Effect of Cr Doping on the Structural, Optical and Dielectric Properties of MoO$_3$ Microrods Synthesized by Sol-Gel Auto Combustion Method

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1. Introduction

Transition metal oxides have been used in recent research innovations due to their excellent properties. They produce different phase structures due to their different metal–oxygen ratios. Molybdenum trioxide (MoO$_3$) has good electrical, optical, and microwave dielectric properties due to its structural orientation [1]. MoO$_3$ has wide band gap energy ($2.8$–$3.6$ eV) with $n$-type semiconductor conductivity [2]. Basically, there exist three polymorphous structures of MoO$_3$: β-MoO$_3$ (monoclinic), α-MoO$_3$ (orthorhombic), and h-MoO$_3$ (hexagonal). Thermodynamically, the structure of α-MoO$_3$ is very stable and
attractive for practical uses because of its anisotropic compositions along the (010) direction [3]. This anisotropic chemistry is created by stacking a bi-layer sheet of octahedral Mo$_2$O$_6$ bonded through Van der Waal forces. Due to intrinsic structural anisotropy and the ability of transformation of oxidation states between molybdenum-IV and V ions, α-MoO$_3$ (orthorhombic) has been verified to have exceptional applications in the fields of catalysis, field emissions, lithium-ion batteries, energy storage devices, gas sensing, and electrochromic and photochromic devices [4,5].

Over the last couple of years, molybdenum trioxide has received extensive attention because of its many applications in various fields. The various significant aspects of molybdenum trioxide have led to this interest, including strong photo catalytic ability, battery device assembly, and Li storage performance [6]. As a result, MoO$_3$ is widely employed in industry, including catalysts [7], field effect transistors [8], gas sensors, and battery electrodes [9]. Many researchers reported that MoO$_3$ has outstanding properties and vast uses in the field of super capacitors, memory devices, OLEDs (organic light-emitting diodes), dielectric resonator devices, and solar cell equipment [10–17]. MoO$_3$ has three polymorphic phases: (a) orthorhombic, (b) hexagonal, and (c) monoclinic. Of these phases, the orthorhombic phase is more stable, and along with bi-layered octahedral distortion it has good electrical, optical, and magnetic properties [18]. Many researchers study it and found it in the form of nanowires, nanorods, thin film, microrods, quantum dots, and nanobelts [19–23].

In the current research work, we focused on synthesizing chromium Cr-doped MoO$_3$ microrods and use the sol gel auto combustion route. The effect of (Cr$^{3+}$) cation substitution is simultaneously evaluated on structural and microstructural development and band gap energy of MoO$_3$ microrods. Correspondingly, the prepared pure and Cr-doped MoO$_3$ microrods were characterized using X-ray diffraction (XRD), scanning electron microscopy (SEM), energy dispersive spectroscopy (EDS), and diffuse reflectance spectroscopy (DRS).

2. Experimental Method

The Cr-substituted MoO$_3$ microrods with 3 wt% and 6 wt% were prepared by the sol–gel auto combustion technique. The stoichiometric amounts of MoO$_3$ (purity 99.97%, Sigma-Aldrich chemicals, St. Louis, MI, USA) and chromium chloride (purity 99.5%, Sigma-Aldrich chemicals, St. Louis, MI, USA) including those with nitric acid were used to prepare the product powders. We used the nitric acid (HNO$_3$) as a chelating agent to obtain a homogenous and straightforward solution. The solution was stirred with the help of a hot plate and magnetic stirrer at 90 $^\circ$C for one hour to dissolve reactants in distilled water. Then, the concentration of chromium chloride (CrCl$_3$) (3 wt%, and 6 wt%) was doped into the solution. At that point, the solution was stirred magnetically at 90 $^\circ$C for 6 h, adding ammonia drop by drop to maintain the pH value at 6–7. At the end, the solution changed into a viscous brown gel and then self-combustion happened, as shown in the graphical abstract. After complete crushing and grinding, the fine powder was then used in vacuum furnace sintering at 500 $^\circ$C for 2 h in the nitrogen and hydrogen atmosphere. X-ray diffractometer (XRD) (JDX-3532, JEOL, Japan) was used for studying the crystal structure of all fabricated samples functioned with Cu-K radiations of wavelength $\lambda$ = 0.1540598 nm, at 45 $\times$ $10^3$ V and 40 $\times$ $10^{-3}$ A in the 2$\theta$ range of 5–60$^\circ$. The microstructures functional at 20 KV were analyzed using a scanning electron microscope (SEM) (JSM-5910, JEOL).

