Article
A Preliminary Evaluation of Morphing Horizontal Tail Design for UAVs
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Abstract: Morphing structures are a relatively new aircraft technology currently being investigated for a variety of applications, from civil to military. Despite the lack of literature maturity and its complexity, morphing wings offer significant aerodynamic benefits over a wide range of flight conditions, enabling reduced aircraft fuel consumption and airframe noise, longer range and higher efficiency. The aim of this study is to investigate the impact of morphing horizontal tail design on aircraft performance and flight mechanics. This study is conducted on a 1:5 scale model of a Preceptor N-3 Pup at its trim condition, of which the longitudinal dynamics is implemented in MATLAB release 2022. Starting from the original horizontal tail airfoil NACA 0012 with the elevator deflected at the trim value, this is modified by using the X-Foil tool to obtain a smooth morphing airfoil trailing edge shape with the same \( C_{L_{\alpha}} \). By comparing both configurations and their influence on the whole aircraft, the resulting improvements are evaluated in terms of stability in the short-period mode, reduction in the parasitic drag coefficient \( C_{D_0} \), and increased endurance at various altitudes.

Keywords: morphing wing; horizontal tail; aircraft performance; longitudinal dynamics

1. Introduction

Morphing wing design concerns an automated shape adaptation to produce smooth and continuous deformation of an aircraft’s fixed or movable lifting surfaces during flight in order to obtain optimal performance in multiple flight phases. A stricter definition of aircraft morphing is laid out by DARPA in its Morphing Aircraft Structures (MAS) project [1], aimed at flying UAVs with variable wings for military applications [2]. Morphing technology was referred to as the ability for an aircraft to perform the following:

- Change state substantially to adapt to changing missions and mission environments;
- Provide superior system capability not possible without reconfiguration;
- Integrate innovative combinations of advanced materials, actuators, flow controllers and mechanisms to achieve the required state change.

Morphing aircraft structures are a relatively new concept. For years, pioneer engineers have been inspired by the seamless shape-changing capabilities of bird wings, and have tried to mimic such a natural ability to realize aircraft wing shape optimization and control [3]. Variable camber concepts were explored since the 1980s to smoothly deform wing leading and trailing edges during different flight conditions [4].

Nowadays, morphing wing devices have become a contemporary concept in aeronautics research due to significant advances in materials, structures and control logics. The real breakthrough came from material technology with the introduction of SMAs (shape memory alloys). Some application of SMAs started in the 1970s, and, by the 1990s, the DARPA program Smart Wings [5] looked at the use of them as compact actuators for morphing wings. Between 2003 and 2007, DARPA launched the Morphing Aircraft Structures (MAS) program, which had as its objective the study of a UAV with variable wings for military...
applications. In 2011, Airbus launched the SARISTU program, which is probably the most major research ever carried out in Europe on adaptive structures. The program included the construction of a 5.5 m span wing section, equipped with three morphing wing devices, in turn realized by DLR, CIRA and EADS-IW. They developed a droop nose [6] aimed at increasing the take-off and landing performance, an adaptive trailing edge device [7] aimed at improving the aircraft performance in cruise and an innovative adaptive winglet [8] for gust alleviation, respectively. These devices were controlled by conventional actuation concepts enabling more mature and practical implementations. In 2015, the assembled wing underwent WT tests at TsAGI, the Russian Aeronautical Research Centre, where the three systems proved their capabilities in a relevant environment (TRL 6). A morphing aileron demonstrator [9] was designed and successfully tested in laboratory conditions to validate the actuation system’s authority and reliability.

In Clean Sky AIRGREEN2, a deformable leading edge morphing device and a multifunctional segmented flap system were considered [10] for the improvement of the aerodynamic performance of a turboprop regional aircraft wing in high-lift conditions. Furthermore, a fault-tolerant adaptive winglet with shape-changing capabilities was developed to enhance wing aerodynamic efficiency ($E = C_L/C_D$) in off-design conditions and reduce maneuver loads on a regional turboprop aircraft. The integrated design of the adaptive winglet is detailed in [11].

