Model Compression for Deep Neural Networks: A Survey

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Abstract: Currently, with the rapid development of deep learning, deep neural networks (DNNs) have been widely applied in various computer vision tasks. However, in the pursuit of performance, advanced DNN models have become more complex, which has led to a large memory footprint and high computation demands. As a result, the models are difficult to apply in real time. To address these issues, model compression has become a focus of research. Furthermore, model compression techniques play an important role in deploying models on edge devices. This study analyzed various model compression methods to assist researchers in reducing device storage space, speeding up model inference, reducing model complexity and training costs, and improving model deployment. Hence, this paper summarized the state-of-the-art techniques for model compression, including model pruning, parameter quantization, low-rank decomposition, knowledge distillation, and lightweight model design. In addition, this paper discusses research challenges and directions for future work.

Keywords: deep neural networks; model compression; model pruning; parameter quantization; low-rank decomposition; knowledge distillation; lightweight model design

1. Introduction

In recent years, due to the rapid development of artificial intelligence, machine learning has received a great deal of attention from researchers, especially regarding deep neural networks (DNNs) [1,2]. DNNs have been applied to various fields with excellent results, such as image classification [3,4], object detection [5–7], and image segmentation [8]. In 2012, AlexNet [9] achieved nearly 11% higher classification accuracy than the second-place finisher to win the ImageNet [10] ILSVRC2012 competition. After this, DNN research became a hotspot in the literature. Since then, researchers have designed various types of DNNs, such as VGG [11], GoogLeNet [12], and ResNet [13], which have emerged one after another. During this time, graphics processing units (GPUs) have been widely used for general-purpose computing with superior performance to central processing units (CPUs). However, hardware updates are quickly rendered inadequate due to the increased computational demand of increasingly complex models, and this increased demand is unlikely to slow down. Therefore, to achieve a feasible compromise between available hardware and computational demands, modern models must be compressed.

Table 1 shows the relationship between accuracy and computation on different models. The more complex the model, the better the classification but the more storage and computing resources consumed. Therefore, reducing the consumption of storage and computing resources has become a focus in the design of DNNs.
Table 1. Classification accuracy and computation complexity of different DNN models on ImageNet.†

<table>
<thead>
<tr>
<th>Model</th>
<th>Layers</th>
<th>Parameter (MB)</th>
<th>FLOPs (G)</th>
<th>Top-1 Error (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>AlexNet [9]</td>
<td>8</td>
<td>233</td>
<td>4.4</td>
<td>43.45</td>
</tr>
<tr>
<td>GoogLeNet [12]</td>
<td>22</td>
<td>51</td>
<td>8.9</td>
<td>34.20</td>
</tr>
<tr>
<td>VGGNet-16 [11]</td>
<td>16</td>
<td>528</td>
<td>15.5</td>
<td>27.30</td>
</tr>
<tr>
<td>DenseNet-121 [14]</td>
<td>121</td>
<td>31</td>
<td>13.4</td>
<td>25.35</td>
</tr>
<tr>
<td>ResNet-50 [13]</td>
<td>50</td>
<td>98</td>
<td>17.9</td>
<td>24.60</td>
</tr>
<tr>
<td>ResNet-152 [13]</td>
<td>152</td>
<td>230</td>
<td>49.1</td>
<td>23.00</td>
</tr>
<tr>
<td>ResNeXt-101 [15]</td>
<td>101</td>
<td>319</td>
<td>71.4</td>
<td>20.81</td>
</tr>
<tr>
<td>SENet-154 [16]</td>
<td>154</td>
<td>440</td>
<td>93.8</td>
<td>18.68</td>
</tr>
</tbody>
</table>

† The FLOPs in the table are the number of floating operations the network makes in inferring a 512 × 512 image. The number of parameters is computed based on FP32.

Efficient deep-learning methods have a significant impact on distributed systems, embedded devices, and field-programmable gate arrays (FPGAs) for artificial intelligence [17–25]. For example, ResNet-50 [13], with 50 convolution layers and 98MB storage space, requires over 3.8 billion floating-point operations to process an image. After pruning the redundant weights, however, the model still operated properly but with 75% fewer parameters and 50% less computational time. Therefore, it is very important to devise methods for model compression, especially for resource-constrained devices, such as mobile phones, Raspberry Pi, and FPGAs. To realize model compression, multiple disciplines must be integrated, including algorithm optimization, computational architecture design, signal processing, and hardware system design.

1.1. Contributions of This Paper

In this paper, we reviewed recent research on DNN model compression. These works have made significant progress in recent years and have received significant attention from researchers. The contribution of this paper was to summarize the methods of model pruning, parameter quantization, low-rank decomposition, knowledge distillation, and lightweight model design. Model pruning was implemented by searching for redundant layers/channels in the model and removing them with little or no impact on the performance. Parameter quantization is a method for converting floating-point calculations to low-bitrate integer calculations. Low-rank decomposition uses matrix/tensor decomposition to estimate the information of the DNNs. Knowledge distillation is used to train a large network (teacher network) that can then train a smaller network (student network) so that the results achieved by the student network are similar to those of the teacher network. A lightweight model is used to design specially structured convolution filters to reduce parameters and computation time. These studies are summarized in Table 2.

In general, model compression has been widely used in the fields of computer vision and natural language processing. In addition, model compression is important for improving the effectiveness of models and increasing their deployment potential. It has the following advantages.

