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Imperfections of Scalar Approximation in Calibration of Computer-Generated Holograms for Optical Surface Measurements

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Abstract: Computer-generated hologram (CGH) null correctors are used as accuracy standards for interferometric measurements of optical surfaces and optical systems. Diffractive optics calibrators (DOCs) have been developed to evaluate the phase tolerance of CGHs based on scalar approximation by measuring variations in duty cycle and etching depth. However, if the grating period of a CGH $< 5\lambda$, the scalar approximation is not accurate for phase analysis and reconstruction. In this study, the measurement errors of DOCs with small-period CGHs were investigated and experimentally verified. Results show that the imperfections of scalar approximation in CGHs cannot be ignored and the development of rigorous evaluation methods to improve the measurement accuracy of CGHs is of great practical significance.



Citation: Bai, Y.; Zhang, Z.; Wang, R.; Chen, T.; Wang, X.; Zhang, X.

Imperfections of Scalar Approximation in Calibration of Computer-Generated Holograms for Optical Surface Measurements. *Appl. Sci.* **2021**, *11*, 6897. <https://doi.org/10.3390/app11156897>

Academic Editor: Hiroshi Yoshikawa

Received: 1 July 2021

Accepted: 24 July 2021

Published: 27 July 2021

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Keywords: computer-generated hologram; optical testing; diffraction optics

1. Introduction

Astronomy is an ancient science that has far-reaching and wide-ranging effects on human beings. However, further development in this field requires new advanced experimental equipment. Astronomical telescopes are an indispensable tool for observing distant planets, galaxies, and other astronomical objects. Aspherical and freeform optics have been extensively used in astronomical telescopes to improve imaging performance, reduce size, and minimize weight [1]. For example, our research team produced a SiC aspherical mirror with a form accuracy and a root-mean-square (RMS) of 18 nm over a 4 m aperture [2,3]. However, aspheric surfaces cannot be measured directly using an interferometer. Instead, it is necessary to use a corrector to change a spherical wavefront to an aspherical one, and the interferometer can then be adopted for aspherical testing, as for a general sphere [4].

In recent years, diffractive optical elements have played an important role in the field of imaging systems [5], X-ray focusing [6], laser beam shaping [7] and optical system testing [8]. Computer-generated holograms (CGHs) are specially designed diffractive optical elements that can create reference wavefronts for arbitrary aspherical surfaces. They are convenient and efficient correctors used to test the form accuracy of aspherical mirrors. To some extent, the accuracy and validity of interferometric measurements depend on the accuracy of the CGHs. Therefore, CGH fabrication errors must be budgeted or calibrated accurately.

The duty cycle and etching depth are two important geometric parameters of CGHs, which determine the diffraction efficiency and phase modulation. These geometric parameters of CGHs can be measured directly using a white light interferometer [9] or a scanning electron microscope [10]. However, these methods represent local micro-investigations, and they cannot be used to evaluate the accuracy of CGHs directly. Diffractive optics

calibrators (DOCs) are a promising method for the accurate measurements of CGHs based on spectroscopic scatterometry [11–13]. According to scalar approximation theory, the duty cycle and etching depth of the CGHs can be determined simultaneously by fitting the measured intensities from spectroscopic scatterometry to the grating parametric model [14]. However, the scalar approximation has imperfections for small-period structures that led to phase errors, which will cause the fitting results to be inaccurate in the DOCs as well.

This study aims to ascertain the measurement errors in DOCs using rigorous finite-difference time-domain (FDTD) simulations for cases when scalar approximation fails to accurately describe CGHs in optical testing. Measurements of the fabrication errors of two gratings will be used to verify the imperfections in the scalar approximation for the evaluation of CGHs. The results will show that the effects of imperfections cannot be ignored in small-period structures. There is great significance in the development of rigorous evaluation methods to improve the accuracy of CGH measurements.

2. Parametric Model and Methods

A binary linear grating model was selected as the simulation model, which was widely used to study the sensitivity of the wavefront to CGH fabrication errors [15–17]. The lithography process forms a sidewall slope in the microstructure of CGHs. Therefore, a trapezoidal geometry was introduced to describe a binary grating with a sidewall slope, as shown in Figure 1. For a normal incident plane wavefront of λ , the output wavefront function can be expressed according to [11],

$$u(x) = A_0 + (A_1 e^{i\phi} - A_0) \cdot \text{rect}\left(\frac{x}{d}\right) * \frac{1}{c} \text{rect}\left(\frac{x}{c}\right) * \frac{1}{S} \text{comb}\left(\frac{x}{S}\right) \quad (1)$$

where the symbol * represents the convolution operation and the related variables are defined in Figure 1.

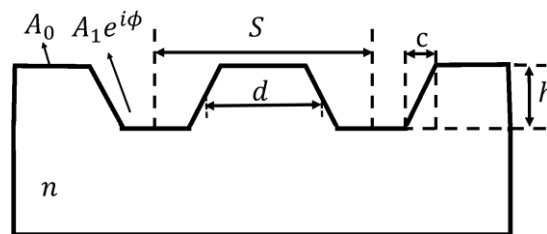


Figure 1. Cross-section of the binary linear grating model. Herein, S is the period, h is the etching depth, c is the project length of sidewall in the horizontal direction and d is the width of the grating ridge. The duty cycle D is defined as $D = d/S$ and the sidewall slope ratio L is given by $L = c/S$. In addition, A_0 and A_1 correspond to the amplitude of the output wavefront from the unetched and etched areas of the grating, respectively. For a phase grating made of a material with refractive index n , the phase step ϕ is defined as $2\pi(n - 1)h/\lambda$, where λ is the wavelength of incident light set to 632.8 nm.

