Maximizing Efficiency in Smart Adjustable DC Link Powertrains with IGBTs and SiC MOSFETs via Optimized DC-Link Voltage Control

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Abstract: In recent years, the push towards electrifying transportation has gained significant traction, with battery-electric vehicles (BEVs) emerging as a viable alternative. However, the widespread adoption of BEVs faces multiple challenges, such as limited driving range, making powertrain efficiency improvements crucial. One approach to improve powertrain energy efficiency is to adjust the DC-link voltage using a DC-DC converter between the battery and inverter. Here, it is necessary to address the losses introduced by the DC-DC converter. This paper presents a dynamic programming approach to optimize the DC-link voltage, taking into account the battery terminal voltage variation and its impact on the overall powertrain losses. We also examine the energy efficiency gains of IGBT-based and silicon carbide (SiC) MOSFET-based adjustable DC-link voltage powertrains during WLTC driving cycles through PLECS and Matlab/Simulink simulations. The findings indicate that both IGBT and MOSFET-based adjustable DC-link voltage powertrains can enhance the WLTC drive-cycle efficiency up to 2.51% and 3.25% compared to conventional IGBT and MOSFET-based powertrains, respectively.

Keywords: battery-electric vehicle (BEV); DC-DC converter; dynamic programming; energy efficiency; silicon carbide (SiC) MOSFET

1. Introduction

The global trend towards electrification of transportation has gained significant momentum in recent years, with battery-electric vehicles (BEVs) emerging as promising alternatives to traditional internal combustion engine vehicles [1–3]. BEVs offer several advantages, including lower emissions, reduced dependence on fossil fuels, and the potential for improved vehicle performance. However, the widespread adoption of BEVs is hindered by several challenges, including limited driving ranges, high battery costs, and limited charging infrastructure [4–7]. One key strategy for overcoming these challenges is to improve the energy efficiency of the BEV powertrain.

A conventional battery-electric vehicle (BEV) powertrain comprises a traction battery, an electric machine (EM), and an IGBT inverter, as illustrated in Figure 1a. However, the dynamic behavior of the battery during vehicle operation cycles, such as variations in state of charge (SoC) and terminal voltage, can lead to a deterioration of the powertrain energy efficiency and performance, as reported in several studies [8–13]. To address the issues arising from battery voltage variation, a common solution is to incorporate a DC-DC converter (as depicted in Figure 1b) to decouple the DC-link voltage from the battery terminal voltage. This approach has been successfully implemented in commercial...
vehicles [14–16]. Additionally, the DC-link voltage can be dynamically adjusted by the DC-DC converter to further optimize the powertrain system efficiency.

![Figure 1. BEV powertrain topologies: (a) Conventional powertrain and (b) powertrain with the incorporated DC-DC converter.](image)

In order to extend the operating speed range of permanent magnet synchronous motors (PMSMs) and reduce copper losses, a DC-DC converter was proposed in [17,18] as a voltage booster between the battery and the inverter. However, the inverter experiences excessive switching loss with higher input DC voltage in low-speed regions [19,20]. This suggests that a lower DC-link voltage can improve inverter efficiency at low-speed operating conditions. Additionally, the DC-DC converter introduces additional loss with adjustable DC-link voltage. To increase overall powertrain efficiency across various operating conditions, the adjusted DC-link voltage should be optimized at a system-level perspective.

Extensive studies have investigated methods to enhance powertrain efficiency by optimizing the DC-link voltage. In previous research, the DC-link voltage was adjusted proportionally to the electric machine (EM) speed according to a mathematical motor model in [21,22], which was shown to improve efficiency. In [19], an online method was proposed for determining the optimal DC-link voltage to minimize losses in the motor and inverter, accounting for non-ideal PMSM effects, spatial harmonic effects, and temperature variation using the fundamental component (FC) model. Despite these advancements, the optimization process has not fully considered the additional loss introduced by the DC-DC converter. In [23], losses from both the buck converter and inverter were considered when searching for the optimal DC-link voltage. In [24], the PMSM d- and q-axis reference currents were mapped by minimizing powertrain losses using a linear PMSM mathematical model. However, most studies typically assumed a fixed battery terminal voltage when optimizing the DC-link voltage and neglect the external loading and SoC drop impact on battery terminal voltage. This might result in underestimated DC-DC converter loss when minimizing the overall powertrain loss. Therefore, further investigation is needed to develop an optimization method that considers the variation of the battery terminal voltage and corresponding DC-DC converter loss to achieve maximum powertrain efficiency under all driving conditions.

On the other hand, silicon carbide (SiC) MOSFETs have shown promise as a viable alternative to IGBTs in electrified vehicle applications in recent years due to their demonstrated ability to improve powertrain efficiency in conventional BEV powertrains [25,26]. MOSFETs exhibit reduced switching losses due to their fast switching transitions in comparison to IGBTs, which suffer from high switching losses induced by the current tail during turn-off events, especially at higher DC-link voltages [27]. Furthermore, MOSFETs can achieve lower conduction losses through their reverse conduction capability [28–30]. These low-loss characteristics of MOSFETs suggest that the energy-saving potential of adjustable DC-link voltage powertrains can be enhanced by utilizing SiC MOSFETs to further reduce unwanted additional DC-DC converter loss. However, to the best of the authors’ knowledge, there have been no comprehensive comparisons between IGBT-based adjustable DC-link voltage powertrain (with IGBT-based DC-DC converter and IGBT-based inverter) and SiC MOSFET-based adjustable DC-link voltage powertrain (with SiC MOSFET-based DC-DC converter and SiC MOSFET-based inverter). For convenience, the SiC MOSFET will be referred to simply as "MOSFET" in the rest of the paper.
Consequently, this paper proposes a DC-link voltage optimization method from a system-level perspective using dynamic programming (DP) for the adjustable DC-link voltage powertrain. The optimized DC-link voltage is used to explore and compare the energy-saving potential between IGBT and MOSFET-based powertrains. The main research contributions of this paper can be summarized as follows:

1. A DC-link voltage optimization method based on dynamic programming (DP) that minimizes overall powertrain losses is proposed, taking into account the impact of battery terminal voltage variation.