- Conserves storage space, especially on edge devices.
- Reduces computational demand and speeds up model inference.
- Reduces the complexity of the model and prevents over-fitting.
- Reduces training time and computational resource consumption, thus reducing training costs.
- Improves the deployability of the model, as smaller models are easier to deploy on edge devices.
<table>
<thead>
<tr>
<th>Core Idea</th>
<th>Operating Object</th>
<th>Architecture</th>
<th>Representative</th>
<th>Advantage</th>
<th>Disadvantage</th>
</tr>
</thead>
<tbody>
<tr>
<td>Model pruning</td>
<td>Con layer, FC layer</td>
<td>Alter</td>
<td>Structured pruning, unstructured pruning.</td>
<td>Structured pruning narrows the network for hardware acceleration. Unstructured pruning compresses the network to any degree.</td>
<td>Structured pruning leads to accuracy reduction. Unstructured pruning leads to irregular architecture and is difficult to accelerate effectively.</td>
</tr>
<tr>
<td>Parameter quantization</td>
<td>Conv layer, FC layer</td>
<td>Unaltered</td>
<td>Post-training quantization, quantization-aware training.</td>
<td>It reduces parameter storage space and memory, speeds up operation, and reduces equipment energy consumption.</td>
<td>It takes a long time to train and fine-tune and is inflexible.</td>
</tr>
<tr>
<td>Low-rank decomposition</td>
<td>Conv layer.</td>
<td>Alter</td>
<td>Binary decomposition, multivariate decomposition.</td>
<td>It has good compression and acceleration effects on large convolution kernels and small and medium-sized networks.</td>
<td>Difficult to decompose simplified convolution kernels, layer-by-layer decomposition is not conducive to global parameter compression.</td>
</tr>
<tr>
<td>Knowledge distillation</td>
<td>Conv layer, FC layer</td>
<td>Unaltered</td>
<td>Knowledge distillation for output layer, mutual information, correlation, and adversarial.</td>
<td>Large-scale models are compressed into small models and deployed to resource-constrained devices.</td>
<td>The network needs to be trained at least twice, and the training time is long.</td>
</tr>
<tr>
<td>Lightweight model design</td>
<td>The entire network.</td>
<td>Alter</td>
<td>Convolution kernel level, layer level, network architecture level.</td>
<td>The network is simple, the training time is short, and the small network with a small storage amount, low calculation amount, and good performance can be obtained.</td>
<td>It is difficult to combine the special architecture with other compression and acceleration methods; poor generalization is not suitable as a pre-trained model to help other models.</td>
</tr>
</tbody>
</table>
1.2. Organization of This Paper

Figure 1 shows the paper organization as follows: Section 2 introduces the method for model pruning, including structured and unstructured pruning. Section 3 provides an overview of the parameter quantization, post-training quantization, and quantization-aware training. Section 4 outlines the method used for low-rank decomposition. Section 5 presents relevant research concepts and methods for knowledge distillation. Section 6 reports the strategies and recent advances in lightweight model design. Section 7 discusses the current state-of-the-art of model compression and future research directions. Section 8 summarizes this article.

Figure 1. Organization of the survey.

2. Model Pruning

The earliest pruning method was biased weight decay [26]. In the 1990s, the objective function was used in a Taylor expansion method to find the neuron with the least impact on the loss [27,28]. These methods focused on removing inessential components from DNNs without having a significant effect on the performance. As the research progressed, model pruning was divided into structured and unstructured methods.

2.1. Structured Pruning

Structured pruning is normally performed with a channel (filter) as the basic pruning unit [29–33]. When one channel is pruned, the corresponding channels are also removed [34,35]. Channel-based structured pruning was realized by evaluating the importance of channels. Li et al. [34] measured the relative importance of channels in each layer by calculating the sum of the absolute weights of the channels [36]. This approach did not require the support of a sparse convolution library, nor did it produce sparse connections. Meanwhile, it reduced time, as compared to layer-by-layer iterative fine-tuning. The time-saving advantage was particularly evident in the pruning process of deep networks. However, this caused a degradation in model performance. Therefore, Lin et al. [37] proposed a global and dynamic pruning scheme to prune redundant channels. First, a global discriminant function based on the prior global knowledge of each channel removed the insignificant channels from all layers. After that, it dynamically updated the accuracy of the filters by comparing the pruned and sparse networks in order to recover any incorrectly pruned channels. Next, it was retrained to improve the performance of the model. Furthermore, Li et al. [38] proposed a fused max-average pooling operation and an improved channel-attention mechanism by using two pooling functions to enhance the
feature representation in DNNs. Kuang et al. [39] obtained the importance of a channel by considering the effect of each channel on a task-dependent loss function. The smaller the loss function value, the less important the channel. According to this characteristic, Li et al. [40] proposed a highly efficient layer-wise refined pruning method for DNNs at the software level that accelerated the inference process at the hardware level [41].