According to the scalar diffraction theory, the far-field diffraction wavefront $U(\xi)$ is obtained via a simple Fourier transform of $u(x)$.

$$U(\xi) = F\{u(x)\} = \left\{ A_0 \delta(\xi) + [A_1 \cos(\phi) - A_0] \cdot D \cdot \text{sinc}(b\xi) \cdot \text{sinc}(c\xi) \cdot \sum_{m=-\infty}^{m=+\infty} \delta\left(\xi - \frac{m}{S}\right) \right\} + i \left\{ A_1 \sin(\phi) \cdot D \cdot \text{sinc}(b\xi) \text{sinc}(c\xi) \cdot \sum_{m=-\infty}^{m=+\infty} \delta\left(\xi - \frac{m}{S}\right) \right\} \quad (2)$$

Therefore, diffraction wavefronts of different orders can be written as follows:

$$U(\xi) = \begin{cases} \{A_0 + [A_1 \cos(\phi) - A_0] \cdot D\} + i\{A_1 \sin(\phi) \cdot D\} & m = 0 \\ \{[A_1 \cos(\phi) - A_0] \cdot D \cdot \text{sinc}(mD) \text{sinc}(mL)\} & m = \pm 1, \pm 2, \dots \\ + i\{A_1 \sin(\phi) \cdot D \cdot \text{sinc}(mD) \text{sinc}(mL)\} & \end{cases} \quad (3)$$

The diffraction efficiency η_{scalar} and output phase ψ_{scalar} can be obtained by,

$$\eta_{scalar} = \begin{cases} A_0^2(1 - D)^2 + A_1^2D^2 + 2A_0A_1D(1 - D) \cos(\phi) & m = 0 \\ \{A_0^2 + A_1^2 - 2A_0A_1 \cos(\phi)\} \cdot D^2 \sin^2(mD) \sin^2(mL) & m = \pm 1, \pm 2, \dots \end{cases} \quad (4)$$

and, as follows:

$$\tan \psi_{scalar} = \frac{\text{Im}\{U(\xi)\}}{\text{Re}\{U(\xi)\}} = \begin{cases} \frac{A_1D \sin(\phi)}{A_0(1-D) + A_1D \cos(\phi)} & m = 0 \\ \frac{A_1 \sin(\phi)}{-A_0 + A_1 \cos(\phi)} & m = \pm 1, \pm 2, \dots \end{cases} \quad (5)$$

If the periods of the CGHs are far larger than the wavelength, the scalar approximation is sufficiently accurate. However, it will exhibit imperfections for regions with small periods. The FDTD simulation is introduced for rigorous calculations, and the flow is illustrated in Figure 2. First, the structure group is constructed according to the parametric grating model. Periodicity is set as a boundary condition in the direction along which the gratings are arranged repeatedly. To calculate the electromagnetic field based on FDTD, the simulation region is discretized into spatial grids, and adjacent field components along any axis are separated by grid space steps of 1/2.

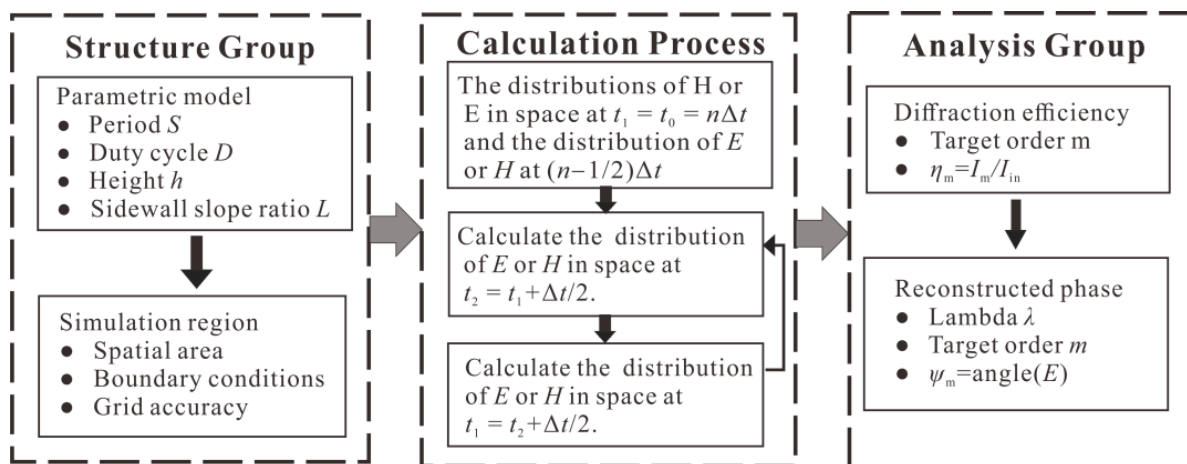


Figure 2. Process of rigorous simulations based on the finite-difference time-domain (FDTD) method. E and H denote the electric and magnetic fields, respectively.

The iterative calculation process is similar to the leapfrog calculation of the time step [18]. The numerical value of the electromagnetic field at the current moment can be obtained using the results of the electromagnetic field at the previous moment. Moreover, the numerical solution for the temporal varying electric and magnetic fields can be obtained by completing the calculation using this process for the entire space domain at each moment. Finally, analysis groups were established to calculate the transmission efficiency and phase based on the above calculations. Following this approach, the output results η_m and ψ_m for different orders m were obtained.

3. Imperfections of Scalar Approximation

3.1. Threshold Value

In DOCs, diffraction efficiencies are the most important reference data for fitting the parametric model to obtain local geometric parameters. Deviations in the intensity distribution directly affect the accuracy of the reconstructed surface relief. To compare the diffraction efficiencies, calculations were conducted for different order transmission gratings with duty cycles D of 0.5. The transmitted light becomes evanescent when the

grating period is less than the incident wavelength, thus the interval from λ to 10λ was discussed.

As shown in Figure 3a, the scalar results were similar to the rigorous values when the period was larger than 4λ . However, the scalar approximation was inaccurate when the period of the CGH was less than 4λ , and the deviation increased as the period decreased. As shown in Figure 3b, the diffraction efficiency was more sensitive to smaller period gratings.

