Abstract: Concrete in saline or coastal settings exposed to freezing temperatures is frequently affected by coupling actions of sulfate assault and freeze–thaw degradation, reducing the service life of concrete structures significantly. This study conducted an accelerated freeze–thaw cycle test in pure water and Na₂SO₄ solution with a mass proportion of 5% to examine the coupling impact of sulfate freeze–thaw on the frost resistance of composite limestone powder (CLP) concrete. Combined with SEM and XRD methods, the performance degradation mechanisms of composite limestone powder (CLP) concrete in coupling sulfate freeze–thaw conditions were analyzed with a microscopic point of view. The findings demonstrated that limestone powder has a filling effect but the activity is low. When the content is 10~20%, the chemical response is higher than the physical response. The pozzolanic effect of fly ash and slag can improve the pore structure and improve the compactness of concrete. The “superposition effect” of limestone powder, fly ash, and slag can improve the frost resistance of CLP concrete. The scenario of salt freezing cycles has negative effects that are worse than those of water freezing cycles on the antifreeze performance of CLP concrete, including apparent morphology, mass loss, relative dynamic modulus of elasticity, and compressive strength. Sulfate’s activation effect boosts slag’s activity effect, which significantly promotes the antifreeze performance of concrete subjected to salt frozen cycles over water frozen cycles. The freeze–thaw damage model of CLP concrete under coupling sulfate freeze–thaw is established through theorem analysis and experiment statistics, laying a theoretical framework for the popularization and use of this concrete.

Keywords: sulfate freeze–thaw; composite limestone powder (CLP) concrete; antifreeze capacity; degradation law; damage model
Therefore, it is of great significance and value to study the effect of sulfate freeze–thaw coupling on the frost resistance of CLP concrete.

Studies have shown that limestone powder can play a role in filling, nucleation, chemistry, and dilution in concrete [10–14]. Fly ash and slag have certain pozzolanic effects on concrete [15,16]. Different types of mineral admixtures are mixed into concrete in proportion to realize the effective and reasonable matching of different particle sizes, different shapes, and different activities, so as to achieve the complementary purpose of the morphological effect, activity effect, and microaggregate effect. The resulting superposition effect can significantly improve the mechanical properties and durability of concrete [17,18]. In the sulfate attack test, due to the addition of limestone powder, the content of gypsum in the erosion product is increased, which leads to the expansion and cracking of concrete, the decrease in strength, and the decrease in sulfate attack resistance coefficient [19]. At the same water–binder ratio, the sulfate resistance of concrete decreases with the increase in limestone powder content [20]. When limestone powder is mixed with fly ash and slag, it shows a complementary synergistic effect, which can effectively improve the performance of concrete against sulfate attack [21,22].

In the freeze–thaw cycle test, due to the low activity of limestone powder, the content of hydration products in the unit volume of cement-based materials decreases, resulting in a decrease in the bond strength between aggregates and a decrease in the resistance to ice crystal expansion pressure. This further leads to the loss of concrete quality, and this quality loss is positively correlated with the amount of limestone powder. At the same time, the relative dynamic elastic modulus will also decrease [23–25]. For conventional strength grade concrete, the addition of limestone powder has little effect on its frost resistance, but it will lead to the reduction in cementitious materials and the loss of strength, thus affecting the durability of concrete. In order to make up for this problem, it can be compensated by reducing the water–binder ratio of limestone powder concrete [26]. As for low strength concrete, increasing the content of limestone powder from 0% to 20% can improve the resistance to chloride ion penetration but will reduce the frost resistance [27]. The results show that when the content of limestone powder is 5%, the mass loss rate is the smallest and the frost resistance is the highest. When the content of limestone powder is between 5% and 10%, the mass loss rate is lower than that of ordinary concrete and the frost resistance is higher than that of ordinary concrete. However, when the content of limestone powder increases to 15–20%, the mass loss rate of concrete exceeds that of ordinary concrete, and the performance will also be affected [28].

The above studies have confirmed that single or double doping of limestone powder, fly ash, slag, and other mineral admixtures in concrete can change the sulfate resistance and frost resistance of concrete. However, there are few studies on the variation of the frost resistance of CLP concrete mixed with limestone powder, fly ash, and slag under sulfate freeze–thaw coupling, and the interaction mechanism between compounds needs to be further clarified. Therefore, in this paper, the freeze–thaw cycle tests of CLP concrete with different blending ratios were carried out in pure water and Na2SO4 solution with mass fraction of 5%, respectively, to study the apparent morphology, mass loss, relative dynamic elastic modulus, and compressive strength of concrete. At the same time, the degradation mechanism of frost resistance of concrete is analyzed from the microscopic point of view. The freeze–thaw damage model of CLP concrete under sulfate freeze–thaw coupling is established, which provides a theoretical reference for the popularization and application of the concrete.
2. Materials and Methods

2.1. Materials

The test materials are as follows:

(1) Cementitious material: P.O 42.5 ordinary Portland cement, with specific surface area of 341 m$^2$/kg; limestone powder, with specific surface area of 450 m$^2$/kg; F1 grade coal fly ash, with specific surface area of 364 m$^2$/kg; S95 slag, with specific surface area of 435 m$^2$/kg.

