

Article

Analysis on Steering Performance of Active Steering Bogie According to Steering Angle Control on Curved Section

Hyunmoo Hur ^{1,*}, Yujeong Shin ¹  and Dahoon Ahn ² 

¹ Advanced Railroad Vehicle Division, Korean Railroad Research Institute, 176 Cheoldobakmulkwon-ro, Uiwang-si, Gyeonggi-do 16105, Korea; yjshin@krri.re.kr

² Department of Mechanical and Automotive Engineering, Kongju National University, 1223-24 Cheonan-daero, Cheonan-si, Chungcheongnam-do 31080, Korea; dhahn@kongju.ac.kr

* Correspondence: hmhur@krri.re.kr; Tel.: +82-31-460-5245

Received: 6 April 2020; Accepted: 23 June 2020; Published: 26 June 2020



Abstract: In this paper, prior to the commercialization of a developed active steering bogie, we want to analyze steering performance experimentally according to steering angle level with the aim of obtaining steering performance data to derive practical design specifications for a steering system. In other words, the maximum steering performance can be obtained by controlling the steering angle at the 100% level of the target steering angle, but it is necessary to establish the practical control range in consideration of the steering system cost increase, size increase, and consumer steering performance requirements and commercialize. The steering control test using the active steering bogie was conducted in the section of the steep curve with a radius of curvature of R300, and steering performance such as bogie angle, wheel lateral force, and derailment coefficient were analyzed according to the steering angle level. As the steering angle level increased, the bogie indicated that it was aligned with the radial steering position, and steering performance such as wheel lateral force and derailment coefficient was improved. The steering control at 100% level of the target steering angle can achieve the highest performance of 83.6% reduction in wheel lateral force, but it can be reduced to about one-half of the conventional bogie at 25% level control and about one-third at 50% level. Considering cost rise by adopting the active steering system, this result can be used as a very important design indicator to compromise steering performance and cost rise issues in the design stage of the steering system from a viewpoint of commercialization. Therefore, it is expected that the results of the steering performance experiment according to the steering angle level in this paper will be used as very useful data for commercialization.

Keywords: active steering bogie; steering angle; steering performance; bogie angle; lateral force; derailment coefficient

1. Introduction

When a railway vehicle runs on curved sections, severe wheel wear and noise occur between the wheel and the rail. This is because the railway vehicle is not equipped with a steering device, so it is difficult to run smoothly in the curved section. That is, an attack angle is generated between the wheel and the rail, which causes unnecessary force in the running and lateral direction of the wheel, which causes wheel wear and noise.

Research on an active steering bogie began in the early 1990s to solve problems caused by existing railway bogies when running on curved sections. Theoretical studies were carried out, such as the control concept for steering control of an active steering bogie to improve the poor steering performance of conventional railway vehicles [1–5].

Recently, a railway vehicle with a combination of active steering technology, active suspension and tilting technologies has been commercialized [6]. However, although the rough concept of active steering is described, details such as specifications of the steering system and steering test results are not described.

Umehara has performed active steering control tests on the curved section of a factory test line using active steering bogie prototypes equipped with an electro-hydraulic type actuators, and analyzed the reduction of wheel lateral force [7].

Suzuki tested the wheel lateral force reduction according to active steering control in the steep curve of a factory test line for a prototype steering bogie with a pneumatic-type active steering system [8].

In the above two experimental papers, wheel lateral forces generated running on curved sections were measured and wheel lateral force reduction was analyzed in order to analyze the performance of the active steering bogie.

To evaluate directly the steering performance of an active steering truck, it is necessary to measure the wear of the wheels and analyze the amount of reduction. However, this requires measuring and analyzing the wear shape of the wheels throughout a long test run, which takes a lot of time and cost. Therefore, in the stage of development, it is efficient to measure the lateral force of the wheel, which directly affects the wheel wear, and analyze the lateral force reduction according to the active steering control. Therefore, the above experimental results analyzed the active steering performance by measuring lateral forces acting on wheels.

Meanwhile, Hur proposed the concept of radial steering position control through real-time curve detection [9]. The feasibility of the curve-detecting method, which is a core technology of steering control strategy, has been verified experimentally [10]. The validity of the proposed control concept has been verified through active steering simulation analysis [11].

In addition, a prototype of an electro-mechanical type steering system was manufactured to be installed on an active steering bogie and performance tests were conducted on the steering system. Steering bogies equipped with steering systems were manufactured and steering control tests simulating curve running prior to the test run on the commercial line were conducted [12].

Based on the results of the above study, Hur constructed a test EMU (Electronic Multiple Unit) train equipped with an active steering bogie and conducted steering performance tests according to active steering control on a commercial line, not on a factory line [13]. The test results showed that the wheel lateral force was reduced by up to 86.2% compared to the conventional bogie. This result was the best of the wheel lateral force test results for the active steering bogie reported to date.

According to the results of the above study, the concept of radial steering position control through real-time curvature radius estimation proposed by Hur was proved with simulation and a test run, and steering performance was also proved to be excellent.

In this paper, prior to the commercialization of a developed active steering bogie, we want to analyze steering performance experimentally according to the steering angle level with the aim of obtaining steering performance data to derive practical design specifications for steering system.

In other words, the maximum steering performance can be obtained by controlling the steering angle at 100% level of the target steering angle, but it is necessary to establish the practical control range in consideration of the steering system cost increase, size increase, and consumer steering performance requirements, and to commercialize this.

Therefore, an experimental study using an active steering bogie was conducted to analyze the steering performance according to the steering angle level. The steering control test was performed on a steep curve section with a radius of curvature of 300 m using an active steering bogie prototype for EMU. This study analyzes the bogie angle, wheel lateral force reduction and derailment safety under the steering angle control of the active steering bogie and describes the results.

2. Active Steering Control Strategy

When the railway vehicle runs on the curved section, attack angle between the wheel and the rail are generated as shown in Figure 1 due to the lack of steering function of the wheel [13]. This causes unnecessary force in the driving direction and the lateral direction of the wheel, which is a major factor causing wear of the wheels and rails and the generation of noise.