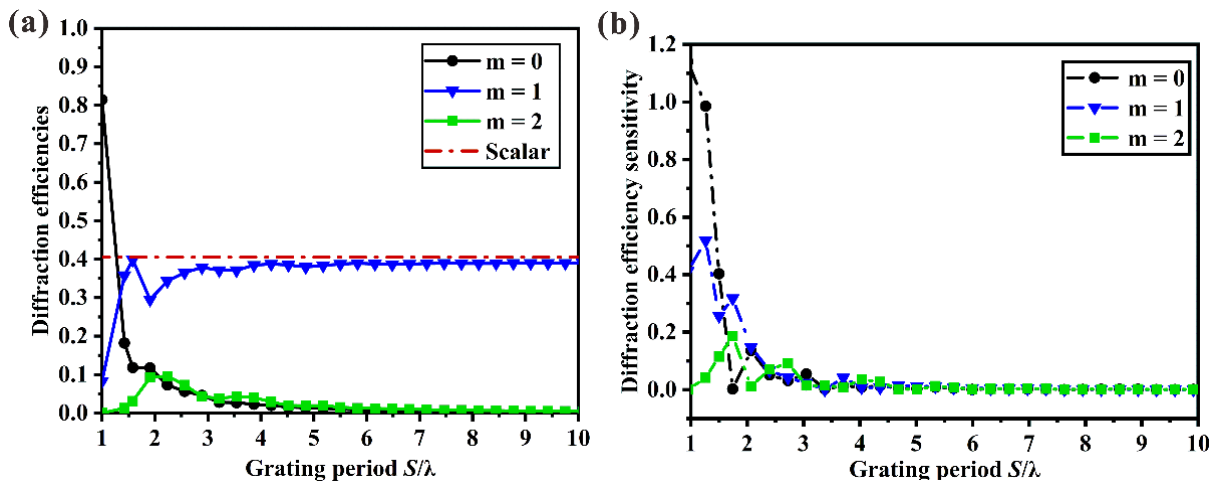


Figure 3. Comparison of the diffraction efficiency of scalar approximation and rigorous simulation for a binary grating with a duty cycle of 0.5. (a) Efficiencies of different orders ($m = 0, m = 1, m = 2$) and (b) sensitivity of the efficiencies of these orders with the respect to the period. The sensitivity function is defined as $\partial\eta_m/\partial S$.

In addition to the diffraction efficiency, the deviation in the transverse electric (TE) and transverse magnetic (TM) polarization calculation results is also different. Polarization must be considered in rigorous calculations, but it is completely ignored in scalar approximations. The calculated results for the first-order diffraction efficiency and phase variance with the grating period subject to TE and TM polarizations are shown in Figure 4. There is a sudden and significant change when the period is approximately equal to 2λ . This is a typical phenomenon caused by the redistribution of energy induced by the abrupt change in the electromagnetic field.

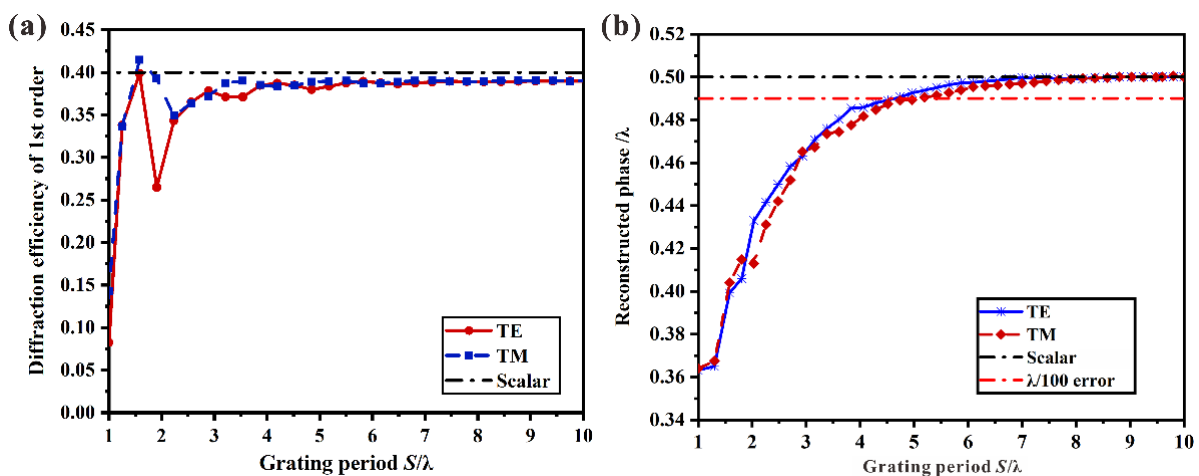


Figure 4. Comparison of illumination in transverse electric (TE) and transverse magnetic (TM) polarized light for (a) diffraction efficiency and (b) phase generated by transmission grating with a variable period.

In Figure 4b, the reconstructed phases subject to TE and TM polarizations are consistent. When the grating period approaches 5λ , the phase deviation between the approximation and rigorous results reaches $1/100\lambda$. In terms of the application of CGHs, the phase accuracy requirement is stricter than the diffraction efficiency. Therefore, the validity of the scalar approximation must be reconsidered when the grating period is less than $3\ \mu\text{m}$ ($\sim 5\lambda$).

3.2. Phase Sensitivity

Another notable imperfection of the scalar approximation for DOCs is the analysis of phase sensitivity. According to Equation (5), the phase reconstructed by scalar approximation is independent of the duty cycle D and sidewall slope L . However, as shown in Figure 5, it is significantly different from the rigorous calculation results for gratings with small periods. The depth of the grating corresponds to a 0.5 wavefront phase change in the simulation. As shown in Figure 5a, the reconstructed phase of the first order is a function of the period and duty cycle. The smaller the grating period, the more sensitive it is to the phase deviation caused by the duty cycle variation. The deviation between the scalar and rigorous phases was set to $1/100\lambda$ as a reference, and the range where the deviation meets the requirement decreased rapidly with decreasing periods.

