

Review

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Review **Ferroelectric Liquid Crystals: Physics and Applications**

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Abstract: Electrooptic modes with fast response and high contrast ratio are highly desirable in modern photonics and displays. Ferroelectric liquid crystals (FLCs) are especially promising for fulfilling these demands by employing photoalignment technology in FLC cells. Three electrooptic modes including surface stabilized FLC (SSFLC), deformed helix ferroelectric (DHF) mode, and electrically suppressed helix (ESH) mode are reviewed with the corresponding electrooptic effects like bi- and multi-stable switching, continuous modulation of grayscale or phase, and high contrast switching. The general operation principles FLC electrooptic modes are described, and then the characteristics of each modes for potential applications are summarized. With the advantages of controllable anchoring energy, the photoalignment provides FLC samples with uniform alignment and high contrast ratio. The fast FLCs with a high resolution and high contrast can be used in the next generation display including field sequential color FLC microdisplays, as well as switchable 2D/3D televisions.

Keywords: ferroelectric liquid crystal; photo-alignment; fast response time; display; photonic devices

1. Introduction

High speed, low power consumption, high resolution and high contrast ratio are in high demand for next generation displays $[1-4]$ $[1-4]$ and modern photonic devices $[5-7]$. However, in terms of response time, liquid crystals (LCs) still have huge space to be improved compared with the competing technologies, such as micro-electro-mechanical system (MEMS) [\[8\]](#page-19-3) or micro-LED [\[9\]](#page-19-4). A fast response time is needed in order to reduce motion blur, achieve field sequential color (FSC), and improve the low-temperature operation. The target response time for FSC displays should be less than 1 ms (240 Hz frame frequency) to provide a high resolution, low power consumption and extended color gamut liquid crystal display (LCD) [\[3\]](#page-19-5). Also, versatile photonic devices, in which the 2π modulation is of crucial importance such as liquid crystal lenses [\[10\]](#page-19-6), tunable focusers [\[11\]](#page-19-7), and wave front correctors [\[12\]](#page-19-8) requires fast response with thick LC layers. Therefore, many efforts are in progress to improve the response time of various LC electrooptic modes, e.g., polymer-stabilized blue phase mode [\[13](#page-19-9)[–15\]](#page-19-10), flexoelectric optical effect [\[4](#page-19-0)[,16](#page-19-11)[,17\]](#page-19-12). However, display devices using the blue phase LC have yet to be commercialized due to limitations such as low transmittance, a narrow operating temperature range, and a high driving voltage of over 50 V for example. Flexoelectric effect in short pitch cholesteric LCs demonstrates fast response of 200 µs, but confronts limits of complicated fabrication procedure. Ferroelectric liquid crystals (FLCs), also known as chiral smectic C or smectic C^* phase, with their fast speed and low power consumption represent the most promising candidate.

There are several basic arrangements of FLC directors resulting in a variety of electrooptical effects. One of the well-known arrangements is in surface stabilized geometry proposed by Clark and Lagerwall in 1980 [\[18](#page-19-13)[,19\]](#page-19-14). Although subsequent papers contribute to different aspects of Clark-Lagerwall effect, such as the character of defects and disclination lines, etc., its applications are hindered by the crucial dependence of surface treatment [\[20\]](#page-19-15). This problem can be effectively solved by a photoalignment technology and achieve high-quality of FLC alignment on sufficiently large surface area [\[21\]](#page-19-16). The asymmetric boundary conditions, in which only one substrate is covered by aligning layer, are preferable for achievement of high uniformity of FLC layer. Moreover, the photo-aligning layer with optimal thickness of around 3–5 nm provides both the highest multiplex operation steadiness and the best contrast ratio of FLC cells [\[22](#page-19-17)[,23\]](#page-19-18).

In this paper, we review the recent advances in FLC electrooptic modes and their applications. Three electrooptic modes including surface stabilized FLC (SSFLC), deformed helix ferroelectric (DHF) mode, and electrically suppressed helix (ESH) mode are reviewed with the corresponding electrooptic effects like bi- and multistable switching, continuous modulation of grayscale or phase, and high contrast switching. For each of these FLC modes, we first describe the general operation principles, and then compare their pros and cons for different aspects of applications.

2. Operation Principle of Electrooptic Modes in FLCs

2.1. Surface Stabilized FLC (SSFLC) Mode

The surface stabilized geometry proposed by Clark and Lagerwall [\[18\]](#page-19-13), as shown in Figure [1,](#page-2-0) is characterized by the electrooptical phenomena that director reorientation from one bistable state to the other when an external electric field changes its sign. In this geometry, the FLC smectic layers are arranged perpendicular to the substrates and the helical structure are totally unwound by substrate surface and strong anchoring. The uniaxial phase plates are formed with two possible final director orientations corresponding to the polarities of the electric field *E*. The electric torque due to the interaction between spontaneous polarization *P^S* and electric field *E* switches one final director orientation to the other. One necessary condition for the existence of SSFLC is *d* << *P0*, where *d* is the FLC layer thickness and *P⁰* is the helical pitch, and we come to the situation that the helix is totally unwound by the surfaces.

Figure 1. Geometry of surface stabilized ferroelectric liquid crystals (FLC) cell.