Channel-based pruning has also been applied in the fields of image segmentation and object detection. Sawant et al. [42] proposed an optimal-score-based filter pruning (OSFP) approach to prune redundant filters according to their similarities in the feature space. OSFP removed redundant filters, improved segmentation performance, and accelerated network learning. As a special pruning method, sparse training [43] and mask learning [44] created new connections during the pruning process. Chu et al. [45] proposed a three-stage model-compression method: (1) dynamic sparse training, (2) group channel pruning, and (3) spatial attention distilling, in the field of object detection. Group channel pruning divided the network into multiple groups according to the scale of the feature layers and the similarity of the module architecture in the network. Then, the channels in each group were pruned according to different thresholds. In addition, Chang et al. [46] proposed an automatic channel pruning method. This method first performed hierarchical channel clustering using feature map similarity and initial network pruning simultaneously. Then, a population initialization method was presented to transform the pruned architecture into candidate populations. Finally, the optimal compression architecture was found via particle-swarm optimization. By evaluating the performance of their parameters, Liu et al. [47] presented a method for network slimming, which did not require any special software/hardware accelerators for the model. During the training process, unimportant channels were automatically identified and later pruned. It employed an $L_1$ regularization [48] on the weights of the batch-normalization (BN) [49] layers to achieve the sparsity of the parameters. Then, iterative pruning was used to achieve high pruning rates.

Yang et al. [50] proposed an energy-aware pruning algorithm. The algorithm guided the process by using the computational consumption of the convolutional neural network (CNN). The pruning was implemented layer by layer and was more effective than previously proposed pruning methods by minimizing the errors in the output feature map, rather than the filter weights. To accomplish this, the weights were first pruned by layer. After that, local fine-tuning was performed by closed-form least squares to recover the accuracy after pruning. Finally, the layers were pruned, and the entire network was globally fine-tuned using back-propagation. In 2021, Fan et al. [51] proposed a hierarchical channel pruning to group different layers by reducing the model accuracy of the pruned network. After pruning each layer in a specific order, the network was retrained. There was a small decrease in the accuracy of the network model, but the computational resources deployed on the hardware were greatly reduced. To reduce the computational cost of multiple training, Chen et al. [52] proposed only-train-once (OTO), a training and pruning framework. OTO greatly simplified the complex multi-stage training channel of current pruning methods. Furthermore, the method of a half-space random projection gradient was proposed, which solved the problem of structured sparsity-induced regularization. As compared to multiple fine-tuning processes, OTO required only one, which significantly simplified the pruning process. Chung et al. [53] pruned certain convolution channels in the first layer of a pre-trained CNN. Pruning of the first layer greatly facilitated the channel compression of the subsequent convolution layers. However, the input of the first layer was a single channel. To address these issues, Chen et al. [54] proposed a solution to strategically manipulate neurons by “grafting” appropriate levels of linearized insignificant rectified linear unit (ReLU) neurons to eliminate the non-linear components. However, this method required the associated slopes and intercepts of the replaced linear components to be optimized in order to restore model performance. With the continuous advances in structured pruning algorithms, whether layer-based or filter-based, the original multiple pruning and fine-tuning approaches were developed to only be used once.
2.2. **Unstructured Pruning**

Unstructured pruning was based on a heuristic approach to zero-out unimportant parameters, such as weight magnitude \[55,56\], gradients \[57\], and hessian \[27\] statistics. It has typically resulted in competitive performance improvements, but it has been difficult to accelerate due to irregular sparsity \[58,59\].

In 1989, LeCun et al. \[27\] suggested the concept of optimal brain damage, which used second-derivative information to determine a compromise between network complexity and training-set error, so unimportant weights would be removed from the network. Han et al. \[56\] described a method, train–prune–retrain, to reduce the storage and computation of neural networks by learning only the important connections. The performance was improved by an order of magnitude without affecting the accuracy. Yang et al. \[50\] utilized the energy consumption of each layer to determine the pruning order. Yang et al. \[60\] created latency tables that utilized greed to determine the layers that should be cropped. Furthermore, Yang et al. conducted comparison experiments using \(L_1\) and \(L_2\) regularization. According to the experimental results, pruning with \(L_1\) regularization achieved better accuracy than \(L_2\) regularization after pruning and without retraining. This occurred because \(L_1\) regularization had converted more parameters closer to zero. However, \(L_2\) regularization outperformed \(L_1\) after retraining pruning. Guo et al. \[61\] proposed dynamic network surgery, which reduced network complexity significantly by pruning connections in real time. In contrast to the previous method, Guo et al. included connected splicing throughout the process to avoid incorrect pruning. By adding a learning process to the process of filtering important and unimportant parameters, it was possible to more accurately identify the optimal parameters. Neill et al. \[62\] proposed two weight regularizers that aimed to maximize the alignment between units of pruned and unpruned networks in order to mitigate alignments in pruned cross-lingual models. Unstructured pruning greatly reduced the number of parameters and computations. However, the unstructured pruning set the redundant neurons to zero, rather than remove them from the network \[63\]. As a result, the non-regular sparsity was not fully utilized to accelerate the model according to current hardware architectures. Therefore, accelerating unstructured pruning techniques for use on current hardware architectures should be further examined.

3. **Parameter Quantization**

Parameter quantization reduces the size and inference time of models \[64–67\]. Parameter quantization is versatile and applicable to most models and hardware devices. Parameter quantization of neural networks is the process of converting the weights and activation values of a network model from high precision to low precision. Algorithm 1 shows the steps of parameter quantization. Parameter quantization has several advantages:

- Less storage overhead and bandwidth requirements.
- Lower power consumption.
- Faster calculation speed.