Morphing wings are an interesting subject to study for different reasons. First of all, the enormous charm of such a technology, which is very innovative and still little studied and implemented. Morphing wing devices have proven to show great potential to obtain augmented aerodynamic efficiency in every flight phase, thus remaining a very attractive factor to reduce fuel consumption and/or to increase endurance. Morphing-wing research for UAVs and micro aircraft (MAVs) is also growing in significance. This interest is mainly driven by the increased chance to mimic bats and insects; of the former, we want to imitate the structure of the wing that branches out over the entire surface in order to create very light devices; of the latter, we are interested in the possibility of creating multi-wing aircraft [12]. Besides, morphing wings are suitable to effectively achieve gust alleviation during flight [13].

Morphing-wing research for UAVs and micro aircraft (MAVs) is also growing in significance [14,15].

However, the majority of the studies carried out so far on morphing wing devices deals with structural and material issues mainly, along with aerodynamic performance [16,17]. From the point of view of flight dynamics, there is a substantial difference whether the geometry variation due to morphing aims to achieve maximum performance in the various flight phases or to replace the traditional surfaces for controlling the aircraft. Numerous dynamic approaches with different levels of complexity and computational efficiency can be found in the literature [18]. The choice of the most suitable model is made while considering many variables. Regarding the computational efficiency, the CPU time represents a qualitative evaluation of the time required for the non-linear simulation based on each method; rapid and continuous wing morphing refer, respectively, to the ability of the method to model rapid geometry changes and large-scale continuum deformations; the actuator model specifies how the morphing variables are handled; the label linearized system characterizes the system after linearization at a trim point as linear time-invariant (LTI) or linear time-varying (LTV); finally, the number of ODEs is a measure of the size of the system of differential equations required for non-linear simulation, with n being the number of bodies of which the system is comprised [12,19].

The aim of present work is to study the impact of the horizontal tail morphing application on the longitudinal dynamics of a reference aircraft, by analyzing the achieved results in terms of stability and transient characteristics of the phugoid and short-period modes, along with the basic performance of the aircraft. This study is a preliminary assessment in which only the trim condition is considered to compare the basic aircraft with that equipped with a morphing horizontal surface.
The present study is conducted on a 1:5 scale model of a Preceptor N-3 Pup by implementing its longitudinal dynamics in the MATLAB environment. The XFOIL program \[20\] is used to obtain the polars of the airfoils analyzed and to model the morphing airfoil. Finally, the Matlab software is used again to analyze the performance of the aircraft by plotting the power-required curves and comparing the results of the basic aircraft with those of the morphing one.

2. Mathematical Model

An accurate non-linear mathematical model of the aircraft constitutes the basis of the present work. The classical rigid body equations of the motion in the body axes have been used \[21\].

\[
\begin{align*}
mu & = -mqw - mgsin\theta + F_x \\
mw & = mqu - mgcos\theta + F_z \\
I_\theta & = M \\
\dot{\theta} & = q \\
\dot{x} & = ucos\theta + wsin\theta \\
\dot{z} & = usin\theta - wcos\theta \\
\end{align*}
\]

where:

\[
\begin{align*}
F_x & = \frac{1}{2}\rho V^2 S C_x \\
F_z & = \frac{1}{2}\rho V^2 S C_z \\
M & = \frac{1}{2}\rho V^2 S m c \\
T & = \frac{1}{2}\rho V^2 S T
\end{align*}
\]

Into (2) as follows:

\[
\begin{align*}
C_x & = C_{Lsina} - C_{Dcosa} + C_T \\
C_z & = -C_{Lcosa} - C_{DSina}
\end{align*}
\]

Into (3) aerodynamic coefficients are expressed by the following:

\[
\begin{align*}
C_L & = C_{L_0} + C_{L_1} \frac{c}{2V_0} + C_{L_2} \frac{c}{2V_0} + C_{L_3} \delta e \\
C_D & = C_{D_0} + f(C_L) \\
C_m & = C_{m_0} \alpha + C_{m_1} \delta \alpha + C_{m_2} \frac{c}{2V_0} + C_{m_3} \delta e \\
C_T & = C_{Tv} \frac{V - V_0}{V_0} + C_{Th} \delta th \\
C_{Tv} & = \frac{3}{3}C_{L_3} + C_{Tv_1} \frac{V}{\eta_e} (\delta \eta_e)
\end{align*}
\]

Mathematical model has been applied to an UAS studied in previous works \[22\]. It is a scaled model (1:5) of ultra-light aircraft Perceptor N3-PUP.

