A New Framework for Winter Wheat Yield Prediction Integrating Deep Learning and Bayesian Optimization

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Abstract: Early prediction of winter wheat yield at the regional scale is essential for food policy making and food security, especially in the context of population growth and climate change. Agricultural big data and artificial intelligence (AI) are key technologies for smart agriculture, bringing cost-effective solutions to the agricultural sector. Deep learning-based crop yield forecast has currently emerged as one of the key methods for guiding agricultural production. In this study, we proposed a Bayesian optimization-based long- and short-term memory model (BO-LSTM) to construct a multi-source data fusion-driven crop growth feature extraction algorithm for winter wheat yield prediction. The yield prediction performance of BO-LSTM, support vector machine (SVM), and least absolute shrinkage and selection operator (Lasso) was then compared with multi-source data as input variables. The results showed that effective deep learning hyperparameter optimization is made possible by Bayesian optimization. The BO-LSTM (RMSE = 177.84 kg/ha, $R^2 = 0.82$) model had the highest accuracy of yield prediction with the input combination of “GPP + Climate + LAI + VIs”. BO-LSTM and SVM (RMSE = 185.7 kg/ha, $R^2 = 0.80$) methods outperformed linear regression Lasso (RMSE = 214.5 kg/ha, $R^2 = 0.76$) for winter wheat yield estimation. There were also differences between machine learning and deep learning, BO-LSTM outperformed SVM, indicating that the BO-LSTM model was more effective at capturing data correlations. In order to further verify the robustness of the BO-LSTM method, we explored the performance estimation performance of BO-LSTM in different regions. The results demonstrated that the BO-LSTM model could obtain higher estimation accuracy in regions with concentrated distribution of winter wheat cultivation and less influence of human factors. The approach used in this study can be expected to forecast crop yields, both in regions with a deficit of data and globally; it can also simply and effectively forecast winter wheat yields in a timely way utilizing publicly available multi-source data.

Keywords: yield prediction; deep learning; BO-LSTM; remote sensing; meteorological data

1. Introduction

Wheat is one of the top three crops in the world and is an important source of calories, protein, and many micronutrients for humans [1,2]. However, there are many constraints in production that pose serious threats to the stable and high yield potential of wheat, for example, increased temperature, increased precipitation variability, and frequent extreme events [3,4]. Therefore, early prediction of crop yield before harvest is of great value for our food security and trade.

Traditional crop yield assessment is carried out through field surveys during the crop growing season or based on previous experience of crop growth conditions, a method that has reliability issues related to sampling and non-sampling errors in data collection and data processing due to small samples and limited human resources to obtain the
required sampling frequency and sample size, and the variability of the climate from year
to year makes traditional yield forecasts inaccurate and unstable [5]. The development
of remote sensing technology has enabled large-scale crop yield prediction. Researchers
have widely used remotely sensed vegetation indices and crop yields to build statistical
regression models for yield estimation. Commonly used vegetation indices (VIs) are
normalized difference vegetation index (NDVI), enhanced vegetation index (EVI), near-
infrared reflectance of vegetation (NIRv), and leaf area index (LAI) [6–8]. Some researchers
have also used the wide dynamic range vegetation index (WDRVI) and solar induced
chlorophyll fluoresence (SIF) to model crop yield estimates [9,10]. Researchers are now
utilizing non-linear models more frequently for yield estimation because crop yield is
intimately tied to external environmental factors; meteorological variables affect crop
growth, development, and final yield in a non-linear manner and often have complicated
relationships [11–14].

