Abstract: Elucidation of the propagation velocity of a laser-supported detonation (LSD) wave and its propagation mechanism is necessary for various engineering applications. This study was conducted to observe an oblique laser-supported detonation wave off the laser axis. The relation between the local laser intensity and detonation-wave propagation velocity was investigated. For this purpose, the time-space distribution of the laser intensity was measured precisely. The change of the LSD wavefront shape was visualized using an ultrahigh-speed camera. The relation between the local laser intensity and the propagation velocity of the oblique LSD wave measured off the laser axis was found to be identical to the relation between the local laser intensity and the detonation propagation velocity at the laser axis.

Keywords: atmospheric discharge; laser propulsion; laser supported detonation; oblique detonation

1. Introduction

Laser-induced discharge and its accompanying blast wave has been an interesting subject for aeronautical and astronautical engineering applications [1–4]. When an incident laser intensity exceeds a certain threshold, such as $10^{12}$–$10^{13}$ W/m$^2$, an ionization front propagates with an attached shock wave in a direction opposite to the laser beam irradiation [1]. This phenomenon is known as laser-supported detonation (LSD). However, when the laser intensity is not sufficiently high to induce the LSD wave, a shock wave precedes an ionization wave and propagates separately. This phenomenon is designated laser-supported combustion (LSC). In the LSD regime, because the laser energy is converted efficiently to blast-wave energy, several studies have been conducted to ascertain its energy conversion efficiency [5–7], termination threshold [7–10], and plasma property with plasma diagnostics [11,12].

The relation between the LSD propagation velocity and laser intensity is an important topic for ascertaining the propagation structure of LSD [13,14]. Several propagation models have been proposed. Raizer deduced the analytical propagation velocity using hydrodynamic equation, which is an analog to Chapman–Jouguet (C–J) detonation. The velocity is proportional to the cubic root of the laser intensity, irrespective of the gaseous species [15]. Additionally, Raizer discussed another model by which ultraviolet radiation from bulk plasma generates seed electrons ahead of the ionization front via the photoionization effect. The precursor, consisting of photoelectrons, plays a role of initiating laser absorption [15].

To validate the propagation model and to elucidate the LSD mechanism, comparison with experimental data is necessary. As presented in Figure 1, however, depending on the study, the relations between propagation velocity and laser intensity mutually differ
The difference in propagation velocity trends is regarded as attributable to the two-dimensional effects of focusing optics, such as the beam quality factor, beam waist, and f-number. These parameters determine the plasma size and affect the lateral enthalpy dissipation, which in turn affects the propagation velocity and termination condition [15]. This two-dimensional effect has been observed by experimentation in several studies. Mori et al. investigated f-number effects on the termination condition and expressed the laser intensity of the termination as a function of the f-number [6]. Ushio et al. observed line-focused LSD with and without confinement to compare the effects of lateral expansion. Results showed that the propagation velocity with confinement was higher than that without confinement [7]. To eliminate two-dimensional effects, Matsui et al. used focusing optics with sufficiently large beam diameters and f-numbers. With focusing optics, the velocity is determined uniquely by the laser intensity [20]. Shimano et al. reported gas-species effects on the propagation velocity with sufficiently large beam diameters. The velocities in argon, helium, and air have mutually differing tendencies in terms of laser intensity [21].

![Figure 1. Earlier studies of relations between laser intensity and propagation velocity [7,10,16–19]. All experiments were conducted in air. Because of different focusing optics, the velocity is not determined uniquely by laser intensity.](image)