In SSFLC regime, the switching time shows $\tau \propto \gamma_{\varphi}$, where γ_{φ} is FLC rotational viscosity, P_S is the FLC spontaneous polarization, and *E* is applied electric field (Figure [1\)](#page-2-0) [\[18,](#page-19-13)[19\]](#page-19-14). Comparing the rise time τ_r and decay time τ_d in nematics (N) and ferroelectric liquid crystals (FLC):

$$
\tau_r^{(N)} \propto 4\pi \gamma_1 / \Delta \varepsilon E_{\tilde{E}}^2,
$$
\n(1)

$$
\tau_d^{(N)} \propto d^2 \gamma_1 / K \pi^2,\tag{2}
$$

$$
\tau_r^{(FLC)} = \tau_d^{(FLC)} \propto \gamma_\varphi / P_S E,\tag{3}
$$

where *K* is the elastic constant of nematics, γ_1 is the rotational viscosity of nematics, *d* is the layer thickness, *P^S* is spontaneous polarization, and *E* is electric field. From Equation (1) to (3), we can draw the conclusion that the response time of SSFLC under electrical driving shows at least two orders faster than that of nematic LCs. Moreover, the decay time of nematics $\tau_d^{(N)}$, as described by Equation (2), sets the main limit, since it cannot be optimized by electric field *E*.

In SSFLC regime, when the FLC cell is placed between crossed polarizers with one of the final director orientations parallel to the polarizer as shown in Figure [1,](#page-2-0) the maximum modulation of transmittance is achieved and described as:

$$
I = \sin^2(4\theta)\sin^2(\Delta\Phi/2),\tag{4}
$$

where ∆Φ = ∆*nd2*π/λ is the phase retardation caused by the optical anisotropy ∆*n* = *n*|| − *n*[⊥] of FLC, and θ is the tilt angle of smectic layer. From Equation (4), it is indicated that the transmittance gets to the maximum value when $\theta = \pi/8$ (22.5[°]) and $\Delta n d/\lambda = 1/2$ are simultaneously satisfied. For $\Delta n = 0.125$ and $\lambda = 0.5$ µm, it gives $d \approx 2$ µm. The small deviation of the thickness, for instance $\Delta d = \lambda/8\Delta n$, leads to considerable fluctuation of the electrooptical response (Figure [2\)](#page-3-0) [\[20\]](#page-19-15). The criteria for a display device require $d = 2 \pm 0.2$ μ m.

Figure 2. Electrooptical response of the surface stabilized FLC (SSFLC) cell for different phase factors k = 1 to 9, the phase factor k is defined as $d\Delta n/\lambda = k/4$ [\[20\]](#page-19-15).

The issues of SSFLC include severe restrictions to the optimal layer thickness, complicated surface treatment for defect-free samples, and no grey scale. The last issue is one of the most crucial factors in display applications [\[18–](#page-19-13)[20\]](#page-19-15). The incapability of generating grayscale by using voltage amplitude hinders Clark-Lagerwall effect from applied in displays devices, leading the possibility for grayscale goes to the pulse width modulation.

2.2. Deformed Helix Ferroelectric (DHF) Mode

The schematics of DHF electrooptic mode is described in Figure [3a](#page-4-0). One necessary condition for the existence of DHF is that the layer thickness is much higher than the value of the helix pitch $d \gg P_0$ [\[20\]](#page-19-15). For planar aligned geometry with smectic layers perpendicular to the substrates, the FLC helical structure becomes deformed by applied electric field. Thus, the corresponding director distribution oscillates symmetrically in \pm E electric fields [\[20\]](#page-19-15). These oscillations result in a variation of the effective refractive index and electrically controlled birefringence.

Figure 3. Cell configuration (**a**) and director distribution (**b**) of deformed helix ferroelectric (DHF) cell [\[20\]](#page-19-15).

β When the light beam with the aperture *a* >> *P⁰* propagates through DHF sample placed between *φ* crossed polarizers, the alignment orientation is set with an angle β deviating from the polarizer. 2 2 2 2 The director distribution is described using azimuthal angle ϕ, which varies along the coordinate *z* parallel to the helical axis, as shown in Figure [3b](#page-4-0). The effect takes place up to the fields of FLC helix unwinding [\[20\]](#page-19-15):

$$
E_{U} = \frac{\pi^2}{16} \frac{K_{22} q_0^2}{P_S},
$$
\n(5)

where K_{22} is FLC twist elastic constant, $q_0 = 2\pi/P_0$ is the helix wave vector, and P_S is the spontaneous polarization.

The characteristic response time τ of the effect in small fields $E/E_U \ll 1$ are independent of the FLC polarization *Ps* and the field *E*, and defined only by the rotational viscosity γ_{φ} , and the helix pitch *P0*:

$$
\tau = \frac{\gamma_{\varphi}}{K_{22}q_0^2},\tag{6}
$$

The dependence Equation (6) is valid only in DHF regime where $E \ll E_U$. If *E* is close to *δ* helix relaxation τ*^d* to the initial state also rises. It is reported that memorable state is observed for *E* the unwinding field *EU*, the FLC helix becomes strongly deformed with the helical pitch *P* sharply increases $P >> P_0$, and response time $\tau \propto E^{-\delta}$, where $0 < \delta < 1$ [\[24](#page-19-19)[,25\]](#page-19-20). Consequently, the time of the comparable with *Eu*, and the electrooptic switching shows pronounced hysteresis when *E* approaches *Eu* [\[26\]](#page-19-21).

In the cases that the helix in FLC samples are slightly deformed by electric field $(E \ll E_U)$, it exhibits symmetric electrooptic switching, as shown in Figure [4.](#page-5-0) The ferroelectric LC cells with the response time less than one millisecond in a broad temperature range from 20 to 80 ◦C were reported [\[27\]](#page-20-0).

The transmission of DHF sample between crossed polarizers depends on the phase retardation as well as the optical axis deflection:

$$
I = \sin^2\left(\frac{\pi \Delta n(z)d}{\lambda}\right) \sin^2(2(\beta - \alpha(z))),\tag{7}
$$

where α represents the deflection of helical axis, defined as the angle between the projection of the optical axis and z-axis on the yz-plane:

$$
\alpha = \arctan(\tan \theta \cos \varphi(z)).\tag{8}
$$

Figure 4. The electrooptic response of the DHF cell, placed between crossed polarizer and analyzer, and helix axis parallel to polarizer. [\[28\]](#page-20-1).