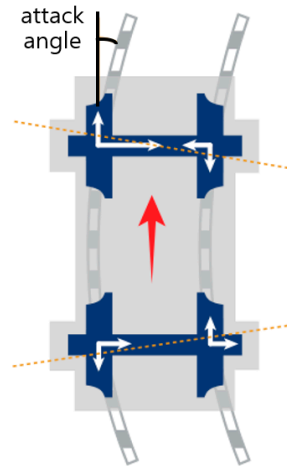


Figure 1. Wheelset alignment of a conventional railway vehicle when running on curved section.

Therefore, in order for the railway vehicle smoothly run the curve section, the angle of attack becomes “0” if the wheelset is aligned with the center of curvature as shown in Figure 2 using active steering control technology. At this time, this geometric position is called the radial steering position.

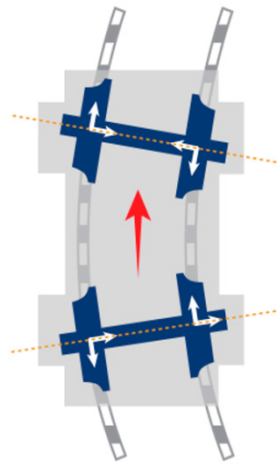


Figure 2. Wheelset alignment of a railway vehicle with active steering technology when running on curved section.

Figure 3 shows the geometrical relationship between the body and the bogies, assuming the vehicle is in the radial steering position in the curve section. In Figure 3, the angle (2δ) formed between two wheelsets is called the steering angle, and the angle (θ) at which the bogie is rotated with respect to the vehicle body is called the bogie angle.

When the bogie and wheelset are aligned with the radial steering position, the bogie angles of the front and rear bogies are the same. At this time, from the geometric relationship of Figure 3, the target

values for wheelset steering angle and bogie angle for the ideal wheelset steering in the curve section of radius R are derived as shown in Equations (1) and (2) [14,15].

$$2\delta = 2d/R \quad (1)$$

$$\theta = L/R \quad (2)$$

where,

2δ : steering angle(rad)

R : radius of curve(m)

$2d$: wheel base(m)

L : semi-spacing of distance between bogie centers(m)

θ : bogie angle between body and bogie(rad)

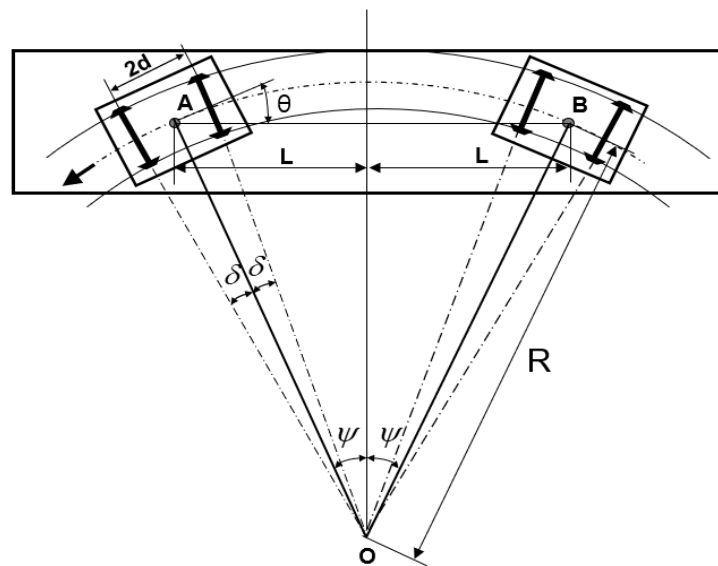


Figure 3. Radial steering position.

When a railway vehicle is run on a curved section as above, it can ideally pass through the curve if it is located in a radial steering position. In other words, if steering control is performed by calculating the target steering angle by applying Equation (1), the railway vehicle will be located in the radial steering position. In order to apply Equation (1), information on the radius of the curved section passing through is required. Previously, a method of pre-input of the curve information according to the position into the controller was applied, but it was inefficient. In this paper, the method of estimating the radius of curvature in real time developed by the author was used, and this method of estimating the radius of curvature was experimentally verified [10].

3. Steering Control Test on the Curved Section

3.1. Active Steering Bogie

To analyze the steering performance according to the steering angle in the curve section, the test run was carried out using the active steering bogie prototype. An active steering bogie prototype was developed for subway EMU trains running on urban railway areas [14,15]. Figure 4 shows the configuration of the active steering bogie and Figure 5 shows the active steering bogie prototype installed on the test train.

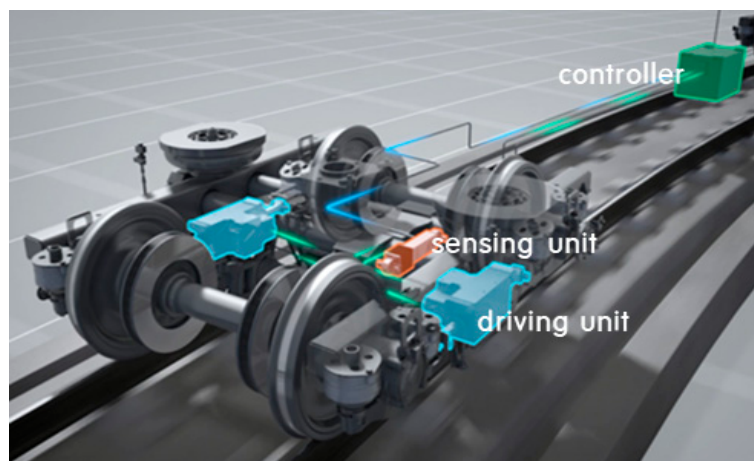


Figure 4. Configuration of the active steering bogie.



Figure 5. Prototype of the active steering bogie.