**Algorithm 1** Parameter quantization.

Step 1: Count the corresponding min\_value and max\_value in the input data (weights or activation values);

Step 2: Choose the appropriate quantization type, symmetric (int-8) or asymmetric (uint-8);

Step 3: Calculate the quantization parameters \(Z/\text{Zero point}\) and \(S/\text{Scale}\) according to the quantization type, min\_value and max\_value;

Step 4: Quantize the model based on the calibration data, converted from FP32 to INT-8;

Step 5: Verify the performance of the quantized model, and if the result is not good, try to use a different way to calculate \(S\) and \(Z\), and re-execute the above operation.
Parameter quantization establishes a data-mapping relationship between fixed-point and floating-point data, allowing for better gains at a smaller cost in terms of accuracy loss. This is shown in Equations (1) and (2),

\[ S = \frac{R_{\text{max}} - R_{\text{min}}}{Q_{\text{max}} - Q_{\text{min}}} \]  
\[ Z = Q_{\text{max}} - \frac{R_{\text{max}}}{S} \]

where \( R \) denotes a real floating-point number, \( Q \) denotes the quantization fixed-point value, \( Z \) denotes the quantization fixed-point value corresponding to the zero floating-point value, and \( S \) is the scale factor of quantization. In addition, \( S \) and \( Z \) are quantization parameters, and the data type of \( S \) is FP32, and that of \( Z \) is INT8. \( Q \) and \( R \) are derived from Equation (3) and Equation (4), respectively, that is, either the quantization \( Q \) or the back-propagated floating-point value \( R \). If they exceed the maximum range that each can represent, then they need to be rounded. The quantization equation from floating point to fixed point is as follows.

\[ Q = \frac{R}{S} + Z \]  

The equation for inverse quantization from fixed point to floating point is as follows:

\[ R = (Q - Z) \times S \]

where \( S \) and \( Z \) are found by the following Equation (5).

\[ Z = Q_{\text{max}} - \frac{R_{\text{max}}}{S} \]

After quantization, the parameters of the model usually need to be adjusted. The process of obtaining a model by retraining is called quantization-aware training (QAT). Similarly, the process of obtaining a model without retraining is called post-training quantization (PTQ). Figure 2 shows the difference between QAT and PTQ.

![Diagram](image)

**Figure 2.** Comparison of quantization-aware training (QAT, left) and post-training quantization (PTQ, right). ⊕ denotes training data, ⊗ denotes calibration data. In QAT, a pre-trained model is quantized and then fine-tuned using the training data to adjust parameters and recover from accuracy degradation. In PTQ, the pre-trained model is calibrated utilizing calibration data (a small portion of the training data) to calculate the shear range and scaling factor. Then, the model is quantified based on the calibration results. The calibration process is usually performed at the same time as the fine-tuning of the QAT.
3.1. Quantization-Aware Training

Quantization introduces perturbations into the parameters of the trained model, causing the model to deviate more from the convergence point than when trained with floating-point precision [68–73]. To make the model converge to a better loss point, the problem can be solved by retraining the quantization parameters. A commonly employed method has been QAT, which quantifies during both forward and backward propagation [74–76]. However, the model’s parameters are quantified after each gradient update. In particular, it is important to perform this calculation after the weight updates in floating-point precision. Similarly, it is important to perform the backward transfer in a floating-point manner, as accumulating gradients with quantization precision can lead to high errors in zero gradients or gradients, especially with low-precision quantization.

3.2. Post-Training Quantization

Post-training quantization was a good alternative to QAT, as it performed quantization and adjusted the weights without any fine-tuning [77–81]. Therefore, the cost of PTQ was very low and negligible. Furthermore, PTQ could be applied with limited or no labeling of data, which was a distinct advantage. However, PTQ required enough training data to retrain but only achieved a low accuracy rate, particularly for low-precision quantization. To address the problem of PTQ’s decreasing accuracy, researchers have proposed various methods [82–85]. For example, Banner et al. [86] and Finkelstein et al. [87] observed an inherent bias in the mean and the variance of the quantified weight values and proposed a bias-correction method. Meller et al. [88] and Nagel et al. [89] showed that balancing the weight ranges across the layers or channels could reduce the quantization errors. ACIQ [86] analytically calculated the optimal clipping range and channel-bit-width settings for PTQ. Although ACIQ achieved low-precision degradation, the channel-wise activation quantization used in ACIQ was difficult to implement effectively in hardware devices. To address this problem, the OMSE [90] approach eliminated channel quantization at activation and proposed PTQ by optimizing the $L_2$ distance between the quantized tensor and the corresponding floating-point tensor. In addition, to better mitigate the adverse effects of outliers in PTQ, Zhao et al. [91] proposed an outlier channel-splitting method, which duplicated and halved the channels containing outliers. Another notable work was AdaRound [92], which proposed an adaptive rounding method that reduced losses more effectively. Although AdaRound restricted the variation in the quantization weights to within $±1$, AdaQuant [93] proposed a more general approach that allowed the weight of the quantization to change as needed. In PTQ, all weights and activation quantization parameters were determined without any retraining of the neural network models. Therefore, PTQ was a very fast way to quantify neural network models. However, PTQ tended to be less accurate than QAT.

4. Low-Rank Decomposition

Low-rank decomposition uses a low-rank matrix to approximate the weight matrix in a neural network [94]. Approaching the weight matrix with a low rank is particularly effective and produces a $3 \times$ compression on the fully-connected layer. However, it does not speed up the model significantly, since the computational operations of CNN are mainly in the convolution layer. Therefore, reducing the number of convolution layers improves the compression rate.

