photorespirometric approach. Kinetic parameters derived from photorespirometry were introduced to a simple process model describing photoautotrophic cyanobacterial growth taking into consideration the oxygen mass transfer characteristics in the liquid phase. This information was used to perform an in-silico scale-up study of two different 5000 L industrial tPBR configurations.
2. Materials and Methods

2.1. Strain and Cultivation Conditions

*A. platensis* PCC7345 was obtained from the Pasteur Culture Collection (PCC, Paris). Cyanobacterial cells were maintained and pre-cultured in a *Spirulina* medium [SAG Göttingen, Spirulina Medium] grown in 300 mL Erlenmeyer flasks at 26 °C, 150 rpm and 75 μmol m⁻² s⁻¹ fluorescent light (light/dark cycles of 16/8 h, WB750, mytron Bio- und Solartechnik GmbH, Heilbad Heiligenstadt, Germany). Liquid stock cultures were subcultivated weekly.

To prepare *A. platensis* PCC7345 cultures for respirometric analyses, a 25 L tPBR (MINT Engineering GmbH, Dresden, Germany) was inoculated from shake flasks and cultivated in batch airlift mode (10 L min⁻¹ ambient air) for 10 days at room temperature (23–26 °C), leading to a final cell dry weight concentration (cₓ) of 1.1 g L⁻¹. To obtain cyanobacterial cells under industrially relevant physiological conditions, the 25 L tPBR cultivation was carried out in a reduced *Spirulina* medium, replacing macro- and micro-nutrients with an inorganic plant fertilizer. For respirometric analysis, 1 L samples were taken from the tPBR and adjusted to the desired cₓ using the reduced Spirulina medium.

2.2. Cell Dry Weight Concentration (cₓ) & Optical Density (OD₇₅₀)

Culture samples of *A. platensis* PCC7345 were analyzed using a GENESYS 150 UV/VIS spectrophotometer (Thermo Fisher, Waltham, MA, USA). The optical density (OD₇₅₀) was measured at 750 nm and was calibrated against cₓ [g L⁻¹] of *A. platensis* PCC7345 using the following correlation (n = 3):

\[ cₓ = 0.86 \cdot \text{OD}_{750} \]  

To determine cₓ, 15 mL of *A. platensis* PCC7345 suspension was passed through a glass microfiber filter (VWR International, Delaware Valley, USA, mesh size: 1 μm, n = 3) followed by washing three times using 15 mL deionized water and drying for 24 h at 103 °C (Memmert GmbH + Co.KG, Schwabach, Germany). Finally, the weight difference of dried biomass was determined to calculate cₓ (Figure S1, Supplementary Materials).

2.3. Quantification of Incident Illumination Intensity (I₀) and Calculation of Average Illumination Intensity (Iav)

The incident illumination intensity I₀ [μmol m⁻² s⁻¹] was detected by a DK-PHAR 2.010BS PAR-quantum sensor (deka Sensor + Technologie Entwicklungs- und Vertriebsgesellschaft mbH, Teltow, Germany). The local illumination intensity I(Z) [μmol m⁻² s⁻¹] was calculated using Lambert–Beer’s law:

\[ I(Z) = I₀ \cdot e^{-(cₓ \cdot \varepsilon \cdot Z)} \]  

where I₀ is the incident illumination intensity (μmol m⁻² s⁻¹); ⍵ (L g⁻¹ cm⁻¹) is the cell-specific light attenuation coefficient; cₓ (g L⁻¹) the cell dry weight concentration of *A. platensis* PCC7345; and Z (cm) the light path lengths. The cell-specific light attenuation coefficient ⍵ was determined experimentally using a measurement chamber developed in-house, as described recently [37]. Briefly, the chamber was filled with 130 mL of cyanobacterial suspension with cₓ ranging from 0.12 to 0.84 g L⁻¹. An adjustable slide, carrying an encapsulated pyranometer (deka Sensor + Technologie Entwicklungs- und Vertriebsgesellschaft mbH, Teltow, Germany) was moved along the light path (Z) while recording the local illumination intensities I(Z), which were used to calculate ⍵ with the least squares method using MATLAB 2012 (MathWorks, Natick, MA, USA). Since both absorption and scattering effects had to be taken into account at increasing cₓ, ⍵ was introduced into the modeling approach with the following correlation:

\[ ⍵ = \begin{cases} -6.83 \cdot cₓ + 5.34, & cₓ \leq 0.355 \text{ g L}^{-1} \\ -0.045 \cdot cₓ + 3.014, & cₓ > 0.355 \text{ g L}^{-1} \end{cases} \]
To calculate the average illumination intensity $I_{av}$, local intensities $I(Z)$ were averaged for eight light-path lengths $Z$ across the diameter of the desired vessel (bottle or tPBR).

$$I_{av} = \frac{\sum_{i=0}^{8} I(Z)}{8} \quad (4)$$

2.4. Photorespirometry Analysis

Photorespirometry was recently developed by Sforza et al. as a quick and simple method to determine the growth kinetics of microalgae [36,38,39], the aim being to examine the effects of high DOCs on microalgae cultures [36].

In this study, respirometry was performed in a 1000 mL DURAN GLS 80 double-walled laboratory bottle (diameter: 7 cm, DWK Life Sciences GmbH, Wertheim, Germany) equipped with oxygen, pH and temperature probes (Figure 1a,b). To avoid gas losses via the headspace, the bottle was filled completely with $A.\ platensis$ PCC7345 liquid culture. The DOC was detected at short time intervals (10 s) by a GMH 3611 oximeter (GWO3600 probe, GHM Messtechnik GmbH, Remscheid Germany) and the EBS 20 M monitoring software. The temperature was adjusted at 30 °C by using a circulating water thermostat mixing the cell suspension by a magnetic stirrer at 300 rpm. To decrease the DOC, a CO$_2$/N$_2$ (20% v/v) mixture was sparged into the liquid phase using sintered stone. The bottle cap was sealed with Teflon tape to create an airtight system. The photorespirometry set-up was illuminated on one side by plant-growth LEDs optimized for photosynthetically active radiation. $I_0$ was measured at the surface of the bottle using a PAR-quantum sensor DK-PHAR 2.010BS (deka Sensor + Technologie Entwicklungs- und Vertriebsgesellschaft mbH, Teltow, Germany). All respirometric experiments were performed in a light-proof box to provide constant illumination conditions (Figure 1b).

The respirometric routine reported by Sforza et al. [36] in 2020 was modified by introducing an exposure phase as indicated in Figure 1c. The routine was carried out in three phases: (1) a reference phase exposing the cells to intermittent light/dark illumination cycles (reference values for oxygen production rate ($OPR$) and oxygen consumption rate ($OCR$), (2) a continuous light phase providing supersaturated DOC conditions and (3) an exposure phase to investigate how high DOCs affected the cellular phycocyanin content. Before the reference phase was initiated, the DOC was adjusted to approx. 4.5 mg O$_2$ L$^{-1}$ by sparging a CO$_2$/N$_2$ mixture (20% v/v) followed by five alternating light/dark illumination cycles (10 min per phase). The data from the first light/dark cycle were discarded to take into account the cells’ adaptation to new environmental conditions. $OPR$ data were derived from the reference phase by the following correlation taking into consideration the oxygen mass transfer coefficient $k_{La}$ and the concentration difference of the current DOC ($c_{O_2}$) and the solubility concentration in the liquid $c^\ast_{O_2}$:

$$r_{O_2} = \frac{dc_{O_2}}{dt} = k_{La} \left( c^\ast_{O_2} - c_{O_2} \right) + OPR \quad (5)$$

The solubility concentration of oxygen $c^\ast_{O_2}$ in water depends on the temperature and can be calculated by Henry’s Law [40]:

$$c^\ast_{O_2} = H_{O_2} \cdot P_{O_2} \quad (6)$$

where $H_{O_2}$ is the temperature-dependent Henry’s law constant and $P_{O_2}$ the oxygen partial pressure in line with [40]:

$$H_{O_2} = H_{ref} \cdot e^{\frac{C \cdot \left( \frac{T}{T_{ref}} - 1 \right)}{T_{ref}}} \quad (7)$$

The oxygen mass transfer coefficient $k_{La}$ of the photorespirometry set-up (Figure 1b, $T = 30 \, ^\circ C, P_{O_2} = 0.21$ atm) was determined to $0.187 \pm 0.009$ h$^{-1}$ using the log deficit procedure (ASCE, 1993 [41]), as proposed by Sforza et al. [39]. Due to the low mass transfer coefficient of the setup, this parameter was neglected in further calculations. $OPR$ data
were connected to the adjusted $c_x$, which was assumed to remain constant during the reference phase.