(2) Aggregate: coarse aggregate is continuous graded crushed stone with particle size of 5~31.5 mm; the natural river sand is selected as the fine aggregate, with the fineness modulus of 2.69 and the apparent density of 2690 kg/m$^3$.

(3) Mixing water: commonly used tap water.

(4) Water reducer: PCA-I polycarboxylate high-performance water reducer with a value of 28% water reduction rate [5].

The mix ratio of CLP concrete is designed with reference to the corresponding national standard and the literature [29–31]. The detailed mix designs are shown in Table 1.

Table 1. Mix ratios of CLP concrete.

<table>
<thead>
<tr>
<th>Number</th>
<th>Water–Binder Ratio</th>
<th>Cement</th>
<th>Ground Limestone</th>
<th>Fly Ash</th>
<th>Slag</th>
<th>Sand</th>
<th>Stone</th>
<th>Water</th>
<th>Additives</th>
</tr>
</thead>
<tbody>
<tr>
<td>L0F0S0</td>
<td>0.49</td>
<td>345</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>765</td>
<td>1110</td>
<td>170</td>
<td>4.49</td>
</tr>
<tr>
<td>L10F0S0</td>
<td>0.49</td>
<td>310</td>
<td>35</td>
<td>0</td>
<td>0</td>
<td>765</td>
<td>1110</td>
<td>170</td>
<td>4.49</td>
</tr>
<tr>
<td>L20F0S0</td>
<td>0.49</td>
<td>276</td>
<td>69</td>
<td>0</td>
<td>0</td>
<td>765</td>
<td>1110</td>
<td>170</td>
<td>4.49</td>
</tr>
<tr>
<td>L20F30S0</td>
<td>0.49</td>
<td>173</td>
<td>69</td>
<td>103.6</td>
<td>0</td>
<td>765</td>
<td>1110</td>
<td>170</td>
<td>4.49</td>
</tr>
<tr>
<td>L20F15S15</td>
<td>0.49</td>
<td>173</td>
<td>69</td>
<td>51.8</td>
<td>51.8</td>
<td>765</td>
<td>1110</td>
<td>170</td>
<td>4.49</td>
</tr>
</tbody>
</table>

Note: In the table number, L refers to limestone powder, F refers to fly ash, S refers to slag, and the lower right is the replacement ratio. For example, “20” refers to the replacement of 20% cement with equal mass.

2.2. Methods

In this study, the rapid freeze–thaw cycle tests on CLP concrete were carried out in pure water and 5% Na$_2$SO$_4$ solution, respectively. The specific test scheme is shown in Table 2. According to the experimental scheme in Table 2, 12 groups of prism specimens with dimensions of 100 mm × 100 mm × 400 mm and 54 groups of cube specimens with dimensions of 100 mm × 100 mm × 100 mm were made. Each group has 3 samples which are used to test the apparent morphology, mass loss, relative dynamic elastic modulus, and compressive strength of CLP concrete after freeze–thaw cycle tests.

Table 2. Experimental scheme of sulfate freeze–thaw resistance of CLP concrete.

<table>
<thead>
<tr>
<th>Research Content</th>
<th>Number</th>
<th>Limestone Powder Mixing Amount (%)</th>
<th>Fly Ash Mixing Amount (%)</th>
<th>Slag Mixing Amount (%)</th>
<th>Number of Freeze–Thaw Cycles (Times)</th>
<th>Testing Numbers (Groups)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Relative dynamic elastic modulus and mass loss</td>
<td>A-DZ-HX</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td></td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>B-DZ-HX</td>
<td>10</td>
<td>0</td>
<td>0</td>
<td></td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>C-DZ-HX</td>
<td>20</td>
<td>0</td>
<td>0</td>
<td></td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>D-DZ-HX</td>
<td>20</td>
<td>30</td>
<td>0</td>
<td></td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>E-DZ-HX</td>
<td>20</td>
<td>0</td>
<td>30</td>
<td></td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>F-DZ-HX</td>
<td>20</td>
<td>15</td>
<td>15</td>
<td></td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>A-DZ-YX</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td></td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>B-DZ-YX</td>
<td>10</td>
<td>0</td>
<td>0</td>
<td></td>
<td>1</td>
</tr>
</tbody>
</table>
The frost resistance tests on CLP concrete were carried out with reference to the relevant literature [32–34]. First of all, the prepared concrete specimens were put into the standard curing room for 24 days and then removed for appearance inspection. Then, the specimens were immersed in water with a temperature of 20 ± 2 °C and 5% Na₂SO₄ solution for 4 days. The liquid was 20 mm higher than the top surface of the specimen during immersion. Finally, the corresponding water freezing cycle and salt freezing cycle tests were carried out on the specimens after 4 days of immersion. The quick freezing test equipment is shown in Figure 1.