The effective birefringence is $\Delta n(z) = n_{\text{eff}}(z) - n_{\perp}$, where the effective refractive index:

$$
n_{eff} = n_{\parallel} n_{\perp} / \left[n_{\perp}^2 + \left(n_{\parallel}^2 - n_{\perp}^2 \right) \sin^2 \theta \sin^2 \varphi \right]^{1/2}
$$
 (9)

Diffraction of light due to the helical structure is avoided, because the helical pitch is minimized $P_0 \propto 0.1$ –0.3 μ m < λ = 0.5 μ m for visible range.

In the case of small angles $|\theta| \ll 1$, the transmission in Equation (7) can be expanded in θ series:

$$
I \propto \left(\sin^2 2\beta - 2\theta \sin 4\beta \cos \varphi + 4\theta^2 \cos 4\beta \cos^2 \varphi\right) \sin^2 \pi \Delta n d / \lambda, \tag{10}
$$

As shown in [\[29\]](#page-20-2) for the small values of the applied field $cos\varphi \propto E/E_U$ and changes its sign for the field reversal *E* ⇒ −*E* (Figure [3\)](#page-4-0). Thus, according to Equation (10) for *sin4*β = 0 we have a quadratic grey scale:

$$
\Delta I \propto \theta^2 \cos^2 \varphi \propto \theta^2 E^2 / E_{U'}^2 \tag{11}
$$

To obtain a linear relationship of gray level and θ , as illustrated by Equation (10), the quadratic component is excluded by setting *cos4*β = 0.

$$
\Delta I \propto \theta \cos \varphi \propto \theta E / E_{U}, \qquad (12)
$$

If driven by a harmonic signal $E(t) = E_0 \cos\omega t$, the transmittance shows double frequency properties as illustrated by Equation (11), which is so called modulation regime. The quadratic (Equation (11)) and linear (Equation (12)) response were verified experimentally [\[26,](#page-19-21)[30\]](#page-20-3). The fast-electro-optical response of DHF is characterized with a V-shaped switching processing with natural and continuous greyscale [\[31\]](#page-20-4). FLC mixtures should be synthesized with short helix pitch (P_0 < 0.3 μ m) and large tilt angle ($\theta > 30^{\circ}$) for obtaining DHF effect [\[31,](#page-20-4)[32\]](#page-20-5). The critical voltage to unwind FLC helix was approximate 2–3 V. Pseudo-bistable switching can also be observed using short-pitch FLC mixtures. The property of V-shape switching provides high possibility of DHF to be applied for next generation active-matrix based FSC display [\[32\]](#page-20-5).

2.3. Electrically Suppressed Helix (ESH) Mode

The new proposed electrooptic mode called electrically suppressed helix (ESH) mode [\[28](#page-20-1)[,33\]](#page-20-6) exhibits attractive properties including fast electrooptic response and high contrast ratio, which makes it promising candidate for display and photonics applications. Before the FLC helix is completely unwind by electric field, FLC cells works in DHF regime at $V \leq V_C = 0.4$ V. After the FLC helix completely suppressed by electric field at $V \geq 1$ V, as shown in Figure [5](#page-6-0) right part, ESH arises with switching time inversely proportional to voltage amplitude as shown in Figure [6.](#page-6-1) This electro-optical behavior of switching time is similar to that of SSFLC in Clark-Lagerwall effect, but they are distinguished by the mechanism of helix unwinding.

Figure 5. Dependence of switching on time of 1.5 μm cell filled with the FLC-595 [\[28,](#page-20-1)[33\]](#page-20-6). Insertions: horizontal scale of all images is 200 μ m; top left—the voltage is not applied, top right—textures at \pm 1 V. bottom right is the driving voltage waveform; top: the FLC layer textures between crossed polarizers,

Figure 6. The frequency dependence of the response time at different voltages under condition $V \le 0.5$ V. The linear frequency dependence of the inverse response time at $V > 1$ V [\[28,](#page-20-1)[33\]](#page-20-6).

Between SSFLC and ESH modes there is only a formal difference in initial conditions (the helix is suppressed by surfaces in SSFLC, but this does not happen with ESH), as the dynamics are identical. The presence of helix without applied voltage is the cause of the unique high alignment quality in ESH mode as shown in the textures in Figure [5.](#page-6-0) The contrast ratio in ESH mode is more than 12000:1 at frequency up to 1 kHz at \pm 1.5 V and up to 2 kHz at \pm 3 V.

Eventy of the second of the second of the second of the second of the condition that the helix elastic
The criteria for achieving the high-quality alignment is to satisfy the condition that the helix elastic energy is comparable but obligatory not less than the anchoring energy normalized to *dFLC*:

$$
Kq_0^2 \ge \frac{2W_Q^0}{d_{FLC}},\tag{13}
$$

here W_Q^0 is the anchoring energy coefficient, which is measured to be W_Q^0 = 4 \times 10^{-4} J/m² for the sample illustrated in Figures [5](#page-6-0) and [6.](#page-6-1)

The uniform orientation of FLC director is obtained when $V > V_C$, where V_C is the critical voltage for helix unwinding. In addition, the ESH cells exhibits good shock stability, as evaluated using contrast ratio measured after removing the mechanical pressure. The contrast can be restored within 10 second after removal of mechanical pressure (Figure [7\)](#page-7-0).