Machine learning and deep learning methods are often used to achieve accurate
predictions of various crop yields, especially deep learning, and the application of deep
learning to estimate crop yields has been a popular algorithm among researchers in recent
years. Different deep learning models have so far been used to estimate yield for various
crops, highlighting the importance of deep learning network frameworks. Mainstream
deep learning models include convolutional neural network (CNN) and recurrent neural
network (RNN) [15–18]. CNN models can better handle the spatial autocorrelation of
remote sensing images, but they cannot adequately consider the complex temporal correla-
tion [19]. And RNN is a sort of neural network that primarily models sequence-type data by
taking sequence data as input and using the correlation between sequence data to execute
recursion in the direction of sequence evolution [20]. RNN, however, suffers from gradi-
ent disappearance, gradient explosion, and inadequate long-term memory capacity with
time step iteration. Long short-term memory (LSTM) is an excellent variant of the RNN
model, which not only has the characteristics of the RNN model, but also effectively avoids
the undesirable situations such as gradient explosion and gradient disappearance, etc.
It introduces the “gate” control structure, sets the internal gate mechanism, trains the
weights of the input gate, forget gate and output gate, realizes the automatic screening
and fusion of temporal features, and has better prediction and fitting performance for
data [21,22]. HAIDER et al. [23] showed that the LSTM neural network model has much
higher yield estimation accuracy than RNN. JIANG et al. [24] estimated county-level maize
yields based on an LSTM neural network model using maize growth period as a time
series by combining crop phenology information, meteorological data, and remote sensing
data. The results showed that the LSTM neural network model was able to extract the
implied relationships contained in the data series, achieve accurate county-level crop yield
estimation, and provide robust yield estimation under extreme weather conditions. Huiren
Tian et al. [25] used LSTM to estimate wheat yield with different time steps, evaluating the
comparison with back propagation neural network (BPNN) and support vector machine.
The results of this study indicated that the LSTM model outperformed BPNN and SVM
in estimating crop yield and is robust to climate and site fluctuations. Time series data as
deep learning samples have been extensively studied at this stage [24,26]. Therefore, the
samples used for training deep learning models mainly include remote sensing data and
meteorological data based on multiple fertility periods and long time series, which provide
a basis for further improving the accuracy of yield estimation.

The network structure of deep learning is complex with many hyperparameters, and
many scholars use deep learning algorithms to estimate crop yield by using empirical
methods to determine the values of these hyperparameters. The combination of hyperpa-
rameters is very important to the prediction accuracy effect of neural network models, and
a good combination of hyperparameters can improve the training accuracy of the model
and the generalization ability of the test set. In order to speed up the training of neural
networks, save training cost, and improve network performance, the optimization of LSTM
neural network model hyperparameters using the Bayesian optimization algorithm is
proposed. Commonly used hyperparameter optimization methods include grid search [27], random search, and particle swarm optimization algorithms [28]. The idea of the grid search algorithm is exhaustive search; the search time of this method increases exponentially with the number of parameters. For the case of more hyperparameters, this method faces performance problems. The results obtained by random search vary widely each time, and there is the problem of poor accuracy. The particle swarm optimization calculation is easy to fall into local optimum, resulting in low convergence accuracy. Compared to other optimization algorithms, Bayesian optimization algorithms are able to find better hyperparameters in a shorter time, compared to other optimization algorithms, and are a very effective global optimization algorithm [29–31].

Based on the current status of the recent studies presented above and the limitations, we take winter wheat in Hengshui City as an example. A BO-LSTM neural network model is proposed to predict winter wheat yield using satellite meteorological data on the basis of crop phenology. This study’s aims are the following three objectives: (i) speed up the training of neural networks, save training costs, and improve network performance. (ii) Determine which combinations of input variables are best for winter wheat yield estimation based on the BO-LSTM model. (iii) Compare the predictive performance of machine learning (SVM), deep learning (BO-LSTM), and linear regression (Lasso). Finally, explore what kind of environment our proposed model BO-LSTM is suitable for in order to obtain the most accurate prediction.

2. Materials and Data
2.1. Study Area

The study area is located in Hengshui, Hebei Province, China, between 115°10′–116°34′ E longitude and 37°03′–38°23′ N latitude, covering two municipal districts, one county-level city, and eight counties, as of 2016 (Figure 1). According to the second soil census, the city’s tidal soil subclass covers 430,000 hectares, accounting for 62% of the total land area, which is widely distributed in all counties and urban areas and is the main soil type for agricultural land. The annual precipitation in Hengshui is 5.66 billion cubic metres, with an average precipitation of 642.1 mm. It belongs to the continental monsoon climate zone, which is warm and semi-arid, and the main types of crops it grows are wheat, corn, sorghum, etc. By 2021, the sown area of grain in Hengshui reached 7191.33 km², of which 3333.3 km² is occupied by winter wheat, accounting for about 1/2 of the sown area of grain in Hengshui. With a total yield of 4.34 billion kg, so the yield of winter wheat has a key influence on the economic development of Hengshui. This study was conducted on winter wheat, which is generally sown in early October and matures in mid-to-late June of the following year in Hengshui. The phenological period of winter wheat is mainly divided into six stages, sowing (early October), tillering (late-November to mid-December), reviving stage (late-February–mid-March), jointing (mid-March–mid-April), tasseling (late-April–mid-May), and mature milking (late-May–mid-June) [32,33].