2. The energy efficiency of powertrains based on IGBTs and MOSFETs with adjustable DC-link voltage is compared and verified through simulations in PLECS. The effectiveness of the comparison was demonstrated under the WLTC.

The rest of the paper is organized as follows. First, in Section 2, the analytical loss model of each powertrain component is described, including the differentiation between IGBT and MOSFET-based power electronics, meanwhile Section 3 illustrates the derivation of optimized DC-link voltage used in the study, followed by Section 4 where the simulation results are shown and discussed. In Section 5 the conclusion of the study is drawn.

2. Analytical Powertrain Model

In this section, the powertrain component losses are analytically modeled, based on which the numerical optimization of DC-link voltage can be carried out in the later section.

2.1. Electric Machine

The EM used in this study is an interior permanent magnet synchronous machine (IPMSM), as shown in Figure 2. The main parameters of the IPMSM are listed in Table 1, given a 350 V DC-link voltage.

![Figure 2. Illustration of IPMSM used in this study.](image)

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Description</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_s$</td>
<td>Number of slots</td>
<td>48</td>
<td>-</td>
</tr>
<tr>
<td>$N_p$</td>
<td>Number of poles</td>
<td>8</td>
<td>-</td>
</tr>
<tr>
<td>$V_{dc}$</td>
<td>DC-link voltage</td>
<td>350</td>
<td>V</td>
</tr>
<tr>
<td>$I_{max}$</td>
<td>Peak current</td>
<td>820</td>
<td>A</td>
</tr>
<tr>
<td>$\omega_s$</td>
<td>Base speed</td>
<td>3500</td>
<td>RPM</td>
</tr>
<tr>
<td>$\omega_{max}$</td>
<td>Maximum speed</td>
<td>14,000</td>
<td>RPM</td>
</tr>
</tbody>
</table>

For IPMSMs, the widely utilized maximum-torque-per-ampere (MTPA) control strategy enables the delivery of specific torques at a certain speed while minimizing the current...
usage, which in turn cuts down on the copper loss in the EM. This strategy, however, is subjected to the supplied DC voltage, as illustrated in Figure 3. In the d- and q-axis current \((I_d - I_q)\) plane, the voltage limit imposed by the DC voltage supplied is represented as an ellipse. The corresponding speed, also denoted as base speed \((\omega_s)\), marks the highest speed at which the motor can maintain the MTPA strategy and adhere to the voltage constraint. When operating beyond the base speed, the field weakening strategy is employed by injecting the negative \(I_d\) to reduce the rotor flux. This allows for higher speeds within voltage constraints but results in increased motor losses and reduced torque output, as the motor operates outside its optimal MTPA range.

![Figure 3. Illustration of maximum-torque-per-ampere (MTPA) control strategy.](image)

With the higher supplied DC voltage, the ellipse in the \(I_d - I_q\) plane becomes larger, and the corresponding base speed also increases. This expansion allows the MTPA area to cover a broader speed range. Within the confines of the voltage constraint and MTPA area, the \(I_d\) and \(I_q\) currents remain relatively unaffected by changes in DC voltage. Consequently, copper loss stays constant despite variations in the supplied DC voltage.

To address the non-linearity of IPMSMs and accurately represent losses, such as AC copper loss and iron loss, finite element analysis (FEA) simulations are employed to calculate the EM losses and the corresponding d- and q-axis reference currents for the MTPA control strategy. The calculations consider a range of supplied DC voltages, spanning from 250 V to 450 V. 250 V and 450 V values act as lower and upper boundaries for the DC-link voltage in this study, which are further discussed in Section 3.1.2. The resulting loss data and d- and q-axis reference currents are stored in a three-dimensional map, with the EM speed, EM torque, and DC-link voltage as reference points. Figure 4 provides an example of the EM loss and corresponding efficiency maps when EM is supplied with 250 V and 450 V DC voltages, respectively.
Figure 4. Voltage-variant characteristic EM maps: (a) Power loss with 250 V DC-link voltage, (b) power loss with 450 V DC-link voltage, (c) efficiency with 250 V DC-link voltage, and (d) efficiency with 450 V DC-link voltage.

2.2. Three-Phase Inverter

Since the operating points of the EM for the investigated drive cycle, discussed in Section 4, are far below the nominal power rating of the inverter, the junction temperatures of the transistors and diodes change only slightly over the drive cycle. Thus, for simplicity, the effect of temperature variation on the losses is omitted in the analytical loss model of the inverter as well as the DC-DC converter described in Section 2.3, and the parameters used for transistors and diodes are obtained at a constant junction temperature of 65 °C.