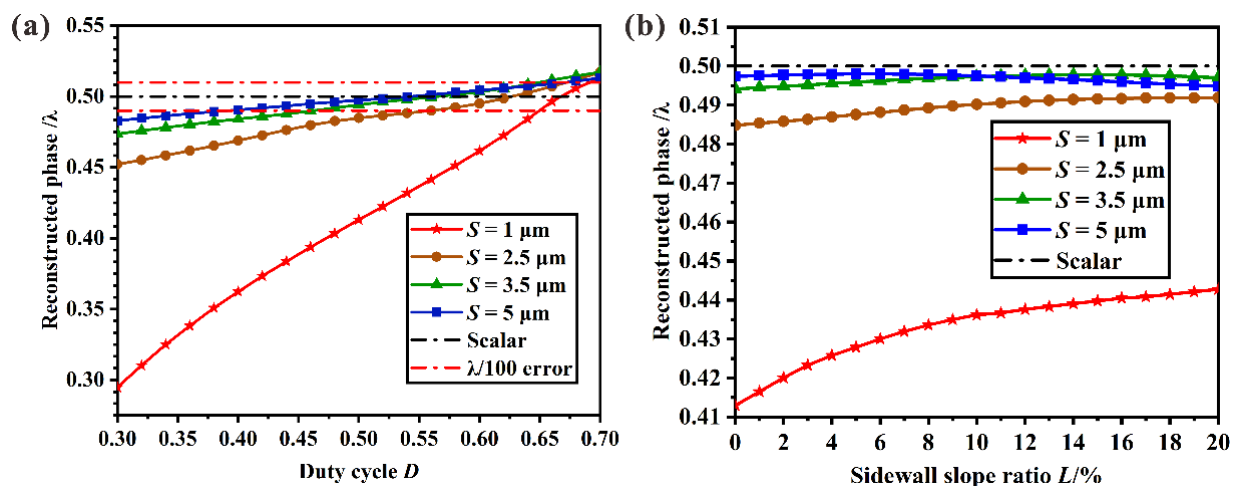


Figure 5. Reconstructed phase based on scalar approximation and rigorous simulation for the grating model with (a) a variable duty cycle or (b) a variable sidewall slope ratio, for different periods subject to TE polarization.

The reconstructed phase of the gratings with sidewall slope errors was also calculated by rigorous simulation, as shown in Figure 5b. The sensitivity of the phase error to the sidewall slope was still dependent on the grating period. Compared with the duty cycle error, the phase deviation caused by the sidewall slope was not obvious, and the fluctuation was globally controlled within $1/100\lambda$ for periods greater than $1\ \mu\text{m}$. Therefore, the phase error caused by the sidewall slope can be ignored.

3.3. Reconstruction Errors

In the above analysis, the scalar approximation has obvious imperfections in the diffraction efficiencies and phase sensitivity when the grating period is less than 5λ . These imperfections lead to errors in the geometric reconstruction of the etching depth and duty cycle of the DOC. Hence, these errors for 2, 4, and $6\ \mu\text{m}$ gratings were analyzed.

For geometric parameter reconstruction by the DOC, several data libraries of diffraction efficiencies were established based on rigorous calculations. Using the rigorous simulation method FDTD, the diffraction efficiencies of different orders $\eta_{\text{rig},i}$ were obtained for various duty cycles and etching depths. With the use of Equation (4), the scalar approximation data $\eta_{\text{scalar},i}$ were calculated, and the diffraction orders from 0 to 7 were selected

for geometric parameter reconstruction. The data libraries were searched for the minimum difference between η_{rig} and η_{scalar} , which corresponds to the duty cycle D and etching depth h , according to the following principle:

$$\min \left\{ \sum_{i=1}^7 |\eta_{rig,i}(D, h) - \eta_{scalar,i}(D_0, h_0)| \right\} \quad (6)$$

where

$$\Delta D = D - D_0 \text{ and } \Delta h = h - h_0 \quad (7)$$

As the period decreased, the deviations in the geometric parameters reconstructions obtained via scalar approximation and rigorous calculation increased. The reconstruction errors were 0.105 for duty cycle and 180 nm for etching depth with 2 μm period gratings. These deviations in the CGH measurement are unacceptable. For the duty cycle error in Figure 6a–c, the obvious reconstruction errors are concentrated in regions where the depth is large. The areas with obvious depth error distributions are concentrated at the two extremes of the small duty cycle in Figure 6d–f. Even though the reconstruction errors decrease as the period increases, the maximum depth error reaches 53 nm, even for a period of 6 μm . In DOCs, geometric errors in the surface relief reconstruction lead directly to the accuracy evaluation for the reference wavefront of a CGH. Thus, it affects the testing and machining accuracy of the aspheric mirrors.