22 °C, wavelength $\lambda = 0.63$ μm [\[28,](#page-20-1)[33\]](#page-20-6). Insertion left: Dependencies on voltage: measured tilt angle $\frac{22}{\sqrt{2}}$ e, wavelength $\sqrt{2}$ = 0.00 μ m $\left[\frac{20,00}{\sqrt{2}}\right]$. Insertion fert. Dependences on voltage. Inclusioned in angle **Figure 7.** Dependencies of the contrast ratio on driving voltage frequency at $V = 1.5$ V and $V = 3$ V. The FLC-595 layer-thickness is 1.5 μ m, no SiO₂ layers, measurements have been carried out at T = polarizers. Insertion right: Contrast ratio dependence on time after the application of mechanical shock.

3. Electrooptic Eff**ects of FLC Modes and Their Applications**

3.1. Bi- and Multi-Stable Switching

The bistable switching in SSFLC geometry can be achieved with electric field above the threshold value $E_{th} \propto W_d/K^{1/2}$, where K is an average elastic constant and W_d is a dispersion anchoring energy [\[20\]](#page-19-15). Thus, with increasing anchoring we need to increase the switching amplitude of the electric field. As the energy of switching electric torque is proportional to the product of *PSE*, the bistability threshold is inversely proportional to the value of the FLC spontaneous polarization *PS*.

A SSFLC structure exhibiting bistability realizes grayscale only by time- or space- averaging instead of amplitude controlled intrinsic grayscale [\[18](#page-19-13)[–20\]](#page-19-15). However, when the spontaneous polarization *Ps* of FLC is sufficiently high, then the multistable states can be obtained based on the ferroelectric domains, then consequently the inherent physical grayscale is achieved in passively addressed FLC samples [\[29\]](#page-20-2). In bookshelf configuration (Figure [1\)](#page-2-0) with helix totally unwound, a variable optical grayscale can be observed due to the ferroelectric domain density, as shown in Figure [8](#page-8-0) [\[34\]](#page-20-7). When a helix-free FLC sample composing ferroelectric domains is driven by voltage pulses, the width of the voltages pulse is critical in the sense of generating memorable domain density, as textures shown in Figure [8,](#page-8-0) with the condition that the width of the voltage pulse is shorter than total switching time. Observed under crossed polarizers, the quasi-periodical structure, which is memorized and remains even the voltage switched off or short-circuited, contains bright and dark smectic layers corresponding to ferroelectric domains completely switched or staying at the intial state. The boundaries between ferroelectric domains follow the smectic layer planes, which verifies that only two possible orientations of FLC directors exist in bookshelf configuration. The spatially averaged transmittance provides continuous grayscale with the condition that the light beam is much wider than the size of ferroelectric domains which is always satisfied. Since the density of the switched domains is determined by the energy of the driving pulse, which is proportional to the product of voltage amplitude and pulse width, the variation of spatially averaged transmittance can be controlled by both the amplitude and the width. The multistable electro-optical mode possessing any intermediate transmittance between maximum and minimum is achieved based on FLC cell (Figure [8\)](#page-8-0).

To obtain the multistable electro-optical response, the following conditions should be satisfied: Firstly, sufficiently high spontaneous polarization FLC mixtures, e.g., *Ps* > 50 nC/cm²; Second, the two orientation states are separated by a relatively low energy boundaries, which is normally satisfied for anti-ferroelectrics [\[18–](#page-19-13)[20\]](#page-19-15). For proper design the cell configuration and driving scheme, both V-shaped and S-shaped electro-optic response with multistability can be realized, as shown in Figure [9a](#page-8-1),b [\[34](#page-20-7)[,35\]](#page-20-8).

Figure 8. Continuous variation of the width of ferroelectric domains between crossed polarizers with a change in the applied voltage of the FLC layer. The image area is $350 \times 400 \mu m^2$ [\[34\]](#page-20-7).

Figure 9. S-shaped (**a**) and V-shape (**b**) FLC multi-stable switching [\[29\]](#page-20-2).

The reverse bistable effect is observed in FLC devices [\[35\]](#page-20-8), as shown in Figure [10.](#page-8-2) Figure [10a](#page-8-2),b shown the electro-optical responses of traditional bistable and reverse bistable effect. The reverse bistable effect exhibits two stable states and is switched between two states by the falling edge of the driving pulses. The anchoring strength and dielectric property of the alignment layer is critical for the existence of the reverse bistable effect [\[35\]](#page-20-8). Potential applications of reverse bistable effect includes new design of energy-saving devices, such as e-paper, etc. Additionally, the clear distinction of traditional and reverse bistability facilitates the elimination of incomplete refreshing or negative images in bistable displays.

Figure 10. Electro-optical response of (**a**) traditional bistable and (**b**) reverse bistable FLC. The polarizer is placed along angle β with respect to helical axis, where $β = θ$ and $θ$ is the tilt angle of ferroelectric liquid crystal. (**c**) is the frequency characteristics of the hysteresis loop width [\[35\]](#page-20-8).

It is validated experimentally that the depolarization field is responsible for the reverse bistability [\[35\]](#page-20-8). Considering the FLC cell with symmetric boundary condition, by applying the driving voltage of V_0 , the magnitude of the actual electric field applied on the FLC layer is:

$$
E_{FLC} = \frac{\varepsilon' V_0 - 2(P_S/\varepsilon_0)d'}{2\varepsilon d' + \varepsilon' d} = \frac{V_0}{d} \cdot \frac{1 - 2P_S d'/V_0 \varepsilon' \varepsilon_0}{1 + 2\varepsilon d'/\varepsilon' d},\tag{14}
$$

where *d* is the FLC layer thickness, ε is the FLC's dielectric permittivity, P_S is the spontaneous polarization of FLC material, and d' and ε' are the thickness and the dielectric permittivity of alignment layers.

The depolarization field is:

$$
E_{FLC}^D = \frac{-2(P_S/\varepsilon)d'}{2\varepsilon d' + \varepsilon'd},\tag{15}
$$

Since the spontaneous polarization P_S as well as the dielectric parameters ε and ε' are frequency-dependent, as illustrated in Figure [10c](#page-8-2), the reverse bistability has been observed only at low-frequency driving voltage condition.