Equation (5), already used in cited previous studies, has been used to model the aircraft polar as follows:

\[
C_D = C_{D_0} + 0.001625C_L^3 + 0.30061C_L^2 + 0.007446C_L
\]

Table 1 shows the geometric characteristics of the studied aircraft.
Table 1. UAS geometric characteristics.

<table>
<thead>
<tr>
<th>Characteristic</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wing mean chord (c)</td>
<td>0.24 m</td>
</tr>
<tr>
<td>Wing span (b)</td>
<td>1.86 m</td>
</tr>
<tr>
<td>Wing area (S)</td>
<td>0.4464 m²</td>
</tr>
<tr>
<td>Mass (W/g)</td>
<td>2.5 kg</td>
</tr>
<tr>
<td>Tail mean chord (c_t)</td>
<td>0.185 m</td>
</tr>
<tr>
<td>Tail span (b_t)</td>
<td>0.44 m</td>
</tr>
<tr>
<td>Tail area (S_t)</td>
<td>0.081 m²</td>
</tr>
</tbody>
</table>

3. Study of Actual Horizontal Tail

The horizontal tail consists of a NACA 0012 airfoil and features a hinged elevator at 60% of the mean chord (Figure 1).

Figure 1. Tail airfoil without (blue) and with (red) elevator deflection.

In order to study the airfoil morphing in the horizontal tail and then compare the original aircraft with the morphed one, it is necessary to define a trim condition. As this is a preliminary feasibility study to analyze the merits of morphing technologies, it will only deal with the equilibrium condition of the aircraft. The weight and lift coefficients at equilibrium have already been obtained in the previous paper [22], defined the equilibrium speed in steady rectilinear flight equal to 24.6305 m/s at sea level ($Re = 313,000$). The following system of trim equations is then set up in order to derive the angle of attack and deflection of the elevator.

\[
\begin{align*}
C_L &= C_{L_0} \alpha + C_{L_\delta} \delta_e \\
C_m &= C_{m_0} + C_{m_\alpha} \alpha + C_{m_\delta} \delta_e \\
\alpha_{eq} &= 3.066^\circ \\
\delta_{eq} &= -12^\circ
\end{align*}
\]

(6) (7)

Calculated the deflection angle of the elevator at trim condition, its aerodynamic characteristics are analyzed by plotting the polars obtained through the XFOIL release 6.99 software.
The polars of the NACA 0012 airfoil and the modified NACA 0012 with elevator deflection of $-12$ deg are shown in Figures 2 and 3, Table 2 shows the aerodynamic coefficients of both airfoils.

![Figure 2](image1.png)

**Figure 2.** $C_L$ vs. $\alpha$ curve for airfoil with (red) or without (blue) elevator deflection.

![Figure 3](image2.png)

**Figure 3.** $C_L$ vs. $C_D$ curve for airfoil with (red) or without (blue) elevator deflection.

<table>
<thead>
<tr>
<th>Airfoil</th>
<th>$\alpha_{\text{max}}$</th>
<th>Value</th>
<th>$C_{L_{\alpha}}$</th>
<th>$C_{D_0}$</th>
<th>$C_{L_{\text{max}}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>NACA 0012</td>
<td>0.09665</td>
<td>0.00755</td>
<td>1.1707</td>
<td></td>
<td>13.5</td>
</tr>
<tr>
<td>NACA 0012 + $\delta_{\text{eq}}$</td>
<td>0.112</td>
<td>0.01388</td>
<td>0.785</td>
<td></td>
<td>17.5</td>
</tr>
</tbody>
</table>