The losses of the IGBT-based three-phase inverter comprise conduction and switching losses of both the insulated gate bipolar transistors (IGBTs) and their anti-parallel diodes, which can be analytically calculated with the following equation [31,32]:

\[
P_{\text{inv,loss,IGBT}} = P_{\text{cond,IGBT}} + P_{\text{cond,diode}} + P_{\text{sw,IGBT}} + P_{\text{sw,diode}}
\]

\[= 6V_{ce0}I_o\left(\frac{1}{2\pi} + \frac{M \cos \phi}{8}\right) + 6r_{ce}I_o^2\left(\frac{1}{8} + \frac{M \cos \phi}{3\pi}\right)
\]

\[+ 6V_{do}I_o\left(\frac{1}{2\pi} - \frac{M \cos \phi}{8}\right) + 6r_{do}I_o^2\left(\frac{1}{8} - \frac{M \cos \phi}{3\pi}\right)
\]

\[+ 6(E_{on} + E_{off})f_{sw}\left(\frac{I_o}{\pi I_{ref}}\right)\left(\frac{V_{dc}}{U_{ref}}\right)^{1.3} + 6E_{rec}f_{sw}\left(\frac{I_o}{\pi I_{ref}}\right)\left(\frac{V_{dc}}{U_{ref}}\right)^{0.6}
\]

where \(V_{ce0}\) is the estimated IGBT forward voltage drop (diode voltage drop behavior from collector to emitter) at zero current, \(I_o\) is the amplitude of AC phase current, \(M\) is the modulation index, \(\cos \phi\) is the power factor, \(r_{ce}\) is IGBT on-state resistance, \(V_{do}\) is the diode
forward voltage drop, $r_d$ is the diode on-state resistance, $V_{dc}$ is DC-link voltage, $f_{sw}$ is the switching frequency, $I_{ref}$ is the reference current used for linearizing the switching loss, $U_{ref}$ is the reference voltage used for linearizing the switching loss, $E_{on}$ is the transistor turn-on loss, $E_{off}$ is transistor turn-off loss and $E_{rec}$ is the diode reverse recovery energy. The IGBT power module selected for this study is the six-pack FS820R08A6P2B from Infineon, with its parameters available in the datasheet.

Compared to IGBT, MOSFETs have a lower current handling capability due to the underdeveloped wafer process technology of MOSFETs and the unavailability of large die sizes for the high current carrying capacity at present [33]. Consequently, in the presented study, two SiC MOSFET CAS300M12BM2 half-bridge modules are connected in parallel for each phase leg. This arrangement ensures the same current rating compared to FS820R08A6P2B and covers the worst operating point of the EM.

Due to the reverse conduction capability of MOSFETs, the MOSFET-based three-phase inverter operates differently during the reverse conduction period depending on the current condition [28,29,34]. For the presented case, the voltage drop across the transistor on-state resistance, $r_{ds}$, is always smaller than the forward voltage drop of the body diode, $V_{sd0}$, according to

$$I_o \cdot r_{ds} = 325 A \cdot 5.14 m\Omega < V_{sd0} = 1.76 V \quad (2)$$

Therefore, it can be assumed that the body diodes of the MOSFETs do not conduct the reverse current during the reverse conduction period; hence, the conduction losses only occur on the transistors. The corresponding three-phase inverter losses can be obtained with the following equation:

$$P_{inv,loss,MOSFET} = P_{cond,MOSFET} + P_{sw,MOSFET} = 12 \left( \frac{1}{4} \right) \left( \frac{I_o}{2} \right)^2 r_{ds} + 12(E_{on} + E_{off}) f_{sw} \left( \frac{I_o}{2 \pi I_{ref}} \right) \left( \frac{V_{dc}}{U_{ref}} \right)^{1.4} \quad (3)$$

where $r_{ds}$ is the MOSFET on-state resistance.

2.3. DC-DC Converter

The adjustable DC-link voltage investigated in this study is realized by a bidirectional boost DC-DC converter as already illustrated in Figure 1. This setup enables boost operation from the battery terminals to the DC-link and buck operation from the three-phase inverter to the battery terminal, corresponding to the propulsion and regeneration modes of electric vehicles, respectively.

For an IGBT-based converter, the losses can be calculated analytically as follows:

$$P_{DCDC,loss,IGBT} = P_{cond,IGBT} + P_{cond,diode} + P_{sw,IGBT} + P_{sw,diode} = \left( V_{ce0} I_{bat} + r_{ce} I_{bat}^2 \right) D + \left( V_{d0} I_{bat} + r_d I_{bat}^2 \right) (1 - D)$$

$$+ E_{sw} I_{bat} \frac{f_{sw}}{I_{ref}} \left( \frac{V_{dc}}{U_{ref}} \right)^{1.3} + E_{rec} I_{bat} \frac{f_{sw}}{I_{ref}} \left( \frac{V_{dc}}{U_{ref}} \right)^{0.6} \quad (4)$$

where $I_{bat}$ denotes battery current with the assumption that the amplitude is constant during one pulse period and current fluctuation is filtered by the inductor and $D$ is the duty cycle. The duty cycle $D$ can be calculated as:

$$D = \begin{cases} \frac{V_{bat}}{V_{dc}} & \text{buck operation} \\ 1 - \frac{V_{bat}}{V_{dc}} & \text{boost operation} \end{cases} \quad (5)$$

For a MOSFET-based converter, the losses can be calculated analytically as follows when MOSFETs’ reverse conduction capability is utilized (parallel conduction of diode is neglected according to (2)):
\[ P_{\text{DCDC,loss,MOSFET}} = P_{\text{cond,MOSFET}} + P_{\text{sw,MOSFET}} \]
\[ = r_{ds}I_{\text{bat}}^{2} + (E_{\text{on}} + E_{\text{off}})f_{\text{sw}} \left( \frac{I_{\text{bat}}}{I_{\text{ref}}} \right) \left( \frac{V_{dc}}{U_{\text{ref}}} \right)^{1.4} \] (6)