**Figure 1.** Photorespirometry setup (a) Schema of experimental setup including (A) a double-walled glass vessel, (B) an airtight cap equipped with pH, temperature and oxygen probe, (C) external monitoring software, and (D) photosynthetically active radiation LED light source; (b) Photograph of a running experiment; (c) Example of course of photorespirometry routine divided into (a) reference phase; (b) continuous illumination phase and (c) exposure phase.

Respirometric tests were conducted under varying process conditions, i.e., at $I_0$ of 100, 150 and 400 $\mu$mol m$^{-2}$ s$^{-1}$ and $c_x$ of 0.1, 0.5, 0.8 and 1 g L$^{-1}$. Using Equation (4), the range of $I_{av}$ for the respirometry setup results in 13–131 $\mu$mol m$^{-2}$ s$^{-1}$. The impact of $I_{av}$ on the photosynthetic activity, indicated by the $c_x$-related $OPR$, can be described by the illumination half-saturation constant, $K_L$ ($\mu$mol photons m$^{-2}$ s$^{-1}$) and the $c_x$-related maximum rate of photosynthesis, $OPR_{max,spec}$:

$$\frac{OPR}{c_x} = \frac{OPR_{max,spec} \cdot I_{av}}{I_{av} + K_L}$$

(8)

This model approach neglects photoinhibition effects under high $I_{av}$ conditions, which were not observed in this study. $K_L$ and $OPR_{max,spec}$ were obtained by fitting experimental data on the reference phase using the least square method in MATLAB$^\text{®}$ 2012 (MathWorks, USA). To take into account the compensation point, at which gross $OPR$ by photosynthesis and the oxygen consumption rate by basal respiration is balanced out (net $OPR = 0$), $OPR$ data were offset in line with the examples used by Vonshak (1997) [42] before applying fitting routines in MATLAB 2012 (Natick, MA, USA).
2.5. In-Vivo Phycocyanin Quantification of Suspended Cells

The quantification of the cellular phycocyanin content of cyanobacteria is usually carried out by consecutive steps of physical or chemical cell disruption (physical steps include ultrasound, high-pressure homogenization, cavitation, osmolysis and freezing cycles; chemical steps include acid/alkali treatments, detergents and enzymes), followed by buffer extraction, salt precipitation, phase separation and spectrometric quantification using empirical equations such as the Bennet and Bogorad correlation [43]. These routines are time-consuming and depend on the efficiency of the individual process steps. For that reason, in this work an optical in-vivo method was established for quantifying the intracellular phycocyanin content while avoiding the steps of cell disruption and phycocyanin purification.

The cellular phycocyanin content \( c_{\text{PC}} \) (mg g\(^{-1}\)) of \( A. \text{platensis} \) PCC7345 was quantified using fluorescence spectrometry (LS-55, Perkin Elmer Inc., Waltham, MA, USA). Culture samples were diluted using saline solution to achieve a final OD\(_{750}\) of 0.1 in a 3 mL cuvette that was clear on all sides and made from polystyrene. The diluted cell suspension was homogenized in the cuvette by a magnetic stirrer during the fluorescence measurement. The intracellular phycocyanin was excited with light in the spectral range of 600–630 nm; the maximum of phycocyanin absorption (step with 5 nm, measurement speed: 1200 nm min\(^{-1}\)). Fluorescence emission was detected ranging from 650–670 nm, yielding a fluorescence heat map (Figure S2, Supplementary Materials). The peak fluorescence intensity \( (I_{f, \text{max}}) \) at 615–620 nm was detected in triplicate and used to calculate the cellular phycocyanin content employing the following correlation (Figure S3, Supplementary Materials):

\[
c_{\text{PC}} = 0.4484 \cdot I_{f, \text{max}}
\]  

Statistical analyses of in-vivo \( c_{\text{PC}} \) quantification were performed in the form of two-way analyses of variance (ANOVA) to investigate how the exposure time and the cultivation conditions influenced \( c_{\text{PC}} \) using the software GraphPad prism and applying a significance level of 5% (\( p < 0.05 \)). The \( c_{\text{PC}} \) was determined after 2, 4, and 20 h of high DOC exposure as shown in Figure 1c.

2.6. Modeling Approaches

2.6.1. Modeling of Respirometric Data

In the literature, only a few models are presented that describe how high DOCs affect the OPR of photosynthetically active organisms. Among them, Costache et al. [35] and Sforza et al. [36] have introduced models for studying OPR and DOC correlation.

Sforza et al. [36] developed a comprehensive model taking into account phenomena that are believed to induce inhibitory effects at high DOCs, involving oxygen consumption due to basal respiration expressed by the oxygen respiration rate \( (\text{OCR}_{\text{resp}}) \), the positive photosynthetic oxygen production rate \( (\text{OPR}_{\text{ph}}) \) and the oxygen inhibition rate \( (\text{OCR}_{\text{inh}}) \) [36]:

\[
\text{OPR}_{\text{net}} = \text{OPR}_{\text{ph}} - \text{OCR}_{\text{resp}} - \text{OCR}_{\text{inh}}
\]  

\( \text{OPR}_{\text{ph}} \) was described as a function of \( I_{av} \), the maximum specific oxygen rate \( \mu_{O_2} \) (d\(^{-1}\)) and the \( O_2:CO_2 \) ratio to include the effects of photorespiration as a counterpart of photosynthesis [36]:

\[
\text{OPR}_{\text{ph}} = \mu_{O_2} \cdot f(I_{av}) \cdot c_x \cdot \frac{c_{CO_2}}{K_{CO_2} \left(1 + \frac{c_{CO_2}}{K_{PR}} \right) + c_{CO_2}}
\]
The oxygen respiration rate (OCR\textsubscript{resp}) in their model can be described by a Monod-type function depending on the DOC (c\textsubscript{O\textsubscript{2}}) including the maximum oxygen respiration rate k\textsubscript{resp} (d\textsuperscript{-1}) and the respiration half-saturation constant K\textsubscript{M,O2} (mg L\textsuperscript{-1}) \[36,44]\:

\[
OCR_{\text{resp}} = k_{\text{resp}} \cdot \frac{c_{O_2}}{K_{M,O2} + c_{O_2}} \cdot c_x
\] (12)