### 4. Study of Morphing Horizontal Tail

To reach the research object, the morphing airfoil should exactly replicate the effect of the elevator with trim deflection. The first condition to be respected is that the airfoil in question must have the same $C_{L_{\alpha}}$ value as the NACA 0012 with the elevator at $-12^\circ$, so for the same angle of attack it must produce the same lift as the airfoil with elevator.
This way, we can evaluate the tail morphing influence on aircraft dynamics without considering other parameters, such as angle of attack or speed variations.

Furthermore, for the two $C_{L_{\alpha}}$ curves to overlap perfectly, a certain tail incidence angle must be considered for the morphing airfoil.

As already mentioned, the morphing technology considered is the morphing of the airfoil camber during the flight.

For the preliminary study in the trim condition, we will look for the camber value and the maximum camber point along the mean chord that the airfoil must replicate for the effect of the deflected elevator at equilibrium. To do this, an experimental function can be found that binds the $C_{L_{\alpha}}$ and the camber of the airfoil; in this way, starting from the $C_{L_{\alpha}}$ of NACA 0012 with $\delta_{eq}$, it will be possible to calculate the camber value of the morphing airfoil.

Three points of maximum camber $X_{c_{max}}$ along the HT mean chord ($c$) were considered, namely, at 0.4$c$, 0.5$c$ and 0.6$c$. Using the XFOIL software, the polar of the airfoils with thickness $t$ equal to 0.12$c$ and camber from $-0.04c$ to $0.04c$ for the three maximum camber points were obtained. Subsequently, the $C_{L_{\alpha}}$ values for each camber were calculated for the three $X_{c_{max}}$ and, plotting the results, the three curves shown in Figures 4–6 were extracted.

![Figure 4. Variation of $C_{L_{\alpha}}$ with camber at $X_{c_{max}} = 0.4$.](image)

![Figure 5. Variation of $C_{L_{\alpha}}$ with camber at $X_{c_{max}} = 0.5$.](image)
The $C_{L_\alpha}$ trend has been transposed in a polynomial through polyfit techniques. To improve the precision of the function, a value of $n$ equal to 12 has been chosen, so the coefficients of the polynomial $p$ for each of the three curves will be $12 + 1$. The form of the polynomial equation is reported below.

$$p(x) = p_1 x^n + p_2 x^{n-1} + \ldots + p_n x + p_{n+1}$$

(8)

Consequently, the functions of the three curves, which link the $C_{L_\alpha}$ with the camber $c$ at the same $X_{c_{max}}$, can be written.

By replacing the $C_{L_\alpha}$ value of NACA 0012 with $\delta_{e_{eq}}$ in the equations, the corresponding camber values are obtained for the three maximum camber points. Obtained results are reported in Table 3.

**Table 3. Camber VS Max camber point.**

<table>
<thead>
<tr>
<th>Camber</th>
<th>$X_{c_{max}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>-0.0071</td>
<td>0.4</td>
</tr>
<tr>
<td>-0.00673</td>
<td>0.5</td>
</tr>
<tr>
<td>-0.00628</td>
<td>0.6</td>
</tr>
</tbody>
</table>

In Figure 7, $C_L$ vs. $\alpha$ curves for NACA 0012 (blue), NACA 0012 with elevator trim deflection (red), morphed airfoil with maximum camber at 0.4c (yellow), at 0.5c (violet) and 0.6c (green) are shown. The obtained results for morphed airfoils are much more similar to original profile than the one with elevator deflection. To reach the object of our valuation, it is necessary to consider a tail incidence angle to ensure that the morphing profiles perfectly replicate the lift contribution of the profile with elevator.

A tail incidence angle $i_{HT}$ equal to $-8.35$ deg was calculated, and, by applying this modification to the airfoils, the polars were obtained.