3. Results and Discussion

3.1. Phase Analysis

The crystal structure of the synthesized pure and Cr-doped MoO$_3$ microrods was investigated by XRD method, as shown in Figure 1a,b. The observed diffraction peaks revealed the formation of a single-phase base composition MoO$_3$ that corresponded to PDF card no. 00-021-0569, which shown the hexagonal crystal structure with space group (P63) [24,25]. The sharp and intense peaks depict the crystalline behavior of all the samples. Among these planes, the (2 1 0) plane at 26.07$^\circ$ revealed the maximum intensity. The base
sample was indexed properly by using WinXpow software. It can also be observed that the lattice parameters as well as lattice volume increased with Cr-doped MoO$_3$ microrods. Compared with the pure MoO$_3$ sample, the corresponding diffraction peaks shifted to lower angles, the intensity of peaks increased, and the width of peaks also increased following the doping of Cr$^{3+}$ contents. Moreover, the change of the peaks’ positions could be ascribed to the inhomogeneity and micro-strain in the samples or may be due to the substitution of the relatively larger ionic radius of Cr$^{3+}$ ($R_{Cr} = 0.61$ Å) than Mo ($R_{Mo} = 0.59$ Å), which is consistent with the deduction of Bragg's diffraction law (2$d$Sin$\theta = m\lambda$), as shown in Figure 1b [26,27].

![Figure 1. (a) XRD patterns of un-doped and Cr-doped MoO$_3$ microrods. (b) Displays the zoomed view of (2 0 0) and (2 1 0) peak shifting toward lower angle.](image)

The Debye Scherer equation is used to calculate the average crystalline size of all samples using the reflection of the 2$\theta$ value of the XRD data [28],

$$D = \frac{k\lambda}{\beta \cos \theta}$$

where 'D' is the average crystallite size, the value of Scherer constant ‘$k$’ is 0.94, $\lambda = 0.15406$ nm is the wavelength of the X-ray beam, and $\beta$ is the full-width half. This technique is used with XRD data, where the crystallite size (D) is associated with the expansion of intensive peaks. The instrumental contribution of $\beta$ was removed before the analysis of the crystallite size and micro-strain.

Figure 2 presents the behavior of crystallite size. The crystallite size depended on the lattice micro-strain and radius of the substituted ions. It has been observed that generally the average crystallite size decreases with the increasing Cr$^{3+}$ content ($x$), and this may be attributed to the growth of the crystal structure, which may be due to that the ionic radius of the substitution element, Cr$^{3+}$, is larger than molybdenum [26].
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Figure 2. Plot of average crystallite size ($D$ and $D_{W-H}$) of un-doped and Cr-doped MoO$_3$ (3 wt% and 6 wt%).

A W–H (Williamson–Hall) plot is a very important technique for measuring the values of lattice parameters and crystallite size as well. Equation (2) was used to plot (W–H) graphs for all the samples [29].