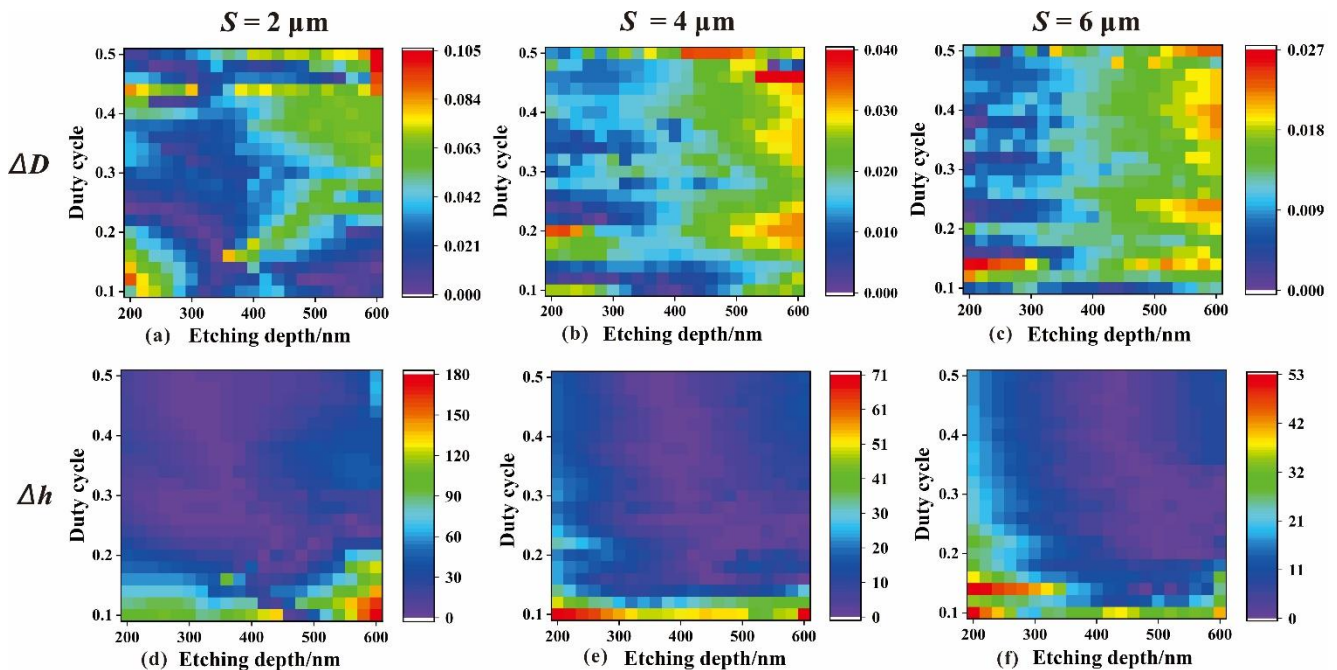


Figure 6. Reconstruction geometric errors for duty cycle D (0.1–0.5) and etching depth h (200–600 nm) with scalar approximation and rigorous calculations. (a–c) and (d–f) indicate the duty cycle errors ΔD and etching depth errors Δh in reconstruction for gratings with periods of 2, 4, or 6 μm , respectively. The step was set to 0.2 for the duty cycle D_0 and 20 nm for the depth h_0 . The sampling of the search step was 0.001 for D and 1 nm for h in the rigorous simulation. The values of the color bars indicate the deviation in D and h (nm).

Based on the above analysis, the deviation of the wavefront caused by reconstruction geometric errors due to the imperfections of scalar approximation in DOC was analyzed. The deviation is given by the absolute phase difference $\Delta\psi$ between the ideal grating and

the grating with variations in geometric parameters such as the duty cycle and etching depth. The wavefront deviation can be expressed as follows:

$$\Delta W_{error} = \frac{\Delta\psi}{2\pi} \quad (8)$$

Duty cycle errors within 10% and depth errors within 100 nm were introduced to the 2, 4, and 6 μm gratings. As shown in Figure 7a–c, the wavefront deviation caused by duty cycle errors was more sensitive to small-period gratings. A 10% duty cycle error in the 2 μm -period produced a wavefront deviation of 0.009λ . When the period was greater than 3 μm , the deviation caused by the duty cycle error was less than 0.005λ . Compared with the duty cycle, the depth error was the primary factor that affected the reference wavefront of the CGH. When the reconstruction depth error exceeds approximately 30 nm, the wavefront deviation is as high as 0.01λ even if the period is greater than 3 μm in Figure 7d–f. These results are vital for quality control during the DOC measurements. Therefore, it is necessary to pay attention to the imperfections of scalar approximation for CGH with small-period structures.