![Figure 1](image1.png)

**Figure 1.** Fast freezing test equipment.

The compressive strength of concrete was tested by the YAW-3000 microcomputer controlled electrohydraulic servo pressure testing machine. During the test, continuous uniform loading was applied. Before loading, we ensured that the specimen was located in the middle of the upper and lower bearing plates, and the surface contact between the specimen and the bearing plate was balanced [35,36]. The concrete cube compressive strength test is shown in Figure 2.

![Figure 2](image2.png)

**Figure 2.** Concrete cube compressive strength test.

<table>
<thead>
<tr>
<th></th>
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</thead>
<tbody>
<tr>
<td></td>
<td>0</td>
<td>10</td>
<td>20</td>
<td>20</td>
<td>20</td>
<td>20</td>
</tr>
<tr>
<td></td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>30</td>
<td>0</td>
<td>15</td>
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<tr>
<td></td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>30</td>
<td>30</td>
<td>15</td>
</tr>
<tr>
<td></td>
<td>0</td>
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<td>5</td>
<td>5</td>
<td>5</td>
<td>5</td>
<td>5</td>
</tr>
</tbody>
</table>

Note: The numbering rules in the table are as follows: A, B, C, D, E, F represent L₀F₀S₀, L₁F₀S₀, L₁F₁S₀, L₁F₁S₁S₁. DZ represents two terms, relative dynamic elastic modulus and mass loss, and KY represents compressive strength. H represents the freeze–thaw cycle in pure water (referred to as “water freeze cycle”). Y represents the freeze–thaw cycle in 5% Na₂SO₄ solution (referred to as “salt freeze cycle”). X represents that the numbers of freeze–thaw cycles were 25, 50, 75, and 100.
3. Results and Discussion

3.1. Apparent Morphology

For the convenience of comparative analysis, Figure 3 divides the apparent morphology of the specimens into left and right columns at the beginning and end of the water freezing cycle. The number of the corresponding concrete formula is marked on the top left or top right of the apparent morphology picture of each specimen. The number of comments can be referred to Table 1. It can be seen from Figure 3 that when the water freezing cycle is 0 times, there are no other defects on the surface of the specimen, except for a small number of tiny pores. After 100 water freezing cycles, the specimen has a darker apparent color due to water absorption and humidity. The apparent morphologies of A-DZ-H100 and B-DZ-H100 specimens did not change significantly. There are a few mortar drops on the surfaces of C-DZ-H100, D-DZ-H100, E-DZ-H100, and F-DZ-F100 specimens, revealing “starry spots” of coarse aggregate. This is similar to the phenomenon observed in references [37,38]. It shows that the damage to the concrete is small within 100 water freezing cycles. In this study, in order to consider the salt freezing cycle and to perform a comparative analysis, only effective data within 100 water freezing cycles were selected.

![Figure 2. Compressive testing on the concrete cube.](image)
Figure 3. Apparent morphologies of the specimens at the beginning and end of the water freezing cycles.

Figure 4 shows the apparent morphologies of the specimens at the beginning and the end of the salt freezing cycles. It can be found from Figure 4 that the salt freezing cycle has a great influence on the damage and failure of the apparent morphologies of the specimens, and the failure phenomena are similar to those observed in the literature [39]. Among them, some specimens (C-DZ-Y50; D-DZ-Y50 and B-DZ-Y75) were subjected to 50 and 75 salt freezing cycles, respectively. The surface mortar peeled off severely, the coarse aggregate was exposed, and the test was stopped. After 100 salt freezing cycles, the coarse aggregate of the A-DZ-Y100 specimen fell off in a large range, and the apparent morphologies of the specimens became incomplete. The coarse aggregates of E-DZ-Y100 and F-DZ-Y100 specimens were more exposed, and the coarse aggregates of F-DZ-Y100 specimen were more obvious.
Comparing the apparent morphologies of the specimens after water freezing cycles and salt freezing cycles, it can be found that the damage of the concrete specimens under salt freezing cycles is much greater than that under water freezing cycles. The reason for this phenomenon is that on the one hand, freeze–thaw damage causes microcracks in concrete, accelerates the invasion of salt solution, and causes expansion damage to concrete; on the other hand, the sulfate solution increases the initial saturation of the pore fluid inside the concrete, which increases the pore wall pressure of the concrete during the freeze–thaw process, thereby aggravating the freeze–thaw damage of the concrete [39,40].

