Joint Placement and Power Optimization of UAV-Relay in NOMA Enabled Maritime IoT System

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Abstract: In this paper, an unmanned aerial vehicle is utilized as an aerial relay to connect onshore base station with offshore users in a maritime IoT system with uplink non-orthogonal multiple access enabled. A coordinated direct and relay transmission scheme is adopted in the proposed system, where close shore maritime users directly communicate with onshore BS and offshore maritime users need assistance of an aerial relay to communicate with onshore BS. We aim to minimize the total transmit energy of the aerial relay by jointly optimizing the UAV hovering position and transmit power allocation. The minimum rate requirements of maritime users and transmitters’ power budgets are considered. The formulated optimization problem is non-convex due to its non-convex constraints. Therefore, we introduce successive convex optimization and block coordinate descent to decompose the original problem into two subproblems, which are alternately solved to optimize the UAV energy consumption with satisfying the proposed constraints. Numerical results indicate that the proposed algorithm outperformed the benchmark algorithm, and shed light on the potential of exploiting the energy-limited aerial relay in IoT systems.

Keywords: maritime communication system; optimization; Uplink NOMA; UAV relay network

1. Introduction

One significant challenge for maritime communication networks is the rapid increasing demand of broadband wireless services, especially for offshore maritime users [1]. For near shore maritime users, it is possible to enjoy broadband wireless service in locations where either mobile operator coverage is available or Wi-Fi-based long distance links can be deployed [2]. However, recently, it is still a challenge to provide seamless mobile broadband coverage for offshore maritime users located over tens of kilometers from shore since the communication infrastructures are difficult to deploy in the ocean [3]. For years, MF/HF/WHF-based communication dominated offshore user wireless communications. However, this communication technology cannot afford a high-rate transmission service on accounts of higher propagation delay and insufficient bandwidth [4]. As a conventional solution for offshore high rate transmission service, satellite communication offers a better quality-of-service as well as higher system maintenance cost and the problem of flexibility [5]. Different from satellites, unmanned aerial vehicles (UAVs) have been considered as an economic on-demand data service solution for offshore maritime users in diverse maritime activities owning to its advantage of highly maneuverable and flexible deployment, especially for various mission-critical applications such as emergency deployment and maritime search and rescue [6,7].

Although UAV-assisted communications have been widely studied for terrestrial communication scenarios [8–11], UAV-integrated maritime communication is still an open
research field. To provide an effective aerial relay service, the distribution of users has
great importance in resource allocation and trajectory optimization. Unlike in the terrestrial
scenario, it is difficult to acquire either accurate location information or real-time channel
state information (CSI) of maritime users since the distribution is scattered within a vast
area [12], which increases the complexity of fly trajectory design. In addition, the energy-
efficient issue is another vital problem for UAV relay communication due to the limited
life time, especially for maritime communication scenarios. After departure, a UAV relay
cannot land on the sea until the assigned mission is accomplished.

1.1. Recent Works

Recently, UAV-assisted communication techniques have attracted lots of attention
in maritime communication systems for their deployment flexibility and line of sight (LoS)
transmission ability. There are some works on UAV deployment and resource allocation
problems in UAV-assisted maritime communication systems [13–17]. In [13], the authors
study the optimal UAV placement problem to achieve the maximum system rate in a mar-
titime downlink caching UAV-assisted decode-and-forward (DF) relay communication
system with both air-to-ground and air-to-sea models considered. In [14], a UAV-assisted
communication system is used to extend the coverage of the onshore BSs in the down-
link communication scenario. The non-orthogonal multiple access (NOMA) protocol is
adopted to enable the aerial BSs and simultaneously sever multiple ships. The authors
have proposed a joint UAV transmit power and transmission duration optimization scheme
to maximize the sum rate of ships. In [15], to facilitate spectrum sharing and efficient
backhaul, UAV-added coverage enhancement is studied for maritime communication
in a hybrid space–air–ground integrated network. The UAV trajectory design and trans-
mited power allocation have been jointly optimized by considering the constraints on UAV
kinematics, tolerable interference, backhaul, and UAV transmit power budget. In [16],
UAV-assisted ocean monitoring network architecture has been constructed for a remote
oceanic data collection. In [17], a fermat-point theory-based fast trajectory planning scheme
is proposed to improve received data throughput of UAV. Although the power optimization
problem of UAV relay is studied in [13–15], these works focused on the rate maximization
problem in a downlink maritime communication scenario and neglect resource allocation
issues in uplink scenarios. References [16,17] focused on trajectory design issues subject
to the constraint on the UAV flying energy budget in UAV-assisted maritime data col-
lection systems and ignored the resource allocation problem of UAV relay. Moreover,
all of the aforementioned works presented a power allocation problem of UAV relay by
formulating a throughput maximization problem with constraints of the UAV power
budget. However, the power minimization problem of UAV relay should be discussed
to shed light on the potential of utilizing an energy-limited aerial platform in a maritime
communication scenario.