$$\beta \cos \theta = \frac{k \lambda}{D} + 4 \varepsilon \sin \theta$$

where $\beta$ is the full width at half maximum (FWHM), $\theta$ is the Braggs angle, $k$ is the size factor, $\lambda$ is the wavelength of X-rays, and $D$ is the average crystallite size. Finding the slope of a linear plotted graph against $4 \sin \theta$ gives the information about the lattice strain and crystalline size ($D_{W-H}$) for all the samples (un-doped and Cr-doped), as shown in Figure 3 [30]. The effective values of crystallite size ($D_{W-H}$) were measured by the Williamson–Hall (W–H) technique and were found to be 104.251 nm, 87.204 nm, and 71.842 nm for each sample. The average values of crystallite size ($D_{W-H}$) and micro-strain ($\varepsilon_{W-H}$) along with uncertainties were measured by the Williamson–Hall (W–H) technique, as shown in Table 1. Around the fitted line, the points are noticed to be widely scattered. It was observed that certain additional parameters of the characterized sample were not taken into consideration or some alternative method should have been adopted.
Table 1. Data on ($D_{W-H}$) and ($\varepsilon_{W-H}$) of un-doped and Cr-doped MoO$_3$ microrods along with uncertainty.

<table>
<thead>
<tr>
<th>Composition</th>
<th>Average Crystalline Size ($D_{W-H}$)</th>
<th>Uncertainty in Average Crystallite Size ($\Delta D_{W-H}$)</th>
<th>Average Micro-Strain ($\varepsilon_{W-H}$)</th>
<th>Uncertainty in Average Micro-Strain ($\Delta \varepsilon_{W-H}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>MoO$_3$</td>
<td>104.251 nm</td>
<td>±0.158</td>
<td>5.828</td>
<td>±0.462</td>
</tr>
<tr>
<td>3 wt% Cr-doped MoO$_3$</td>
<td>87.204 nm</td>
<td>±0.006</td>
<td>2.255</td>
<td>±0.391</td>
</tr>
<tr>
<td>6 wt% Cr-doped MoO$_3$</td>
<td>71.842 nm</td>
<td>±0.222</td>
<td>1.308</td>
<td>±1.392</td>
</tr>
</tbody>
</table>

3.2. Surface Morphology

Figure 4a–c show the surface micrographs of un-doped and Cr-doped MoO$_3$ microrods with (×20,000) magnification, respectively. In Figure 4a,b it can be clearly observed from SEM images that the size of microrods grow with the increase in Cr content. The surfaces of the synthesized rods are clean, but their crystal structures are found in spherical shape whose sizes are in the range of microns, which indicates its one-dimensional hexagonal rod geometry [6,31]. Figure 4c shows irregular surface structure microrods. Basically, these are the small microrods that are stacked together in a cluster shape, and their appearance shows to develop on the microrods’ surface [32]. It is clear from the image that the nanorods have poor morphology because the lengths and diameters of the nanorods are not uniform. The diameter of the microrods varies from 0.07 μm to 0.21 μm, seen by using ImageJ software. In addition, they are not well aligned in the direction perpendicular to the substrate. The reason for that may be that the surface of the substrate may not be smooth at the microscale or due to the miss-matching lattice structure, which greatly affects the morphology of microrods [33].
using ImageJ software. In addition, they are not well aligned in the direction perpendicular to the substrate. The reason for that may be that the surface of the substrate may not be smooth at the microscale or due to the mismatching lattice structure, which greatly affects the morphology of microrods [33].

Figure 4. The SEM and EDX micrographs of the (a) un-doped, (b) 3%, (c) 6% Cr-doped MoO₃.

Figure 4a–c show that the EDX analysis was used to confirm the exact deposited number of elements in un-doped and Cr-doped MoO₃ microrods. Figure 4b,c confirm the presence of Cr elements. The 3 wt% and 6 wt% of Cr was doped in the solid solution of MoO₃ microrods. These compositions of Cr by atom % were calculated by using the following formulae:

\[
C'_{1} = \frac{C_{1}A_{2}}{C_{1}A_{2} + C_{3}A_{1}} \times 100\%
\]  

(3)
\[
C'_2 = \frac{C_2 A_1}{C_1 A_2 + C_2 A_1} \times 100\% \tag{4}
\]

where \(C'_2\) is the atom %, \(C_1\) is weight %, and \(A_1\) is the atomic number of the un-doped elements, while \(C'_2\) is the atom %, \(C_2\) is weight %, and \(A_2\) is the atomic number of the doped elements. Equations (3) and (4) represent the conversion of wt% into atom % of two elements. The values of all the samples by weight % and atom % are shown in Table 2.