### 3.2. Mass Loss

Figure 5 shows the mass losses of concrete specimens under different freeze–thaw cycles. It can be found from Figure 5a that the mass loss rate of the specimens did not exceed 3% after 100 water freezing cycles, which was lower than the limit of 5% in the corresponding national standard [32]. This shows that the incorporation of limestone powder, fly ash, and slag has little effect on the mass loss rate of concrete after 100 freeze–thaw cycles. Among them, the mass losses of specimens A, B, and C decrease first and then increase during the water freezing cycles. This is because the quality of the water absorbed by the concrete is greater than the quality of the peeling mortar on its surface, which leads to an increase in the early quality of the specimen during the freeze–thaw cycle [15,37].

It can be found from Figure 5b that the effect of salt freezing cycles on the mass loss of CLP concrete specimens is much greater than that of water freezing cycles. During the salt freezing cycles, the mass loss of the specimen increased. Among them, the mass loss rate of E specimen was the smallest, which was 6.11%. The mass loss rates of B, C, and D specimens reached 20.23%, 25.16%, and 39.83%, respectively, when the salt freezing cycles were 50 and 75. The mass loss was large and the test was stopped. This shows that the coupling effect of sulfate attack and freeze–thaw damage has a great influence on the damage of concrete [5,39].

![Figure 5](image_url)  
*Figure 5. Mass losses of the concrete specimens under different freeze–thaw cycles.*
3.3. Relative Dynamic Modulus of Elasticity

Figure 6 shows the relative dynamic elastic moduli of concrete specimens under different freeze–thaw cycles. It can be seen from Figure 6a that the relative dynamic elastic modulus of the CLP concrete specimen decreases rapidly during the water freeze–thaw cycles. After 100 water freezing cycles, the relative dynamic elastic moduli of the specimens are in the following order: $E_{DZ-H100} > F_{DZ-H100} > A_{DZ-H100} > D_{DZ-H100} > C_{DZ-H100}$. Comparing Figure 6b, it can be found that the damage effect of salt freezing cycles on the relative dynamic elastic modulus of concrete is much greater than that of water freezing cycles, but the incorporation of 15% and 30% slag in CLP concrete can effectively improve this performance. After 50 salt freezing cycles, the relative dynamic elastic moduli of C and D specimens decreased to 35.06% and 37.44% of the original values. Below the limit of 60% of the corresponding national standard [32], the test was stopped.

The reasons for the above phenomenon are given as follows.

1. The relative dynamic elastic modulus of concrete specimens is related to the density of its internal structure [15,37]. Limestone powder has a certain filling effect at the physical level, which can optimize the particle gradation of the cementitious material system. However, its activity effect at the chemical level is low, which will reduce the relative content of hydration products in unit volume concrete, resulting in a decrease in the compactness of concrete and a decrease in the relative dynamic elastic modulus [41,42]. The chemical response of limestone powder with 10–20% content in concrete is higher than its physical response, and the frost resistance of concrete decreases with the increase in the limestone powder content.

2. The pozzolanic effects of fly ash and slag increase the secondary hydration products, optimize the pore structure, and improve the compactness of concrete [43–45]. However, in the case of the fixed total content of 50%, fly ash is used to replace slag in equal proportion. At the physical level, the specific surface area of fly ash (364 m$^2$/kg) is less than that of slag (435 m$^2$/kg), and its particle filling effect in the cementitious system is lower than that of slag, which will make the internal structure of CLP concrete loose and reduce the compactness. At the chemical level, the activity of fly ash is lower than that of slag, thereby reducing the hydration products in CLP concrete and increasing the porosity.

3. Sulfate has a certain stimulating effect on the hydration activity of slag in Portland cement [46,47]. As a result, the incorporation of slag in concrete can effectively improve the relative dynamic elastic modulus of the specimens under freeze–thaw cycles.
cycles, and the improvement effect under the salt freezing cycles is better than that under the water freezing cycles.

Therefore, the “superposition effect” of limestone powder, fly ash, and slag can optimize the frost resistance of CLP concrete. Therefore, the frost resistances of the CLP concrete follow the indicated order: $L_{20}F_{30}S > L_{20}F_{15}S > L_{10}F_{30}S > L_{20}F_{0}S > L_{20}F_{0}S_{0}$, which corresponds to the relative dynamic elastic modulus.