2.2. Winter Wheat Yield and Planting Distribution

The historical county-level winter wheat yield data record of Hengshui City came from the 2005–2019 statistical yearbook sharing platform, recording yield data (unit: kg/ha). In Hengshui City, there are two municipal districts and one county-level city; there are 11 counties, since we all consider these to be county-level levels. Spatial distribution data of winter wheat in Hengshui at 250 m spatial resolution from 2005–2019 were provided by Chinese Academy of Agricultural Sciences [34]. The extraction results were evaluated in terms of area quantity and spatial location, and the average relative error of area quantity compared with the statistical yearbook for 20 years was 16.1%. In terms of spatial location, the extraction results of 2015 were verified by selecting sample points in Google Earth high-resolution historical images, and the overall accuracy was 86.8% with a kappa coefficient of 0.69. The results indicated that the winter wheat distribution data had a high extraction accuracy.
2.2. Winter Wheat Yield and Planting Distribution

In this study, we collected from TerraClimate datasets a dataset of high spatial resolution (1/24°, ~4 km) monthly climate and climatic water balance for global terrestrial surfaces from 1958–2015 [37]. TerraClimate uses climate-assisted interpolation to combine high spatial resolution climate normals from the WorldClim dataset with coarser resolution time-varying (i.e., monthly) data from other sources to generate monthly datasets of precipitation, maximum and minimum temperatures, wind speed, vapour pressure, and solar radiation. This dataset has been widely used by many scholars to calculate various drought indices to assess the effects of drought on vegetation physiological activity and yield [38–41]. The main climate variables chosen for this paper include precipitation (pr), maximum temperature (tmmx), downgradient surface shortwave radiation (srad), and the Palmer drought index (Pdsi).

2.3. Remote Sensing Data

The NASA Terra MODIS vegetation index (VI) products (MOD13Q1, Version 6.1) provide consistent spatial and temporal time series comparisons of global vegetation conditions that can be used to monitor the Earth’s terrestrial photosynthetic vegetation activity in support of phenologic, change detection, and biophysical interpretations. In this study, NDVI and EVI data from the NASA-produced MOD13Q1 dataset with a temporal resolution of 16 days and a spatial resolution of 250 m were used. The MOD15A2H product provides a terrestrial LAI at 500 m resolution every 8 days, and it has been available since 2000 and allows analysis of LAI time series data over multiple growing seasons over long periods of time.

2.4. Gross Primary Productivity

Gross primary productivity (GPP) is the amount of organic carbon fixed by photosynthesis per unit time by organisms, mainly green plants. MOD17A2H offers GPP products as 8-day, 500 m resolution composite products. This data product uses MODIS land cover data, leaf area index, photosynthetically active radiation fraction, and meteorological data from DAO and is fed into a light energy utilisation model. It is important for crop yield estimation, global carbon, and carbon trade [35,36].

2.5. Meteorological Data

In this study, we collected from TerraClimate datasets a dataset of high spatial resolution (1/24°, ~4 km) monthly climate and climatic water balance for global terrestrial surfaces from 1958–2015 [37]. TerraClimate uses climate-assisted interpolation to combine high spatial resolution climate normals from the WorldClim dataset with coarser resolution time-varying (i.e., monthly) data from other sources to generate monthly datasets of precipitation, maximum and minimum temperatures, wind speed, vapour pressure, and solar radiation. This dataset has been widely used by many scholars to calculate various drought indices to assess the effects of drought on vegetation physiological activity and yield [38–41]. The main climate variables chosen for this paper include precipitation (pr), maximum temperature (tmmx), downgradient surface shortwave radiation (srad), and the Palmer drought index (Pdsi).