As described above, the propagation velocity dependence on laser intensity is necessary for validation using the calculation model. However, some studies have relied on evaluation using the average laser intensity, whereas others have relied on evaluation using the peak laser intensity. Figure 2 portrays a typical image of the ionization front of the LSD wave. The wavefront forms a bow shape, which suggests that the spatial distribution of laser intensity affects the formation of the structure. An earlier study by the authors [20] evaluated the propagation velocity with a large beam diameter and f-number with the averaged laser intensity. For this study, we investigated the dependence of local propagation velocity on local laser intensity by considering the laser intensity profile. Also, we evaluated the local propagation velocity as the velocity in the direction normal to the wavefront, similarly to analysis of oblique detonation of chemical explosives. Oblique detonation is observed around a hypersonic projectile in a detonative gas [22,23]. The propagation velocity of oblique detonation is found using the C–J velocity. The wavefront angle is expressed as the ratio of the C–J velocity to the projectile velocity. After calculating the wavefront angle as taken by a high-speed camera with high resolution, we used the laser intensity profile to elucidate the relation between the local propagation velocity of oblique laser-supported detonation and the local laser intensity.
Figure 2. Typical image of a bow-shaped ionization front. The oblique propagation velocity is calculated from $V$ and the angle of the ionization wave front.

2. Measurement of the Laser Intensity Distribution

A laser-induced discharge is produced using a Transversely Excited Atmospheric (TEA) CO$_2$ laser with typical maximum pulse energy and wavelength of 10 J/pulse and 10.6 μm, respectively. The laser energy deviation was ±5% before and after the experiment. The laser power profile is measured with a photon-drag detector (B749, Hamamatsu photonics). The FWHM of the spike of the profile was 0.12 ± 0.02 μs. The historical profile of power and cumulative energy is depicted in Figure 3. The laser beam cross-section before focusing was a 30 mm × 30 mm rectangular shape, with spatial intensity profiles of Gaussian in the horizontal direction and top-hat in the vertical direction. The direction for which the laser intensity profile of Gaussian is defined as $r_1$, as depicted in Figure 3; that of top-hat is $r_2$. Also, $W_{G0}$ and $W_{T0}$, respectively, stand for beam radii at the beam waist of Gaussian and the top-hat distribution. They are defined, respectively, as half-lengths of the region that includes 86% of the total beam power in each plane. The laser intensity has a non-axisymmetric distribution. This characteristic leads to the difference between the spot sizes at the beam waist of both directions. The equivalent beam diameter $D$ is defined as shown below.

Figure 3. Historical profile of laser power and cumulative energy of the CO$_2$ laser, with the burn pattern of the laser before focusing.
As portrayed in Figure 4, the laser beam is focused onto an aluminum plate to initiate breakdown by ZnSe lenses ($f = 127$ mm and $317.5$ mm) or parabolic mirrors ($f = 400$ mm and $500$ mm) for which the beam diameters at focus are, respectively, $1.2$ mm ($W_{G0} = 0.4$ mm, $W_{T0} = 0.6$ mm), $2.9$ mm ($W_{G0} = 1.1$ mm, $W_{T0} = 1.6$ mm) and $4.1$ mm ($W_{G0} = 1.7$ mm, $W_{T0} = 2.0$ mm). Table 1 shows the focal length, F-number, beam radii at the beam waist, and the equivalent beam diameter of each focusing optics. Figure 5 shows the measured and fitted intensity profiles with $D = 4.1$ mm in the $r_1$ and $r_2$ directions for which the profiles are Gaussian and top-hat. The beam quality factors are found by measuring the intensity profile near the beam waist by ISO 11146 [24]. The beam quality factors are $15$ and $21$, respectively, in the $r_1$ and $r_2$ directions. Relation between beam radius in $r_2$ direction and distance from beam waist of each focusing optics is shown in Figure 6.

![Figure 4](image_url)

**Figure 4.** Schematics showing the experiment setup. (a) Focusing optics of $D = 4.1$ mm, which consist of two mirrors with focal lengths of $500$ mm in $r_1$ and $400$ mm in $r_2$ direction. (b) Focusing optics of $D = 2.9$ mm and $D = 1.2$ mm, with respective focal lengths of $317.5$ mm and $127$ mm.