This concept of low-rank decomposition was derived from the speculation that there was a structural capacity in a 3-dimensional (3D) tensor. The convolution kernel was viewed as a 3D tensor by [95], and the fully connected (FC) layer was considered as a 2D matrix or 3D tensor. Low-rank filters were used to accelerate convolutional operations. For example, a high-dimensional discrete cosine transform (DCT) and wavelet systems were constructed from 1D DCT transforms and 1D wavelets, respectively, using tensor products. Learning separable 1D filters was proposed by [96] using a dictionary learning approach. Denton et al. [97] proposed clustering schemes with low-rank decomposition and convolution kernel for simple DNN models. They achieved a $2 \times$ increase in speed.
in a single convolution layer. However, the classification accuracy decreased by 1.00%. Jaderberg et al. [98] proposed using a different tensor decomposition scheme and showed a 4.5× increase in speed, while the accuracy of the text recognition decreased by 1.00%

Low-rank decomposition was an operation on layers, and the analysis was performed layer-by-layer. The parameters of one layer were fixed upon completion, and the layers above were fine-tuned according to the reconstruction error criteria. Figure 3 describes the kernel decomposition of the low-rank decomposition matrix.

![Figure 3. Kernel approximation of low-rank decomposition matrix.](image)

Lebedev et al. [99] proposed a canonical polyadic (CP) decomposition of the kernel tensor, using nonlinear least squares to calculate the CP decomposition. Tai et al. [100] proposed a new algorithm for computing low-rank tensor decompositions for training low-rank constrained CNNs from the start. This method used BN to convert the activation of the internal hidden cells. In general, both CP and BN decomposition schemes could train CNNs from scratch. However, there was little difference between the CP and BN decomposition schemes. For example, finding the best low-rank decomposition in the CP decomposition was an unsolvable problem, and the best rank-K (where K is the number of ranks) decomposition did not always exist. Decomposition was always present in BN. Table 3 shows the comparison between the different models on ILSVPRC-2012.

![Figure 4. A typical framework for low-rank regularization methods, with the original convolutional layer on the left and the low-rank, constrained convolutional layer with rank-K on the right.](image)

<table>
<thead>
<tr>
<th>Model</th>
<th>Top 5 Accuracy</th>
<th>Speed-Up</th>
<th>Compression Rate</th>
</tr>
</thead>
<tbody>
<tr>
<td>AlexNet</td>
<td>80.03%</td>
<td>1.00</td>
<td>1.00</td>
</tr>
<tr>
<td>BN Low-rank</td>
<td>80.56%</td>
<td>1.09</td>
<td>4.94</td>
</tr>
<tr>
<td>CP Low-rank</td>
<td>79.66%</td>
<td>1.82</td>
<td>5.00</td>
</tr>
<tr>
<td>VGG16</td>
<td>90.60%</td>
<td>1.00</td>
<td>1.00</td>
</tr>
<tr>
<td>BN Low-rank</td>
<td>90.47%</td>
<td>1.53</td>
<td>2.72</td>
</tr>
<tr>
<td>CP Low-rank</td>
<td>90.31%</td>
<td>2.05</td>
<td>2.75</td>
</tr>
<tr>
<td>GoogleNet</td>
<td>92.21%</td>
<td>1.00</td>
<td>1.00</td>
</tr>
<tr>
<td>BN Low-rank</td>
<td>91.88%</td>
<td>1.08</td>
<td>2.79</td>
</tr>
<tr>
<td>CP Low-rank</td>
<td>91.79%</td>
<td>1.20</td>
<td>2.84</td>
</tr>
</tbody>
</table>

Table 3. A simple comparison of the two methods is presented to measure the performance of each, based on the actual increases in speed and the compression ratio.
There are several methods for exploiting low rankings in FC layers \[97,101\]. For example, Denil et al. \[102\] reduced the number of dynamic parameters in a deep model using a low-rank method. Sainath et al. \[103\] explored a low-rank matrix factorization of the final weight layer in DNNs for acoustic models. Lu et al. \[104\] used a truncated singular value decomposition (SVD) to decompose the FC layers to design compact multi-task DNN models. The low-rank decomposition method was straightforward for model compression. However, the low-rank decomposition method was difficult to implement due to the decomposition operation itself. Another problem was that the modern approaches employed layer-by-layer low-rank decomposition, so global parameter compression was not possible since different layers had different information. These methods identified redundant parameters of DNNs by employing the matrix and tensor decomposition. The filter of a neural network was viewed as a tensor with four dimensions: width $W$, height $H$, number of channels $C$, and a number of convolution kernels $N$. As $C$ and $N$ have a large impact on the overall network architecture, network compression was performed using low-rank decomposition methods based on the characteristics of information redundancy of the convolution kernel $(W \times H)$ matrix and its low-rank property.

Since the weight vectors were mostly distributed in a low-rank subspace, the convolution kernel matrix was reconstructed with a small number of basis vectors to reduce memory requirements. Low-rank decomposition methods had good compression and speed improvements for large convolution kernels and in small and medium-sized networks. However, new networks increasingly use $1 \times 1$ convolution in recent years. A $1 \times 1$ convolution is not conducive to the use of low-rank decomposition. In addition, the matrix decomposition operation is expensive, layer-by-layer decomposition is not conducive to global parameter compression, and it requires significant retraining to achieve convergence. To address this problem, Jaderberg et al. \[98\] proposed a two-step method for accelerating convolution layers in large convolutional neural networks based on tensor decomposition and discriminative fine-tuning \[105\].