2.6. Data Preprocessing

Based on the spatial resolution of winter wheat planting area in Hengshui City being 250 m, in order to maintain the consistent spatiotemporal resolution of all data, we resampled satellite vegetation index, GPP, and meteorological data to 250 m and one-month intervals. Satellite and meteorological data were masked using the distribution of winter wheat cultivation from 2005 to 2019, and all variables of the county-wide monthly average

Figure 1. Location of the study area.
were summarized. All data are pre-processed on the Google Earth Engine (GEE) platform, a free geoprocessing service launched by Google, which provides a large number of geoprocessing algorithms and massive image datasets based on the Google Cloud Platform, and the summary of data is performed on Python and Excel.

3. Methodology

3.1. Long Short-Term Memory

The LSTM network was proposed by Hochreiter et al. [42] in 1997 based on an extension of RNN, which is mainly used to solve the problems that exist in traditional RNN, both gradient disappearance and explosion. The most fundamental difference between RNN and LSTM is that the hidden layer of the LSTM network is a gated unit, where information is added and removed through a ‘gate’ structure that learns which information to keep or forget during training. The LSTM has three types of gate structures: forgetting gates, input gates, and output gates (Figure 2a).

![Figure 2a](image)

**Figure 2.** (a) The structure of the LSTM neural network; (b) Structure of the phenology-based LSTM model.

The forgetting gate will decide which information should be forgotten from the neural network unit states, which is implemented by a sigmoid function. The gate is determined by the previous output, \( H_{t-1} \), and the new input, \( X_t \), to determine which information was...
removed from the previous cell state, $C_{t-1}$. The output is a number between 0 and 1, where 0 means that the information is completely discarded, and 1 means that the information is completely retained, and is calculated as in Equation (1):

$$f_t = \sigma \left( W_f [X_t, H_{t-1}] + b_f \right)$$  \hspace{1cm} (1)

where $\sigma$ is the sigmoid function, $f_t$ is the forgetting gate, $H_{t-1}$ denotes the output of the previous node, $X_t$ denotes the current input, $W_f$ is the forgetting gate weight, and $b_f$ is the forgetting gate bias.

The input gate determines which information should be stored from the neural network unit states. Implementing this requires two steps: first the sigmoid layer generates the activation value, $i_t$, for the input gate based on $H_{t-1}$ and $X_t$. The tanh function creates a candidate vector state, $c'_t$, which is the alternative to be used for the update, calculated as in (2) and (3):

$$i_t = \sigma (W_i [X_t, H_{t-1}] + b_i) \hspace{1cm} (2)$$

$$c'_t = \tanh (W_c [X_t, H_{t-1}] + b_c) \hspace{1cm} (3)$$

where $i_t$ denotes the input gate output, $c'_t$ denotes the current candidate node state, $W_i$ and $W_c$ denote the weights of the input gate and the input candidate unit, respectively, and $b_i$ and $b_c$ denote the bias of the input gate and the input candidate unit, respectively. The old cell state, $C_{t-1}$, is updated to the new cell state, $C_t$, using the results obtained from the first two orders, calculated as in (4):

$$C_t = f_t \cdot C_{t-1} + i_t \cdot c'_t \hspace{1cm} (4)$$

Finally there is the output gate, which determines which information in the cell state will be taken as the output of the current state. The sigmoid layer is first run, which determines which cell states are output; then the tanh value of the cell state is multiplied by the output of the sigmoid (normalize the output value) threshold, which ultimately gives the output new cell state $H_t$, calculated as in (5) and (6).

$$O_t = \sigma (W_o [X_t, H_{t-1}] + b_o) \hspace{1cm} (5)$$

$$H_t = O_t \cdot \tanh (C_t) \hspace{1cm} (6)$$

where $O_t$ denotes the output gate output, $H_{t-1}$ denotes the output of the previous node, $X_t$ denotes the current input, $W_o$ denotes the output gate weight, and $b_o$ denotes the output gate bias.

In this study, the deep neural network model of LSTM winter wheat yield estimation based on the phenological stages is shown in Figure 2b. The input layers of this model are VIs, LAI, GPP, pr, tmmx, srad, and Pdsi for six growing stages of winter wheat. Two layers of LSTM layers are set, and other hyperparameters are set according to the results of Bayesian optimization algorithm in Section 3, with a total of six times steps. To prevent overfitting of the training data a dropout layer is added to the network architecture. All input data need to be normalized before being fed into the model and, finally, back-normalised for output. The ratio of training data to test data is set to 8:2, where 80% is training data and 20% is test data.