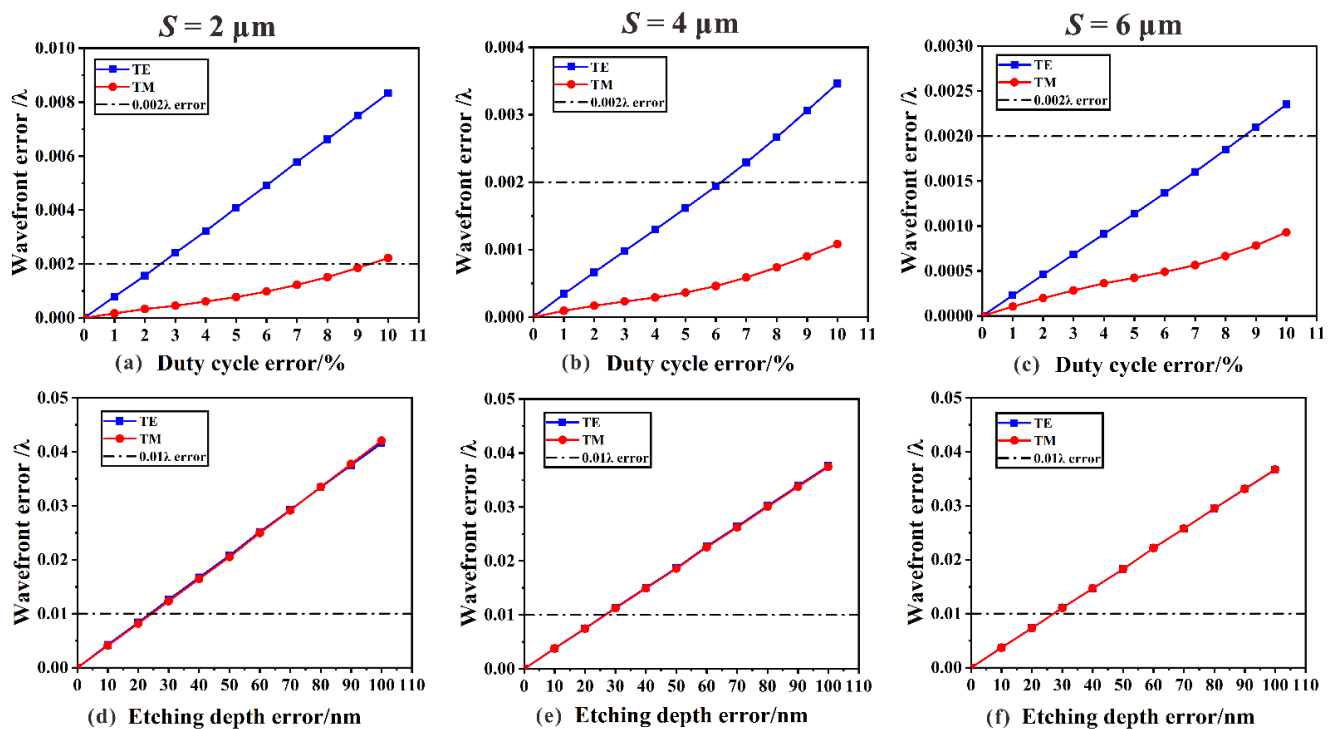


Figure 7. Wavefront deviations caused by errors in the duty cycle (a–c) or etching depth (d–f) from the geometric reconstruction of 2, 4, and 6 μm gratings. The duty cycle error was less than 10% and the depth error was less than 100 nm. The grating model had an etching depth of 400 nm and a duty cycle of 0.5.

4. Experimental Verification and Discussion

To verify the imperfections of scalar approximation, two gratings with periods of 2 and 4 μm were measured and compared experimentally. The design parameters included a duty cycle of 0.5 and an etching depth of 400 nm. They were manufactured using laser direct writing and scanning ion beam etching [19].

4.1. Profile Consistency of Gratings

Ten sample points of two experimental gratings were respectively measured to examine the profile consistency. A confocal microscope (OLS 4100, Olympus, Japan) with the objective lens MPLAPON100XLTEX was used to observe and measure the geometric parameters. The local profiles of the two gratings are shown in Figure 8 and the measurement

data are listed in Table 1. Meanwhile, the average (AVG) and standard deviation (STD) of measurement data were calculated. For linear gratings, the duty cycle D and etching depth h were the main sources of fabrication errors. The linewidth d was measured using the midpoint of the ridge as the reference.

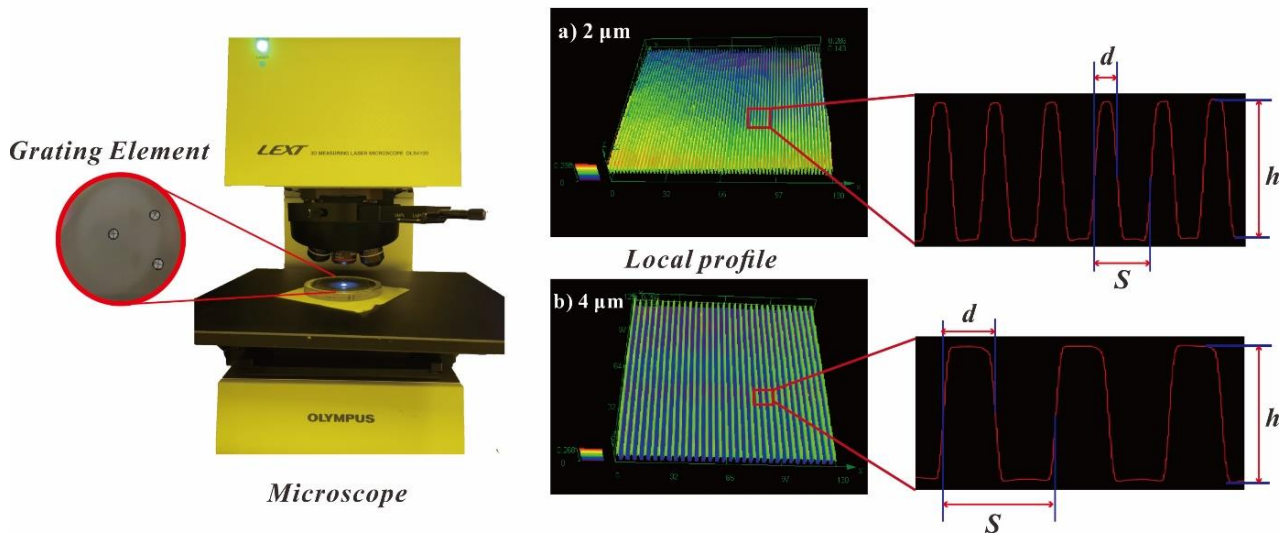


Figure 8. Parameter measurements for grating profiles observed with confocal microscopy. The lateral resolution of the confocal microscope was $0.12\ \mu\text{m}$ and the vertical was $0.01\ \mu\text{m}$. S , d and h represents period, ridge width and etching depth of gratings, respectively. (a,b) are the local profiles of $2\ \mu\text{m}$ and $4\ \mu\text{m}$ gratings.

Table 1. Measurement data for the gratings with periods of 2 and $4\ \mu\text{m}$.

Points	$S = 2\ \mu\text{m}$				$S = 4\ \mu\text{m}$			
	$S\ [\mu\text{m}]$	$d\ [\mu\text{m}]$	$h\ [\text{nm}]$	D	$S\ [\mu\text{m}]$	$d\ [\mu\text{m}]$	$h\ [\text{nm}]$	D
1	2.032	0.904	390	0.4449	4.064	1.829	392	0.4500
2	1.905	0.850	389	0.4462	3.937	1.772	390	0.4501
3	2.032	0.904	388	0.4449	4.064	1.829	393	0.4500
4	2.032	0.902	390	0.4439	4.064	1.832	391	0.4508
5	2.032	0.904	391	0.4449	4.064	1.829	391	0.4500
6	2.032	0.904	389	0.4449	3.937	1.772	390	0.4501
7	1.905	0.850	389	0.4462	4.064	1.829	392	0.4500
8	2.032	0.904	390	0.4449	4.064	1.832	392	0.4508
9	2.032	0.902	390	0.4439	3.937	1.772	391	0.4501
10	2.032	0.902	388	0.4439	4.064	1.829	393	0.4500
AVG	2.007	0.893	389	0.4448	4.026	1.812	391	0.4502
STD	0.054	0.022	1	0.0008	0.061	0.028	1	0.0003

According to the measurement data in Table 1, the etching depth is the main source of fabrication errors, and the depth errors of two gratings are all approximately equal to 10 nm. As for the duty cycle errors, the consistency of the $4\ \mu\text{m}$ grating is better than that of the $2\ \mu\text{m}$ grating. However, the duty cycle errors can be ignored in scalar approximation. Therefore, the evaluation results of the two grating wavefronts are almost the same based on scalar approximation.