2.4. Battery

To keep capturing the dynamic behavior of the battery and the corresponding variations in the terminal output under different operating conditions, the battery is modeled simply as an equivalent electric circuit consisting of an open circuit voltage \( V_{\text{oc}} \) and an internal resistance \( R_{i} \) [35–37]. The battery open circuit voltage and internal resistance are dependent on the state of charge as illustrated in Figure 5. Therefore, the battery is only subject to ohmic losses due to the presence of internal battery resistance, which can be described as follows:

\[ P_{\text{bat,loss}} = I_{\text{bat}}^{2}R_{i} \] (7)

Moreover, the battery terminal voltage can be rewritten as:

\[ V_{\text{bat}} = V_{\text{oc}} - I_{\text{bat}}R_{i} \] (8)

![Figure 5. Battery pack data tested under charge and discharge conditions: (a) Open circuit voltage and (b) internal battery resistance relative to the battery SoC.](image)

3. DC-Link Voltage Optimization

In order to fully optimize powertrain efficiency across various operating conditions by adjusting the DC-link voltage, it is essential to consider the losses of the entire powertrain, including the additional losses of the DC-DC converter, as well as the impact on the battery voltage variation.

DP algorithm is a powerful optimization tool that has been extensively used in recent years to develop optimal control strategies for energy management systems in electrified vehicle applications [38–40]. It is suitable for decision-making scenarios where choices are made at each stage to minimize or maximize a specific cost function and obtain a globally optimal solution. In this section, the DP method to determine the optimal DC-link voltage for specific drive cycles is described.

3.1. Problem Formulation

3.1.1. Vehicle Dynamics

In EV applications, the motor operating points can be quickly determined by longitudinal vehicle dynamics during a predefined driving cycle which is a standardized sequence of vehicle speed and power levels that represent typical driving conditions and usages of the vehicle. The opposing force to a vehicle’s motion in the longitudinal direction is comprised of four terms: gradient resistance, aerodynamic resistance, tire rolling resistance,
and acceleration contribution. To balance these resistance terms, traction torque from EM is calculated as:

\[
\text{Tract. force} = \frac{T_m i \eta}{R_t} = mg \sin(\theta) + \frac{1}{2} \rho_{\text{air}} C_d A_f v_o^2 + C_r m g \cos(\theta) + m \ddot{v} \tag{9}
\]

where \(T_m\) is the EM torque, \(i\) is the transmission ratio between EM and wheel, \(\eta\) is the transmission efficiency, \(R_t\) is the tire rolling radius, \(m\) is the vehicle mass, \(g\) is the gravitational acceleration, \(\theta\) is the road gradient, \(\rho_{\text{air}}\) is the air density, \(C_d\) is the aerodynamic drag coefficient, \(A_f\) is the vehicle frontal area, \(v\) is the vehicle speed, and \(C_r\) is the tire rolling resistance coefficient. The EM speed is calculated as:

\[
\omega_m = \frac{60 vi}{2\pi R_t} \tag{10}
\]

The main parameters of the vehicle investigated in this study are listed in Table 2.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Description</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>(m)</td>
<td>Vehicle mass</td>
<td>2640</td>
<td>kg</td>
</tr>
<tr>
<td>(C_d)</td>
<td>Aerodynamic resistance coefficient</td>
<td>0.372</td>
<td>-</td>
</tr>
<tr>
<td>(A_f)</td>
<td>Frontal area</td>
<td>2.8</td>
<td>m²</td>
</tr>
<tr>
<td>(R_t)</td>
<td>Tire rolling radius</td>
<td>377</td>
<td>mm</td>
</tr>
<tr>
<td>(C_r)</td>
<td>Tire rolling resistance coefficient</td>
<td>0.01</td>
<td>-</td>
</tr>
</tbody>
</table>

3.1.2. DC-Link Voltage Operating Range

In an adjustable DC-link voltage powertrain, the DC-link voltage is considered a degree of freedom. However, the choice of DC-link voltage must be compatible with other powertrain components, necessitating the determination of upper and lower operating boundaries for the DC-link voltage. The blocking voltage of the chosen IGBT pack is 750 V. In order to protect the power module from potential damage caused by voltage spikes occurring during switching events, a safety margin is incorporated. As a result, the upper boundary of the DC-link voltage operating range is set at 450 V for the IGBT-based powertrain. Conversely, while the MOSFET module can handle a 1200 V voltage level, significantly higher than IGBT, the study focuses on a generalized comparison of powertrain energy efficiency gains resulting from the MOSFET’s low-loss characteristic. This approach avoids emphasizing substantial loss reduction in the EM by raising the DC-link voltage to an excessively high level, which could lead to insulation issues in the EM winding. Therefore, for the MOSFET-based powertrain, the upper boundary of the DC-link voltage operating range remains at 450 V, consistent with the IGBT-based powertrain.

Regarding the lower boundary, the worst-case scenario is considered when the battery is depleted to the minimum SoC, which in this case is 10%. This corresponds to a 280 V open circuit voltage, as shown in Figure 5a. If the vehicle undergoes a high-power demand operation, such as full-throttle acceleration, a 10% voltage drop may occur due to internal resistance, resulting in the lowest DC-link voltage reaching as low as 250 V. Consequently, the operating range of DC-link voltage is defined as between 250 V and 450 V.