3.2. V-Shape Electrooptic Response

The DHF samples exhibit symmetrical response to voltage polarities, as shown in Figure [11a](#page-9-0),b with the configuration that helical axis parallel to polarizer $\beta = 0^{\circ}$ [\[31\]](#page-20-4). The transmittance of DHF sample between crossed polarizers reaches maximum value when $\alpha(z) = 45^\circ$ and $\Delta n(z)d = \lambda/2$ are satisfied simultaneously as illustrated by Equation (7). In the case of $\beta = 0$, the optimal tilt angle θ of FLC should be 45° in terms of getting maximum transmission. α *(2)* = +*3* and $\Delta n(z) = N$.

Figure 11. Symmetric (voltage sign independent) electro-optic response of DHF–FLC [\[31\]](#page-20-4). (**a**) Top—the driving voltage waveform applied to the cell, bottom—the electro-optical response of the cell. (**b**) V-shaped mode in the envelope curve of light transmission saturation states measured at electro-optical response frequency 2 kHz. The light transmission T_h evaluated in comparison with transmission of empty cell placed between parallel polarizers; this transmission is defined as $T_h = 1$.

Let us point to certain advantages of the DHF electrooptical effect for applications as compared with SSFLC mode.

1. Fast switching time under low driving voltage. The electrically controlled transmittance is based on small distortion of molecular distribution in helical structure near equilibrium. As a result, real-time response achieved by Clark-Lagerwall effect has negligible time delay.

2. High tolerance of surface treatment and inhomogeneous cell gap. Strong anchoring and defect-free alignment is critical for SSFLC, whereas for DHF the alignment provides orientation of helical axis.

3. Continuous grayscale controlled by voltage amplitude. The DHF effect operates with the amplitude-dependent grayscale (both linear and quadratic), which provides the possibility of implementation of various of photonic and display devices. Moreover, in $E \approx E_U$ regime, long-term optical memory states are possible.

The V-shape response under high frequency driving also shows a high contrast of bright and dark state, as shown in Figure [11.](#page-9-0) Two unique properties of DHF preferable of active-matrix displays are as follows [\[36,](#page-20-9)[37\]](#page-20-10): Firstly, symmetrical performance to voltage polarities, which is similar to nematic cells, operates in the speed of two orders faster than nematics, i.e. $\tau_{on} \sim 80$ µs and $\tau_{off} \sim 60$ µs; secondly the response exhibiting V-shaped performance under rectangular voltage waveform, as shown in Figure [11,](#page-9-0) is suitable for FSC display devices. The continuously modulated grayscale for RGB colors independently can be achieved as shown in Figure [11.](#page-9-0)

In particular, the unique electro-optical characteristics of fast switching V-shape occurs with designed cell configuration and driving waveform. Compared with other known V-shaped FLC modes, DHF operates in a broad frequency range up to several kilohertz instead of a specific frequency. The independency switching on frequency allows V-shape DHF operates under a high frequency for FSC displays, which is a practical method to reduce color breakup effect.

One unique property of DHF mode is the independence of the response time on applied voltage at *V* < *VC*. Another characteristic feature of DHF mode is frequency dependence of the electro-optical response time, which is observed experimentally, as shown in Figure [12.](#page-10-0) We have found that the switching time of DHF decreases with higher frequency of the applied voltage [\[38\]](#page-20-11).

Figure 12. Frequency dependence of response time in DHF regime [\[38\]](#page-20-11).

 display should be less than 1 ms (240 Hz frame frequency). The RGB LEDs backlight with around 200 The DHF FSC display cell with red, green and blue LEDs forming sequential fields to generate full color has been elaborated [\[38\]](#page-20-11). An FSC display does not need color filters and has the advantages of increased light transmission and higher spatial resolution. The target response time for an FSC µs duration of each color were synchronized to the driving voltage pulses with the DHF cell. In this regime, the transmission is continuously tunable independently for each color using the amplitude modulation of voltage signals, as show in Figure [13.](#page-10-1)

Figure 13. Bottom is the electrooptical response of the DHF. Top is driving signal applied and synchronized sequentially with corresponding red, green, and blue light emitting diodes [\[38\]](#page-20-11).

*3.3. Orientational "Kerr E*ff*ect"*

Vertically aligned DHFs (VADHFs) with helical pitch shorter than wavelength exhibits Kerr effect of pure phase modulation due to the inclination of optical axis of FLC helix, thus it is called orientational Kerr effect [\[39,](#page-20-12)[40\]](#page-20-13). In this regime, the distribution of FLC molecule is modulated by electric field, introducing a deformation of the helix. In order to exclude the selective Bragg reflection, the FLC mixture with helical pitch around 150 nm was synthesized. The cell configuration operates [∥]*−* [⊥] [∥] [⊥] with orientational Kerr effect, as shown in Figure [14a](#page-11-0), smectic layers are arranged parallel to substrates with helical axis vertically aligned, and electric field is applied parallel to the substrate surface with inter-digital electrodes. In the initial state, the vertically aligned helix shows optical isotropic property π for the incident beam perpendicular to the substrates. In this case, the standing FLC helix can be μ considered as uniaxial optical medium with optical axis vertically. The deformation of the helix induced by electric field perpendicular to the helical axis introduces optical anisotropy with birefringence of Δn_{ind} = *n*_{||} − *n*_⊥, where *n*_{||} $/n_$ are the in-plane refractive indices along and perpendicular to the field. The electrically induced birefringence exhibits Kerr effect and is proportional to the square of electric field: ∆*nind* ∝ *E 2* . In this configuration, pure phase modulation of over 2π modulation depth showing a constant ellipticity and no hysteresis is realized with switching time less than 100 µs. It has various potential applications in modern photonic devices.