4.2. Wavefront Aberrations Evaluation

To specify the errors of the gratings, an absolute interferometric test method based on a Fizeau interferometer was introduced. The He–Ne laser was operated at a wavelength

of 632.8 nm in the interferometer. The gratings were measured in reflection as shown in Figure 9, where the incident angle α and diffraction angle θ conform to:

$$S(\sin \alpha + \sin \theta) = m\lambda \tag{9}$$

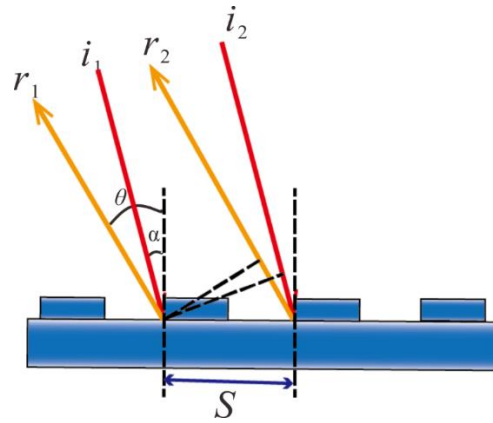


Figure 9. Linear grating in the case of reflection.

If α is equal to θ , the tested grating and interferometer would be collimated, and the incident wave diffracted back along the same optical path. The incident angle α of the plane wave satisfies the following equation:

$$\alpha = \arcsin\left(\frac{m\lambda}{2S}\right) \tag{10}$$

The light path for testing realized self-collimation. As shown in Figure 10, the wavefronts of the +1st (W_{+1}) and -1st (W_{-1}) diffracted orders were measured to determine the effects of fabrication errors.

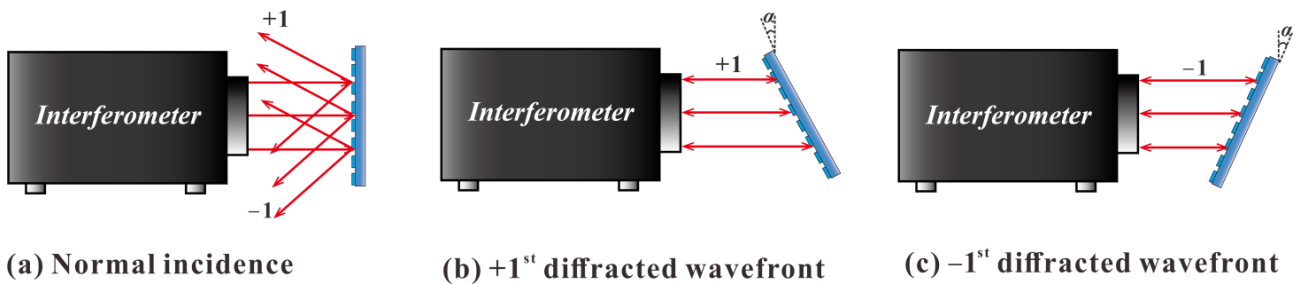


Figure 10. Schematics of the absolute test method for linear gratings. Optical configuration includes (a) normal incidence, (b) +1st diffracted wavefront and (c) -1st diffracted wavefront.

The direct measurement interferometry W_{+1} or W_{-1} contained aberrations from the interferometer system W_{inf} , the substrate surface figure error W_{sub} , and the fabrication error of elements W_{fab} . Thus, the wavefront of tests W_{+1} and W_{-1} can be respectively expressed by the following two equations:

$$W_{+1} = W_{inf} + W_{sub} + W_{fab+1} \tag{11}$$

and,

$$W_{-1} = W_{inf} + W_{sub} + W_{fab-1} \tag{12}$$

When the wavefront was generated in the -1^{st} diffracted order, the aberration of the fabrication errors was complementary to the $+1^{\text{st}}$ diffracted order. That is, as follows:

$$W_{fab-1} = -W_{fab+1} \tag{13}$$

Thus, the aberrations in W_{inf} and W_{sub} could be eliminated by subtracting Equation (12) from Equation (11), and the effect of the fabrication errors was obtained as follows:

$$W_{fab+1} = \frac{1}{2}(W_{+1} - W_{-1}) \tag{14}$$

Based on this absolute testing method, the wavefront quality evaluation of the two gratings was executed. The test results were recorded in Table 2. As shown in Figure 11, the wavefront aberration of the $4 \mu\text{m}$ grating had a RMS value of 0.005λ , while that of the $2 \mu\text{m}$ grating had a RMS value of 0.01λ . The wavefront of small period grating appears more sensitive to fabrication errors.

Table 2. The RMS values of test results in Figure 11.