### Table 2. Elemental compositions by atom % and weight % of the Cr-doped MoO\(_3\) samples.

<table>
<thead>
<tr>
<th>Elements</th>
<th>Atom % (MoO(_3))</th>
<th>Atom % (MoO(_3)-3%Cr)</th>
<th>Atom % (MoO(_3)-6%Cr)</th>
<th>Weight % (MoO(_3))</th>
<th>Weight % (MoO(_3)-3%Cr)</th>
<th>Weight % (MoO(_3)-6%Cr)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Molybdenum</td>
<td>66.66</td>
<td>65.25</td>
<td>63.83</td>
<td>53.77</td>
<td>52.96</td>
<td>52.12</td>
</tr>
<tr>
<td>Chromium</td>
<td>–</td>
<td>1.10</td>
<td>2.21</td>
<td>–</td>
<td>1.52</td>
<td>3.10</td>
</tr>
<tr>
<td>Oxygen</td>
<td>33.34</td>
<td>33.65</td>
<td>33.96</td>
<td>46.23</td>
<td>45.52</td>
<td>44.78</td>
</tr>
<tr>
<td>Total</td>
<td>100</td>
<td>100</td>
<td>100</td>
<td>100</td>
<td>100</td>
<td>100</td>
</tr>
</tbody>
</table>

### 3.3. Diffuse Reflectance Spectroscopy

The optical absorption characterization of pure and Cr-doped MoO\(_3\) microrods was performed by diffuse reflectance spectra (DRS) in the range of 200 to 800 nm, as depicted in Figure 5. It was observed that there was a strong reflectance behavior between 450 nm and 500 nm that revealed the high absorption behavior within the visible region [34]. The sharp characteristic absorption band edge was found to be around 325 to 475 nm for each rod and the transition of the band gap was attributed to it by absorbing light from the visible range. The reflectance spectra demonstrated that the reflection percentage increased from 350 nm to 800 nm for upper absorption. The 340 nm spectrum indicated that the reflectance percentage was decreased due to the absorption behavior of the sample [35].

![DRS spectra of un-doped and Cr-doped MoO\(_3\) samples.](image-url)
3.4. Optical Properties

Figure 6a–c show that the defect-free band structure was identified and the optical band gap was derived from the Kubeka–Munk function, which is [36];

\[ F(R) = \frac{K(\lambda)}{s(\lambda)} = \frac{(1 - R)^n}{2R} \propto \alpha = \frac{(h\nu - E\text{\_g})^n}{h\nu} \]

where ‘F(R)’ is the re-emission function, ‘s(\lambda)’ is the scattering coefficient, ‘K(\lambda)’ is the absorption coefficient, ‘h\nu’ is the photon energy, ‘E\text{\_g}’ is the band gap energy, ‘R’ is the diffuse reflectance, and ‘n’ is the exponent term that identifies the transition types, i.e., indirect transition \( (n = 1/2) \), direct transition \( (n = 2) \), indirect forbidden energy gap transitions \( (n = 1/3) \), and direct forbidden energy gap transition \( (n = 2/3) \). In this work, only indirect transition was considered for all samples. The band gap energy was predictable from the plot of \( F(R)^2 \) and energy. Figure 6d shows the band gap energy of the un-doped and Cr-doped MoO\(_3\) microrods. The energy band gap of the pure MoO\(_3\) (2.98 eV) is greater than that of the Cr-doped MoO\(_3\) (2.71 eV). The band gap energy increases due to decreasing the particle size of the synthesized sample and reduces with increasing the dopants’ concentration, i.e., Cr or Ni [37–39]. Generally, band gap energy decreases with increasing doping compositions.