Now, as shown in Figure 8, the $C_L$ vs. $\alpha$ curves of NACA 0012 with $\delta_{e_{eq}}$ and of the three morphing profiles overlap.

The first important obtained result (Figure 9) is that, even if the slope of the curve is the same, morphing profiles allow to reach to higher $C_L$ for the same value of $C_D$ respect to profile with elevator. Their results are comparable with NACA 0012 airfoil without mobile surface.
It is specified that, although in the graph the curves do not coincide perfectly, they have the same $C_{L_\alpha}$ value and that their not perfectly straight trend is due to the fact that they have been obtained through experimental data.

**Figure 7.** $C_L$ vs. $\alpha$ curve of NACA 0012, NACA 0012 + $\delta_{e_\text{eq}}$ and the three morphing airfoils.

**Figure 8.** $C_L$ vs. $\alpha$ curve of NACA 0012, NACA 0012 + $\delta_{e_\text{eq}}$ and the three morphing airfoils with $i_{HT}$. 
Figure 9. $C_L$ vs. $C_D$ curve of NACA 0012, NACA 0012 + $\delta_{eq}$ and the three morphing airfoils with $i_{HT}$.

Besides, as it is possible to note by Figure 10, the same drag coefficient has been obtained for the higher values of the angle of attack.

Figure 10. $C_D$ vs. $\alpha$ curve of NACA 0012, NACA 0012 + $\delta_{eq}$ and the three morphing airfoils with $i_{HT}$.

In Figure 11, the aerodynamic efficiency’s ($E$) trend, as the $C_L$ variation, is reported. It shows how morphing airfoil characteristics are much more compliant with the NACA 0012 airfoil than the airfoil with elevator.
The trends in the aerodynamic coefficients and a summary table (Table 4) of the main characteristics are shown in order to be able to face a reasoned choice.

Table 4. Aerodynamic main characteristics.

<table>
<thead>
<tr>
<th>Airfoil</th>
<th>$C_{D_0}$</th>
<th>$C_{L_{max}}$</th>
<th>$E_{max}$</th>
<th>$\alpha_{max}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>NACA0012 + $\delta_e$</td>
<td>0.01388</td>
<td>0.785</td>
<td>25.6722</td>
<td>17.5</td>
</tr>
<tr>
<td>Airf 0.4</td>
<td>0.00766</td>
<td>1.12</td>
<td>46.74</td>
<td>21.2</td>
</tr>
<tr>
<td>Airf 0.5</td>
<td>0.00792</td>
<td>1.1353</td>
<td>48.365</td>
<td>22.2</td>
</tr>
<tr>
<td>Airf 0.6</td>
<td>0.00832</td>
<td>1.1355</td>
<td>48.957</td>
<td>22.5</td>
</tr>
</tbody>
</table>

Even just from the analysis of the morphing profiles it is possible to notice a notable improvement compared to the NACA 0012 with $\delta_{eq}$; from Figures 10 and 11, it can be seen that the value of $C_{D_0}$, and of drag in general, is greatly reduced, this means that for the same angle of incidence, the morphing airfoils are able to produce the same lift as the airfoil with elevator deflection but with much less drag production.

Furthermore, there is a great improvement in the values of $E_{max}$, the key index for the evaluation of range and which will be discussed in detail later. In light of the above and taking into account the values shown in the table, it was decided to choose the morphing airfoil with camber equal to $-0.00673$ at $X_{c_{max}} = 0.5$ as it is the right compromise between the improvement in $C_{D_0}$ and in the other aerodynamic coefficients.