Analyzing C. protothecoides, Sforza et al. \[36\] found an exponential correlation to describe the oxygen inhibition rate OCR\textsubscript{inh} under varying cultivation conditions, introducing the oxygen inhibition coefficient k\textsubscript{inh} (d\textsuperscript{-1}) and oxygen inhibition exponent ζ (L mg\textsuperscript{-1}) \[36\]:

\[
OCR_{\text{inh}} = k_{\text{inh}} \cdot e^{ζ \cdot c_{O_2}}
\] (13)

The model introduced by Costache et al. \[35\] originates in a description of product inhibition to take into account the competitive inhibition of the carboxylase function of RuBisCO by oxygen during photorespiration. By applying the oxygen inhibition constant KO\textsubscript{2} (mg L\textsuperscript{-1}) and the form factor z (–), the normalized biomass-related OPR is described as a function of the DOC (c\textsubscript{O\textsubscript{2}}) \[35\]:

\[
OPR[c_{O_2}] = 1 - \left( \frac{c_{O_2}}{K_{O_2}} \right)^z
\] (14)

2.6.2. Photoautotrophic Growth Modeling

The biomass growth rate \( r_x \) (g\textsubscript{x} L\textsuperscript{-1} h\textsuperscript{-1}) of microorganisms is described by the specific growth rate \( µ \) (h\textsuperscript{-1}) and the cell dry weight concentration \( c_x \) (g\textsubscript{x} L\textsuperscript{-1}):

\[
r_x = µ \cdot c_x
\] (15)

Assuming that there is an excess supply of nutrients and carbon source (HCO\textsuperscript{-3}), a constant pH and constant temperature conditions, \( µ \) (h\textsuperscript{-1}) can be expressed as a function of the average illumination intensity \( I_{av} \) (\(\mu\text{mol m}^{-2} \text{s}^{-1}\)), the maximum growth rate \( µ_{max} \) (h\textsuperscript{-1}) and the half-saturation constant \( K_L \) (\(\mu\text{mol photons m}^{-2} \text{s}^{-1}\)):

\[
µ = µ_{max} \cdot \frac{I_{av}}{I_{av} + K_L}
\] (16)

It was reported that OPR (\( r_{O_2} \)) correlates to the photoautotrophic growth rate \( µ \) of cyanobacteria \[25,45\]. Therefore, OPR can be identified by the yield coefficient \( Y_{O_2} \) :

\[
OPR = r_{O_2} = Y_{O_2} \cdot r_x
\] (17)

Applying the model developed by Costache et al. \[35\], the rate of biomass growth can be formulated as a function of the DOC (c\textsubscript{O\textsubscript{2}}):

\[
r_x = µ_{max} \cdot \frac{I_{av}}{I_{av} + K_L} \cdot \left( 1 - \left( \frac{c_{O_2}}{K_{O_2}} \right)^z \right) \cdot c_x
\] (18)

2.7. In-Silico Scale-Up Study at Industry-Scale tPBR

For in-silico studies on biomass growth of A. platensis PCC7345 in large-scale cultivation systems, a horizontal tPBR system for industrial use is assumed, consisting of a solar array, a degassing unit and a harvesting unit (Figure 2). The continuous system is based on the partial recycling of biomass that is grown in a solar array consisting of 4 tubes with a length of 450 m, a diameter of 6 cm and a total volume of 5000 L. The tubes can be operated in parallel or linked in series, resulting in a total tube length of 1800 m. Biomass growth and oxygen accumulation in the solar unit lead to an increased biomass concentration \( c_{x,\text{out}} \).
and DOC \((c_{O_2,\text{out}})\) at the end of the tube compared to the tube inlet \((c_{x,0}; c_{O_2,0})\). A sub-flow of the biomass-enriched suspension is removed from the system by a harvesting unit \((\dot{V}_H)\). The residual flow \((\dot{V}_{\text{rec}})\) is recycled to a degassing unit, where the DOC is reduced to air saturation \((c_{O_2,0})\) and the suspension is enriched with fresh medium \((\dot{V}_I)\), before being recycled to the solar unit. Assuming that biomass growth occurs solely in the tubes of the solar unit and that operation is steady-state, then, in line with the plug flow reactor model, the biomass growth over the tube length \(l\) (running coordinate) can be described by the flow velocity \(v\) in the solar loop and the biomass growth rate \(r_x\) [34]:

\[
\frac{dc_x}{dl} = \frac{1}{v} \cdot r_x
\]  

(19)

Figure 2. (a) Assumptions behind a continuous operating tPBR system for an in-silico scale up study, (b) tPBR system in a serial configuration with a total tube length of 1800 m and in a parallel configuration with a total tube length of 450 m.

The accumulation of oxygen over the tube length depends on the OPR \((r_{O_2})\); the gas-liquid mass transfer of oxygen in the system, and the gas hold-up \(\varepsilon_g\) [27,46]:

\[
\frac{dc_{O_2}}{dl} = \text{OPR} = \frac{1}{v} \left( k_{L,a} \cdot \left( c_{O_2}^* - c_{O_2} \right) + r_{O_2} \cdot \left( 1 - \varepsilon_g \right) \right)
\]  

(20)

Taking into account the increase in the biomass concentration over the tube length and the residence time \(\tau\) in the solar loop, which can be determined by connecting the solar loop length \(L\) to the flow velocity \(v\), the volumetric productivity \(P_x\) of the continuously operated tPBR can be obtained. The increase in biomass over the tube length can be derived from the difference between the biomass concentration at the outlet of the solar loop \(c_{x,\text{out}}\) and that at the inlet \(c_{x,0}\):

\[
P_x = \frac{c_{x,\text{out}} - c_{x,0}}{\tau}
\]  

(21)

3. Results and Discussion

3.1. Impact of High Dissolved Oxygen Concentration (DOC) on the Oxygen Production Rate (OPR) of A. platensis PCC7345

Photorespirometric analyses were carried out to study how rising DOCs influence the OPR of A. platensis PCC7345 under varying \(c_x\) (0.1, 0.5, and 1.0 g L\(^{-1}\)) and incident illumination conditions \((I_0 = 100, 150\) and 400 \(\mu\)mol m\(^{-2}\) s\(^{-1}\) equal to \(I_{av}\) of 13–131 \(\mu\)mol m\(^{-2}\) s\(^{-1}\)).

Figure 3a presents the \(c_x\)-related OPR and rate of oxygen consumption due to basal respiration (OCR) obtained in experiments with varying average illumination conditions.
Figure 3. Biomass-related oxygen production rate at an increasing average illumination intensity ($I_{av}$) separated into measurable net photosynthetic OPR (positive) and respirometric OCR (negative): determination of the photosynthetic half-saturation constant $K_L$ (49.4 µmol m$^{-2}$ s$^{-1}$; SE: 10.9 µmol m$^{-2}$ s$^{-1}$) and maximum OPR$_{max}$ (2.7 gO$_2$ g$^{-1}$ d$^{-1}$; SE: 0.3 gO$_2$ g$^{-1}$ d$^{-1}$) by fitting to a MONOD-type model. Data were obtained during light/dark cycles of the reference phase under air-saturated DOCs. Error bars represent standard deviation of two independent experiments.