| Table 1. Properties of focusing optics and beam diameter. |
|-----------------|--------|--------|--------|--------|--------|
| Property        | $r_1$  | $r_2$  | $r_1$  | $r_2$  | $r_1$  | $r_2$  |
| $f$ [mm]        | 500    | 400    | 317.5  | 127    |        |        |
| $F$             | 16.7   | 13.3   | 10.6   | 4.2    |        |        |
| $W_{G0}$ [mm]   | 1.7    | 1.1    | 0.4    |        |        |        |
| $W_{T0}$ [mm]   | 2.0    | 1.6    | 0.6    |        |        |        |
| $D$ [mm]        | 4.1    | 2.9    | 1.2    |        |        |        |
Figure 5. Measured and fitted laser intensity profiles at the beam waist with \( D = 4.1 \) mm in the \( r_1 \) and \( r_2 \) directions, with Gaussian and top-hat profiles. \( W_{G0} \) and \( W_{T0} \) are beam radii at the beam waist.

![Figure 5](Image)

**3. Propagation Velocity of Laser-Supported Detonation along the Laser Axis**

The ionization wave image was taken using a high-speed ICCD camera (512 x 512 pixel resolution, 10 ns minimum exposure time, Ultra8; DRS Hadland Ltd., Hertfordshire, UK), which can take eight images sequentially in each laser shot. To measure the propagation velocity in the direction normal to the wavefront, we used another high-speed camera (pixel resolution: 2560 x 2160, 3 ns minimum exposure time, iStar sCMOS; Andor Technology, Belfast, UK) because the wavefront shape must be captured with as high a resolution as possible. The exposure time was set to 10 ns in Ultra 8 and to 5 ns in iStar sCMOS. The shutter timing and laser pulse signal are synchronized using a pulse delay generator.

![Figure 6](Image)

**Figure 6.** Relation between beam radius in \( r_2 \) direction and distance from beam waist of each focusing optics. Typical LSD propagation limits for beam diameters are displayed as broken lines. The detonation wave propagates from left to right in this figure.
The laser-induced plasma is projected to the camera via two lenses. Spatial resolution is 0.009 mm/pixel. All experiments were conducted in air at 1 atm pressure. Figure 7 presents the relation between the propagation velocity of an ionization front $V$ and laser intensity $S_{peak}$ at the laser axis with various beam diameters. The propagation velocity was calculated from eight images per laser shot, and the plot was drawn by performing the experiment five times. Error bars indicate the standard error of the five data. With $D \geq 2.9$ mm, the propagation velocity shows a unique tendency in terms of laser intensity, which is the same as earlier results. The beam diameter was measured more accurately than in previous studies conducted by the authors [21]. Also, the laser intensity is evaluated as the local laser intensity at the laser axis, with $D = 1.2$ mm. However, the propagation velocity trend differs from that of $D \geq 2.9$ mm. Therefore, with $D = 1.2$ mm, the result suggests that two-dimensional energy dissipation affects the propagation velocity. The measured value is fitted using a power function. The results are $V = 2.2 \times 10^{-1} S^{0.46}$ and $V = 3.9 \times 10^{-2} S^{0.65}$, respectively, with $D \geq 2.9$ mm and $D = 1.2$ mm. Although this experiment is conducted in air as described above, evaluation using the Mach number is important for comparison with other gas species. Therefore, we normalized the propagation velocity by the speed of sound $a$ as shown below.

$$\bar{V} = \frac{V}{a}$$  \hspace{1cm} (2)

The laser intensity is normalized using the Chapman–Jouguet velocity [15].

$$V = \left\{2(y_2^2 - 1) \frac{S}{\rho_1}\right\}^{\frac{1}{3}}$$ \hspace{1cm} (3)

In that equation, $y_2$ and $\rho_1$, respectively, represent the specific heat ratio behind the wavefront and the atmospheric density. The Mach number is obtained by dividing Equation (3) by the speed of sound.

$$\frac{V}{a} = \left\{2(y_2^2 - 1) \frac{S}{\rho_1 a^3}\right\}^{\frac{1}{3}}$$ \hspace{1cm} (4)

Here, the Mach number is a function of laser intensity. We defined normalized laser intensity $\bar{S}$ as

$$\bar{S} = \frac{S}{\rho_1 a^3}$$ \hspace{1cm} (5)
Figure 7. Dependence of propagation of an ionization front with various beam diameters on laser intensity at the laser axis. All experiments were conducted in air at a pressure of 1 atm. Trends against laser intensity differ between $D \geq 2.9$ mm and $D = 1.2$ mm. Fitted lines with power function are shown as line 1 and line 2.