3.1.3. Dynamic Programming

The optimization target for the adjustable DC-link voltage powertrain is to determine the optimal control input \(u(k)\), which is the DC-link voltage at each stage \(k\), which minimizes the powertrain losses during each stage of a specific driving cycle. The powertrain losses of interest include battery loss, DC-DC converter loss, inverter loss, and EM loss, as explained in Section 2. For the EM and inverter, the losses can be obtained in relation to the EM operating speed and torque under a specific DC-link voltage \(V_{dc}\). However, the DC-DC...
converter and battery losses are influenced by the battery current and voltage, which are affected in turn by the DC-DC converter loss. Therefore, in order to calculate the battery and converter losses, it is necessary to compute the battery current first. To do so, the power balance at the DC-link is taken into account as:

\[ P_{\text{bat}} - P_{\text{DCDC,loss}} = P_{\text{inv,loss}} + P_{\text{EM,loss}} + P_{\text{mech}} \]  

where \( P_{\text{bat}} \) is the battery terminal voltage and \( P_{\text{mech}} \) is the mechanical power of the EM, which can be obtained as:

\[ P_{\text{mech}} = \omega_m T_m \frac{2\pi}{60} \]  

where \( \omega_m \) is the EM speed and \( T_m \) is the EM torque. The battery terminal power, \( P_{\text{bat}} \), can be rewritten as:

\[ P_{\text{bat}} = (V_{\text{oc}} - I_{\text{bat}} R_i) I_{\text{bat}} \]

For convenience, the right-hand side of (11) can be denoted as the DC-link power demand \( P_{\text{dc}} \), which is in reference to the DC-link voltage, EM speed, and EM torque, as:

\[ P_{\text{dc}}(V_{\text{dc}}, \omega_m, T_m) = P_{\text{inv,loss}}(V_{\text{dc}}, \omega_m, T_m) + P_{\text{EM,loss}}(V_{\text{dc}}, \omega_m, T_m) + P_{\text{mech}}(V_{\text{dc}}, \omega_m, T_m) \]

By combining (1) to (14), the battery current can be resolved as a cubic polynomial equation for an IGBT-based powertrain as:

\[ a I_{\text{bat}}^3 + b I_{\text{bat}}^2 + c I_{\text{bat}} + d = 0 \]  

and a quadratic equation for a MOSFET-based powertrain as:

\[ b I_{\text{bat}}^2 + c I_{\text{bat}} + d = 0 \]

where \( a, b, c, \) and \( d \) are the coefficients for the polynomial equations listed in Table A1 in Appendix A. This provides the possibility to determine the battery current, hence the corresponding DC-DC converter loss under different operating conditions and battery states during the DP process. Since \( V_{\text{oc}} \) and \( R_i \) are battery SoC dependent [41], the battery SoC is defined as a state variable \( x(k) \). Moreover, the propagation of \( x(k) \) is expressed in its discrete form for numerical optimization purposes:

\[ x_{k+1} = - \frac{I_{\text{bat},k}(x_k, u_k)}{Q_c} T_s + x_k, \quad k = 0, 1, \ldots, N - 1 \]

where \( Q_c \) is the battery capacity and \( T_s \) is the time step used in the DP algorithm. The cost function of the optimization problem, representing the accumulated overall powertrain losses, \( J \), can then be described as:

\[ \min J = \sum_{k=0}^{N-1} \left[ P_{\text{bat,loss}}(u(k), x(k)) + P_{\text{inv,loss}}(u(k), \omega_m, T_m) + P_{\text{EM,loss}}(u(k), \omega_m, T_m) + P_{\text{DCDC,loss}}(u(k), x(k)) \right] T_s \]

Moreover, the optimization problem is subject to the following constraints:

\[ 0.05 \leq \text{SoC} \leq 0.95 \]
\[ T_{m,\text{min}}(\omega_m, V_{\text{dc}}) \leq T_m \leq T_{m,\text{max}}(\omega_m, V_{\text{dc}}) \]
\[ V_{\text{bat}} \leq V_{\text{dc}} \leq 450 \text{ V} \]
\[ \max(I_{\text{bat,\text{min}}}, -820 \text{ A}) \leq I_{\text{bat}} \leq \min(I_{\text{bat,\text{max}}}, 820 \text{ A}) \]

A step-by-step description of the DP algorithm used in this study is presented in Table 3. As mentioned before, the algorithm aims to calculate the optimal DC-link voltage for each stage of a specific driving cycle to minimize powertrain losses.
Table 3. Step-by-step description of the applied DP algorithm.

<table>
<thead>
<tr>
<th>Step 1: Grid generation</th>
<th>Define state variable (battery SoC) grid ( x(k) \in [0.05 : 0.01 : 0.95] ) and control variable (DC-link voltage) grid ( u(k) \in [250 : 5 : 450] ).</th>
</tr>
</thead>
<tbody>
<tr>
<td>Step 2: Initialization</td>
<td>Set initial SoC ( x(0) ) and define the constraints of the problem.</td>
</tr>
<tr>
<td>Step 3: Discretization</td>
<td>At the stage of the time step ( k ), set battery SoC input ( x(k) ) and calculate the EM operating points ( (\omega(k), T_m(k)) ). Based on the sign of the torque, ( T_m(k) ), select the coefficients for polynomial Equations (15) or (16) listed in Table A1 for propulsion and regeneration cases, as well as the battery resistance ( R_i(x, k) ) on the ( x(k) ) and ( u(k) ) space grid.</td>
</tr>
<tr>
<td>Step 4: Determine battery current</td>
<td>Solve (15) or (16) and remove the infeasible roots to obtain the estimated battery current, ( I_{bat}(x, k) ). Then, calculate the battery terminal voltage ( V_{bat}(x, k) ) using (8) and remove the infeasible solutions where ( V_{bat}(x, k) ) is smaller than DC-link voltage ( u(k) ).</td>
</tr>
<tr>
<td>Step 5: Choose the optimal output at ( k )-th stage</td>
<td>Find out the optimal DC-link voltage ( u(k) ) with the minimum cost function, given in (18), at the current stage.</td>
</tr>
<tr>
<td>Step 5: Update ( x(k + 1) )</td>
<td>Update ( x(k + 1) ) based on the obtained ( u(k) ).</td>
</tr>
</tbody>
</table>