The OPR increased at a constant rate under $I_{av}$ conditions <64 µmol m$^{-2}$ s$^{-1}$ but remained at a constant level at $I_{av}$ > 64 µmol m$^{-2}$ s$^{-1}$ indicating a light-saturated state. As described in several studies [45,47–49] for different phototrophic microorganisms, the dark respiration rate OCR correlates with their growth rate and the availability of photosynthetically active radiation, indicated by a 40% increase in OCR at 131 µmol m$^{-2}$ s$^{-1}$ compared to the low $I_{av}$ conditions of 13 µmol m$^{-2}$ s$^{-1}$ in this study. Photoinhibitory effects were not observed under the illumination conditions considered in this study (max. $I_0$ = 400 µmol m$^{-2}$ s$^{-1}$, max. $I_{av}$ = 131 µmol m$^{-2}$ s$^{-1}$). Based on photorespirometric data on A. platensis PCC7345, the half-saturation constant $K_L$ was quantified to 49.4 µmol m$^{-2}$ s$^{-1}$ (SE: 10.9 µmol m$^{-2}$ s$^{-1}$; Equation (8)). According to Vonshak (1997), the light dependence of photoautotrophic growth of A. platensis, and thus the related OPR$_{max}$ and $K_L$ value depend strongly on the experimental conditions, as photoadaptation effects, for example, may affect growth kinetics [42]. Moreover, $K_L$ values reported in the literature are derived from varying modeling approaches [50,51] or are based on incident illumination intensities (in contrast to the use of average illumination conditions $I_{av}$ in this study). The half-saturation constant $K_L$ of A. platensis was quantified in recent studies as approx. 90 µmol m$^{-2}$ s$^{-1}$ assuming incident illumination intensities [52,53], whereas Vonshak (1997) proposed that the onset of light saturation in different Spirulina strains occurs at incident illumination intensities of 115–165 µmol m$^{-2}$ s$^{-1}$ [42]. However, the impact of cell-specific light attenuation under dynamically changing $c_x$ conditions due to mutual shading effects by the cells has not been taken into consideration in most studies.

3.2. Correlation of DOC and OPR of A. platensis PCC7345

Photorespirometry is a powerful tool for rapidly and reproducibly analyzing how environmental factors such as a high DOC affects the cellular physiology of photoautotrophic cells.

Figure 4 shows the course of a normalized OPR at DOCs rising to 24 mg L$^{-1}$ (approx. 300% air saturation) with varying $c_x$ and $I_0$ conditions. The data indicate that a rising concentration of dissolved oxygen considerably affects the OPR. However, the inhibition kinetics are highly dependent on both the illumination conditions and adjusted $c_x$. An
exponential decrease in a normalized OPR was detected when low $c_x$ were exposed to incident illuminations $>150 \, \mu$mol m$^{-2}$ s$^{-1}$ yielding a full inhibition of the OPR at a DOC of approx. 10 mg L$^{-1}$. The inhibitory effect of the DOC declined at higher $c_x$ (0.5 g L$^{-1}$ and 1.0 g L$^{-1}$) or under lower $I_{av}$ conditions, causing a linear decrease in the normalized OPR up to a critical DOC of about 22 mg L$^{-1}$. The OPR inhibition kinetics of Figure 4 indicate that A. platensis PCC7345 is highly sensitive to rising DOCS at low $c_x$, which are representative for early phases of large-scale cultures; however, the effect is weakened under higher $c_x$ conditions.

Figure 4. Normalized OPR at increasing DOCS. Data were obtained during the continuous illumination phase of the photorespirometry experiments under varying cell dry weight concentrations and illumination conditions. Two independent experimental runs are presented per condition (legend).

A similar exponential decrease in OPRs has been reported in recent studies for microalgae such as S. almeriensis [35] or C. protothecoides [36] showing a comparable maximum DOC for C. protothecoides (20–30 mg L$^{-1}$). The physiological reasons for inhibitory effects at high DOCS have been discussed variously in the literature. First, reversible effects such as photorespiration have been suggested as a cause of photosynthesis inhibition in microalgae at high DOCS [35,36]. Second, enhanced photo-oxidative processes are known to impair the photosynthetic activity of cells. It was reported that a high DOC is able to initialize destructive photo-oxidative effects even at low illumination intensities [24,54], i.e., the generation of harmful reactive oxygen species (ROSs) by Mehler (-peroxidase) reactions can affect important cellular repair and protection mechanisms [55,56] and interact with photosynthesis pigments [57]. In a previous study, Allahverdiyeva et al. [58] showed that the extent of “Mehler-like” reactions of cyanobacteria correlated with the illumination intensity. Raven et al. [59] stated that the degree of oxygen uptake, and the ROS generation by Mehler-peroxidase reactions, is significantly higher for cyanobacteria compared to eu-karyotic green microalgae. Table 1 provides an overview of recent studies addressing how DOCS affect the growth kinetics and biomass composition of phototrophic microorganisms.

It was proposed that high DOCS do not affect the pigment content of microalgae at low illumination intensities [26,60]. However, for cyanobacteria the authors found a significant reduction in the cellular pigment content (e.g., chlorophyll, phycocyanin) at rising DOCS and low illumination intensities [61,62]. Table 1 reveals that the growth rate of A. platensis seems to be generally less affected by high DOCS compared to eukaryotic microalgae. Nevertheless, it was recommended to avoid DOCS $>30$ mg L$^{-1}$ [25,63] or even $>20$ mg L$^{-1}$ [64] when culturing A. platensis, which shows the need for a systematic analysis of this interplay of the process parameters. To take an example, the daily productivity of an outdoor IPBR cultivation was reduced by approximately 20% at high DOCS ($53.0 \pm 9.4$ mg L$^{-1}$) compared to similar process conditions at lower DOCS ($20.8 \pm 1.8$ mg L$^{-1}$) [64].
Table 1. Overview of the impact of highly dissolved oxygen concentrations (DOCs) on growth parameters such as the specific growth rate $\mu$, volumetric biomass productivity $P_x$, oxygen production rate $OPR$, biomass concentration $c_x$ and pigment composition of different microalgae and cyanobacteria. SS: sub-saturation light; NS: near-saturation light; IL: inhibiting light; $c_{\text{Chl}}$: chlorophyll content; $c_{\text{Car}}$: carotenoid content; $c_{\text{PC}}$: phycocyanin content; $c_p$: protein content, Y(II): effective PS II quantum yield; the unit $\mu$E corresponds to $\mu$mol m$^{-2}$ s$^{-1}$.