1.2. Motivation and Contributions

Motivated by [18,19], we study the joint UAV hovering position and power alloca-
tion in UAV-assisted maritime communication systems. Particularly, we focus on a UAV
transmit power consumption minimization issue subject to maritime user’s minimum
rate requirements and transmit power constraints. NOMA-enabled relay is introduced
to the maritime IoT system to improve the spectrum efficiency [20,21]. It worth noting that
the uplink NOMA scheme is introduced to boost the system spectrum reuse in our work,
which is different from the downlink relay system discussed in [13,15,18]. Furthermore,
the NOMA scheme was not employed in [19]. The main contributions of this paper are
outlined as follows:
1. In this paper, we study the power minimization problem subject to user’s minimum rate requirement and UAV transmit power budget in a maritime IoT system with A2A and A2S link model considered. A coordinated direct and relay transmission scheme employing uplink NOMA scheme is proposed and investigated, where maritime close-shore users (MCU) directly communicate with onshore BS, whereas maritime remote users (MRU) communicate with the onshore BS by a half-duplex DF UAV relay.

2. In the proposed maritime IoT system, an interference cancellation parameter is introduced to summarized UAV’s received data expression in transmission phase 1, which facilitates solving the proposed UAV power transmission minimization problem.

3. The successive convex approximation method is applied to deal with non-convex inequality constraints of the formulated optimization problem. The block coordinate descent method (BCD) is used to decouple the original problem into two subproblems, namely power allocation and optimal UAV placement. After that, an iterative algorithm is proposed to optimize power allocation coefficients and optimal UAV coordinates alternately.

1.3. Paper Organization

The rest of this work is organized as follows. In Section 2, the interested UAV-assisted maritime IoT system model and formulated optimization problem are proposed. Section 3 presents joint power allocation and an optimal UAV placement solution to the optimization problem. Numerical results are presented in Section 4. Finally, Section 5 concludes our paper.

2. System Model and Problem Formulation

2.1. System Model

As shown in Figure 1, a UAV-assisted maritime IoT system model, including one onshore base station (BS), one mobile UAV relay, and multiple maritime users deployed on a certain area for data collection, is considered. These maritime users are divided into two groups, including \( K \) maritime close-shore users (MCU) and \( K \) maritime remote users (MRU), according to communication service type. \( K_c = \{ k' \in K_c | |K_c| = K \} \) and \( K_r = \{ k \in K_r | |K_r| = K \} \) denote the MRUs set and MCUs set, respectively. It is assumed that all transmission nodes in this model are equipped with a single antenna, \( K_r \cap K_c = \emptyset \). MCUs are deployed closely along the coastline and can be served directly by the onshore BS. MRUs are deployed far away from the coastline and must rely on a UAV relay for data ferrying. A coordinated direct and relay transmission is introduced, where an MCU directly communicates with an onshore BS, whereas an MRU communicates with an onshore BS by a half-duplex DF UAV relay. A two-user uplink NOMA scheme is considered by an MRU coexisting with an MCU in a spectrum resource block. In this paper, we focus on total transmit power minimum optimization of UAV relay by jointly optimizing power allocation and UAV hovering position. It is assumed that \( |K_r| = |K_c| = K \). Thus, there are \( K \) NOMA pairs in the proposed networks.
Figure 1. System model of maritime IoT system with a UAV relay.