Figure 12 shows the NACA 0012 airfoil with $\delta_{eq}$ and the chosen morphing airfoil:
5. Study of Longitudinal Dynamic of the Morphing Tail Aircraft

In the longitudinal dynamics of the aircraft, the horizontal tail plays a central role, as many stability derivatives depend on it, in particular, on its $C_{L\alpha}$ value. The parameters that are influenced by $C_{L\alpha HT}$ are shown below, making this dependence explicit.

\[
C_{L\alpha} = C_{L\alpha w} + C_{L\alpha HT} \left( \frac{S}{S_1} (1 - \frac{d\epsilon}{d\alpha}) \right) \quad (9)
\]

\[
C_{m\alpha} = -C_{L\alpha} MS \quad (10)
\]

\[
C_{L\dot{\alpha}} = 2C_{L\alpha HT} V_H f(\frac{\dot{\epsilon}}{\dot{\alpha}}) \quad (11)
\]

\[
C_{m\dot{\alpha}} = -2C_{L\alpha HT} V_H l_t \frac{\dot{\epsilon}}{\dot{\alpha}} \quad (12)
\]

\[
C_{Lq} = 2 \cdot C_{L\alpha HT} V_H \quad (13)
\]

\[
C_{mq} = -C_{Lq} \frac{l_t}{c} \quad (14)
\]

It was considered that the distance $l_t$ between the aerodynamic center of the horizontal tail and that of the wing remains constant because the displacement of the aerodynamic center of the HT caused by the airfoil morphing is negligible and, moreover, being a model in the scale of 1:5, the distances are so small that a small variation would be inconsistent.

To take into account the morphing, it is considered that, compared to the basic aircraft, the horizontal tail is now made up of the morphing airfoil chosen; that is, the airfoil with a camber equal to $-0.00673 c_{mHT} \pi$ at an $X_{c_{max}}$ of 0.5 $c_{mHT}$ and with a thickness $t$ of 0.12 $c_{mHT}$. Therefore, the $C_{L\alpha}$ of this airfoil will have to be considered to obtain the new $C_{L\alpha HT}$.

To calculate $C_{L\alpha HT}$ starting from airfoil one, the following relationship have been considered:

\[
C_{L\alpha HT} = \frac{C_{L\alpha morph}}{1 + \frac{57.3 c_{mHT}}{\pi A R_{HT}}}.
\]

The obtained stability derivatives are reported in Table 5.

**Table 5. Aerodynamic main characteristics.**

<table>
<thead>
<tr>
<th>$C_{L\alpha}$</th>
<th>$C_{L\dot{\alpha}}$</th>
<th>$C_{Lq}$</th>
<th>$C_{D\alpha}$</th>
<th>$C_{m\alpha}$</th>
<th>$C_{mq}$</th>
<th>$C_{mq}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>3.5582</td>
<td>0.5585</td>
<td>3.4182</td>
<td>0.389</td>
<td>-0.8259</td>
<td>-0.0074</td>
<td>-9.286</td>
</tr>
</tbody>
</table>

Figure 12. NACA 0012 + $\delta_{\text{eq}}$ and morphing airfoil.
In regards to the control derivatives $C_{L\delta e}$ and $C_{M\delta e}$, since the deflection of the elevator has been replaced with the morphing airfoil, they will be equal to the following:

$$C_{L\delta e} = C_{LaHT-morph}$$

$$C_{M\delta e} = -C_{LaHT-morph} \cdot \dot{l}_T$$

Basically, the lift contribution of the elevator given by $C_{L\delta e}$ times the elevator deflection has been replaced by $C_{La}$ of HT with the morphing airfoil times the tail incidence angle. Same thing regarding $C_{m\delta e}$ as follows:

$$C_{L\delta e}\delta e = C_{LaHT-morph}l_T$$

$$C_{M\delta e}\delta e = -C_{LaHT-morph}l_T \cdot \dot{l}_T$$

After calculating the stability derivatives modified due to the morphing of the horizontal tail, the new dynamic matrix is written and the new eigenvalues are obtained as follows:

$$\lambda_{1,2} = -0.0642 \pm 0.0809i$$

$$\lambda_{3,4} = -0.0006 \pm 0.0021i$$

From the longitudinal dynamic analysis of the morphing aircraft, it emerges that its short-period mode is more stable than that of the initial configuration since the stability derivatives on which its damping depends; that is, $C_{L\alpha}$, $C_{mq}$, and $C_{m\dot{\alpha}}$, have been modified by morphing. This is an important result as the short-period is the mode that involves the greatest stresses on the aircraft and must necessarily be stable since, having a high frequency, it could not be controlled. In regards to the phugoid mode, this is not substantially modified like the short-period mode, as its damping depends on stability derivatives that have nothing to do with the influence of the horizontal tail on the aircraft. So, the modification obtained through airfoil morphing technology makes the short-period mode more stable, leaving the phugoid mode more or less unchanged. The following Tables 6 and 7 show the variations in the transient characteristics of the longitudinal proper modes of the morphing aircraft with respect to the basic one.