3.4. Compressive Strength

Figure 7 shows the compressive strengths of the concrete specimens under different freeze–thaw cycles. The letters “A, B, C, D, E, and F” in the specimen number in the figure represent the six concrete formulations of “$L_{0}F_{0}S_{0}$, $L_{10}F_{0}S_{0}$, $L_{20}F_{0}S_{0}$, $L_{20}F_{30}S_{0}$, $L_{20}F_{0}S_{30}$, and $L_{20}F_{15}S_{15}$”, respectively. It can be seen from Figure 7 that when the contents of limestone powder are between 10~20%, the compressive strength of concrete will be reduced, and with the increase in the content, the strength loss will be greater. The incorporation of fly ash will reduce the early strength of CLP concrete. The incorporation of slag can improve the compressive strength of CLP concrete. In the freeze–thaw cycles (water freezing or salt freezing), the compressive strengths of all specimens decrease with the increase in the number of freeze–thaw cycles. The damage degree of salt freezing cycles to the compressive strength of the specimen is greater than that of water freezing cycles. The incorporation of limestone powder and fly ash accelerates the loss of compressive strength of concrete specimens in freeze–thaw cycles, but the incorporation of slag can slow down the loss of compressive strength of CLP concrete in freeze–thaw cycles and enhance its frost resistance [45,46].

The reason for this phenomenon is that the chemical response of limestone powder with the 10~20% content is higher than the physical response. The compressive strength of concrete decreases with the increase in limestone powder content. When the mineral admixture is fixed at 50%, because the fineness of fly ash is less than that of slag, replacing slag with fly ash in equal proportion will make the internal structure of CLP concrete loose and reduce the strength of the concrete. At the same time, the activity of fly ash is lower than that of slag, which reduces the hydration products in CLP concrete, increases the porosity, and reduces the compressive strength of concrete. In the freeze–thaw cycles, freeze–thaw damage and sulfate freeze–thaw coupling damage will cause damage inside the concrete and reduce its compressive strength, and the latter has a greater impact. At the same time, due to the “superposition effect” of limestone powder, fly ash, and slag,
the change law for the compressive strength loss of CLP concrete is the same as that for the relative dynamic elastic modulus.

4. Micro-Degradation Mechanism Analysis

4.1. Analysis of SEM

Considering the cost of the tests, this study only focuses on the microstructure and phase composition of the CLP concrete samples after 0, 50, and 100 salt freezing cycles. The SEM images and XRD images are shown in Figure 8 and Figure 9, respectively.
Figure 8. SEM images of the concrete samples after 0, 50, and 100 salt freezing cycles.
Figure 9. XRD images of the concrete samples after 0, 50, and 100 salt freezing cycles.

Due to the failure of B specimen sampling during the test, the data were not collected successfully, which was not shown in Figure 8. It can be seen from Figure 8 that the fibrous hydration C-S-H products were found in A, D, and F specimens without salt freezing cycles, and there were more in the A specimen. The spherical particles of fly ash can be clearly seen in the D specimen, indicating that a large amount of fly ash is still not involved in the secondary hydration, and the pozzolanic effect is not fully reflected [43,44]. There are obvious cracks in the cement stone found in specimens A and E, indicating that the concrete specimens have initial defects. The white needle in the C specimen is CaCO$_3$, indicating that the limestone powder mainly plays a filling role, and the activity effect is relatively low [41,48].

After 50 salt freezing cycles, flocculent fibrous hydration C-S-H products were found in the C specimen, and the microcrystalline nucleation effect of limestone powder was obvious [41,48]. The spherical particles of fly ash can still be clearly seen in the D specimen, and white needle-like and rod-like ettringite were found in E and F specimens, indicating that sulfate had an obvious excitation effect on the hydration activity of slag in Portland cement. The expansion of ettringite produced by hydration fills the internal pores of the concrete, which can enhance the frost resistance of concrete [39,46]. Flake or block gypsum
was found in specimens A, D, and F. Gypsum caused concrete to expand and crack, which reduced its strength and durability. After 50 salt freezing cycles, the damage of specimens C and D was serious, and the test was stopped.

After 100 salt freezing cycles, needle-like thaumasite was found in specimen A, which was shorter and thicker than ettringite crystals. The internal flocculent fibrous hydration C-S-H product was reduced, resulting in low strength and weakened frost resistance. E and F specimens contained many small flocculent fibrous hydration C-S-H products, which have a certain strength and improved frost resistance. There were many flakes or block gypsum in the F specimen, leading to decreases in strength and frost resistance, which were lower than those of the E specimen but higher than those of the A specimen [39].

In summary, it can be seen that ordinary concrete produces gypsum and thaumasite successively in salt freezing cycles. Single limestone powder easily makes the concrete produce thaumasite earlier in the process of salt freezing cycles, and the content is higher. The incorporation of fly ash makes CLP concrete produce gypsum during salt freezing cycles. The incorporation of slag makes CLP concrete produce ettringite in the process of salt freezing cycles, and C-S-H can still be found in the later stage of salt freezing cycles.