3.2. Bayesian Optimization of LSTM Hyperparameters

The process of building LSTM network models involves the determination of many hyperparameters, such as network depth, learning rate, batch size, and so on. The most intuitive way is to find the optimal parameters by manual trial and error, but the manual trial and error method is too inefficient. It lacks a certain exploration process, and the parameters can only be adjusted manually repeatedly for different problems and data. It takes a lot of time, and the final combination of model hyperparameters may not be optimal,
which will affect the prediction of the model, including the degree of network fit and the
generalization ability to the test set [43,44]. Bayesian optimization, as a very effective global
optimization algorithm, requires only a small number of iterations to obtain a desired
solution by designing a proper probabilistic agent model and a payoff function [43,44]. The
main optimized hyperparameters and the range of values are shown in Table 1.

Table 1. LSTM hyperparameter setting and range.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Range</th>
<th>Parameter Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>NumHiddenUnits</td>
<td>(200, 600)</td>
<td>Number of hidden units</td>
</tr>
<tr>
<td>MaxEpochs</td>
<td>(200, 800)</td>
<td>Maximum number of epochs</td>
</tr>
<tr>
<td>MiniBatchSize</td>
<td>(8, 20)</td>
<td>Size of mini batch</td>
</tr>
<tr>
<td>InitialLearnRate</td>
<td>0.01</td>
<td>Initial learning rate</td>
</tr>
<tr>
<td>Dropout</td>
<td>(0.1, 0.7)</td>
<td>Abstention factor</td>
</tr>
<tr>
<td>SolverName</td>
<td>adam</td>
<td>Solver for training network</td>
</tr>
<tr>
<td>LearnRateSchedule</td>
<td>piecewise</td>
<td>Learning rate strategy</td>
</tr>
<tr>
<td>Objective function</td>
<td>RMSE</td>
<td></td>
</tr>
</tbody>
</table>

The number of hidden units corresponds to the amount of information remembered
between time steps (the hidden state). The hidden state can contain information from all
previous time steps, regardless of the sequence length. If the number of hidden units is too
large, then the layer might overfit to the training data.

Epoch indicates the number of iterations of the data set during model training. If the
number of iterations is set too large, the training time of the model is longer, resulting in
overfitting of the model, over-reliance on training data, and poor prediction of unknown
data, which makes the generalization ability of the model lower. If the number of iterations
is set too small, it will make the model fit poorly and affect the prediction accuracy of
the model.

Size of the mini-batch to use for each training iteration is indicated, specified as the
comma-separated pair consisting of ‘MiniBatchSize’ and a positive integer. A mini-batch
is a subset of the training set that is used to evaluate the gradient of the loss function and
update the weights. If the number of iterations is set too large, the training time of the
model is long, causing the model to be overfitted and overly dependent on the training
data. The prediction ability of the unknown data is poor, thus making the generalization
ability of the model lower. If the number of iterations is set too small, it will make the
model not fit well and affect the prediction accuracy of the model.

The initial learning rate, \( \alpha \), is a relatively important hyperparameter in the LSTM
model. When the learning rate is too large, it will cause the parameters to be optimized
to fluctuate around the minimum value, thus skipping the optimal solution. When the
learning rate is set too small, it will affect the convergence speed of the model, resulting in
a slow convergence rate. In this paper, \( \alpha \) is set to 0.01 based on the empirical value.

Dropout means that, during the training process of the model, for the network units,
they are temporarily dropped from the network according to a certain probability. This
hyperparameter plays a crucial role in preventing model overfitting and improving the
generalization ability of the model.

The key hyperparameters searched in this paper are data batch size, number of
iterations, discard factor, and number of nodes in the hidden layer. The remaining hyperpa-
rameters are based on experience, the optimizer is selected as “adam”, LearnRateSchedule
is set to “piecewise”, and the root mean square error is selected as the target loss function.

The optimization of the LSTM network model hyperparameters using the Bayesian
method is a five-step process as follows (Figure 3, the implementation of the whole process
is implemented in matlab R2021b):

Step 1: All data of six winter wheat phenological periods are normalized to divide the
training set and validation set for parameter learning and model result validation of the
training network model.
Step 2: The LSTM hyperparameters to be optimized and the range are set; a random set of initialized hyperparameters as the initial hyperparameters of the LSTM model are generated. The training set is input for the training of the LSTM neural network. The RMSE is used as the objective function for the hyperparameter optimization of the LSTM model.