5. Knowledge Distillation

As shown in Figure 5, knowledge distillation is a teacher–student architecture \[106–108\]. The teacher network is a complex pre-trained network, and the student network is a simple small network. The teacher network provides the student network with prior knowledge so that the student network achieves similar performance to that of the teacher network.

![Figure 5. Model compression based on knowledge distillation.](image)

Deploying deep models in mobile devices is challenging due to the limited processing power and memory of these devices. To address these issues, Buciluă et al. \[109\] first proposed model compression to transfer information from a large model to train a small model without significant accuracy degradation. Henceforth, the training of small models by large models was called knowledge distillation \[108,110,111\]. Chen et al. \[112\] posited that feature embedding from deep neural networks could convey complementary information...
and, thus, proposed a novel knowledge-distilling strategy to improve its performance. The main idea of knowledge distillation was that the student model imitated the teacher model to achieve competitive, or even superior, performance. The key focus was how to transfer knowledge from a large teacher model to a small student model.

In the process of knowledge distillation, knowledge types, distillation strategies, and teacher–student architectures have played key roles in the student learning process. The activations, neurons, and features of the middle layer were available as knowledge to guide the learning of the student model [113–117]. The relationship between different activations, neurons, and features contained the rich knowledge learned by the teacher model [118–122]. As shown in Figure 6, three methods of knowledge distillation were introduced. These three distillation methods are described in detail in the following sections.

![Figure 6](image-url)

**Figure 6.** (a) The generic response-based knowledge distillation. (b) The generic feature-based knowledge distillation. (c) The generic instance-relation-based knowledge distillation.

### 5.1. Response-Based Knowledge

Response-based knowledge distillation is a simple and effective model compression method that has been widely used in a variety of tasks [108,110]. Response-based knowledge is the final output layer of the teacher model, and the main idea is to directly mimic the final prediction of the teacher network. The response-based image knowledge is called a soft target, which is the probability of different classes of inputs that can be estimated by the Softmax function, as in Equation (6):

\[
q(z_i, T) = \frac{\exp(Z_i / T)}{\sum_j \exp(Z_j / T)}
\]  

(6)

where \(Z_i\) is the logit for the \(i\)-th class, \(j \in (1, 2, \cdots, k)\), \(k\) is the total number of classes, \(\exp\) is an exponential operation, and \(T\) is the temperature parameter to control the importance of each soft target. If \(T = 1\), it is the original Softmax function.

### 5.2. Feature-Based Knowledge

Deep neural networks are excellent at learning multiple-level representations of features. This became defined as representational learning [123–125]. Therefore, the feature map, as the output of the final and middle layers, is available as knowledge to supervise the training of student models. The feature-based knowledge from the middle layer is a good extension of the response-based knowledge. The feature-based knowledge-distillation loss was defined by Equation (7):

\[
L_{FeaD}(f_t(x), f_s(x)) = \mathcal{L}_F(\phi_t(f_t(x)), \phi_s(f_s(x)))
\]  

(7)
where $f_t(x)$ and $f_s(x)$ are feature maps of the middle layers of the teacher and student networks, respectively. The transformation functions $\phi_t(f_t(x))$ and $\phi_s(f_s(x))$ transform the feature maps of the teacher and student networks into the same shape, respectively. In addition, $\mathcal{L}_f(\cdot)$ is the similarity function used to match the feature maps of the teacher and student networks.

5.3. Relation-Based Knowledge

Both response-based and feature-based knowledge methods use the output of a particular layer in the teacher model. The relation-based knowledge method further explores the relationship between different layers. Yim et al. [118] proposed the flow of the solution process (FSP), which was defined by the Gram matrix between the different layers. The FSP matrix reflected the relationship between the feature map by the inner product between the two layers of features. Correlations between feature maps were used as prior knowledge. Knowledge distillation by SVD extracted information from the feature maps [126].

Zhang et al. [127] proposed a graph-based distillation framework to use the knowledge of multiple teachers. Lee et al. [119] proposed a multi-headed graph-based knowledge-distillation method. The student network simulated the mutual information flow of the paired queuing layers of the teacher network to explore paired-queuing information. Usually, the distillation loss of relation-based knowledge over the relations of the feature map is expressed as Equation (8):

$$L_{RelD}(f_t, f_s) = L_{R1}(\Psi_t(\hat{f}_t, \tilde{f}_t), \Psi_s(\hat{f}_s, \tilde{f}_s))$$

where $f_t$ and $f_s$ are the feature maps of the teacher network and the student network, respectively. $\hat{f}_t$, $\tilde{f}_t$ and $\hat{f}_s$, $\tilde{f}_s$ are a pair of feature maps in the teacher network and student network, respectively. $\Psi(\cdot)$ is the similarity function of a pair of feature maps. $L_{R1}$ denotes the correlation function between the teacher and student feature maps.