<table>
<thead>
<tr>
<th>Microorganism</th>
<th>Culture Conditions</th>
<th>DOC (mg L$^{-1}$)</th>
<th>Effects on the Growth ($\mu$, $P_x$, $OPR$, $c_x$)</th>
<th>Effects on Pigment Composition</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>Neochloris oleobundans</td>
<td>200 $\mu$E (SS); 25 $^\circ$C</td>
<td>$\approx$26</td>
<td>decrease in $\mu$ by: $\approx$25%</td>
<td>no impact on $c_{\text{Chl}}$ and $c_{\text{Car}}$</td>
<td>[65]</td>
</tr>
<tr>
<td></td>
<td>500 $\mu$E (NS); 25 $^\circ$C</td>
<td>$\approx$26</td>
<td>$\approx$32%</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>$\approx$35</td>
<td>$\approx$50%</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Nannochloropsis sp.</td>
<td>100 $\mu$E (SS); 25 $^\circ$C</td>
<td>$\geq$6</td>
<td>linear decrease in $\mu$ $\approx$38% of $\mu$ left</td>
<td></td>
<td>[66]</td>
</tr>
<tr>
<td>Chlorella vulgaris</td>
<td>250 $\mu$E; 25 $^\circ$C</td>
<td>$\leq$25</td>
<td>no impacts</td>
<td>maximum $OPR$</td>
<td></td>
</tr>
<tr>
<td></td>
<td>220 $\mu$E; 25 $^\circ$C</td>
<td>31</td>
<td>30% decrease in $P_x$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Scenedesmus almeriens</td>
<td>200 $\mu$E (SS); 25 $^\circ$C</td>
<td>9–23</td>
<td>decrease in $OPR \leq 20%$</td>
<td></td>
<td>[35]</td>
</tr>
<tr>
<td></td>
<td>24 $^\circ$C</td>
<td>32</td>
<td>exponential decline</td>
<td>$OPR = 0$</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$\approx$21–26</td>
<td>32</td>
<td>exponential decline</td>
<td>$OPR = 0$</td>
<td></td>
</tr>
<tr>
<td>Chlorella protothecoides</td>
<td>150 $\mu$E (SS); 24 $^\circ$C</td>
<td>$\leq$16</td>
<td>no impacts</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>1000 $\mu$E(NS)</td>
<td>$\approx$27</td>
<td>$OPR = 0$</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>1500 $\mu$E (IL)</td>
<td>$\approx$30</td>
<td>$OPR = 0$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Arthrospira maxima</td>
<td>$\approx$125 $\mu$E, 30 $^\circ$C</td>
<td>$\approx$16</td>
<td>no significant effects</td>
<td></td>
<td>[62]</td>
</tr>
<tr>
<td>Arthrospira platensis</td>
<td>$\approx$140 $\mu$E (SS); 30 $^\circ$C</td>
<td>$\approx$10</td>
<td>decrease in $\mu$ by: $10%$</td>
<td>reduction of $c_p$ (50%); $c_{\text{PC}}$ (70%); $c_{\text{Chl}}$ (20%)</td>
<td>[61]</td>
</tr>
<tr>
<td></td>
<td>$\approx$20</td>
<td>$\approx$20</td>
<td>$20%$</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$\approx$30</td>
<td>$\approx$33</td>
<td>$33%$</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$\approx$40</td>
<td>$\approx$46</td>
<td>$46%$</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>32 $\mu$E (SS); 30 $^\circ$C</td>
<td>$\approx$13</td>
<td>decrease in $\mu$ by: $13%$</td>
<td>reduction of $c_{\text{PC}}$; $c_{\text{Chl}}$; $c_{\text{Car}}$ (all up to approx. 80%)</td>
<td>[67]</td>
</tr>
<tr>
<td></td>
<td>$\approx$25</td>
<td>$\approx$25</td>
<td>$25%$</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>$\geq$80</td>
<td>$\approx$25</td>
<td>no growth</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>350 $\mu$E (NS-IL); 35 $^\circ$C</td>
<td>36</td>
<td>max. 18% lower $c_x$; chlorotic after long exposure (&gt;32 h)</td>
<td>reduction of $c_{\text{Chl}}$ (30%)</td>
<td>[64]</td>
</tr>
</tbody>
</table>

3.3. Estimating Kinetic Parameters with Photorespirometry

To study how the DOC affects growth kinetics, photorespirometry data were analyzed in line with Sforza et al. [36]. Since photorespirometry experiments carried out under carbon limitation (N$_2$ sparging, data not shown) revealed no significant impact on $OPR$ trends at rising DOCs, the $OPR_{ph}$ term used by Sforza et al. [36] (Equation (11)) was assumed to be constant for A. platensis PCC7345 in this study and was calculated from the sum of $OPR$ and OCR data obtained during the reference phase under moderate oxygen conditions.

To quantify the $OCR_{resp}$—the negative contribution caused by basal respiration—(Equation (12)) and the $OPR_{net}$ (Equation (10)), OCR data of the reference phase (Equation (12): $k_{resp} = 0.266$ d$^{-1}$ SE: 0.006 d$^{-1}$; $K_{M,O_2} = 0.181$ mg L$^{-1}$ SE: 0.029 mg L$^{-1}$ imply constant OCR data in the DOC range of air saturation and higher), and $OPR$ data on the continuous
illumination phase were applied, respectively. Thus, the inhibitory effect at high DOCs expressed by \( OCR_{\text{inh}} \) was derived following Equation (10).

### 3.3.1. Model by Sforza et al.

The experimental data on \( c_x \)-related \( OCR_{\text{inh}} \) are shown in Figure 5. Significant differences were observed between \( c_x \)-related \( OCR_{\text{inh}} \) for *A. platensis* PCC7345 in experiments performed under different process conditions (Figures 3 and 4), indicating that \( OCR_{\text{inh}} \) of *A. platensis* PCC7345 cannot be characterized by one set of kinetic parameters as shown for microalgae (Sforza et al. [36]; Figure 5b). Both the oxygen inhibition coefficient \( k_{\text{inh}} \) and the oxygen inhibition exponent \( \zeta \) ranged between \( 5.72 \times 10^{-5} \text{ d}^{-1} \) and \( 5.24 \times 10^{-2} \text{ d}^{-1} \), and 0.11 L mg\(^{-1}\) to 1.25 L mg\(^{-1}\), respectively. To conclude, in contrast to the study by Sforza et al. [36], the oxygen inhibition rate \( OCR_{\text{inh}} \) was found to be light-dependent for *A. platensis* PCC7345 and the need was identified to take into account both the illumination intensity and \( c_x \) conditions of each experimental setup.

**Figure 5.** Comparison of the biomass-related inhibiting term \( OCR_{\text{inh}} \) depending on the DOC conditions, using (a) the cyanobacterium *A. platensis* PCC7345 in this study—data are calculated using photorespirometry—and (b) *C. protothecoides* microalgae in the study by Sforza et al. [36] under varying \( c_x \) and illumination conditions indicating that the two microorganisms behave differently at high DOCs. The figure shows that a kinetic relationship can be achieved for microalgae (right) under varying \( c_x \) and \( I_{\text{av}} \) conditions (each symbol represents one experimental setting). Such a general kinetic correlation between DOC and \( OCR_{\text{inh}} \) is not possible for *A. platensis* PCC7345.

### 3.3.2. Model by Costache et al.

As a second approach, the oxygen model developed by Costache et al. [35] (Equation (14)), was applied to the photorespirometry data. A typical fitting result of experimental data is presented in Figure 6b).

To compare the two modeling approaches, Table 2 summarizes the model parameters obtained. Both models were able to fit OPR data on the continuous light phase with a high coefficient of determination (Costache: \( R^2 > 0.96 \); Sforza: \( R^2 > 0.91 \)). It was found that the oxygen inhibition constant \( KO_2 \) followed a correlation with the average illumination intensity \( I_{\text{av}} \), which can be mathematically described by an exponential correlation (\( R^2 > 0.83 \), Figure 6a):

\[
KO_2 = 80.489 \ I_{\text{av}}^{-0.476}
\]  

During the experimental data acquisition, high incident \( I_0 \) intensities were revealed to be mitigated by an increasing \( c_x \) (higher \( KO_2 \)) compared to equivalent \( I_{\text{av}} \) conditions at low \( c_x \) (red circle in Figure 6a). This indicated that a buffering effect occurred under higher \( c_x \) conditions, related to the DOC sensitivity.
Table 2. Comparison of model parameter resulted by fitting experimental photorespirometry data using the model developed by Costache et al. [35] and Sforza et al. [36].