Step 3: Gaussian process is used to find the posterior probability distribution of the objective function. The hyperparameter sample points are selected in the modified Gaussian model according to the acquisition function. The acquisition function chosen in this paper is ‘expected-improvement-plus’, which gives preference to the optimal hyperparameter to achieve the update of the hyperparameter.

Step 4: The number of iterations (40) is completed and the minimum objective function and the corresponding trained LSTM model hyperparameters are returned.

Step 5: The validation set is fed into the trained LSTM model to construct an LSTM winter wheat yield estimation model based on Bayesian optimization algorithm.

The general framework of this study is shown in Figure 3a. Based on the indicators required for winter wheat phenology calculation, the influence of different input variables on winter wheat yield prediction was analysed on the BO-LSTM model. Then the performance of different prediction models for winter wheat yield estimation was compared; finally, the robustness of BO-LSTM was explored. All models used were run in matlab R2021b environment.

Figure 3. (a) A research framework of BO-LSTM neural network model for county-level winter wheat yield estimation; (b) Bayesian optimization of LSTM hyperparameters process.

3.3. Model Performance Evaluation

In this study, coefficient of determination \( R^2 \), root mean square error \( \text{RMSE} \), and mean absolute percentage error \( \text{MAPE} \) were used as indicators to assess the model performance [45]. The equations are written as follows:

\[
R^2 = \left[ \frac{\sum (o_i - \bar{o})(y_i - \bar{y})}{\sqrt{\sum (o_i - \bar{o})^2(y_i - \bar{y})^2}} \right]^2
\]
\[
RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (o_i - y_i)^2} \tag{8}
\]
\[
MAPE = \frac{1}{n} \sum_{i=1}^{n} \left| \frac{y_i - o_i}{y_i} \right| \tag{9}
\]

where \( n \) is the number of samples, and \( y_i \) and \( o_i \) are the measured and predicted values of winter wheat yield, respectively. \( R^2 \) is a measure of the strength of the linear relationship between the predicted and measured values of the model, with larger \( R^2 \) indicating that the measured and predicted values have similar trends. \( RMSE \) is used to assess the deviation between measured and predicted values. The smaller the value, the smaller the deviation is between the measured and predicted values of the model; the higher \( R^2 \), the smaller \( RMSE \) is and the better the model. For the \( MAPE \) range \([0, +\infty)\), the smaller the \( MAPE \), the better the model simulation results are. Compared to \( RMSE \), \( MAPE \) is equivalent to normalizing the error at each point, reducing the effect of absolute error from individual outliers.

4. Results and Analysis

4.1. Performance of LSTM Hyperparameter Combination Output Based on Bayesian Optimization

This study aims to optimise the hyperparameters of the LSTM neural network model based on a Bayesian optimisation algorithm, evaluating both the time efficiency, “time”, and the accuracy, \( RMSE \), of the model after tuning the parameters. The first three optimal parameter combinations were selected, along with the corresponding accuracy and time consumption (Table 2). The results demonstrate that the minimum \( RMSE \) of the Bayesian optimised LSTM model on the training set is 149.51 kg/ha, and the time efficiency of finding the optimal hyperparameter combination is 14 min. The Bayesian optimisation algorithm makes full use of historical information when selecting the optimal hyperparameter combination, allowing the optimal hyperparameter combination to be found within a short time and number of iterations.

<table>
<thead>
<tr>
<th>Methods</th>
<th>NumOfUnits</th>
<th>MaxEpochs</th>
<th>MinBatchSize</th>
<th>DropoutLayer</th>
<th>Time/min</th>
<th>RMSE</th>
</tr>
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<tbody>
<tr>
<td>Bayesian optimization</td>
<td>202</td>
<td>314</td>
<td>9</td>
<td>0.1</td>
<td>14</td>
<td>149.51</td>
</tr>
<tr>
<td></td>
<td>335</td>
<td>501</td>
<td>10</td>
<td>0.1</td>
<td>14</td>
<td>181.57</td>
</tr>
<tr>
<td></td>
<td>354</td>
<td>510</td>
<td>11</td>
<td>0.025</td>
<td>14</td>
<td>182.80</td>
</tr>
</tbody>
</table>