An active steering bogie adopts a radial steering position control strategy based on real-time curvature radius estimation [9–11]. The active steering system of the bogie is composed of a sensor unit, a control unit and a driving unit [14].

The sensor unit estimates the radius of curvature of the curve in real time, the controller calculates the target steering angle for active steering, and the steering driving unit conducts steering the wheelset according to the controller command.

The minimum radius of the curved section that can be detected by the active steering bogie is R80 with a radius of curvature of 80 m and the maximum controllable steering angle is 0.5 degrees. In other words, steering control is possible up to R250, a radius of curve of 250 m, the smallest curve on commercial lines.

The steering driving unit is adopting an electro-mechanical type actuator, with a maximum steering thrust force of more than 50,000 N. Table 1 shows the specifications of the active steering system of the active steering bogie

Table 1. Specifications of the active steering system.

Category	Specification
Detectable curve radius	min 80 m
Steering angle	0.5 degrees
Supply voltage	three phase 380 VAC
Maximum current (per vehicle)	16 A
Thrust force(per driving unit)	above 50,000 N

The steering controller is mounted on the body to perform steering control of the front and rear steering bogies. The control algorithm of the steering controller is shown in the block diagram in Figure 6. The controller for steering estimates the radius of curvature through the signal detected in real time from the curvature sensor and calculates the target steering angle. Figure 7 shows the mechanism by which the drive unit works to achieve the target steering angle. This control method has been experimentally verified through a test run using a test train equipped with an active steering bogie [15].

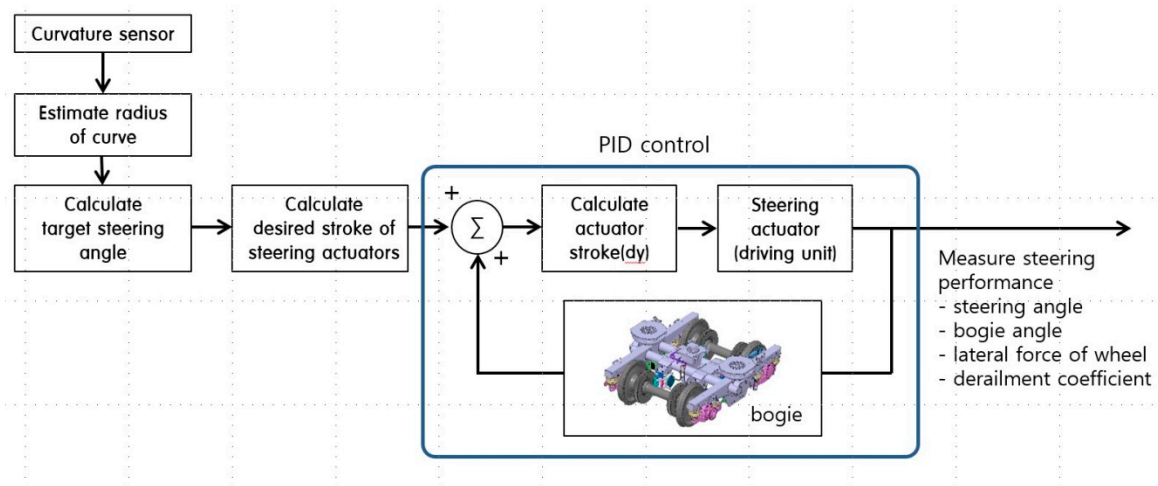


Figure 6. Block diagram of the active steering control by estimating the radius of the curve.

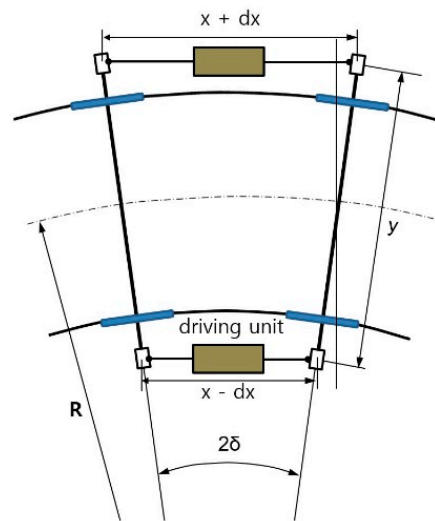


Figure 7. The steering angle produced between the front and rear wheelsets of the bogie.

3.2. Test Curve Section

The steering control test to analyze the steering performance according to the steering angle in the curve section was performed on the R300 curve with a radius of 300 m of the commercial line. Figure 8 shows the curvature of the test section measured by the curvature sensor unit mounted on the active steering bogie for real-time curve detection. The total length of the test curved section is 450 m and the length of the circular curve is 250 m.

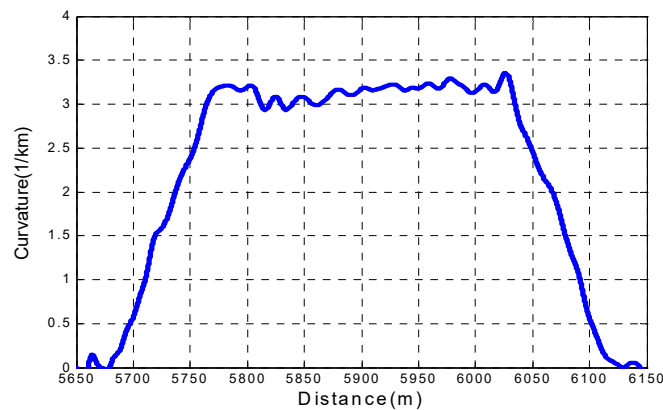


Figure 8. Curvature of the test curve section.

3.3. Test Condition for Active Steering Condition

Table 2 shows the test conditions for analyzing the steering performance according to the steering angle on the curved section. Passive is the running condition of the curved section of the existing bogie not equipped with the active steering system. Active (25%) refers to the case when the active steering bogie is run on the test section while controlling to 25% of the target steering angle.

Table 2. Test condition for active steering control.