**Table 6. Short-period mode characteristics.**

<table>
<thead>
<tr>
<th>Aircraft</th>
<th>Re ($\lambda$)</th>
<th>Period (s)</th>
<th>$t_{\text{half}}$ (s)</th>
<th>$N_{\text{half}}$ (cycle)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Basic</td>
<td>$-0.0608$</td>
<td>0.3768</td>
<td>0.055</td>
<td>0.1474</td>
</tr>
<tr>
<td>Morph HT</td>
<td>$-0.0642$</td>
<td>0.3783</td>
<td>0.0526</td>
<td>0.139</td>
</tr>
<tr>
<td>$\Delta$</td>
<td>$-0.0034$</td>
<td>+0.0015</td>
<td>$-0.0029$</td>
<td>$-0.0084$</td>
</tr>
<tr>
<td>$\Delta%$</td>
<td>$-5.6%$</td>
<td>+0.4%</td>
<td>$-5.225%$</td>
<td>$-5.7%$</td>
</tr>
</tbody>
</table>

**Table 7. Phugoid mode characteristics.**

<table>
<thead>
<tr>
<th>Aircraft</th>
<th>Re ($\lambda$)</th>
<th>Period (s)</th>
<th>$t_{\text{half}}$ (s)</th>
<th>$N_{\text{half}}$ (cycle)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Basic</td>
<td>$-0.0006$</td>
<td>13.9117</td>
<td>5.7101</td>
<td>0.4105</td>
</tr>
<tr>
<td>Morph HT</td>
<td>$-0.0006$</td>
<td>13.9117</td>
<td>5.9428</td>
<td>0.4274</td>
</tr>
<tr>
<td>$\Delta$</td>
<td>0</td>
<td>$+0.4341$</td>
<td>$-0.2097$</td>
<td>$+0.0021$</td>
</tr>
<tr>
<td>$\Delta%$</td>
<td>0%</td>
<td>$+3.12%$</td>
<td>3.67%</td>
<td>$+0.51%$</td>
</tr>
</tbody>
</table>

6. Effects of Morphing on Aircraft Performance: Power Required Curves Analysis

The aim of the present and other studies is to study technological innovations for surveillance unmanned, so the goal is to maximize its endurance. We will then look for the condition for which $C_{L^{3/2}}/C_D$ is maximized, this condition corresponds to the maximum endurance. The power required curves of the aircraft with the deflected elevator by the
trim $\delta_e$ and with the morphing airfoil in the HT are plotted at zero altitude, reporting in the curves the point of the minimum power required ($W_n$); that is, the one corresponding to the maximum $C_L^{3/2}/C_D$ and, therefore, to the maximum endurance.

Analyzing Figures 13 and 14, it can be seen that the minimum of the curve is at a lower required power value and at a lower velocity for the morphing aircraft than that of the basic aircraft. That is to say, the basic aircraft can certainly fly at their speed of minimum power to maximize endurance, but with the morphing aircraft a higher maximum endurance value is obtained, as its $C_{D_0}$ is lower and the $C_L^{3/2}/C_D$ is higher. This means that, through morphing technology, at the same altitude, the aircraft is able to fly in trim by spending less energy and, consequently, there is an increase in terms of endurance.

The improvement in $C_L^{3/2}/C_D$ varying $C_L$ is shown in Figure 15.

![Figure 13. Aircraft power required curves (HT with NACA 0012+$\delta_e$) at $z = 0$.](image13)

![Figure 14. Aircraft power required curves (HT with morphing airfoil) at $z = 0$.](image14)
In Table 8, it is reported that the percentage of endurance increase at each considered altitude.