6. Lightweight Model Design

Lightweight DNN model design refers to the redesign based on the existing DNN structure to achieve a reduction in the number of parameters and the computational complexity. Table 4 shows the design skills for the lightweight model. Iandola et al. [128] proposed SqueezeNet, which replaced $3 \times 3$ convolution kernels with a $1 \times 1$ convolution kernel. The parameters of a $1 \times 1$ convolution kernel were 1/9 of the parameters of a $3 \times 3$ convolution kernel. However, this also decreased the number of input channels available as compared to $3 \times 3$ convolution. By learning ResNet and adding bypass branches to the original network, the classification accuracy was improved by approximately 3%. Howard et al. [129] proposed MobileNet, which divided convolution into depth-wise convolution and point-wise convolution. Each convolution kernel filter of a depth-wise convolution performed convolutional operations on only one specific input channel. Point-wise convolution used a $1 \times 1$ size convolution kernel to combine the multi-channel outputs of the depth-wise convolution layer. Zhang et al. [130] proposed ShuffleNet, which shuffled the input groups into channels, thus ensuring that the perceptual fields of each convolutional kernel were spread across the inputs of different groups to increase the learning ability of the model.
Table 4. Skills for lightweight models.

<table>
<thead>
<tr>
<th>Model</th>
<th>Methods</th>
</tr>
</thead>
<tbody>
<tr>
<td>SqueezeNet [128]</td>
<td>• 1 x 1 convolution instead of 3 x 3 convolution.</td>
</tr>
<tr>
<td></td>
<td>• Reducing the number of input channels for 3 x 3 convolution.</td>
</tr>
<tr>
<td></td>
<td>• Downsampling operation.</td>
</tr>
<tr>
<td>SqueezeNext [131]</td>
<td>• Number of compressed feature map channels.</td>
</tr>
<tr>
<td></td>
<td>• Low-rank separable convolution.</td>
</tr>
<tr>
<td></td>
<td>• Reducing the number of input channels in the FC layer.</td>
</tr>
<tr>
<td>MobileNetV1 [129]</td>
<td>• Depthwise separable convolution.</td>
</tr>
<tr>
<td></td>
<td>• Two hyperparameters, ( \alpha ) and ( \rho ).</td>
</tr>
<tr>
<td>MobileNetV2 [132]</td>
<td>• Reducing the use of 1 x 1 convolution.</td>
</tr>
<tr>
<td></td>
<td>• Linear bottleneck structure.</td>
</tr>
<tr>
<td></td>
<td>• Two hyperparameters, ( \alpha ) and ( \rho ).</td>
</tr>
<tr>
<td>ShuffleNetV1 [130]</td>
<td>• 1 x 1 group convolution.</td>
</tr>
<tr>
<td></td>
<td>• Channel shuffle.</td>
</tr>
<tr>
<td>ShuffleNetV2 [133]</td>
<td>• Replacing 1 x 1 group convolution with 1 x 1 dense convolution.</td>
</tr>
<tr>
<td></td>
<td>• Keeping the number of input and output channels consistent.</td>
</tr>
<tr>
<td></td>
<td>• Using concatenating instead of adding.</td>
</tr>
<tr>
<td></td>
<td>• Channel segmentation.</td>
</tr>
<tr>
<td></td>
<td>• Channel shuffle.</td>
</tr>
</tbody>
</table>

Gao et al. [134] improved the effectiveness of lightweight models in self-supervised learning. Tan et al. [135] proposed MnasNet, a neural architecture search (NAS) method. The time consumption of the model on the device was incorporated into the search space through multi-objective optimization. Next, using a decomposed hierarchical search space allowed the network to maintain layer diversity while maintaining a simplified search space. This enabled a better compromise between accuracy and time consumption in the search model. Huang et al. [136] proposed that group convolution was learnable. Learning group convolution continued the training by combining the training process with pruning for more accurate pruning. Mehta et al. [137,138] proposed an end-to-end speech processing network (ESPNet), which was a lightweight network for semantic segmentation, and its core was an ESP module. The ESP module contained point-wise convolution and a spatial pyramid of dilated convolution, which were more efficient than to MobileNet and ShuffleNet. Depth-wise separable convolution reduced the computation time and the number of parameters of the network, whereas point-wise convolution used the highest number of parameters. Motivated by this, Gao et al. [139] proposed a channel-wise and depth-wise separable convolution. ChannelNet was constructed by replacing the FC layer and the global pooling layer of the network.

The interleaved group convolution (IGC) series network was an extreme use of group convolution [140–142]. IGC decomposed the regular convolution into multiple group convolutions, reducing a large number of parameters. Furthermore, the complementarity principle and the sorting operation ensured the flow of information between groups with a minimum number of parameters. The FBNet series [143–145] was a lightweight network series based entirely on the NAS method. FBNet [143] combined DNA and resource constraints. FBNetV2 [144] added a channel and input resolution search. FBNetV3 [145] used accuracy prediction to perform a fast network structure search. Currently, DNN performance optimization is carried out to improve the following three areas.