4.2. Analysis of XRD

Due to the failure of sampling of specimen B in the test, the data were not collected successfully, which are not shown in Figure 9. It can be seen from Figure 9 that after 50 salt freezing cycles, for the C specimen, when $2\theta = 29.672^\circ$, the peak value of CaCO$_3$ is the largest. This is mainly affected by the incompletely removed sand and gravel in the sample. When $2\theta = 30.792^\circ$ and $36.277^\circ$, gypsum and thaumasite appear. For the D specimen, when $2\theta = 26.766^\circ$, SiO$_2$ appears, and the peak value is larger. When $2\theta = 11.305^\circ$, $31.142^\circ$, and $43.317^\circ$, gypsum appears and exists in many places. When $2\theta = 18.17^\circ$ and $47.226^\circ$, Ca(OH)$_2$ appears. When $2\theta = 29.528^\circ$, there is CaCO$_3$, and the peak value is higher. Due to the influence of incompletely removed sand in the sample, the diffraction peak of SiO$_2$ is higher. After 100 salt freezing cycles, the damage of specimens C and D was serious, and the test was stopped.

After 100 salt freezing cycles, for specimen A, when $2\theta = 26.852^\circ$, the diffraction peak is SiO$_2$ and exists in many places. When $2\theta = 9.126^\circ$, thaumasite appears, and the microstructure is shown in Figure 8c. For the E specimen, when $2\theta = 49.754^\circ$, C-S-H appears. When $2\theta = 50.338^\circ$ and $60.179^\circ$, the diffraction peak of SiO$_2$ appears and exists in many places. For the F specimen, when $2\theta = 26.708^\circ$ and $29.508^\circ$, the diffraction peaks of SiO$_2$ and CaCO$_3$ increase. This is mainly affected by the incompletely removed sand and gravel in the sample. When $2\theta = 19.259^\circ$ and $31.259^\circ$, C-S-H and C$_2$S appear. This shows that the C$_2$S reaction is slow during the hydration process, and it still exists when the salt freezing cycles are 100.

By analyzing the changes in the composition of each sample during the salt freezing cycles, it can be known that A, D, and F specimens produced gypsum during salt freezing cycles, and thaumasite was found in the A specimen when the salt freezing cycles were 100, resulting in a large decrease in macroscopic strength. The D specimen has low cement content, less cementitious material, low early strength, and slow secondary hydration rate of fly ash, resulting in gypsum mold damage [43,44]. E and F specimens produce ettringite, and early ettringite expands and fills the internal pores of concrete [39,46]. After 100 salt freezing cycles, there is still flocculent fibrous hydration C-S-H product which improves the macroscopic strength of concrete.

4.3. Analysis of MIP

The frost resistance of concrete is closely related to its pore structure [15,39]. In this study, due to the consideration of the cost of the test, only the samples of each concrete formula at the age of 28 d were selected for the MIP test. The pore structure data obtained are used as a supplement to the overall analysis. The pore characteristic parameters of each sample are shown in Table 3.
The following can be seen from Table 3. (1) The porosity of concrete with mineral admixtures is higher than that of ordinary concrete \((L_0 F_0 S_0)\), but the most probable pore sizes are smaller than those of ordinary concrete. Among them, the most probable aperture of \(L_2 F_0 S_0\) concrete is the smallest. (2) For \(L_2 F_0 S_30\) concrete, its total pore area is the largest, but its total pore volume is not the largest. This is because the pore is assumed to be cylindrical in the mercury injection test. The total pore size is small and the total pore area is large, which means that the pore size is smaller. The average pore size of \(L_2 F_0 S_30\) concrete is the smallest, which conforms to the law.

4.4. Analysis of Mechanism

Under the coupling effect of sulfate and freeze–thaw, the first freeze–thaw damage of CLP concrete will cause cracks and microcracks in concrete, accelerate the invasion of salt solution, and cause expansion damage to concrete. Secondly, the sulfate solution will increase the initial saturation of the pore fluid inside the concrete, resulting in an increase in the pore wall pressure of the concrete during the freeze–thaw process. At the same time, the pressure generated by the supersaturated crystallization of the sulfate solution in the pores will also aggravate the freeze–thaw damage. The coupling effect of sulfate attack and freeze–thaw cycles makes the damage degree of CLP concrete in the process of salt freeze–thaw cycles much larger than that of water freeze–thaw cycles. However, sulfate has a certain stimulating effect on the hydration activity of slag in Portland cement [46,47]. When the concrete specimen is subjected to rapid freeze–thaw cycles in a \(Na_2SO_4\) solution with a mass fraction of 5%, the following reactions occur:

\[
Na_2SO_4 + Ca(OH)_2 + 2H_2O \rightarrow CaSO_4\cdot2H_2O + NaOH
\]