4. Simulation Results and Discussion

4.1. Drive Cycle Simulation Setup

A complete vehicle and powertrain model, including the detailed power electronics loss models and control, is established in PLECS and Simulink environment to verify the proposed topologies with optimized DC-link voltage for the adjustable DC-link voltage powertrain. In addition, the DP-based algorithm, achieving an optimized DC-link voltage, is implemented in MATLAB.

The control structure is shown in Figure 6. The DP optimization block takes vehicle speed information as input and generates optimized, time-sequenced DC-link voltage values. In this study, the complete 1800-s WLTC drive cycle is provided to the DP algorithm prior to the driving mission, allowing it to function as an offline optimization method for obtaining a globally optimal solution. This is because the WLTC drive cycle is a known standard, and the main aim of this paper is to examine the full energy efficiency gain potential of the optimized DC-link voltage. However, if necessary, the DP block can be adapted for online execution over a shorter time horizon, in conjunction with GPS data or velocity prediction algorithms [42,43]. The optimal reference DC-link voltage, \( V_{dc}^* \), highlighted with a turquoise line, is then sent to the DC-DC converter controller and field-oriented current controller of the IPMSM. The field-oriented current control scheme, including active damping (marked by the dashed green box) and anti-windup (marked by the dashed green box), is highlighted with blue lines. A description of the parameterization of the control parameters, such as the PI controller gains, can be found in [44]. The measured mechanical system quantities, such as the vehicle speed, \( v \), are highlighted with orange lines.
Figure 6. Schematic illustration of the inverter/PMSM and DC-DC converter control when using an optimized DC link voltage for the WLTC.

The energy efficiency of powertrains is significantly influenced by driving cycles, as demonstrated in previous studies [45, 46]. As mentioned before, the Worldwide Harmonized Light Vehicles Test Cycle (WLTC) is utilized as the test scenario in this study, given its comprehensive representation of urban and suburban driving conditions through its low, medium, high, and extra-high-speed sections, as illustrated in Figure 7.

Figure 7. WLTC vehicle speed profile.
To evaluate the efficiency gains provided by the adjustable DC-link voltage powertrain, which employs the optimal DC-link voltage obtained using the proposed optimization method, a baseline powertrain without a propulsion DC-DC converter is also simulated. Consequently, four distinct topologies are examined: (1) Baseline powertrain with an IGBT-based inverter, (2) adjustable DC-link voltage powertrain with IGBT-based DC-DC converter and inverter, (3) baseline powertrain with a MOSFET-based inverter, and (4) adjustable DC-link voltage powertrain with MOSFET-based DC-DC converter and inverter.

It is worth noting that the battery’s open circuit voltage can exhibit substantial variation, as shown in Figure 5a. This variation affects the battery terminal voltage during drive cycle operation, potentially leading to varying energy efficiencies for both baseline and adjustable DC-link voltage powertrains. To assess the impact of battery terminal voltage deviations resulting from different states of charge (SoC) on powertrain energy efficiency, initial battery SoC values of 20% and 80% are investigated in the simulations, representing low and high SoC scenarios.

4.2. Optimized DC-Link Voltage

The optimized DC-link voltage trajectories for the adjustable DC-link voltage powertrain from DP calculation and the DC-link voltage (battery terminal voltage) for the baseline powertrain are depicted in Figure 8. In addition, the corresponding powertrain component instantaneous loss power over the WLTC cycle for low battery SoC case is illustrated in Figure 9.

![Figure 8. Optimized DC-link voltage in adjustable DC-link voltage powertrain compared with DC-link voltage in baseline powertrain: (a) IGBT-based powertrains with low battery SoC, (b) MOSFET-based powertrains with low battery SoC, (c) IGBT-based powertrains with high battery SoC and (d) MOSFET-based powertrains with high battery SoC.](image-url)

It is observed that in all four cases, the optimal DC-link voltage of the adjustable DC-link voltage powertrain remains relatively low and is generally close to the battery terminal voltage during low-speed operating conditions. This outcome is anticipated because when the vehicle operates at a low speed that results in the EM running below its
base speed at the given battery terminal voltage (e.g., below 28 km/h at 280 V), the EM loss is insensitive to the DC-link voltage. Meanwhile, the current remains low enough that the power electronics’ switching losses become more dominant, which can be minimized by employing a lower DC-link voltage.

Conversely, in high-speed and extra-high-speed operating conditions, the optimal DC-link voltages for both IGBT and MOSFET-based adjustable DC-link voltage powertrains reach the upper boundary. It is observed that even when the battery SoC is at a higher level, resulting in a higher terminal voltage, it is still insufficient for the powertrain to operate at optimal efficiency. This occurs because, in high and extra-high-speed operations with significant current demand, the conduction losses in the EM winding and power electronics become more dominant than the switching losses of the power electronics. As a result, it is preferable to boost the DC-link voltage as high as possible.