The three-dimensional Cartesian coordinate is considered, where the coastline is approximated as the $x$-axis, the $y$-axis extends into the ocean, and the $z$-axis represents the altitude. The coordinate of the onshore BS is $c_B = (0, 0, h)$. Although locations of maritime users may change along with time according to sea surface waves, their coordinates can still be regarded as approximately fixed in a certain period, which can be denoted as $c_k = (x_k, y_k, 0), \forall k \in K_r$ and $c_{k'} = (x_{k'}, y_{k'}, 0), \forall k' \in K_c$, respectively. The UAV departs from the starting point $J_0$, then flies to the optimal hovering position $J^*$ for the data relaying mission, and finally returns to the original location. According to the pre-planned deployed position of maritime users, the optimal hovering position of the UAV can be predetermined before its mission executes. Thus, the coordinates of the UAV can be expressed as $(x_u, y_u, h_u)$ during the transmission mission’s executed duration. Denote the distances between BS and the UAV, between the UAV and the $k$-th MRU, and between the $k'$-th MCU, respectively, as:

\[
d_{UB} = \| c_u - c_B \| = \sqrt{(x_u - x_B)^2 + (y_u - y_B)^2 + h_u^2} \tag{1}
\]

\[
d_{Bk} = \| c_B - c_k \| = \sqrt{(x_k - x_B)^2 + (y_k - y_B)^2 + h^2} \tag{2}
\]

\[
d_{Uk} = \| c_u - c_k \| = \sqrt{(x_u - x_k)^2 + (y_u - y_k)^2 + h_u^2}, \forall k \in K_r \tag{3}
\]

\[
d_{Uk'} = \| c_u - c_{k'} \| = \sqrt{(x_u - x_{k'})^2 + (y_u - y_{k'})^2 + h_u^2}, \forall k' \in K_c \tag{4}
\]

We assume that the UAV flies high enough to enable an LoS transmission. An air-to-sea (A2S) channel model is composed by large-scale and small-scale fading [15]. Thus, the channel between UAV and $k$-th MRU can be represented as:

\[
h_{Uk} = \frac{1}{(L_{Uk})^{1/2}} \tilde{h}_{Uk}, \forall k \tag{5}
\]

where $L_{Uk}$ denotes the path loss component and $\tilde{h}_{Uk}$ denotes the Rician fading component. Then, the path loss model can be expressed as:

\[
L_{Uk}(dB) = A_U + 10\zeta_U \log 10 \left( \frac{d_{Uk}}{d_0} \right) + X_U \tag{6}
\]
where \( d_0 \) refers to the reference distance, \( A_{UL} \) denotes the path loss at \( d_0 \), \( \xi_{UL} \) denotes the path loss exponent, and \( X_{UL} \) is a zero-mean Gaussian random variable with standard deviation \( \sigma_{X_{UL}} \). Rician fading can be represented as:

\[
\tilde{h}_{UL} = \sqrt{\frac{S_U}{1+S_U}} + \sqrt{\frac{1}{1+S_U}} g_{UL}
\]

(7)

where \( g_{UL} \sim \mathcal{CN}(0,1) \) and \( S_U \) indicates the Rician factor that corresponds to the ratio between the LoS power and the scattering power [24]. In the proposed system, the maritime users are deployed on pre-planned positions, then their location data can be pre-measured. Although locations of MRUs and MCUs may change along with time according to sea surface waves, their coordinates can still be regarded as approximately fixed in a certain period. Thus, their corresponding large-scaled channel state information (CSI) can be obtained. Similarly, the A2S channel between onshore BS and \( k' \)-th MCU is denoted as:

\[
h_{UBk} = \left( \frac{d_0}{d_{UB}} \right) \frac{X_U}{10^{-\frac{A_{UB}+X_{UB}}{10}}} \left( \sqrt{\frac{S_{UB}}{1+S_{UB}}} + \sqrt{\frac{1}{1+S_{UB}}} g_{UB} \right)
\]