<table>
<thead>
<tr>
<th>$I_0$ (μmol m$^{-2}$ s$^{-1}$)</th>
<th>$I_{av}$ (μmol m$^{-2}$ s$^{-1}$)</th>
<th>$c_x$ (g L$^{-1}$)</th>
<th>$KO_2$ (mg O$_2$ L$^{-1}$)</th>
<th>$z$ (-)</th>
<th>$R^2$ (-)</th>
<th>$k_{inh}$ (d$^{-1}$)</th>
<th>$\xi$ (L mg O$_2$$^{-1}$)</th>
<th>$R^2$ [-]</th>
</tr>
</thead>
<tbody>
<tr>
<td>100</td>
<td>16</td>
<td>0.5</td>
<td>16.13</td>
<td>2.35</td>
<td>0.9835</td>
<td>1.24 × 10$^{-2}$</td>
<td>0.22</td>
<td>0.9463</td>
</tr>
<tr>
<td></td>
<td>14.45</td>
<td>2.30</td>
<td>0.9882</td>
<td>1.42 × 10$^{-2}$</td>
<td>0.18</td>
<td>0.9947</td>
<td></td>
<td></td>
</tr>
<tr>
<td>13</td>
<td>1</td>
<td>24.51</td>
<td>1.61</td>
<td>0.9761</td>
<td>2.58 × 10$^{-2}$</td>
<td>0.09</td>
<td>0.9805</td>
<td></td>
</tr>
<tr>
<td></td>
<td>23.76</td>
<td>1.66</td>
<td>0.9831</td>
<td>2.67 × 10$^{-2}$</td>
<td>0.08</td>
<td>0.9914</td>
<td></td>
<td></td>
</tr>
<tr>
<td>150</td>
<td>49</td>
<td>0.1</td>
<td>10.16</td>
<td>5.49</td>
<td>0.9606</td>
<td>1.52 × 10$^{-4}$</td>
<td>0.61</td>
<td>0.9103</td>
</tr>
<tr>
<td></td>
<td>10.44</td>
<td>8.69</td>
<td>0.9710</td>
<td>1.25 × 10$^{-4}$</td>
<td>0.93</td>
<td>0.9378</td>
<td></td>
<td></td>
</tr>
<tr>
<td>24</td>
<td>0.5</td>
<td>19.14</td>
<td>1.62</td>
<td>0.9610</td>
<td>3.86 × 10$^{-2}$</td>
<td>0.13</td>
<td>0.9126</td>
<td></td>
</tr>
<tr>
<td></td>
<td>21.40</td>
<td>2.07</td>
<td>0.9844</td>
<td>1.05 × 10$^{-2}$</td>
<td>0.18</td>
<td>0.9413</td>
<td></td>
<td></td>
</tr>
<tr>
<td>21</td>
<td>0.8</td>
<td>22.80</td>
<td>1.78</td>
<td>0.9847</td>
<td>5.24 × 10$^{-2}$</td>
<td>0.11</td>
<td>0.9442</td>
<td></td>
</tr>
<tr>
<td></td>
<td>27.36</td>
<td>1.71</td>
<td>0.9870</td>
<td>4.49 × 10$^{-2}$</td>
<td>0.09</td>
<td>0.9466</td>
<td></td>
<td></td>
</tr>
<tr>
<td>400</td>
<td>131</td>
<td>0.1</td>
<td>8.97</td>
<td>5.08</td>
<td>0.9886</td>
<td>6.47 × 10$^{-3}$</td>
<td>0.64</td>
<td>0.9896</td>
</tr>
<tr>
<td></td>
<td>8.45</td>
<td>6.70</td>
<td>0.9990</td>
<td>1.16 × 10$^{-3}$</td>
<td>0.85</td>
<td>0.9971</td>
<td></td>
<td></td>
</tr>
<tr>
<td>64</td>
<td>0.5</td>
<td>21.09</td>
<td>2.80</td>
<td>0.9937</td>
<td>3.68 × 10$^{-2}$</td>
<td>0.17</td>
<td>0.9763</td>
<td></td>
</tr>
<tr>
<td></td>
<td>21.37</td>
<td>3.19</td>
<td>0.9928</td>
<td>3.82 × 10$^{-2}$</td>
<td>0.17</td>
<td>0.9831</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Figure 6. (a) Estimation of the oxygen inhibition constants $KO_2$ by the model proposed by Costache et al. [35] depending on average illumination intensity $I_{av}$. The red circle corresponds to high $I_0$ illumination at high $c_x$ yielding (similar $I_{av}$ conditions such as low $I_0$ and low $c_x$), indicating that high $c_x$ conditions may be less sensitive to high DOCs. The solid line marks the course of a power-type function that resulted from fitting the correlation between $KO_2$ and $I_{av}$ ($R^2 = 0.83$). (b) Example of a typical fitting process according to the model described by Costache et al. [35].

3.4. Impact of DOCs on Cellular Phycocyanin Content ($c_{PC}$)

Besides the impact on growth kinetics, there has been little research so far on how DOCs affect the cellular metabolites of phototrophic microorganisms such as the phycobiliprotein phycocyanin of *A. platensis*. Here, the exposure phase was introduced in the photorespirometry routine to investigate the temporal impact of high DOCs (approx. 25 mg L$^{-1}$) on the $c_{PC}$ of *A. platensis* PCC7345. Sampling and phycocyanin analytics were performed as shown in Section 2.5.

Figure 7 shows a constant $c_{PC}$ at a $c_x$ of >0.5 g L$^{-1}$ exposed to low $I_{av}$ of <49 μmol m$^{-2}$ s$^{-1}$ during 20 h of high DOC exposure. A significant reduction in $c_{PC}$ was obtained if either a low $c_x$ of 0.1 g L$^{-1}$ was used (0.66 ± 0.02 at $I_{av} = 49$ μE) or $I_{av}$ was >49 μmol m$^{-2}$ s$^{-1}$, indicating that *A. platensis* PCC7345 cultures at low biomass concentrations are more strongly affected by high DOCs. Moreover, high exposure times seemed to exacerbate the harmful effects on $c_{PC}$ under high $I_{av}$ conditions: after 2 and 4 h the $c_{PC}$ was reduced by
less than 20% followed by a significant further reduction in $c_{PC}$ to 35% after 20 h of DOC exposure. Statistical analysis revealed that the phycocyanin content is significantly affected by the exposure duration and the cultivation conditions ($p < 0.0001$).

Figure 7. Course of the normalized cellular phycocyanin content $c_{PC}$ during exposure of *A. platensis* PCC7345 cultures to high DOC levels ($\approx 25$ mg L$^{-1}$) during the exposure phase of photorespirometry conducted under different light conditions and biomass concentrations.

It was reported that *A. platensis* responds to high illumination intensities by reducing cellular light harvesting pigments to prevent the harmful effects of photoinhibition, among other things [42]. Vonshak et al. [64] detected a decrease in the cellular chlorophyll content of up to 30% for *A. platensis* exposed to high illumination intensities and oxygen gassing (DOC: 36 mg L$^{-1}$) compared to experiments with air gassing. The authors reported that *A. platensis* cultures became chlorotic after exposure to both high DOCs and high illumination intensities ($I_0 = 350$ µmol m$^{-2}$ s$^{-1}$), indicating that the cells were lastingly damaged by photo-oxidative processes. Marquez et al. [61] observed that after 72 h of cultivation the phycocyanin content of *A. platensis* was reduced by 85% when exposed to a DOC of 40 mg L$^{-1}$ (connected to air saturation) and an $I_0$ of 140 µmol m$^{-2}$ s$^{-1}$ [61]. In conclusion, in the case of *A. platensis*, the cellular phycocyanin content—one of the major cellular constituents responsible for light harvesting and further industrial valorization—is highly susceptible to high DOC levels, particularly at high illumination intensities and under low $c_x$ conditions.