	+1st Order/ λ	-1st Order/ λ	Final Result/ λ
S = 2 μm	0.016	0.017	0.010
S = 4 μm	0.011	0.011	0.005

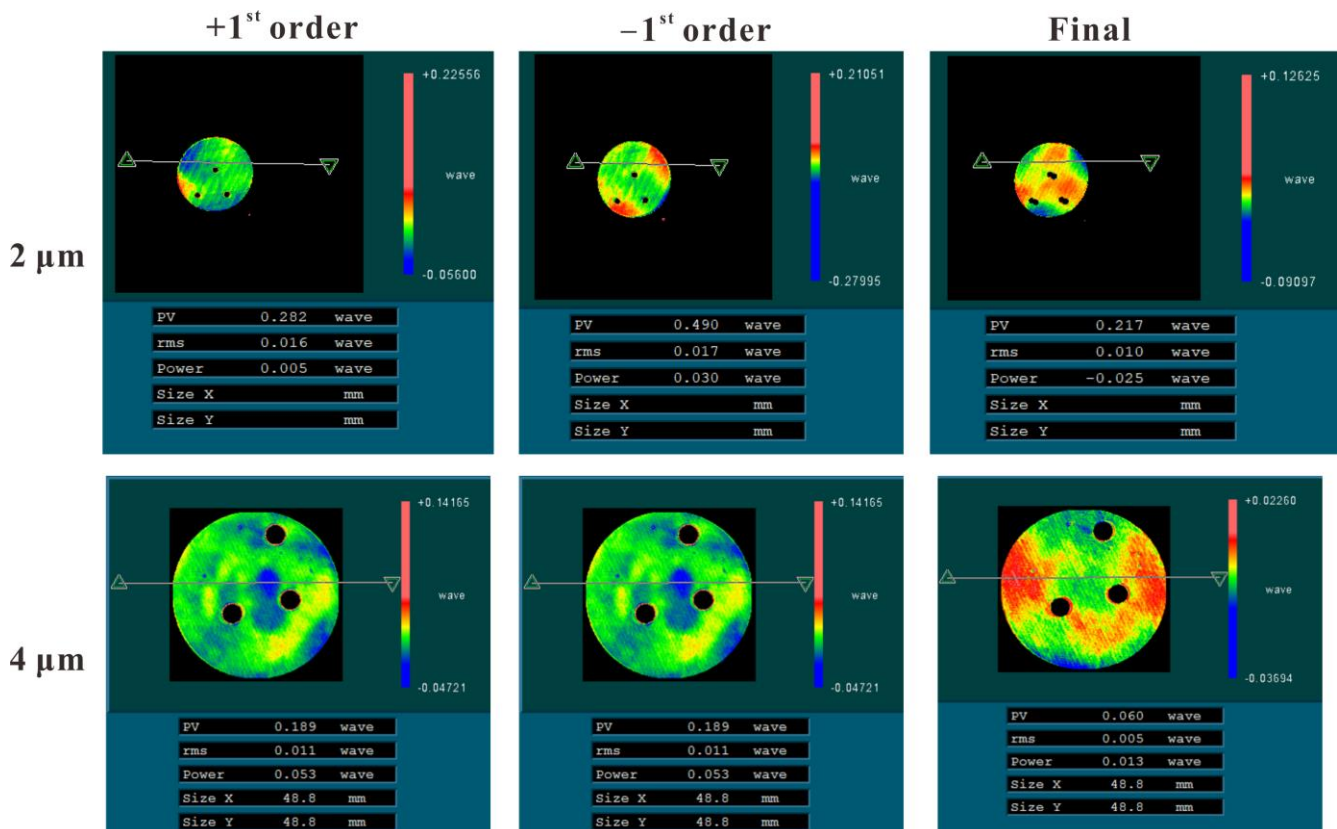


Figure 11. Wavefront aberration of ± 1 diffraction orders and final data for $S = 2$ and $4 \mu\text{m}$ grating elements caused by fabrication errors.

The wavefront aberrations of two gratings are distinguished, but the scalar approximation indicates that the wavefront aberrations are almost the same. Therefore, experimental

results show the inaccuracy of scalar approximation in measuring CGHs with small periods, and the imperfections cannot be ignored.

Conversely, the wavefront aberrations caused by duty cycle errors, which are not considered in scalar approximation, cannot be ignored according to our rigorous analysis in Section 3. The aberration of the 2 μm grating in Figure 11 is more serious than that of the 4 μm grating and proves the imperfections of scalar approximation for structures with small periods.

Scalar approximation fails to accurately describe and evaluate CGHs with small periods in optical testing due to the imperfections. If the rigorous methods can be promoted and developed, the reconstruction accuracy of CGH can be greatly improved. However, it is difficult to design CGHs with rigorous vector method today due to the complex description of light propagation and lack of no effective vector optimization methods. Based on the latest research results [20], we are now developing a more effective and flexible method to design perfect CGHs to solve the limitations of imperfections.

5. Conclusions

This study explored the imperfections of scalar approximation for diffractive optics calibrators in calibration of computer-generated holograms. The findings are summarized as follows:

- (1) When the grating period is less than 5λ , the scalar approximation fails to accurately describe the characteristics of CGH by diffractive optics calibrators.
- (2) Reconstruction geometric errors are concentrated in cases in which the period is small and the depth is large. For example, a 10% error for the duty cycle and a 180 nm error for the depth are introduced owing to the imperfections of scalar approximation in the 2 μm grating case.
- (3) Wavefront aberration is more sensitive to fabrication errors in small-period regions of a CGH, and the effect of the duty cycle error on the wavefront cannot be ignored.

In future, the developing method for CGHs with small periods to solve the imperfections of scalar approximation will be presented in another article.

Author Contributions: Performing conceptualization, investigation, experimental methodology and drafting the original manuscript, Y.B.; supervision, funding acquisition, writing—review & editing, Z.Z.; guiding the research conducted, treatment of the experimental data, R.W. and T.C.; resources, funding acquisition, X.W.; resources and project administration, X.Z. All authors have read and agreed to the published version of the manuscript.

Funding: This work was supported by the National Nature Science Foundation of China (Nos. 51775531, 11803037). This work was partially supported by the Advanced Science Key Research Project, Chinese Academy of Science (No. QYZDJ-SSW-JSC038), Key Foreign Cooperation Projects of International Cooperation Bureau, Chinese Academy of Science (181722KYSB20180015).

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: Not applicable.

Conflicts of Interest: The authors declare that they have no conflicts of interest.

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