Case	Test Condition
Passive	No active steering
Active (25%)	Control to 25% of the target steering angle
Active (50%)	Control to 50% of the target steering angle
Active (75%)	Control to 75% of the target steering angle
Active (100%)	Control to 100% of the target steering angle

Active (50%) and Active (75%) represent when steering control is conducted at the 50% and 75% levels of the target steering angle, respectively. Active (100%) means that steering control is conducted completely to 100% level of the target steering angle.

4. Test Results of the Active Steering Control

4.1. Analysis Method

In order to analyze the steering performance according to the steering angle on the curved section, the bogie angle of the front and rear bogies, which are related to the radial steering position of the bogie, and the lateral force and the derailment coefficient of the wheel, which are dynamic factors, were measured.

To confirm the test conditions for steering angle implementation, steering angle was measured using a steering angle sensor as shown in Figure 9. To measure the bogie angle, which is the rotating angle between the body and the bogie, the geometric displacement between the body and the bogie was measured and converted into the bogie angle.

To measure the lateral force and the derailment coefficient of the wheel, a measuring wheelset was manufactured to measure the lateral and vertical force applied to the wheel and it was installed on the active steering bogie [15]. Figure 10 shows the measuring wheelset to measure wheel forces such as wheel lateral force and derailment coefficient. The method of measuring the action force applied to the wheels of a railway vehicle proposed by Ham was used [16].

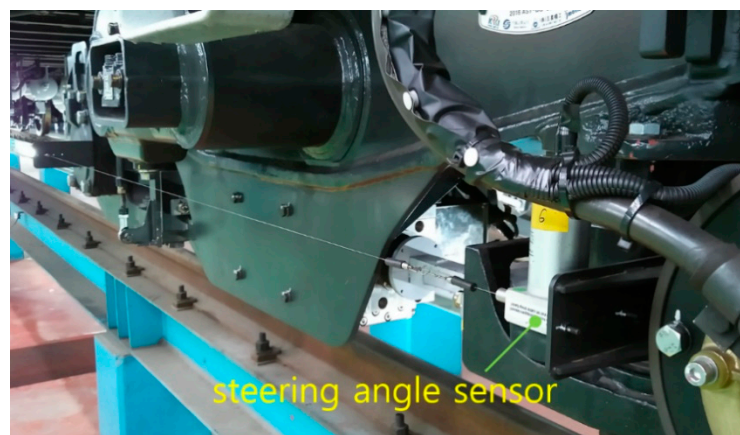


Figure 9. Steering angle sensor.



Figure 10. Wheel force measuring wheelset.

4.2. Steering Angle

The steering control test was performed according to the test conditions in Section 3.3 to analyze the steering performance according to the steering angle on the curved section. Figure 11 shows the steering angle test results measured by the steering angle sensor to verify that the active steering control test conditions are properly implemented. Table 3 shows the mean values for the steering angles when the steering bogie runs in the circular section of the test section.

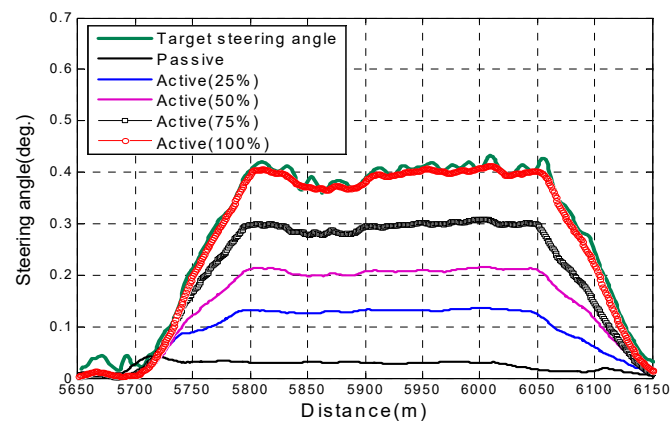


Figure 11. Measured steering angle according to steering control condition.

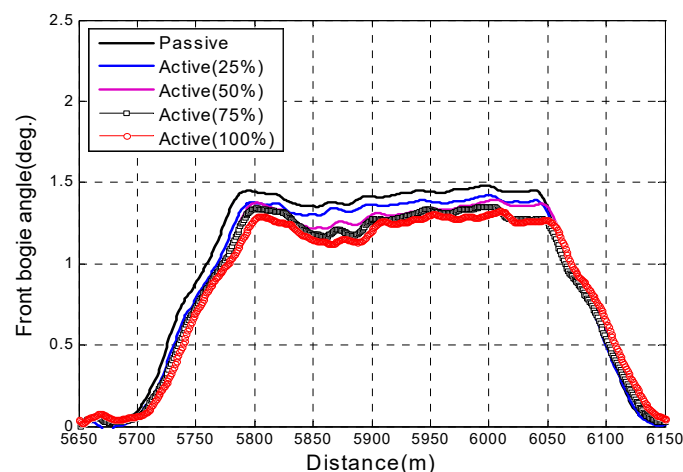
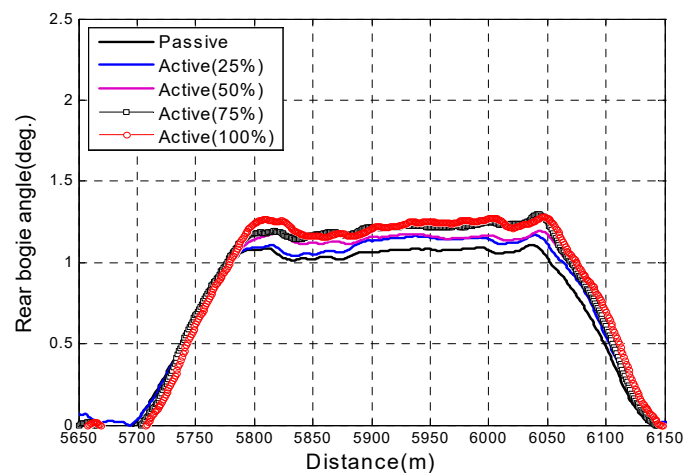
Table 3. Mean steering angle for the circular section of the test section.