(VADHF) cell placed between crossed polarizers at $V = 0$ V. The red mark is 20 μ m. **Figure 14.** Schematic representation of geometry of a vertically aligned DHF cell [\[40\]](#page-20-13): (**a**) 1—glass plates, 2—in-plane electrodes, 3—smectic layers parallel to glass substrates, 4—a voltage generator. (**b**) The chemical structure of stearic acid chromium salt. (**c**) The texture of Vertically aligned DHFs

layers [\[40\]](#page-20-13). The electrodes are designed with width of 2 μm and with gap of 50 μm in between. The adopted vertical alignment material is stearic acid chromium salt with chemical formula shown in The cell geometry is shown in Figure [14a](#page-11-0), in which the helical structure is aligned vertically and inter-digital electrode on the bottom substrate for applying electric field parallel to the smectic Figure [14b](#page-11-0), which is fabricated by spin coating on substrates of with 40 nm-thick layer and soft-backing at 100 ◦C for 10 min. The Figure [14c](#page-11-0) illustrates the textures of vertically aligned DHF sample under polarized microscope in the absence of electric field.

With electric field applied along x axis through inter-digital electrodes under the condition that E < Ec, the principle axis of helical structure in VADHF sample is deflected from z axis by the angle of ∆α on y-z plane, as show in Figure [15a](#page-12-0) [\[40\]](#page-20-13). Consequently, the field induced biaxiality (∆*nind*) appears with $n_{E\|}/n_{E\perp}$ as the refractive index of the helical structure along/perpendicular to the electric field, as illustrated by Figure [15b](#page-12-0).

Figure 15. (**a**) Illustration of the deflection of principal axis in the presence of electric field. (**b**) Schematic representation of the refractive indices ellipsoid in the absence (left) and in the presence (right) of electric field [\[40\]](#page-20-13).

For normally incident light, the electrically controlled birefringence is [\[39,](#page-20-12)[40\]](#page-20-13):

$$
\Delta n_{ind} = n_{\parallel E} - n_{\perp E} = K_{Kerr} E^2, \qquad (16)
$$

where *n*_{||E} and *n*_{⊥E} are the effective parallel and perpendicular refractive indices induced by applied electric field. The Kerr constant is derived as:

$$
K_{Kerr} = 2n_{E=0}\left(1 - n_{\perp}^2 / n_{E=0}^2\right) \left(\chi_E / P_S\right)^2,\tag{17}
$$

where P_S is the spontaneous polarization, and χ_E is the averaged dielectric susceptibility along the field direction The Kerr constant is proportional to the "isotropic" refractive index with zero electric field $\alpha_{Kerr} \sim n_E = 0$, shown below:

$$
n_{E=0}^2 = \left[n_{\parallel}^2 n_{\perp}^2 / \left(n_{\perp}^2 + \left(n_{\parallel}^2 - n_{\perp}^2 \right) \cos^2 \theta \right)^{1/2} + n_{\perp}^2 \right] / 2, \tag{18}
$$

The transmittance *T* between two crossed polarizers shows quadratic changing with *E 2* . The transmittance curve shown in Figure [16](#page-13-0) indicates that 2π phase modulation is obtained at the voltage of \sim 2.1 V/ μ m with the VADHF sample. The light transmission is [\[39,](#page-20-12)[40\]](#page-20-13):

$$
T = \sin^2 2\Psi \sin^2 \frac{\pi \Delta n_{ind} d_{FLC}}{\lambda},
$$
\n(19)

where *dFLC* is the FLC layer thickness, and Ψ is the angle between the polarization plane of incident light and the direction of electric field. From Equation (16), the induced birefringence ∆*nind* can be derived. The experiment result, shown as open circular line in Figure [16,](#page-13-0) fits well with the theoretial plot, shown as blue solid line in Figure [16.](#page-13-0) The saturation value of induced birefringence ∆*nind* of FLC-587 mixture is 0.05, meaning that 2π phase modulation requires the ratio of FLC thickness to wavelength to be $d_{FLC}/\lambda = 20$ (Figure [16\)](#page-13-0). For wavelength in IR region, the corresponding cell gap is also easy to fabricated with good alignment-quality [\[39,](#page-20-12)[40\]](#page-20-13).

Ψ VADHF cell placed between crossed polarizers A at Ψ = 45◦ [\[40\]](#page-20-13). The solid blue line is the theoretical **Figure 16.** The dependence of transmittance and induced birefringence on amplitude of electric field for fitting. Insertion shows the frequency dependence of Kerr constant.

Δ The experiment results of *Kkerr*, calculated from detected ∆*nind* by using Equation (16), shows *χ* higher than 2kHz results from the dispersion of dielectric susceptibility χ*^E* defined as [\[39](#page-20-12)[,40\]](#page-20-13): frequency-independence at frequency up to 2 kHz, as illustrated in the insertion of Figure [16.](#page-13-0) The Kerr constant of VADHF ($K_{\text{kerr}} = 27 \text{ nm}/V^2$) is evaluated in comparison with commonly used materials. It is two-order larger than that of nitrobenzene, and twice larger than that of polymer stabilized blue phase LC (PSBPLC) [\[41\]](#page-20-14). As in Equation (17) the dispersion of Kerr constant *Kkerr* of VADHF at frequency

$$
\chi_E = \frac{P_s^2}{2Kq_0^2},\tag{20}
$$

m where *K* is the elastic constant and $q_0 = 2\pi/P_0$ is the wave vector of the helix. From Equation (20), we can see that *Kkerr* can be further improved by the optimization of FLC material parameters.