4.2. Yield Estimation Performance for Different Combinations of Inputs

To evaluate the performance of yield estimation from different data sources, we put different combinations of input variables in a BO-LSTM model for analysis. Figure 4 shows the yield estimation performance of BO-LSTM for winter wheat with five different input variables. We found that yield estimates using GPP (\( R^2 = 0.72, RMSE = 186.13 \) kg/ha) alone were more accurate than those using LAI (\( R^2 = 0.67, RMSE = 221.32 \) kg/ha) alone. When combined with meteorological data, the accuracy of GPP combined with meteorological data was higher (\( R^2 = 0.81, RMSE = 180.66 \) kg/ha) compared to the remotely sensed vegetation index (\( R^2 = 0.78, RMSE = 190.96 \) kg/ha), because GPP more directly reflects the process of organic matter accumulation by vegetation photosynthesis. The yield estimation accuracy of winter wheat gradually increased as the input data increased, indicating that the estimation accuracy of fusing multiple sources of data was better than the input from a single data source. The highest estimation accuracy was achieved by integrating all data together (\( R^2 = 0.83, RMSE = 177.84 \) kg/ha). The addition of the data improved the model’s ability to capture spatial heterogeneity in yield, capturing more features associated with winter wheat yield. In particular, the yield estimation accuracy of the LSTM model improved significantly when combined with meteorological data, suggesting that meteorological data provide unique and irreplaceable information.
4.3. Comparison with Other Methods

The analysis in the previous section led us to conclude that the highest accuracy in winter wheat yield estimation can be achieved by integrating all data, so we used data with “GPP + Climate + LAI + VIs” as the final input data for the BO-LSTM. To further evaluate the yield estimation performance of the BO-LSTM, we used a machine learning SVM and a linear regression Lasso to estimate the yield of winter wheat. Figure 5 presents a scatter plot of our yield estimates and statistical annals for all county test data for Hengshui city using the three prediction models. Based on the $R^2$ and RMSE values, it can be intuitively seen that the SVM (RMSE = 185.7 kg/ha, $R^2 = 0.80$) and BO-LSTM (RMSE = 177.8 kg/ha, $R^2 = 0.82$) model methods perform significantly better than Lasso (RMSE = 214.5 kg/ha, $R^2 = 0.76$). The potential reason could be that SVM and BO-LSTM methods capture the complex and nonlinear relationships between input variables and winter wheat yield better than linear regression models. Further, it is found that the BO-LSTM model slightly outperformed the SVM method in estimating winter wheat yield in Hengshui City. This is largely attributed to the fact that machine learning non-temporal models focus on information extraction for unordered data and do not optimize the structure for temporal data. The LSTM is a recurrent neural network structure that transmits cumulative effective information during different growth stages. It is similar to the growth process characteristics of crops: crop growth and progressive developmental changes and biomass accumulation. The effects of environmental factors on winter wheat yield are complex and non-linear. The LSTM inputs the observations into the model network structure in a temporal order, and the gate mechanism is set internally. The weights of input gates, forgetting gates, and input gates are trained to achieve automatic screening and fusion of timing features.

Immediately afterwards, we used the BO-LSTM with better estimation accuracy and SVM to estimate winter wheat yield for all counties in Hengshui (Figure 6). In general, there was some spatial variation in the estimation advantage of different regions. The estimation performance of BO-LSTM was still slightly higher than that of SVM, regardless of the county region. Using the BO-LSTM model with better yield estimation accuracy, we can see that the RMSE is more than 300 kg/ha in Rao Yang County, Jizhou City, Taocheng District, Anping County, and Fucheng County. The highest is in Rao Yang County with an
RMSE of 444.77 kg/ha and a MAPE of 6.18. The areas with RMSE between 200–300 kg/ha are Shecheng County, Jing County, Shenzhou City, and Zaojiang County. Areas with RMSE less than 200 kg/ha include Wuyi County and Wuqiang County, with the smallest being located in Wuyi County (RMSE = 117.30 kg/ha, MAPE = 1.64).