![Figure 6. K-M function graph of (a) un-doped, (b) 3 wt%, (c) 6 wt% Cr-doped MoO\(_3\). (d) Optical band gap energy.](image-url)
There is also the possibility of creating oxygen vacancy, which can also reduce the band gap energy of MoO$_3$. The band gap energy values of pure and doping samples are shown in the Table 3.

<table>
<thead>
<tr>
<th>Composition</th>
<th>a = b (Å)</th>
<th>c (Å)</th>
<th>D (nm)</th>
<th>$E_g$ (eV)</th>
</tr>
</thead>
<tbody>
<tr>
<td>MoO$_3$</td>
<td>10.53</td>
<td>14.88</td>
<td>76.69</td>
<td>2.98</td>
</tr>
<tr>
<td>3% Cr-doped MoO$_3$</td>
<td>10.54</td>
<td>14.88</td>
<td>71.88</td>
<td>2.80</td>
</tr>
<tr>
<td>6% Cr-doped MoO$_3$</td>
<td>10.55</td>
<td>14.89</td>
<td>70.57</td>
<td>2.71</td>
</tr>
</tbody>
</table>

$E_g$ = band gap energy; a, b and c = lattice parameters; D = average crystallite size.

3.5. Dielectric Properties

Figures 7 and 8 show the frequency dependence of the dielectric constant ($\varepsilon_r$) and dielectric loss (Tan$\delta$) of un-doped and Cr-doped MoO$_3$ microrods. The value of the dielectric constant of MoO$_3$ decreases with the increases in frequency as well as Cr$^{3+}$ (Figure 7). This might be due to the alignment of permanent dipoles with the direction of the electric field at lower frequencies, which contributes to the dielectric material’s total polarization. On the other hand, the dipole can no longer follow the field at higher frequencies since the field rapidly varies [40]. The dielectric loss of MoO$_3$ increases with the increases in frequency as well as Cr$^{3+}$ contents (Figure 8). It increases to a maximum value, after which it goes to a lower value. The peak is observed between 1.6–1.8 GHz frequency ranges. This may be due to the dielectric relaxation phenomena occurring in the compound [41]. The tangent loss (tan$\delta$) caused by the dipole relaxation phenomena decreases with frequency, as seen in the tan$\delta$ frequency plots [42].

![Figure 7. Dielectric constant as a function of frequency of un-doped and Cr-doped MoO$_3$.](image-url)
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Figure 7. Dielectric constant as a function of frequency of un-doped and Cr-doped MoO₃.

Figure 8. Dielectric loss as a function of frequency of un-doped and Cr-doped MoO₃.

4. Conclusions

In the current study, pure and Cr-doped MoO₃ microrods were successfully synthesized via the sol gel auto combustion method. The average crystallite size, lattice parameter, and average micro-strain value change when Cr³⁺ ions are doped in MoO₃ were found. The formation of a hexagonal structure with P6₃ symmetry was confirmed by phase analysis. The average crystallite size (D) also decreased from 76.69 nm to 70.57 nm. The optical band gap energies of 2.98, 2.80, and 2.71 eV were recorded for 0 wt%, 3 wt%, and 6 wt% Cr-doped MoO₃ microrods, respectively. The surface morphology of all the samples revealed the formation of microrods with different sizes (small and large). The micropores were observed in the group of hexagonal microrods. Dielectric studies showed that both the dielectric constant and tangent loss are frequency- as well as concentration-dependent. The obtained results declared that MoO₃ is an appropriate host material for all the transition metals or minerals which are used for the application of optoelectronic devices.

Author Contributions: This work was carried out in collaboration among all authors. A.Z., N.K.S. and V.T. writing, review, editing and analysis of the manuscript. A.A. (Asad Ali) and M.A. (Mujahid Abbas) did the final review, corrections, and editing. M.M., A.A. (Aiyeshah Alhodaib), M.A. (Mona AlHarbi), N.K.S. and V.T. helps in Software and Validation. Z.H.K., A.H.J. and M.A. (Mohammed Aljohani) helps in prepared Content analysis, graphical arrangements and Formal analysis. All authors read and approved the final manuscript.

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