During outdoor cultivation, extreme values of incident illumination intensities (e.g., 1700 µmol m$^{-2}$ s$^{-1}$) and DOCs (e.g., 80 mg L$^{-1}$) can be reached temporarily [24,25]. To tackle the challenges of high illumination intensities, shading devices for PBRs or gas stripping approaches were proposed to prevent cell damage and biomass losses and keep the DOC at a non-critical level. To name an example, Torzillo et al. [24] examined an increase of 50% in the volumetric biomass productivity of outdoor *A. platensis* cultivation in tPBRs caused by the application of nitrogen gassing, which lowered the average DOC in the tPBR from around 60 to 22 mg L$^{-1}$.

3.5. Computational Scale-Up Study and Assessment of Biomass Productivity Using Industrial tPBRs with Different Configurations

The kinetic studies performed on the basis of photorespirometry were used for an in-silico scale-up study for the cultivation of *A. platensis* PCC7345 on an industrial scale. For this purpose, two different configurations of tPBR were assumed, as described in Section 2.7, having a constant total liquid volume of 5000 L but with different tube lengths: a serial configuration with an 1800 m tube and a parallel configuration with a 450 m tube.
Table 3 lists the model input parameters including the experimental kinetic parameters which were examined in this study and process parameters derived from literature sources.

Table 3. Input model parameter for in-silico scale-up study on *A. platensis* PCC7345 in industrial tPBRs with varying configurations.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Remarks/Source of Supply</th>
</tr>
</thead>
<tbody>
<tr>
<td>(d)</td>
<td>6 cm</td>
<td>Assumption; tube diameter equal to the light path length (Z)</td>
</tr>
<tr>
<td>(L)</td>
<td>1800 m</td>
<td>Serial configuration</td>
</tr>
<tr>
<td>(L)</td>
<td>450 m</td>
<td>Parallel configuration</td>
</tr>
<tr>
<td>(I_0)</td>
<td>variable</td>
<td></td>
</tr>
<tr>
<td>(c_{x,0})</td>
<td>variable</td>
<td></td>
</tr>
<tr>
<td>(k_L)</td>
<td>4 h(^{-1})</td>
<td>Assumption, inspired by [28]</td>
</tr>
<tr>
<td>(\varepsilon_g)</td>
<td>0.02</td>
<td>Assumption, inspired by [28]</td>
</tr>
<tr>
<td>(c_{O_2,0})</td>
<td>7.4 mg(\text{O}_2) L(^{-1})</td>
<td>Solubility concentration of oxygen at 30 °C</td>
</tr>
<tr>
<td>(\nu)</td>
<td>0.35 m s(^{-1})</td>
<td>Based on [68]</td>
</tr>
<tr>
<td>(T)</td>
<td>30 °C</td>
<td>Assuming constant temperature conditions</td>
</tr>
<tr>
<td>(p_{O_2})</td>
<td>0.21 atm</td>
<td>[39]</td>
</tr>
<tr>
<td>(H_{ref})</td>
<td>1.2 (\times) (10^{-3}) mol m(^{-3}) Pa(^{-1})</td>
<td>[69]</td>
</tr>
<tr>
<td>(K_L)</td>
<td>49.4 (\mu)mol m(^{-2}) s(^{-1})</td>
<td>This work</td>
</tr>
<tr>
<td>(Y_{O_2})</td>
<td>1.97 g(\text{O}_2) g(\text{x})(^{-1})</td>
<td>[25]</td>
</tr>
<tr>
<td>(\varepsilon)</td>
<td>(\varepsilon) [L cm(^{-1}) g(^{-1})]</td>
<td>This work</td>
</tr>
<tr>
<td>(K_{O_2})</td>
<td>80.489 (I_{av})((\cdot)0.476)</td>
<td>This work</td>
</tr>
<tr>
<td>(z)</td>
<td>1.85</td>
<td>This work</td>
</tr>
<tr>
<td>(\mu_{max})</td>
<td>0.032 h(^{-1})</td>
<td>Experimentally determined</td>
</tr>
</tbody>
</table>

In order to investigate how DOC inhibition kinetics influence the process performance, first a comparative study was carried out assuming a continuously operated serial tPBR configuration (a) neglecting DOC inhibition kinetics (Figure 8a) and (b) taking into account DOC inhibition kinetics (Figure 8b).

As can be seen from Figure 8a, the predicted biomass productivity at low incident illumination \(I_0\) increases with a rising biomass concentration \(c_{x,0}\). In the case of rising \(I_0\) conditions, the predicted \(P_x\) increased steadily up to a maximum of approx. 0.8 g L\(^{-1}\) d\(^{-1}\). However, this scenario did not correspond to real process performances, as \(P_x\) was reported to range between 0.4 and 0.6 g L\(^{-1}\) d\(^{-1}\) for *A. platensis* cultivations in tPBRs [70–72].

Considering the DOC inhibition kinetics in the model, a different process performance was indicated as the predicted \(P_x\) was reduced by up to 300% (approx. 0.25 g L\(^{-1}\) d\(^{-1}\)) compared to non-limited biomass growth. The maximum predicted \(P_x\) of the continuous operating serial tPBR was reached under moderate illumination conditions in the range of 200–250 \(\mu\)mol m\(^{-2}\) s\(^{-1}\) with a high initial \(c_{x,0}\). This study found that the DOC inhibition effect is highly dependent on the illumination intensity (illumination-dependent \(K_{O_2}\)) for *A. platensis* PCC7345. Accordingly, the predicted \(P_x\) decreased significantly in the in-silico study with an increasing incident \(I_0\) as a high illumination intensity triggers the photoautotrophic growth and oxygen production, leading to a rising DOC inhibition effect.

In computational studies, Trentin et al. [34] investigated the growth-inhibiting effects of oxygen on the microalgae *C. protothecoides* in a continuously operated tPBR. This revealed a reduced biomass growth rate in the range of 200–280% alongside the tube length at high \(I_0\) intensities (400–1000 \(\mu\)mol m\(^{-2}\) s\(^{-1}\)) [34], which is in the same order of magnitude found in this study.
Figure 8. Process modeling of the productivity $P_x$ related to cell dry weight concentration ($g \, L^{-1} \, d^{-1}$) of *A. platensis* PCC7345 in industrial tPBRs: (a) serial tPBR with a tube length of 1800 m neglecting DOC inhibition, $\left( \frac{c_{O_2}}{K_{O_2}} \right) = 0$, (b) serial tPBR with a tube length of 1800 m considering DOC inhibition and (c) parallel tPBR with a tube length of 450 m considering DOC inhibition.

To reduce the DOC in the liquid phase and mitigate the inhibitory DOC effect, various PBR design options are available such as a reduced tube length and improved degassing units. To quantify the impact of the DOC on $P_x$, a parallel tPBR configuration with a maximum tube length of 450 m was also analyzed (Figure 8c). Assuming the $k_{L,a}$ and total liquid volume to be the same, the maximum $P_x$ during continuous operation was increased nearly five-fold to approx. 1.16 g L$^{-1}$ d$^{-1}$ ($l_0 = 190 \, \mu$mol m$^{-2}$ s$^{-1}$), indicating the impact of DOC inhibition kinetics with non-optimal process configurations. Trentin et al. [34] predicted that the tube length for tPBRs would avoid the inhibitory effects of DOCs, ensuring stable $r_x$ in *C. protothecoides*. The authors concluded that to prevent growth from being limited by high DOCs, the tube length should not exceed 200 m, especially for tPBR cultivations with high $c_{x,0}$ (approx. 1 g L$^{-1}$) and high $l_0$ (approx. 700–1000 \, \mu$mol m$^{-2}$ s$^{-1}$) [34]. Further studies have confirmed that the tube length of tPBRs needs to be limited to prevent high levels of oxygen accumulation [25,63,73] because parts of the tPBRs become non-productive due to oxygen inhibition [27].