 \overline{a}

In orientational Kerr effect of VADHF, pure phase modulation without changing the ellipticity of incident light is observed, since the electrically induced variation lies in the regime of refractive indices (Figure [17\)](#page-13-1). Before the helix unwinding process (*E* < *Ec*), the induced birefringence ∆*nind* increases *Δ* quadratically with electric field and the ellipticity of output light remains unchanged. When the electric field goes in to the helix unwinding region (near or higher than *Ec*), the quadratic relation is broken and also leads to the increase of output ellipticity, which is due to the ration of polarization plane.

μ **Figure 17.** The induced birefringence and the ellipticity of the emerging light of 18 µm thick VADHF cell at the frequency of 40 Hz [\[40\]](#page-20-13). The insertion represents the variation of the switching on and off time with respect to the applied voltage.

μ the driving frequency to be over 1 kHz. Compared with competing technologies like PSBPLC, VADHFThe dependence of switching-on and -off time *tON* and *tOFF* on voltage applied is shown in the insertion of Figure [17.](#page-13-1) The response time of VADHF is in the range of less than 100 µs, which allows

possesses the advantages of higher Kerr constant, faster response, and hysteresis-free performance, which are preferable in developing phase or amplitude modulation devices for emerging displays and modern photonics.

3.4. Fast Shutter with High Contrast Ratio

ESH mode can be applied as fast response shutters for amplitude, phase and polarization modulation. For instance, ESH plate sandwiched between polarizer and quarter wave plate acts as a polarization selector of two orthogonal circular polarizations with sub-millisecond response, which can be placed before passive polarization gratings for fast beam steering purpose, as shown in Figure [18a](#page-14-0)–d [\[42\]](#page-20-15). The switching time for beam steering achieved is below 100 µs with voltage within μ 10 V as shown in Figure [19.](#page-14-1)

Figure 18. Schematic illustration of ESH as a polarization shutter in a beam steering set up. (**a**) The optical setup with FLC phase shutter. (**b**,**c**) are FLC textures (right) under two voltage polarities recorded by polarized microscope with polarizer and analyzer illustrated (left), the helical axis is shifted θ angle θ from polarizer. (**d**) Texture of polarization grating [\[42\]](#page-20-15).

Figure 19. The dependence of switching time on applied electrical field [\[42\]](#page-20-15).

μ viewing angle are obtained. This display also has an opportunity to be applied for 3D LCD applications.The Pulse width modulation technique is adopted to control the residual light and thus to generate gray levels [\[38\]](#page-20-11). The numbers of displayed color are determined by the response time of ESH. Gray level can be generated by changing with the bright time of the cell, as shown in Figure [20a](#page-15-0). Considering the ESH cells show less than 50 µs under 5 V fast response time, large color triangle as well as wide

Figure 20. (**a**) Driving scheme for ESH FSC. Top three are the waveforms applied to three sequential RGB LEDs. The fourth waveform is the driving signal of ESH cell. (**b**) Some of the achieved colors with different gray levels [\[38\]](#page-20-11).

3.5. Fast Switching Gratings

Diffractive optical elements based on liquid crystals have been massively documented recently [\[43–](#page-20-16)[50\]](#page-21-0). These can be classified into three basic categories: (1) the intrinsic diffractive structure such as cholesterics or ferroelectrics [\[43\]](#page-20-16); (2) non-uniform electric field deployed by patterned electrodes [\[44\]](#page-20-17); (3) periodical initial orientation by surface or volume alignment [\[45\]](#page-20-18).

The diffraction due to the intrinsic structure like ferroelectric domains or periodic helix brings diffraction lobes, which influence the dark-state quality of displays, as shown in Figure [21a](#page-15-1) of the viewing angle chart in terms of Luminance (cd/m²) of dark state of FLC display illumined by white LED. The intensity profile along the diffraction lobe shown in Figure [21b](#page-15-1) illustrates the energy distribution in bright and dark states along. In addition, the larger spontaneous polarization and higher electric amplitude contribute to the inherent diffraction of FLC, as shown in the right insertion of Figure [21b](#page-15-1) [\[50\]](#page-21-0). Then enhancement of the diffraction efficiency can be obtained by introducing chiral single wall carbon nano tubes (SWCNT) into FLC mixtures [\[44\]](#page-20-17). In this manner, one faces the tradeoff between improvement of diffraction and the confinement of electronic conductivity. Thus, further research is necessary for the intrinsic diffraction of FLCs to be improved and explore potential applications.

Figure 21. (**a**) The luminance viewing angle plot for the FLC in the dark state, (**b**) the intensity profile along the diffraction lobe. The left insertion shows the photograph of the bright and dark state under crossed polarizers, and right insertion shows the intensity profile of the diffraction lobe [\[44\]](#page-20-17).

With applying non-uniformly distributed electric field by properly designing the patterned electrodes, one can realize tunable diffraction based on LCs. Figure [22a](#page-16-0),b shows two designs of inter-digital electrode and periodically vertical field for FLCs. In this case, the combination of periodic electric field and intrinsic structure needs to be taken into consideration to achieve desired diffraction profile [\[45\]](#page-20-18). Moreover, the defects induced at the boundary between areas of different electric field may arise, as shown in Figure [22d](#page-16-0) on top on ITO electrode, which ought to be solved for the device robustness.

Figure 22. (**a**) The schematic of the FLC grating cell with inter-digital electrodes, the blue means positive and red means negative charge. (**b**) the schematics of the FLC grating cell with periodic vertical electric field. (**c**) Diffraction pattern of FLC grating describe in (a). (**d**) Texture of defects after several cycle of operations on the top of ITO electrodes of FLC grating cell described in (a) [\[45\]](#page-20-18).