The generated \(CaSO_4\cdot2H_2O\) (gypsum) has small grains, large dispersion, and high activity, and the reaction rate with \(CaS\) is accelerated so that \(AF_t\) (ettringite) is rapidly generated, which greatly accelerates the hardening rate. Moreover, after the consumption of \(Ca(OH)_2\), the hydration of \(CaS\) is promoted, the hydration products are increased, and the compactness of cement stone is improved. At the same time, the presence of limestone powder causes the excess aluminum phase to react with calcium carbonate rather than with \(AF_t\) (ettringite):

\[
\text{No reaction: } CaA + AF_t \rightarrow AF_m \text{ (monosulfoaluminate)}
\]
Reaction: $\text{C}_3\text{A} + \text{CaCO}_3 \rightarrow \text{M}_c/\text{H}_c$ (single carbon/half carbon calcium aluminate)  \hspace{1cm} (3)

Therefore, the addition of limestone powder can inhibit the formation of AF$_m$ (monosulfoaluminate) and stabilize the early formed AF$_t$ (ettringite). The molar volume of AF$_t$ is larger than that of AF$_m$, and the solid volume of hydration products increases, which reduces the porosity of the specimen. Moreover, calcium carbonate is harder and larger than AF$_m$, which can reduce the porosity of the specimen, reduce the pore size of the test piece, and improve the strength of the test piece, thereby improving the salt frost resistance of the CLP concrete (F and E specimens).

5. Model of Freeze–Thaw Damage

According to the theory of damage mechanics, an internal state variable “$D_n$” needs to be defined. It is used to describe the development of and change in material damage state and its effect on the mechanical properties of materials. It is defined as a damage variable [50]. In this section, based on the change in relative dynamic elastic modulus, the corresponding macroscopic damage evolution equation of CLP concrete is established as follows [25,51]:

$$D_n = 1 - \frac{E_n}{E_0} = 1 - P_n \hspace{1cm} (4)$$

where $D_n$ is the damage variable of concrete after $n$ freeze–thaw cycles under different freeze–thaw cycle conditions; $P_n$ is the relative dynamic modulus of elasticity after $n$ freeze–thaw cycles.

According to the test results, the freeze–thaw damage variables are calculated, and the results are shown in Table 4.

Table 4. The damage variable values of the concrete specimens under different freeze–thaw cycle conditions.

<table>
<thead>
<tr>
<th>Number</th>
<th>Limestone Powder Mixing Amount (%)</th>
<th>Fly Ash Mixing Amount (%)</th>
<th>Slag Mixing Amount (%)</th>
<th>Freeze–Thaw Conditions</th>
<th>$D_n$ (%) at Different Numbers of Freeze–Thaw Cycles</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>0</td>
</tr>
<tr>
<td>A-DZ-HX</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>Water freezing cycle</td>
<td>0</td>
</tr>
<tr>
<td>B-DZ-HX</td>
<td>10</td>
<td>0</td>
<td>0</td>
<td></td>
<td>0</td>
</tr>
<tr>
<td>C-DZ-HX</td>
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<td>0</td>
<td>0</td>
<td></td>
<td>0</td>
</tr>
<tr>
<td>D-DZ-HX</td>
<td>20</td>
<td>30</td>
<td>0</td>
<td></td>
<td>0</td>
</tr>
<tr>
<td>E-DZ-HX</td>
<td>20</td>
<td>0</td>
<td>30</td>
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<td>0</td>
</tr>
<tr>
<td>F-DZ-HX</td>
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<td>15</td>
<td>15</td>
<td></td>
<td>0</td>
</tr>
<tr>
<td>A-DZ-YX</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>Salt freezing cycle</td>
<td>0</td>
</tr>
<tr>
<td>B-DZ-YX</td>
<td>10</td>
<td>0</td>
<td>0</td>
<td></td>
<td>0</td>
</tr>
<tr>
<td>C-DZ-YX</td>
<td>20</td>
<td>0</td>
<td>0</td>
<td></td>
<td>0</td>
</tr>
<tr>
<td>D-DZ-YX</td>
<td>20</td>
<td>30</td>
<td>0</td>
<td></td>
<td>0</td>
</tr>
<tr>
<td>E-DZ-YX</td>
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<td>0</td>
<td>30</td>
<td></td>
<td>0</td>
</tr>
<tr>
<td>F-DZ-YX</td>
<td>20</td>
<td>15</td>
<td>15</td>
<td></td>
<td>0</td>
</tr>
</tbody>
</table>