The kinetic studies and in-silico scale-up showed that the DOC had a significant impact on the productivity of photoautotrophic bioprocesses, which have to be taken into account in the PBRs’ design to ensure they perform optimally. However, the impact is a multidimensional problem, depending on a variety of factors such as the tube diameter, power input, degassing concepts, and the cells’ OPR capacity and sensitivity to the DOC. The authors would like to emphasize that the in-silico study was designed by assuming a set of hydrodynamic parameters which may be different for other PBR configurations.
Supplementary Materials: The following supporting information can be downloaded at: https://www.mdpi.com/article/10.3390/chemengineering6010014/s1. Supplementary materials can be downloaded at: Figure S1: Calibration line to quantify dry weight concentration from OD750; Figure S2: Calibration routine for in-vivo phycocyanin quantification from diluted suspended cells; Figure S3: Calibration line for in-vivo phycocyanin quantification from diluted suspended cells by fluorescence spectroscopy; Figure S4: Fluorescence intensity obtained at increasing cell density (OD750). An optimum range was detected between OD750 0.1–0.4. A higher cell density leads to a high re-absorption of fluorescence emission and should be avoided for fluorescence spectroscopy; Table S1: Experimental data of Figure 3 (OPR_D/OCR and OPR_L/OPR) and Figure 6a (KO2); Table S1: Experimental data of Figure 7.

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Abbreviations

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>H2O2</td>
<td>Henry’s constant (Henry’s law)</td>
<td>mol m⁻³ Pa⁻¹</td>
</tr>
<tr>
<td>H_ref</td>
<td>reference Henry’s constant (Henry’s law)</td>
<td>mol m⁻³ Pa⁻¹</td>
</tr>
<tr>
<td>I</td>
<td>light intensity</td>
<td>µmol photons m⁻² s⁻¹</td>
</tr>
<tr>
<td>I0</td>
<td>incident light intensity</td>
<td>µmol photons m⁻² s⁻¹</td>
</tr>
<tr>
<td>Iav</td>
<td>average light intensity</td>
<td>µmol photons m⁻² s⁻¹</td>
</tr>
<tr>
<td>I_f, max</td>
<td>maximum fluorescence intensity</td>
<td>kg_c m⁻³</td>
</tr>
<tr>
<td>KCO2</td>
<td>half-saturation constant for CO₂ (model by Sforza)</td>
<td>kg m⁻³</td>
</tr>
<tr>
<td>KL</td>
<td>light half-saturation constant</td>
<td>kg m⁻³</td>
</tr>
<tr>
<td>KM,O2</td>
<td>oxygen half-saturation constant for respiration (model by Sforza)</td>
<td>kg m⁻³</td>
</tr>
<tr>
<td>KO2</td>
<td>oxygen inhibition constant (model by Costache)</td>
<td>kg_m⁻³</td>
</tr>
<tr>
<td>KPR</td>
<td>photorespiration constant (model by Sforza)</td>
<td>kg m⁻³</td>
</tr>
<tr>
<td>L</td>
<td>tube length of the solar unit</td>
<td>m</td>
</tr>
<tr>
<td>OCR</td>
<td>oxygen consumption rate</td>
<td>kgO2 m⁻³ s⁻¹</td>
</tr>
<tr>
<td>OCR_inh</td>
<td>oxygen inhibition rate (model by Sforza)</td>
<td>kgO2 m⁻³ s⁻¹</td>
</tr>
<tr>
<td>OCR_resp</td>
<td>oxygen respiration rate (model by Sforza)</td>
<td>kgO2 m⁻³ s⁻¹</td>
</tr>
<tr>
<td>OPR</td>
<td>oxygen production rate</td>
<td>kgO2 m⁻³ s⁻¹</td>
</tr>
<tr>
<td>OPR_max</td>
<td>biomass-related maximum rate of photosynthesis</td>
<td>kgO2 kg⁻¹ s⁻¹</td>
</tr>
<tr>
<td>OPR_net</td>
<td>net oxygen production rate (Sforza model)</td>
<td>kgO2 m⁻³ s⁻¹</td>
</tr>
<tr>
<td>OPR_ph</td>
<td>photosynthetic oxygen production (Sforza model)</td>
<td>kgO2 m⁻³ s⁻¹</td>
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<tr>
<td>OD750</td>
<td>optical density at a light wavelength of 750 nm</td>
<td>kgO2 m⁻³ s⁻¹</td>
</tr>
<tr>
<td>T_ref</td>
<td>reference temperature (Henry’s law)</td>
<td>K</td>
</tr>
<tr>
<td>YO₂</td>
<td>yield of oxygen produced per biomass</td>
<td>kgO2 kg⁻¹ s⁻¹</td>
</tr>
<tr>
<td>Z</td>
<td>light path length</td>
<td>m</td>
</tr>
<tr>
<td>cCO₂</td>
<td>concentration of dissolved CO₂</td>
<td>kg_c m⁻³</td>
</tr>
<tr>
<td>cO₂</td>
<td>oxygen concentration in the liquid phase</td>
<td>kgO2 m⁻³</td>
</tr>
<tr>
<td>cO₂,0</td>
<td>oxygen concentration at the inlet of the solar unit</td>
<td>kgO2 m⁻³</td>
</tr>
</tbody>
</table>
\[c_{O_2,\text{out}}\] oxygen concentration at the outlet of the solar unit \(\text{kg}_O_2 \text{ m}^{-3}\)
\[c_{O_2} \] saturation concentration of oxygen in the liquid phase \(\text{kg}_O_2 \text{ m}^{-3}\)
\[c_{PC} \] phycocyanin content (biomass-related) \(\text{kg}_PC \text{ kg}_x^{-1}\)
\[c_x \] biomass concentration \(\text{kg}_x \text{ m}^{-3}\)
\[c_{x,0} \] biomass concentration at the inlet of the solar unit \(\text{kg}_x \text{ m}^{-3}\)
\[c_{x,\text{out}} \] biomass concentration at the outlet of the solar unit \(\text{kg}_x \text{ m}^{-3}\)
\[k_{1,a} \] oxygen mass transfer coefficient \(\text{s}^{-1}\)
\[l \] tube length of the solar unit (running coordinate) \(\text{m}\)
\[p_{O_2} \] oxygen partial pressure \(\text{Pa}\)
\[r_{O_2} \] oxygen production rate \(\text{kg}_O_2 \text{ m}^{-3} \text{ s}^{-1}\)
\[r_x \] biomass growth rate \(\text{kg}_x \text{ m}^{-3} \text{ s}^{-1}\)
\[v \] flow velocity \(\text{m} \text{ s}^{-1}\)
\[z \] form factor (model by Costache) \(\text{m}^2 \text{ kg}^{-1}\)
\[e_g \] fractional gas hold-up \(\text{s}^{-1}\)
\[\mu \] specific growth rate \(\text{s}^{-1}\)
\[\mu_{O_2} \] maximum specific oxygen rate (model by Sforza) \(\text{s}^{-1}\)
\[\mu_{\text{max}} \] maximum growth rate \(\text{s}^{-1}\)
\[\zeta \] oxygen inhibition exponent (model by Sforza) \(\text{m}^3 \text{ kg}^{-1}\)
\[\tau \] residence time \(\text{s}\)

References


33. Trentin, G.; Barbera, E.; Bertucco, A.; Sforza, E. Role of oxygen in tubular photobioreactors: Model-Based design and operating conditions to minimize productivity losses. Chem. Eng. Processing-Process Int. 2020, 157, 108151. [CrossRef]