Case	Steering Angle (Degrees)	Ratio to Target Steering Angle (%)
Passive	0.029	7.3
Active (25%)	0.131	32.8
Active (50%)	0.208	52.0
Active (75%)	0.295	73.8
Active (100%)	0.393	98.3

The steering angle of passive condition with insufficient steering function is 0.029 degrees. This indicates that the measured value is very low at 7.3% of the target value, considering that the target steering angle required to pass the R300 curve is 0.4 degrees according to Equation (1). As the steering angle implementation level increases with active steering control, the steering angle is approximated to the test conditions. That is, in the case of Active (50), it is 0.208 degrees., which is 52% of the target steering angle. In the case of Active (100) which performs 100% steering control, the measured value is 0.393 degrees., which is controlled well as 98.3% of the target steering angle.

4.3. Bogie Angle

Figures 12 and 13 show the measured bogie angles generated in the front and rear bogie according to the steering angle test conditions. Figure 14 shows the bogie angle difference between the front and rear bogie. Table 4 shows the mean values for the bogie angles when the steering bogie run the circular section of the test section.

**Figure 12.** Measured bogie angle of the front bogie.**Figure 13.** Measured bogie angle of the rear bogie.

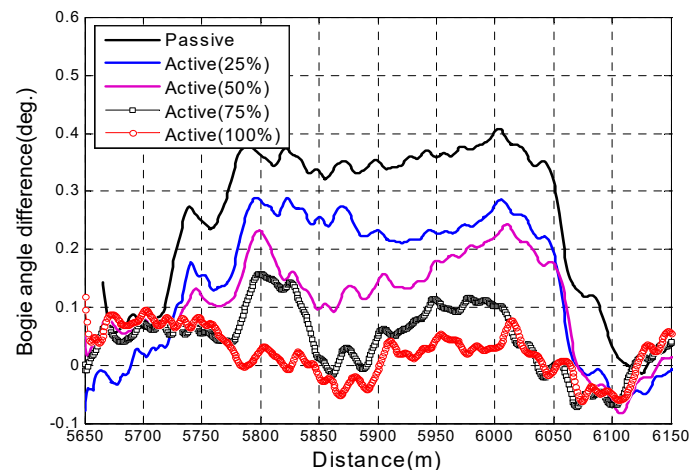


Figure 14. Bogie angle difference between front and rear bogies according to steering control conditions.

Table 4. Mean bogie angle for the circular section of the test section.

Case	Bogie Angle (Degrees)		
	Front	Rear	Difference
Passive	1.404	1.055	0.349
Active (25%)	1.363	1.118	0.244
Active (50%)	1.317	1.151	0.165
Active (75%)	1.278	1.211	0.067
Active (100%)	1.242	1.228	0.014

In the case of a passive state with insufficient steering function, the bogie angle for the front bogie is 1.404 degrees and that for the rear bogie is 1.055 degrees and the difference is 0.349 degrees, which is very large. This result is due to the lack of steering function and the bogie is not aligned in the radial steering position when running on the curved section.

On the other hand, as the steering angle level increases with active steering control, it is shown that the bogie angle for the front bogie decreases and that for the rear bogie tends to increase. In addition, the bogie angle difference is also gradually decreasing. That is, in the case of Active (100) which performs 100% steering control, the bogie angle for the front bogie is 1.242 degrees, that for the rear bogie is 1.228 degrees, and the difference is only 0.014 degrees. This shows that the bogie is aligned in the radial position when running the curved section with active steering control.

4.4. Lateral Force of the Wheel

Figure 15 is test data obtained by measuring the lateral force generated on the front outer wheel of the test vehicle according to the steering angle test conditions. For lateral force analysis, UIC 518 OR “Testing and approval of railway vehicles from the point of view of their dynamic behaviour—Safety—Track fatigue—Running behaviour”, the world’s railway standard, is applied [17]. When the test standard was applied to calculate the maximum permissible limit of wheel lateral force, the maximum permissible limit was 34 kN, and all measurement results were within the allowable limit.

Figure 16 is the result of analyzing the lateral force test data by subdividing 70 m into small sections and arranging them in the cumulative distribution order to extract 99.85% of the values as the representative sections of the small sections. Table 5 shows the mean values of the small section representative values for the analysis results in Figure 15 and the reduction rate for the lateral force of each test case for the passive case.

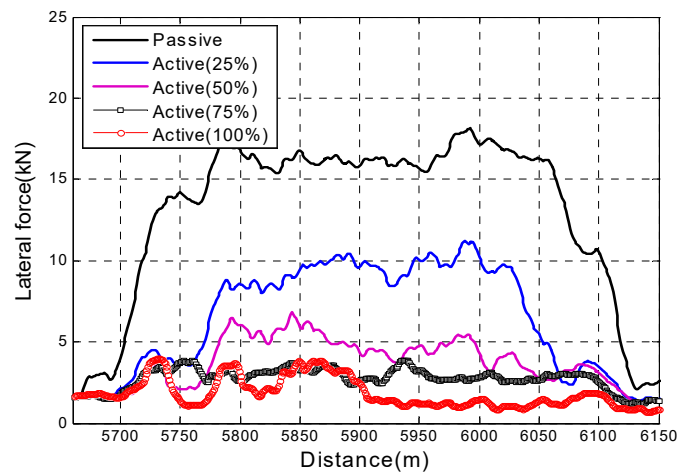
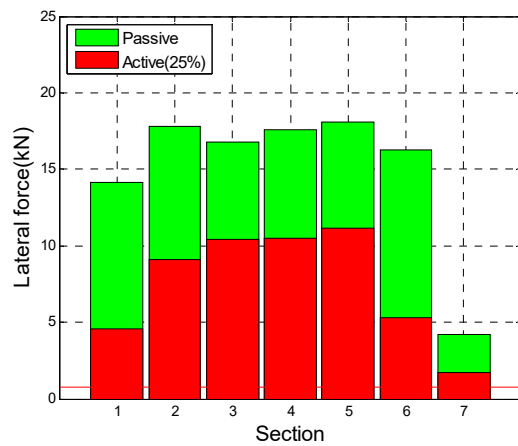
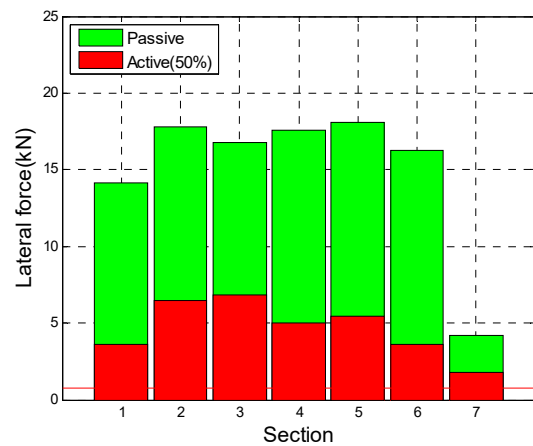