- Increase the width of the network.
- Increase the depth of the network.
- Increase the resolution of input images.
It is easy to directly improve the accuracy of a network by revising one dimension. However, revising two or three dimensions of the network at the same time requires tedious manual tuning and is difficult to optimize. To address these problems, Tan et al. [146] proposed a hybrid scaling method for model scaling that could better select the width, depth, and resolution dimensional scaling, thus enabling the model to achieve higher accuracy. Han et al. [147] proposed a Ghost module to extract more features using fewer parameters. First, the Ghost module used the output with the fewest raw convolution operations for the output. Then a series of simple linear operations were used on the output to generate more features. GhostNet was proposed based on the Ghost module, replacing the original convolution layer with the Ghost module. The experimental results showed that GhostNet compressed well and maintained good accuracy. Ma et al. [148] proposed a simple and efficient dynamic generative network, WeightNet, which integrated the features of squeeze and excitation networks (SENet) [16] and CondConv [149] in the weight space. WeightNet dynamically generated convolutional kernel weights based on sample features and adjusted the hyperparameters to achieve a compromise between accuracy and speed. Li et al. [150] proposed MicroNet, which contained micro-factorized convolution and dynamic shift-max. Micro-factorized convolution maintained the input-output connectivity and reduced the number of connections through low-rank decomposition. Dynamic shift-max compensated for the performance degradation caused by the reduced network depth by dynamically fusing features between groups to increase node connectivity and improve non-linearity. Radosavovic et al. [151] proposed RegNet, which was a new network design paradigm that combined the advantages of manually designed networks and NAS. Finally, self-supervised representation learning (SSL) has received significant attention. However, recent studies have concluded that when the model size decreased, its performance decreased substantially. Since current SSL methods rely heavily on contrast learning to train a network, Gao et al. [134] proposed a simple and effective method called distillation contrast learning (DisCo) to alleviate this problem. DisCo aligned the final embedded constraints of lightweight students with those of teachers, maximizing the transfer of teacher knowledge.

7. Discussion

With the rapid development of hardware, DNNs have become the dominant algorithm for computer vision tasks. The growth in overall computational power has improved the data-processing power of DNNs, which has substantially improved the generalization ability of the models. Furthermore, DNN architecture design is a hotspot in the research and may become one of the most widely used artificial intelligence techniques in the future. In addition, deploying models on edge devices facilitates the development of model compression techniques. For the application of DNNs on edge devices, lightweight network architecture is one of the mainstream research topics. In this survey, we summarized the research achievements in recent years. The challenges and prospects of DNN development are as follows.

In model-pruning algorithms, most existing approaches remove redundant connections or neurons from the network. This low-level pruning introduces unstructured risks. Therefore, it is important to propose more effective methods to evaluate the impact of pruned objects on their models.

Parameter quantization greatly reduces the size of the model. However, the quantization operation increases the complexity of the operation. During the quantization process, some special processing is required. Otherwise, the accuracy loss is more severe. In addition, quantization usually results in a loss of accuracy. An appropriate quantization strategy reduces the complexity of the model while minimizing the loss of accuracy. In addition, mixed accuracy quantization strategies have been used to reduce the size of the parameters to a reasonable level on a contribution basis.

Low-rank decomposition speeds up the computational process of the model, and the mathematical principles of the decomposition process are more helpful for explaining the optimization mechanism of the network structure. However, low-rank decomposition
is not effective in accelerating models with small convolutional kernels, and it cannot compress the size of the network model.

Knowledge distillation guides the training of student networks by teacher networks. However, the training difficulty varies for different student network architectures. Therefore, building a student network architecture requires designers to have a richer theoretical foundation and nuclear engineering experience.

Currently, the determination of hyperparameters relies on manual expertise and ablation experiments. Over the course of experiments, small changes in hyperparameters have led to inconsistent results overall. Therefore, a standardized design approach for hyperparameter optimization is needed. A neural architecture search algorithm is also necessary to design a network, as it automatically searches for the correct network architecture.

Training DNN models requires powerful hardware resources. Therefore, the deployment of DNN models on mobile devices needs to be explored. Most model-acceleration methods implement optimization for image recognition tasks, and few are dedicated to accelerating tasks in other areas of computer vision. Furthermore, the evaluation system of network compression algorithms is rather weak and generally focuses on comparing network parameters and running time. As a future research direction, researchers should balance the size and speed of a network and provide a network performance evaluation system for different scenarios.

Model compression significantly reduces model size, improves model inference speed, and reduces computational demands. Many model compression techniques have achieved model compression by removing some parameters, which results in the loss of model performance. In addition, model compression increases the training time and may also lead to model over-fitting. Therefore, these limitations should be considered before performing model compression to ensure the accuracy and stability of the model. According to the survey of lightweight model designs, the application of neural architecture search technology increased the speed in the lightweight model designs. For example, both MnasNet and RegNet utilized a neural architecture search approach. Therefore, in the process of designing a lightweight model, it is necessary to consider methods to reduce the resource consumption during neural architecture searches.

8. Conclusions and Future Work

This paper provided a survey of deep neural network model compression. Five deep neural network model compression methods were discussed. Structured and unstructured pruning were discussed from the perspective of model pruning. The advantages and disadvantages of the two quantization methods, quantization-aware training and post-training quantization, were compared. The method of low-rank decomposition was introduced. Three applications of knowledge distillation in model compression were presented. Lightweight models achieved performance improvements by designing efficient architectures and have become the dominant model-compression and -acceleration methods in recent years. By analyzing and discussing areas related to model compression, this literature review intended to provide researchers with new information and research directions and to promote the further development of deep neural network model compression.

In future work on deep neural network model compression, model size should be reduced by utilizing hybrid precision without losing model performance. Model pruning and low-rank decomposition reveal hidden information in the model (e.g., the importance of layers and channels), which facilitates a better understanding of the model and provides insights for model design. Knowledge distillation transfers knowledge between different models, resulting in a shorter training time and better performance. In addition, model compression has been achieved faster and more efficiently by merging multiple model compression methods. For example, by merging knowledge distillation and neural architecture search, a lightweight model is obtained faster. As neural architecture search technology
develops, more lightweight models will be discovered. Therefore, neural architecture search will play a crucial role in the design of future lightweight models.

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