The speed of sound and atmospheric density are 347 m/s and 1.18 kg/m³, respectively, in the atmospheric conditions of 1 atm and 300 K. The functions for line 1 and line 2 are normalized and expressed using Equations (2) and (5) as shown below.

$$V = 1.6 \times 10^{-1} S^{0.46}$$  \hspace{1cm} (6)

$$\overline{V} = 1.4 \times 10^{-2} S^{0.65}$$ \hspace{1cm} (7)

These fitted lines are depicted as line 1 and line 2 in Figure 7. The obtained relations are used in the next chapter for analysis of oblique detonation.

4. Propagation Velocity of Oblique Laser-Supported Detonation

Figure 8 presents photographs of propagating ionization fronts in the $r_1$ direction with 2.9 mm beam diameter and the historical profiles of the laser intensity distribution and wavefront shapes. The wavefront shape presented in Figure 8b with solid lines is deduced by detecting the wavefront shape from images taken by iStar sCMOS presented in Figure 8a. The wave head positions are aligned at $z = 0$ mm in Figure 8b. To calculate the local propagation velocity in a direction normal to wavefront $V \cos \theta$, the velocity in the direction of the laser axis is given as Equations (6) and (7). The wavefront angle is deduced by differentiating a polynomial fitted curve obtained from the wavefront shape presented in Figure 8b. Because the time variation of the wavefront shape is negligible compared to the propagation velocity, the propagation velocity along the laser axis for each $r$ is unique at a certain time. To elucidate the propagation velocity dependence on the laser intensity, we evaluated the local intensity as $S(r) \cos \theta$ because the cross section of the laser beam projected onto the oblique wavefront is enlarged by $1/\cos \theta$ and because the local laser intensity is reduced by a factor of $\cos \theta$. From these profiles of the laser intensity distribution and the wavefront shapes, relations between local propagation velocity in the direction normal to the wavefront and local laser beam intensity are deduced as shown in Figure 9. Figure 9a,b show propagation velocities in the $r_1$ and $r_2$ directions. Their respective laser intensity profiles are Gaussian and top-hat distribution, as shown in Figure 5. The propagation velocity is shown for $\cos \theta$ from 0.6 to 1. To investigate the condition of LSD termination, we took schlieren images in which a shock front and an
ionization front are projected simultaneously, as in Figure 10, which presents a typical Schlieren image of LSD with \( D = 4.1 \text{ mm} \) in the \( \rho_1 \) direction. As \( r/W \) increases, the region in which a shock front is separated from an ionization front, which is in the LSC state, is enlarged. By analyzing the separation points, the state of LSD is shown as a filled plot. The state of LSC is shown as an open plot. In Figure 9, the result shows unique trends of local laser intensity, irrespective of the wavefront angle in both directions. Although the result of \( D = 1.2 \text{ mm} \) shows the same tendency as that of the velocity in the direction of the laser axis, the velocity of \( D \geq 2.9 \text{ mm} \) is higher than that within a region below 500 GW/m\(^2\). In this region, the function of the fitting curve is given as shown below.

\[
\bar{V} = 3.3 \times 10^{-1} S^{0.30} \tag{8}
\]