On the other hand, during medium-speed operating conditions, the selection of the DC-link voltage becomes crucial for the powertrain’s energy efficiency from a system

![Figure 9. Simulated powertrain component loss power during the WLTC with 20% initial SoC: (a) DC-DC converter loss in IGBT-based powertrains, (b) DC-DC converter loss in MOSFET-based powertrains, (c) inverter loss in IGBT-based powertrains, (d) inverter loss in MOSFET-based powertrains, (e) EM loss in IGBT-based powertrains and (f) EM loss in MOSFET-based powertrains.](image-url)
perspective. This is because the magnitude of the switching losses in the power electronics is comparable to the conduction losses in the power electronics and the EM. Consequently, the IGBT-based adjustable DC-link powertrain exhibits different optimal DC-link voltages than the MOSFET-based powertrain, as the trade-off among the loss components largely depends on the characteristics of the chosen MOSFETs and IGBTs. Furthermore, it is worth noting that a smaller DC-link voltage boosting ratio is required for cases with a higher battery state of charge (SoC), as a higher battery terminal voltage is involved.

4.3. Energy Consumption and Breakdown of Energy Losses

The simulation results, including the drive cycle energy consumption and the individual powertrain component losses, are summarized in Table 4 and illustrated in Figure 10.

Table 4. Summary of the energy consumption and powertrain component losses obtained from simulations.

<table>
<thead>
<tr>
<th>Init. SoC</th>
<th>Powertrain</th>
<th>Battery [kJ]</th>
<th>DC-DC [kJ]</th>
<th>Inverter [kJ]</th>
<th>EM [kJ]</th>
<th>Energy cons. [kWh/100 km]</th>
<th>Diff</th>
</tr>
</thead>
<tbody>
<tr>
<td>20%</td>
<td>Baseline IGBT</td>
<td>574.41</td>
<td>-</td>
<td>705.08</td>
<td>1830.90</td>
<td>20.28</td>
<td>-</td>
</tr>
<tr>
<td></td>
<td>Adj. DC-link voltage IGBT</td>
<td>550.63</td>
<td>229.69</td>
<td>545.67</td>
<td>1356.46</td>
<td>19.77</td>
<td>2.51%</td>
</tr>
<tr>
<td>20%</td>
<td>Baseline MOSFET</td>
<td>561.47</td>
<td>-</td>
<td>250.95</td>
<td>1829.64</td>
<td>19.72</td>
<td>-</td>
</tr>
<tr>
<td></td>
<td>Adj. DC-link voltage MOSFET</td>
<td>532.94</td>
<td>57.60</td>
<td>156.76</td>
<td>1353.42</td>
<td>19.08</td>
<td>3.25%</td>
</tr>
<tr>
<td>80%</td>
<td>Baseline IGBT</td>
<td>420.95</td>
<td>-</td>
<td>675.05</td>
<td>1652.12</td>
<td>19.85</td>
<td>-</td>
</tr>
<tr>
<td></td>
<td>Adj. DC-link voltage IGBT</td>
<td>412.51</td>
<td>213.47</td>
<td>566.729</td>
<td>1358.52</td>
<td>19.62</td>
<td>1.16%</td>
</tr>
<tr>
<td>80%</td>
<td>Baseline MOSFET</td>
<td>413.34</td>
<td>-</td>
<td>214.79</td>
<td>1651.31</td>
<td>19.29</td>
<td>-</td>
</tr>
<tr>
<td></td>
<td>Adj. DC-link voltage MOSFET</td>
<td>402.26</td>
<td>47.58</td>
<td>150.45</td>
<td>1356.40</td>
<td>18.92</td>
<td>1.92%</td>
</tr>
</tbody>
</table>

The comparison between the baseline and adjustable powertrains, as well as the IGBT and MOSFET powertrains, reveals that when the battery has a low state of charge (SoC), adopting MOSFETs for the inverter in baseline powertrains results in a significant decrease in energy consumption over the WLTC cycle by around 2.8% for both low and high battery SoC levels. As reported in [26,34], MOSFETs achieve, on average, three times lower inverter losses. The energy consumption in IGBT-based powertrains is reduced by 2.51% with optimized DC-link voltage. Although the energy efficiency gain is significant in IGBT-based powertrains with adjustable DC-link voltage, this energy consumption reduction gain is further increased to 3.25% when it comes to MOSFET-based powertrains.

When considering high battery SoC levels, this trend remains the same. However, the efficiency improvement is slightly less compared to low battery SoC levels when adopting adjustable DC-link voltage. This is because baseline powertrains with high battery SoC already result in better powertrain efficiency, mainly due to large loss reductions in EMs and batteries with higher battery terminal voltages, as shown in Figure 10. Nevertheless, adjustable DC-link voltage powertrains still provide significant energy consumption reductions compared to baseline powertrains, with improvements of 1.16% to 1.92% for IGBT and MOSFET respectively.