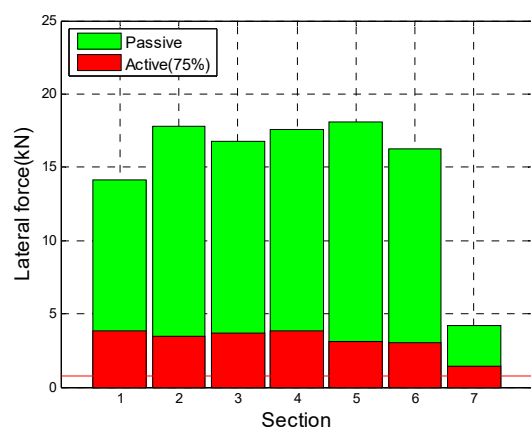
Figure 15. Wheel lateral force test data according to steering control test conditions.



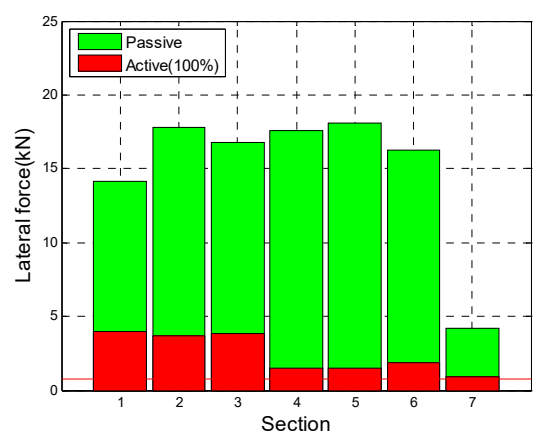
(a) Passive



(b) Active(25%)



(c) Active(50%)



(d) Active(100%)

Figure 16. Analysis results for wheel lateral force according to steering control test conditions.

Table 5. Mean lateral force for the circular section of the test section.

Case	Force (kN)	Reduction (%)
Passive	14.99	-
Active (25%)	7.53	49.8
Active (50%)	4.68	68.8
Active (75%)	3.20	78.6
Active (100%)	2.46	83.6

The mean lateral force of the wheel in the passive case with insufficient steering is 14.99 kN. On the other hand, in the active steering control test condition, the wheel lateral force decreases as the steering angle implementation level increases. In the case of Active (25), it is 7.53 kN, which is 49.8% lower than the Passive case. In the case of Active (50) and Active (75), the mean lateral forces were 4.68 kN and 3.20 kN, respectively, decreasing by 68.8% and 78.6%, respectively. In the case of Active (100) with 100% steering control, the mean lateral force is 2.46 kN, which is 83.6% lower than the passive case.

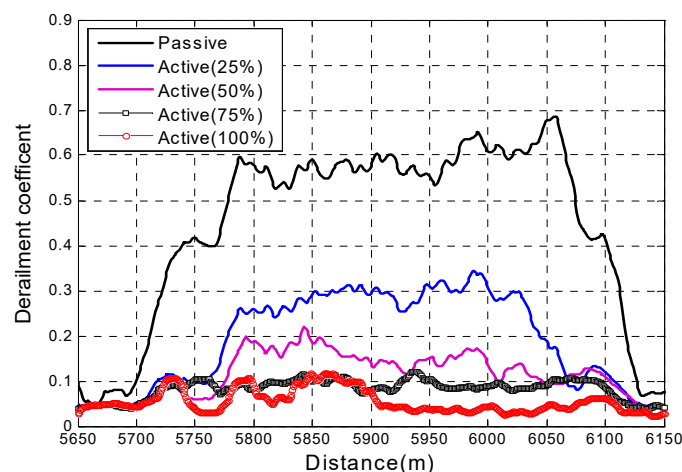
Therefore, it was confirmed that the bogie was aligned with the radial position as the steering angle increased to meet the target steering angle as the test train passed through the curved section, and the wheel lateral force was also significantly reduced.

4.5. Derailment Coefficient

Derailment coefficient is a factor that indicates derailment safety when the vehicle is running and is defined as the ratio of the lateral force to the vertical force acting on the wheel. Figure 17 shows the measured derailment coefficient test data of the front outer wheel of the test vehicle according to the steering angle test conditions using the wheel force measuring wheelset.

For the analysis of the derailment coefficients, the UIC 518 OR test standard used for wheel lateral force analysis was applied [17]. Figure 18 is the result of analyzing the derailment coefficients test data by subdividing 70 m into small sections and arranging them in the cumulative distribution order to extract 99.85% of the values as the representative sections of the small sections. Here, according to the test standard, the allowable limit of the derailment coefficient is 0.8 and all the results of the analysis are within the tolerance limit.

Table 6 shows the mean values of the small section representative values for the analysis results in Figure 18 and the reduction rate for the derailment coefficient of each test case for the passive case.