**Table 8.** Improvement in $C_{L}^{3/2}/C_{D}$ and endurance due to morphing.

<table>
<thead>
<tr>
<th>Altitude (m)</th>
<th>$E \sqrt{C_{L}^{3/2}/C_{D}}$ and Endurance Variation (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>500</td>
<td>+2.3</td>
</tr>
<tr>
<td>1000</td>
<td>+2.335</td>
</tr>
<tr>
<td>1500</td>
<td>+2.527</td>
</tr>
<tr>
<td>2000</td>
<td>+2.519</td>
</tr>
<tr>
<td>2500</td>
<td>+2.67</td>
</tr>
</tbody>
</table>

The improvement in the aerodynamic efficiency ($E$) with the variation in $C_{L}$ is shown in Figure 16. As it is easy to note, the efficiency of the aircraft equipped with a morphing tail is much more than the $E$ of the traditional tail one. The mean improvement is about 1.8%.
A range of different altitudes has then been considered (from 0 to 2500 m); above this altitude range, the ambient temperature decreases to values below the optimal operating temperature range of the model battery. Figures 17 and 18 show the power required curves for classical aircraft and morphing aircraft at the following various considered altitudes:

Figure 17. Aircraft power required curves (HT with NACA 0012 + $\delta_{\text{eq}}$) at studied altitudes.

Figure 18. Aircraft power required curves (HT with morphing airfoil) at studied altitudes.

Comparing Figures 17 and 18, it can be seen that the morphing aircraft increase the endurance at all considered altitudes.

Figure 19 shows a detail of Figure 18 focused on trim speed. It can be seen that at the same altitude and $V_e$, the aircraft with the airfoil morphing in the HT needs less power than the aircraft in traditional configuration.

Figure 19. Detail of aircraft power required curves at the studied altitudes.
7. Discussion

In the present work, a feasibility study is conducted to evaluate any potential improvements brought by replacing the conventional elevator of a reference UAV with a morphing horizontal tail.

Firstly, the aircraft model, its dynamics and the equilibrium condition, around which the entire study is based, has been implemented. Starting from the trim deflection of the elevator at equilibrium, through an experimental relationship, we obtained the camber that airfoil morphing must have to exactly replicate the effect of the elevator. At this point, to go back to the three-dimensional that was found for the airfoil, a comparison between the reference and the morphed aircraft has been made by analyzing the dynamic part, with the calculation of the transient characteristics of the longitudinal modes.

The results showed that the application of morphing improves the stability of the aircraft and, in particular, that of the short-period, improving its transient characteristics.

In addition, the following various improvements have been found in performance: starting from the aircraft’s $C_{D_0}$ up to the $C_{L}^{1/2}/C_D$ and aerodynamic efficiency, all aerodynamic parameters have undergone an improvement compared to reference aircraft.

It has been showed that, considering the same trim speed, at each considered altitude, the necessary power required by the morphing aircraft is significantly reduced, whereas the endurance is improved by more than 2.3% at various altitudes. Besides, the efficiency increase of about 1.8% that implies an improvement in aircraft range.

Future studies will be focused on morphing airfoils that produce the same tip deflection as the conventional elevator, as well as investigating the aircraft performance in conditions other than trim. Furthermore, further developments will regard a pull-up maneuver by comparing the achieved results and time between conventional and morphing tails.

Present work represents the first step towards a gust rejection procedure, in fact, airfoil modifications are morphing technologies that allow the change in the camber or the thickness of the wing profile during flight. This approach could be efficiently applied to gust alleviation modifying aerodynamic surfaces to generate an aerodynamic coefficient modification to contrast the wind-induced ones.

The final objective of these studies will be to develop an active system, coupled with the automatic gust identification system in [22], to reject gust effects on the unmanned vehicle performance.

Once the study of morphing tail is completed, the combined morphing wing–tail combinations will be analyzed.

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