![Figure 5](image1)

**Figure 5.** Performance of the 2005–2019 test set for winter wheat yield estimation in different forecasting models.

![Figure 6](image2)

**Figure 6.** BO-LSTM performance of yield estimation for all counties in Hengshui city: (a) RMSE; (b) MAPE.
5. Discussion

In this study we highlight the advantages of BO-LSTM fusing multi-source data for winter wheat yield estimation. The results show that the deep learning model fusing multi-source data provides reliable winter wheat yield estimation at the regional scale. In general, GPP, LAI, and VIs are suitable for large-scale crop yield estimation. The estimation accuracy can be improved by combining meteorological data. The highest estimation accuracy is achieved when all predictors are combined and entered into the estimation model, which is very similar to previous studies [25,46,47]. Since this paper uses SVM, LSTM, and LASSO as the yield estimation models, which are regularized, we do not need to consider the problem of multicollinearity.

The Bayesian optimizer can determine an acceptable value very quickly, which is especially advantageous when the time complexity of finding the value of any function of the black box function is high, and the Bayesian optimizer does not have a limit on the search fineness. The disadvantage is that the returned result is not necessarily the true minimum objective function value (grid search may not find it either), and the result of each optimization will vary. Therefore, several optimizations are needed when optimizing the LSTM hyperparameters with Bayesian, and the best optimization result is finally selected.

For the problem of different estimation accuracies in different regions (Figure 6), we analysed the distribution of winter wheat cultivation over 15 years and found that we only listed four of them (Figure 7), and the distribution of wheat cultivation in Taocheng, Jizhou, Anping, and Rao Yang regions was more scattered with less cultivated area. Among them, Taocheng District and Jizhou District are the city centre of Hengshui City. The marginal effects of various factors in cities within a certain region affect climate factors, and local climate is difficult to obtain accurately compared to other regions, resulting in differences between the meteorological data we obtained and the actual meteorological data [48]. This explains the large discrepancy between estimated yields and official yield records in these areas. Our method is therefore more suitable for areas where the distribution of cultivation is concentrated, far from urban building sites, and with relatively little human interference.

In the process of analysis, we found that there are still some limitations. The first is that we focus on estimating county-level crop yields, which leads to smaller training samples due to the difficulty of obtaining data. The problem of data scarcity makes the learning information aspect of the LSTM neural network model insufficient in the training process. Second, the essence of deep learning is feature extraction from data to data, and neural network modelling converts the original input variables into high-level representations through nonlinear activation and squeeze functions. The description and mechanistic expression of the crop growth process cannot be learned, which weakens the traceability and interpretability of the LSTM model. The data-driven crop growth model has great potential. The crop growth model can take the crop, environment, and cultivation technology as a whole. The principles and methods of systems analysis can be applied to provide theoretical generalizations and quantitative analyses of the physiological processes of crop growth and development, photosynthetic production, organogenesis, and yield formation and their feedback relationships to environment and technology. Following that, the corresponding mathematical models are developed to carry out the dynamic quantitative simulation of the crop growth process. Therefore, fusing deep learning with crop mechanism models can improve the interpretability of deep learning models. To address the problems, our future work focuses on expanding the study area to integrate process-based models and deep learning techniques to develop hybrid models. The BO-LSTM model provides a data-driven approach to crop growth time series feature extraction by combining the crop weathering characteristics. The spatiotemporal scalability of the BO-LSTM model is worth exploring in future research. The spatial transfer learning capability of the BO-LSTM can be evaluated to quantify the model’s ability to estimate crop yields in areas without many historical yield records. A deep learning approach based on BO-LSTM to learn the spatiotemporal heterogeneity of crop growth can help to better understand the impact of global climate change on agricultural production.
6. Conclusions

In this research, we proposed a BO-LSTM model that integrates crop phenology and meteorological and remote sensing data to predict county-level winter wheat yields. Yield estimation performance was then compared using three predictive models, including linear regression, machine learning, and deep learning. The conclusions are as follows:

(1) Using Bayesian optimization of LSTM neural network model hyperparameters can achieve identification of the optimal combination of hyperparameters in a shorter period of time.

(2) Multi-temporal remote sensing data based on BO-LSTM model combined with meteorological data can provide effective information to obtain more accurate yield prediction models to estimate regional scale winter wheat yield.

(3) Among the three prediction models, BO-LSTM achieves higher yield estimation accuracy relative to Lasso and SVM.

(4) There is some spatial variation in the estimated yield advantage in different areas, and our method is more suitable for places where crop cultivation is concentrated, far from urban building sites and with less residential land.

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