Regarding the impact of battery SoC, when it drops from 80% to 20%, the energy consumption decreases by around 2.1% for both IGBT-based and MOSFET-based baseline powertrains. However, this energy efficiency deterioration due to battery SoC levels is mitigated when using adjustable DC-link voltage powertrains. The deterioration percentage decreases to around 0.8% for adjustable DC-link voltage powertrains, making the powertrain efficiency less sensitive to battery SoC. This implies that another advantage of the adjustable DC-link voltage powertrain is its ability to maintain similar energy efficiency regardless of battery SoC compared to baseline powertrains.
Upon examining Figure 10, it can be observed that the battery losses are similar for each case with the same battery SoC level. However, with a higher battery SoC, the higher open-circuit voltage results in a lower current, given a similar power level drawn from the battery. Consequently, this leads to a reduction in both the current and ohmic losses of the battery. Between the baseline powertrain and the adjustable DC-link voltage powertrain, the main contribution to the powertrain energy efficiency improvement comes from the EM loss reduction and a slight reduction in inverter losses, which outweighs the additional loss brought by the DC-DC converter. However, in the IGBT-based adjustable DC-link voltage powertrain, the additional DC-DC converter loss still constitutes a significant part of the powertrain losses. On the other hand, when MOSFETs are used in the adjustable DC-link powertrain, the same improved EM efficiency can be achieved as in the IGBT-based adjustable DC-link powertrain, but with much lower losses on the power electronics. The additional DC-DC converter losses are almost negligible, fully utilizing the energy-saving potential of the adjustable DC-link voltage powertrain while mitigating unwanted DC-DC converter losses.

5. Conclusions

This study investigated the potential for improving the energy efficiency of an adjustable DC-link voltage powertrain incorporated with a regular DC-DC boost converter. The utilization of a DC-link voltage adjustment during vehicle operation reduces the overall powertrain losses. The study proposed a DP-based optimization method that considers battery voltage variation during drive cycle operations. The study also assessed the impact
of IGBTs and MOSFETs on the energy-saving potential of the adjustable DC-link voltage powertrain. The energy efficiency improvement of the adjustable DC-link voltage powertrain with the optimized DC-link voltage from the proposed optimization method was verified through simulations carried out in PLECS and MATLAB/Simulink software.

The simulation results demonstrate significant energy efficiency improvements for both IGBT-based and MOSFET-based adjustable DC-link voltage powertrains compared to the reference IGBT-based and MOSFET-based powertrains. At high battery SoC levels, the total energy consumption is reduced by 1.16% and 1.92% over the WLTC cycle, respectively. However, when considering low battery SoC levels, the energy consumption reductions are even more substantial, with improvements reaching up to 2.51% and 3.25%, respectively. These findings indicate that the benefits of adjustable DC-link voltage in improving powertrain energy efficiency are further amplified when MOSFETs are adopted, building on the already observed improvements in baseline powertrains with MOSFET in comparison to IGBTs. The main drivers behind this efficiency improvement are the reductions in the EM and inverter losses. Moreover, the additional DC-DC converter loss is almost negligible when MOSFETs are used, which maximizes the energy-saving potential of adjustable DC-link voltage powertrains.

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Conflicts of Interest: The authors declare no conflict of interest.
### Appendix A

Table A1. Coefficients of polynomial equations for solving battery currents.

<table>
<thead>
<tr>
<th>Transistor Operation</th>
<th>Operation</th>
<th>a</th>
<th>b</th>
<th>c</th>
<th>d</th>
</tr>
</thead>
<tbody>
<tr>
<td>Propulsion boost</td>
<td>I_{ref} \cdot R_i \cdot r_d - I_{ref} \cdot R_i \cdot r_{ce}</td>
<td>I_{ref} \cdot V_{oc} \cdot r_{ce} + I_{ref} \cdot R_i \cdot V_{d0} - I_{ref} \cdot V_{oc} \cdot r_d - E_{sw} \cdot \left( \frac{V_{dc}}{V_{ref}} \right)^{1.3} \cdot \frac{V_{dc}}{I_{ref}}</td>
<td>-I_{ref} \cdot P_{dc} \cdot V_{dc}</td>
<td></td>
<td></td>
</tr>
<tr>
<td>MOSFET</td>
<td>Propulsion boost</td>
<td>-</td>
<td>r_{ds}</td>
<td>2 \cdot \frac{E_{sw} \cdot f_{sw}}{I_{ref}} \cdot \left( \frac{V_{dc}}{I_{ref}} \right)^{1.4}</td>
<td>P_{dc} - V_{oc} \cdot R_i</td>
</tr>
<tr>
<td>MOSFET</td>
<td>Regeneration buck</td>
<td>-</td>
<td>r_{ds} + R_i</td>
<td>-V_{oc} - 2 \cdot \frac{E_{sw} \cdot f_{sw}}{I_{ref}} \cdot \left( \frac{V_{dc}}{I_{ref}} \right)^{1.4}</td>
<td>P_{dc}</td>
</tr>
<tr>
<td>IGBT</td>
<td>I_{ref} \cdot R_i \cdot r_d - I_{ref} \cdot R_i \cdot r_{ce}</td>
<td>I_{ref} \cdot V_{oc} \cdot r_{ce} + I_{ref} \cdot R_i \cdot V_{d0} - I_{ref} \cdot V_{oc} \cdot r_d - E_{sw} \cdot \left( \frac{V_{dc}}{V_{ref}} \right)^{1.3} \cdot \frac{V_{dc}}{I_{ref}}</td>
<td>-I_{ref} \cdot P_{dc} \cdot V_{dc}</td>
<td></td>
<td></td>
</tr>
<tr>
<td>IGBT</td>
<td>Regeneration buck</td>
<td>I_{ref} \cdot R_i \cdot r_{ce} - I_{ref} \cdot R_i \cdot r_d</td>
<td>I_{ref} \cdot V_{oc} \cdot r_d + I_{ref} \cdot R_i \cdot V_{d0} - I_{ref} \cdot V_{oc} \cdot r_d - E_{sw} \cdot \left( \frac{V_{dc}}{V_{ref}} \right)^{1.3} \cdot \frac{V_{dc}}{I_{ref}}</td>
<td>-I_{ref} \cdot P_{dc} \cdot V_{dc}</td>
<td></td>
</tr>
</tbody>
</table>


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