**Figure 17.** Derailment coefficient test data according to steering control test conditions.

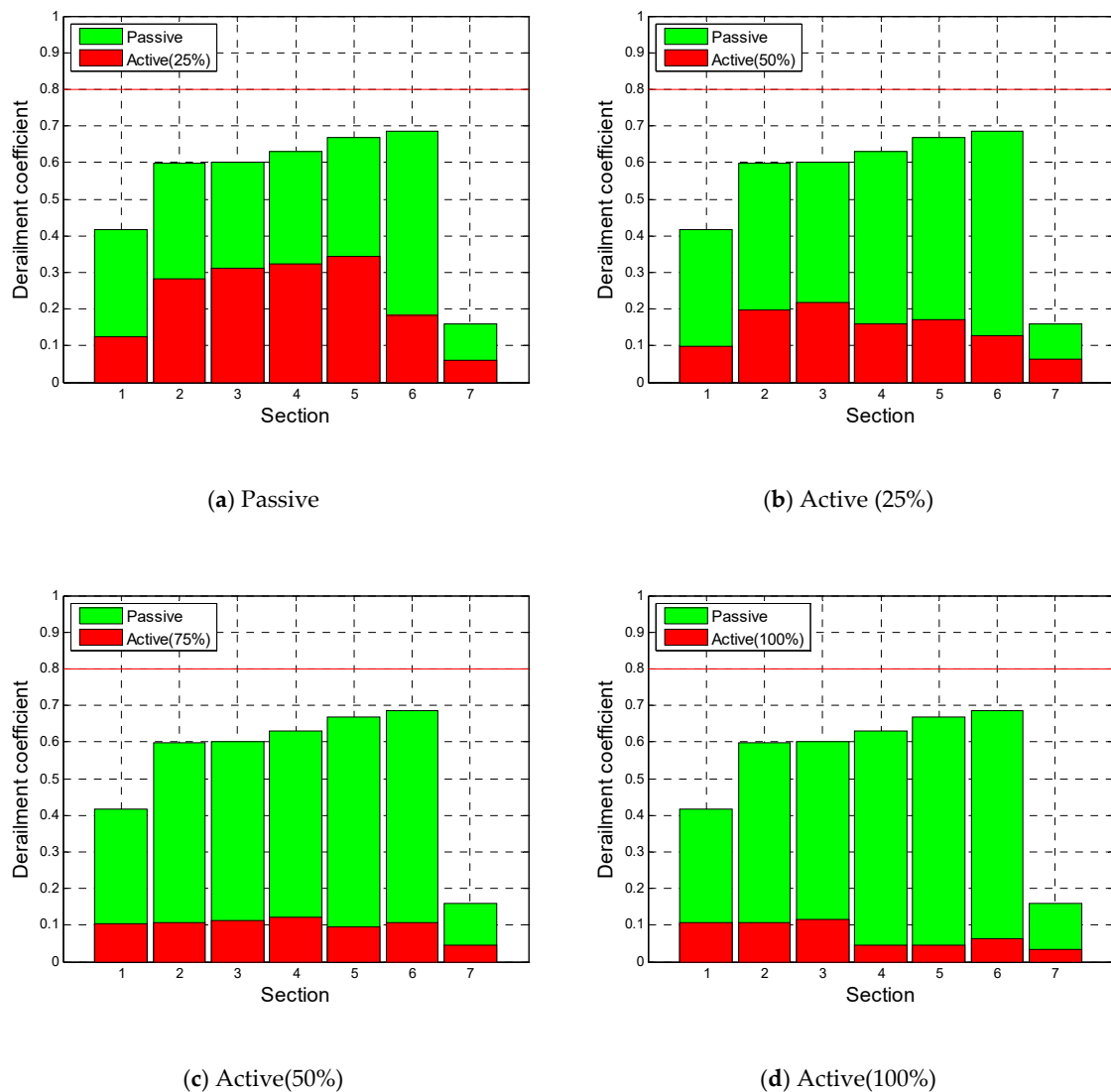


Figure 18. Analysis results for derailment coefficient according to steering control test conditions.

Table 6. Mean derailment coefficient for the circular section of the test section.

Case	Derailment Coefficient	Reduction (%)
Passive	0.537	-
Active (25%)	0.232	56.7
Active (50%)	0.148	72.5
Active (75%)	0.099	81.6
Active (100%)	0.074	86.3

The mean derailment coefficient of the wheel in a passive case with insufficient steering is 0.537. On the other hand, in the active steering control test condition, the derailment coefficient decreases as the steering angle implementation level increases. In the case of Active (25), the mean derailment coefficient is 0.232, which is 49.3% lower than the Passive case. In the case of Active (50) and Active (75), the mean derailment coefficients were 0.148 and 0.099, respectively, with 72.5% and 81.6% reduction rates.

In the case of active (50) and active (75), the average derailment coefficients were 0.148 and 0.099, respectively, decreasing by 72.5% and 81.6%, respectively. In the case of Active (100) with 100% steering control, the mean derailment coefficient is 0.074, which is 86.3% lower than the passive case. This means that the derailment coefficient is naturally reduced if the wheel lateral force is reduced

because the derailment coefficient is the ratio of the lateral force to the vertical force of the wheel. Accordingly, it can be seen that the wheel lateral force is reduced by the active steering control and the derailment coefficient, which is a vehicle running safety evaluation factor, is also significantly reduced.

5. Conclusions

In this paper, a steering performance experiment according to steering angle level was conducted with the aim of obtaining steering performance data for the purpose of deriving practical design specifications for a steering system prior to the commercialization of an active steering bogie to be developed.

The test was carried out in a curved section with a radius of curvature of R300, and steering performance such as bogie angle, wheel lateral force, and derailment coefficient were analyzed according to the steering angle level of the active steering bogie. Here, the steering angle level was assumed to be 25%, 50%, 75%, and 100% of the target steering angle.