This function, which is defined as line 3, is presented in Figure 11 along with the results of the local propagation velocity presented in Figure 9a. The exponent of the function is similar to that of C–J velocity, as shown Equation (3). The variation of the exponents in each region suggests that the propagation structure transitions at a certain intensity, which is also observed in argon [25]. Figure 12 presents the velocity in the direction of the laser axis with three lines. The velocity of \( D \geq 2.9 \text{ mm} \) shows the same tendency as that of line three within the error bars. This result indicates that propagation velocities of the LSD wave in the direction of the laser axis and that of oblique laser-supported detonation off the laser axis can be described as the same functions of \( S(r) \cos \theta \). For future works, a physical reason of the unique tendency of the velocity with \( D \geq 2.9 \text{ mm} \) and the velocity of the oblique detonation should be clarified with a 2D numerical calculation that contains the complex plasma dynamics.
Figure 8. (a) Photograph of an ionization front propagating from $t = 0.675 \, \mu\text{s}$ to $1.835 \, \mu\text{s}$ with $D = 2.9 \, \text{mm}$ in the $r_1$ direction. Laser is irradiated from upper side of photographs. (b) Historical change of wavefront shape analyzed from Figure 4a and estimated laser intensity profile with $D = 2.9 \, \text{mm}$ in the $r_1$ direction. The elapsed time from starting points of laser irradiation is shown.
Figure 9. Relation between local propagation velocity in a direction normal to the wavefront and local laser intensity of each beam diameter. Closed and opened plots, respectively, show LSD and LSC conditions: (a) $r_1$ direction (Gaussian profile), (b) $r_2$ direction (top-hat profile).

Figure 10. Schlieren image of LSD of $r_1$ direction with $D = 4.1$ mm. The shock front is separated from the ionization front at large $r/W_{G0}$.
Figure 11. Relation between local propagation velocity in the direction normal to the wavefront and local laser intensity of each beam diameter in the $r_1$ direction. In a region below 500 GW/m² of $D \geq 2.9$ mm, the velocity is larger than that of the laser axis. It shows a tendency as Line 3.

Figure 12. Relation between propagation velocity and laser intensity at the laser axis. Line 3 is obtained from analysis of the local propagation velocity. It shows the same tendency as the velocity in the direction of the laser axis.

5. Conclusions

The propagation velocity at the laser axis was measured using beam diameters of 4.1 mm, 2.9 mm, and 1.2 mm. That of $D \geq 2.9$ mm showed a unique tendency for peak laser intensity. By analyzing the wavefront shape, the relation between the local propagation velocity in the direction normal to the wavefront and the local laser intensity $S(r)\cos \theta$ were deduced. The local propagation velocity showed a unique tendency on $S(r)\cos \theta$, irrespective of the wavefront angle. Compared to the tendency obtained from the analysis of local propagation velocity with the velocity at the laser axis, good agreement was found. This result suggests the velocity of the oblique laser-supported detonation off the laser axis can be described as the same function, with the propagation velocity of the LSD wave in the direction of the laser axis.
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Nomenclature

\[ \begin{align*}
  a &= \text{Speed of sound, m/s} \\
  D &= \text{Equivalent beam diameter, mm} \\
  f &= \text{Focal length, mm} \\
  F &= \text{F-number} \\
  M^2 &= \text{Beam quality factor} \\
  S(r) &= \text{Local laser intensity, W/m}^2 \\
  S_{\text{peak}} &= \text{Laser intensity on the beam axis, W/m}^2 \\
  \bar{S} &= \text{Normalized laser intensity} \\
  t &= \text{Elapsed time after laser breakdown, s} \\
  r, z &= \text{Cylindrical coordinates, m} \\
  \rho_1 &= \text{Direction of Gaussian intensity profile} \\
  \rho_2 &= \text{Direction of top-hat intensity profile} \\
  V &= \text{Propagation velocity, m/s} \\
  \bar{V} &= \text{Normalized propagation velocity} \\
  W_{\text{c0}} &= \text{Beam waist size of } \rho_1 \text{ direction, m} \\
  W_{\text{t0}} &= \text{Beam waist size of } \rho_2 \text{ direction, m} \\
  \theta &= \text{Angle of a wavefront, rad} \\
  \gamma_2 &= \text{Specific heat ratio behind shock wave}
\end{align*} \]

References


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