Another approach is based on the periodic alignment of the FLCs [\[46](#page-20-19)[–49\]](#page-20-20). The periodical volume-alignment ban be obtained with polymer stabilized FLCs with properly index-matching between adopted polymer and FLC material. However, the additional diffraction and hysteresis due to the polymer network may appear [\[45](#page-20-18)[,46\]](#page-20-19). Another approach is to pattern the helix orientations by surface alignment for instance by photoalignment technology. With the advantages of re-writability and controllable anchoring energy of sulfonic azo-dyes, the high quality of periodic orientation and hysteresis-free operation are possible to achieve [\[47,](#page-20-21)[49\]](#page-20-20).

Based on the optimal aligning condition described by Equation (13), the diffractive optical elements made by ESH FLCs inherit the properties like high contrast, no diffraction lobe as shown in Figure [23a](#page-16-1), and fast switching under low voltage [\[23\]](#page-19-18). Two step exposure deployed with single mask as shown in Figure [23b](#page-16-1) is normally applied for generation of two-domain pattern [\[47\]](#page-20-21). In this process, the easy axis of two domains can be arranged orthogonally or with arbitrary angle depending on the application circumstances. Figure [23](#page-16-1) shows the fabrication process as well as the textures of orthogonally aligned domains forming 1D or 2D binary ESH gratings with period of 50 µm.

Figure 23. (**a**) The intensity profile of the diffraction of ESH cell between crossed polarizers in bright and dark state and insertion shows photographs of the respective states. (**b**) The two-step exposure fabrication procedure. (**c**) and (**d**) shows the textures of 1D and 2D ESH gratings [\[45\]](#page-20-18).

The diffraction pattern and the intensity profile for 1D and 2D grating are shown in the insertion of Figure [24a](#page-17-0),b, respectively. The dark states of the FLC grating shown in Figure [24c](#page-17-0) are identical for 1D and 2D ESH gratings. The optical quality of both diffractive and non-diffractive mode as well as the contrast between them is evaluated by plot of intensity distribution shown in Figure [24d](#page-17-0),e. The diffraction efficiency calculated from the transmittance of diffractive orders gets to saturated value over 70% with electrical field over $1.3 \text{ V/}\mu$ m as illustrated in Figure [24](#page-17-0) [\[45](#page-20-18)[,48\]](#page-20-22).

ff (**a**) 1D grating, (**b**) 2D grating and (**c**) black state; (**d**,**e**) are intensity profiles of 1D and 2D gratings **Figure 24.** The dependence of first order transmittance on electric field in bright and dark state of ESH grating theoretically (solid line) and experimentally (dotted line). Insertions: Diffraction pattern of measured at $V = 5 V [47]$ $V = 5 V [47]$.

Besides optical quality, the dynamic response is also a critical parameter to evaluate LC based diffractive elements. By using ITO electrodes uniformly coated on substrates, the response of diffractive orders is similar to that of planar aligned ESH cell, as shown in Figure [25.](#page-17-1) The peak of switching time represent the helix unwinding process, so the accordance voltage is defined as critical voltage. After the helix is totally unwound by electric field, the switching time follows proportional decay along the increase of applied voltage as described by Equation (3). When the applied electric field averaged by cell gap reaches 6.6 V/ μ m, the switching time is around 20 μ s, which can be further minimized by improvement of material parameters. The insertion of Figure [25](#page-17-1) shows the waveform of response under high driving frequency of 5 kHz. The contrast ratio of the first diffractive order, defined as *Imax*/*Imin*, is over 7000:1 at 6 V/µm of 2 kHz and decreases slightly due to small modulation time. The high contrast can be enhanced by higher voltage even for higher frequency [\[39,](#page-20-12)[47\]](#page-20-21). With the advantages of fast switching, high contrast and high efficiency, ESH mode can be applied for various diffractive elements, such as Dammann gratings, Fresnel plates and so on.

Figure 25. Voltage dependence of the response time at frequency of 500 Hz (solid circles) and frequency dependence of the first order contrast ratio at voltage of 10 V (open circles). Insertion shows the waveforms of the applied voltage (bottom) and the transmittance of first order (top) at frequency of 5kHz [\[47\]](#page-20-21).

Diffractive Fresnel lens composed of ESH domains is shown in Figure [26a](#page-18-1)–d, in which the angle of adjacent aligning orientations is set to be 45°. Thus, Figure [26a](#page-18-1),b show textures containing bright and dark circles under polarized microscope [\[51](#page-21-1)[,52\]](#page-21-2). The photograph of diffractive and non-diffractive state is also shown. The spatial resolution of ESH patter is in submicron region by using photoalignment technology [\[53\]](#page-21-3). In summary, the ESH diffraction mode in association with photoalignment exhibiting high optical quality as well as fast switching time providing high flexibility in design and fabrication of various diffractive elements.

Figure 26. (**a**,**b**) illustrate the textures of the ESH Fresnel lens under polarized microscope. (**c**,**d**) show the photographs of the diffractive and non-diffractive states [\[51\]](#page-21-1).

4. Conclusions

With the advantage of photoalignment technology, FLC electrooptical modes providing a fast response and a high contrast, including SSFLC mode, DHF mode, and ESH mode, are described and analyzed for applications in next-generation displays and modern photonic devices. The possible applications include high-resolution micro-displays based on FSC displays, 2D/3D switchable LCDs based on switchable goggles or lenses, and so on. Further research for improvement of FLC displays can focus on certain aspects: (i) development of new fast responded FLC materials with fast switching and a sufficient number of switchable gray levels (V-shape switching); (ii) implementation of the working prototypes of novel FSC FLC displays, including the 3D version; (iii) investigations of regimes of operation to allow to use efficient addressing of FLC displays including TFT drivers enabling a high switching current; (iv) solving the problem of a mechanical stability of FLC layers; (v) mass production of new FLC materials with optimal characteristics.

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