As a result of the test, as the steering angle was increased to match the target steering angle, the bogie angle difference between the front and rear bogies was gradually decreased. When steering control was conducted at 100% level, the bogie angles of the front and rear bogie were almost the same, and the difference was only 0.014 degrees. This means that the bogie is aligned in the radial steering position of the curved section by steering control. Wheel lateral force also tended to decrease significantly with increasing steering angle.

When steering control was performed at 25%, 50%, 75%, and 100% of the target steering angle, respectively, 49.8%, 68.8%, 78.6%, and 83.6% decreased compared to passive conditions. This means that the steering control at 100% level of the target steering angle can achieve the highest performance of 83.6% reduction in wheel lateral force, but it can be reduced to about one-half of the conventional bogie at 25% level control and about one-third at 50% level.

Considering cost rise by adopting the active steering system, this result can be used as a very important design indicator to compromise steering performance and cost rise issues in the design stage of the steering system from a viewpoint of commercialization. Therefore, it is expected that the results of the steering performance experiment according to the steering angle level in this paper will be used as very useful data for commercialization.

Author Contributions: Conceptualization, H.H., D.A.; Methodology, H.H., Y.S. and D.A.; Formal analysis, Y.S., D.A.; Writing—original draft preparation, H.H.; Supervision, H.H., Y.S. and D.A.; Project administration, H.H.; Writing—review and editing, H.H., Y.S. and D.A. All authors have read and agreed to the published version of the manuscript.

Funding: This work was supported by a grant from the R&D Program of the Korea Railroad Research Institute (PK2002D1), Republic of Korea.

Conflicts of Interest: The authors declare no conflict of interest

References

1. Mei, T.X.; Goodall, R.M. Modal controllers for active steering of railway vehicles with solid axle wheelsets. *Veh. Syst. Dyn.* **2000**, *34*, 25–41. [CrossRef]
2. Perez, J.; Busturia, J.M.; Goodall, R.M. Control strategies for active steering of bogie-based railway vehicles. *Control. Eng. Pract.* **2002**, *10*, 1005–1012. [CrossRef]
3. Mei, T.X.; Goodall, R.M. Recent development in active steering of railway. *Veh. Syst. Dyn.* **2003**, *39*, 415–436. [CrossRef]
4. Shen, S.; Mei, R.X.; Goodall, R.M.; Pearson, J.; Himmelstein, G. A study of active steering strategies for railway bogie. *Veh. Syst. Dyn. Suppl.* **2004**, *41*, 282–291.
5. Molatefi, H.; Hecht, M.; Bokaeian, V. Stability and safety analysis of an active steering bogie according to EN 14363 standard. *J. Braz. Soc. Mech. Sci. Eng.* **2017**, *39*, 2945–2956. [CrossRef]
6. Railway Technology, Bombardier TWINDEXX Double-Deck Trains. Available online: <http://www.railway-technology.com/projects/bombardier-twindexx-double-decktrains> (accessed on 23 June 2015).

7. Umehara, Y.; Kamoshita, S.; Ishiguri, K.; Yamanaga, Y. Development of electro-hydraulic actuator with fail-safe function for steering system. *Q. Rep. RTRI* **2014**, *55*, 131–137. [[CrossRef](#)]
8. Suzuki, M.; Kodama, S.; Tanaka, T.; Umehara, Y.; Kamoshita, S.; Miyamoto, T. Evaluation of the performance of the bogie to control the decrement of wheel load using the test line of RTRI. *RTRI Rep.* **2016**, *30*, 17–22. [[CrossRef](#)]
9. Hur, H.M.; You, W.H.; Kim, M.S.; Park, J.H. Active Steering Control Device and Method for Railroad Vehicle. Patent No. PCT/KR2010/005362, 30 July 2011.
10. Hur, H.M.; Park, J.H.; You, W. Curvature estimation method of curve section using relative displacement between body and bogie of rolling-stock. *Trans. Korean Soc. Mech. Eng. A* **2012**, *36*, 1479–1485. [[CrossRef](#)]
11. Sim, K.S.; Hur, H.M.; Song, H.S.; Park, T.W. Study of the Active Radial Steering of a Railway Vehicle using Curvature Measuring Method. *J. Mech. Sci. Technol.* **2014**, *28*, 4583–4591. [[CrossRef](#)]
12. Hur, H.M.; You, W.H.; Shin, Y.J.; Sim, K.S.; Park, T.W. Analysis on the actuator force of active steering bogie for radial steering. In Proceedings of the KSPE Spring Conference, Jeju, Korea, 14–16 May 2014; p. 994.
13. Ahn, D.H.; Hur, H.M.; Park, J.H.; Choi, J.H. Design of an actuation system for an active steering bogie. In Proceedings of the KSPE Autumn Conference, Changwon, Korea, 29–31 October 2014; pp. 751–752.
14. Hur, H.M.; Ahn, D.H.; Shin, Y.J. Steering performance evaluation of active steering system for a railway vehicle by simulating real track running. *Int. J. Precis. Eng. Manuf.* **2018**, *19*, 1487–1494. [[CrossRef](#)]
15. Hur, H.M.; Shin, Y.J.; Ahn, D.H. Steering Performance Evaluation of Active Steering Bogie to Reduce Wheel Wear on Test Line. *Int. J. Precis. Eng. Manuf.* **2019**, *10*, 35–41. [[CrossRef](#)]
16. Ham, Y.S.; Lee, D.H.; Kwon, S.J.; You, W.H.; Oh, T.Y. Continuous Measurement of Interaction Forces between Wheel and Rail. *Int. J. Precis. Eng. Manuf.* **2009**, *20*, 1591–1600. [[CrossRef](#)]
17. UIC 518 OR. *Testing and Approval of Railway Vehicles from the Point of View of Their Dynamic Behavior-Safety-Track Fatigue-Running Behavior*, 4th ed.; International Union of Railways: Paris, France, September 2009.



© 2020 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (<http://creativecommons.org/licenses/by/4.0/>).