In physics, the problem of the flat throwing of objects can be considered as the damage of gravity acceleration to height. If there is no influence of gravity acceleration, the object will be thrown to infinity. The damage reflected in the mathematical formula is the gravity acceleration $g$; so, the gravity acceleration can also be called the height damage acceleration of the object, in essence. Combined with the theory of damage mechanics and the principle of physics, the freeze–thaw cycles of concrete can be understood as $e_2$ causing the relative dynamic elastic modulus damage of concrete, resulting in the nonlinear
reduction in $P_n$ [51]. The freeze–thaw damage model of CLP concrete is established as follows:

$$D_n = \frac{1}{2} e_g n^2$$  \hspace{1cm} (5)

where $e_g$ is the acceleration of the relative dynamic elastic modulus of concrete; $n$ is the number of freeze–thaw cycles.

The relative dynamic elastic modulus of CLP concrete is greatly affected by different freeze–thaw cycle conditions (water freezing or salt freezing), resulting in great differences in its frost resistance. The concentration parameter $i$ ($0\%$, $5\%$ Na$_2$SO$_4$ solution) of the freeze–thaw soaking solution is introduced here [25]. Considering different freeze–thaw cycle conditions, Origin 2022 software was used to fit the damage variable data of A, E, and F specimens under water freezing and salt freezing cycle conditions, and the freeze–thaw damage model of CLP concrete with a soaking solution concentration factor was obtained, as shown in Table 5 and Figure 10.

**Table 5. Freez–thaw damage model for concrete under different freeze–thaw cycles.**

<table>
<thead>
<tr>
<th>Specimen</th>
<th>Freeze–Thaw Damage Models</th>
<th>Correlation Coefficient $R^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>$D_n = \frac{1}{2} \times (4.92 \times 10^{-3} + 1.84 \times 10^{-3} \times i) \times n^2$</td>
<td>0.9919</td>
</tr>
<tr>
<td>E</td>
<td>$D_n = \frac{1}{2} \times (3.88 \times 10^{-3} - 4.42 \times 10^{-4} \times i) \times n^2$</td>
<td>0.9076</td>
</tr>
<tr>
<td>F</td>
<td>$D_n = \frac{1}{2} \times (4.53 \times 10^{-3} - 5.14 \times 10^{-4} \times i) \times n^2$</td>
<td>0.8194</td>
</tr>
</tbody>
</table>

It can be seen from Table 5 and Figure 10 that the model fits the damage variable value data of A, E, and F specimens under the conditions of water freezing and salt freezing cycles, and the fitting effect is better. However, with the increase in mineral admixtures, the fitting effect of the model gradually decreases, indicating that mineral admixtures have a high impact on the frost resistance of concrete, and the impact of slag is greater than that of fly ash and limestone powder.
6. Conclusions

The variation rule and degradation mechanism of frost resistance of different concrete mixtures were examined from both macro and micro perspectives through the experimental investigation of CLP concrete under sulfate freeze–thaw coupling tests. The following conclusions can be drawn.

(1) Limestone powder has a filling effect, but the activity is low. When the content is between 10~20%, the chemical response is higher than the physical response. The pozzolanic effects of fly ash and slag increase the secondary hydration products, optimize the pore structure, and improve the compactness. The “superposition effect” of limestone powder, fly ash, and slag can optimize the frost resistance of CLP concrete.

(2) In the case of the fixed total content, fly ash replaces slag in equal proportion. At the physical level, the fineness of fly ash is less than that of slag, which will make the internal structure of CLP concrete loose and reduce the compactness. At the chemical level, the activity of fly ash is lower than that of slag, thereby reducing the hydration products in CLP concrete and increasing the porosity. Therefore, the frost resistances of the CLP concrete follow the indicated order: \( L_{20}F_0S_{30} > L_{20}F_{15}S_{15} > L_{20}F_3S_0 \).

(3) The coupling effect of freeze–thaw damage and sulfate attack makes the damage of salt freezing cycles to the frost resistance of CLP concrete greater than that under water freezing cycles. However, the activation of sulfate can enhance the activity effect of slag, so that the effect of slag on improving the frost resistance of concrete under salt freezing cycles is better than that of water freezing cycles.

(4) Based on the theory of damage mechanics, the freeze–thaw damage model of CLP concrete was established. Considering different freeze–thaw conditions, the damage variable values of \( L_0F_0S_0, L_0F_3S_0, \) and \( L_0F_3S_{15} \) specimens under freeze–thaw cycles are fitted, and the fitting effect is better. However, mineral admixtures have a great influence on the frost resistance of concrete. With the increase in mineral admixtures, the applicability of this presented model might need more research effort.

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Writing—review and editing, and resources. Q.Y.: Data curation. All authors have read and agreed to the published version of the manuscript.

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**References**


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