(8)

where \( g_{UBk} \sim \mathcal{CN}(0,1) \). The interference A2S link between UAV and \( k' \)-th MCU is denoted as:

\[
h_{ULk} = \left( \frac{d_0}{d_{ULk}} \right) \frac{X_U}{10^{-\frac{A_{ULk}+X_{ULk}}{10}}} \left( \sqrt{\frac{S_U}{1+S_U}} + \sqrt{\frac{1}{1+S_U}} g_{ULk} \right)
\]

(9)

where \( g_{ULk} \sim \mathcal{CN}(0,1) \). On the other hand, The air-to-air (A2A) channel between onshore BS and UAV has a high LoS probability, which can be represented as:

\[
h_{UB} = \left( \frac{d_0}{d_{UB}} \right) \frac{X_U}{10^{-\frac{A_{UB}+X_{UB}}{10}}} \left( \sqrt{\frac{S_{UB}}{1+S_{UB}}} + \sqrt{\frac{1}{1+S_{UB}}} g_{UB} \right)
\]

(10)

where \( A_{UB} \) denotes the path loss at \( d_0 \), \( \xi_{UB} \) denotes the path loss exponent, \( X_{UB} \) is a zero-mean Gaussian random variable with standard deviation, \( S_{UB} \) is the Rician factor, and \( \sigma_{X_{UB}} \) and \( g_{UB} \sim \mathcal{CN}(0,1) \).

For each transmission duration, the UAV receives data from an MRU in Phase 1 and then forwards it to BS in phase 2; meanwhile, an MCU transmits data to BS in the same subchannel with the MRU in both phases by uplink NOMA. With loss of generality, we consider \( |h_{UBk}|^2 \geq |h_{ULk}|^2 \geq |h_{BK}|^2 \).

1. **Phase-1 \((t_1)\)**

   In an uplink NOMA transmission scenario, an MCU and an MRU transmit symbols \( x_1 \) and \( y_1 \) simultaneously with \( a_{k'} P_t \) and \( a_k P_t \), where \( P_t \) denotes the total transmit power in phase 1. \( a_{k'} \) and \( a_k \) are the power allocation coefficient in phase 1. To guarantee an efficient SIC decoding at the NOMA receiver, it is assumed that \( a_{k'} + a_k = 1 \). Thus, data received at onshore BS and the UAV in Phase 1 can be given, respectively, by:

\[
y_{BK}^{t_1} = |h_{BK}| \sqrt{a_{k'} P_t} x_1^{t_1} + w
\]

(11)

\[
y_{UL}^{t_1} = |h_{UL}| \left( \sqrt{a_{k'} P_t} x_1^{t_1} + \sqrt{a_k P_t} y_1^{t_1} \right) + w
\]

(12)

where \( w \sim \mathcal{CN}(0, \sigma^2) \) denotes the background noise. Due to the half-duplex relay scheme, the achievable rate of the \( k' \)-th MCU at BS in phase 1 can be represented as:

\[
R_{BK}^{t_1} = \frac{1}{2} \log_2 \left( 1 + \frac{a_{k'} P_t |h_{BK}|^2}{\sigma^2} \right) = \frac{1}{2} \log_2 \left( 1 + a_{k'} P_t |h_{BK}|^2 \right)
\]

(13)
where $\frac{P_1}{P_t} = \rho_t$. Because of the simultaneous transmission of MRU and MCU, UAV is able to receive the signal from both of them. We assume perfect time synchronization between MRU and MCU. According to the uplink NOMA principle, the UAV relay obtains the decoded symbol $y_1$ by considering the following two conditions.

- $|h_{Uk}|^2 \geq |h_{UK}|^2$

$$R_{Uk}^{t1} = \frac{1}{2} \log_2 \left( 1 + \frac{\alpha_k P_t |h_{UK}|^2}{\sigma^2} \right) = \frac{1}{2} \log_2 \left( 1 + \frac{\alpha_k P_t |h_{UK}|^2}{\sigma^2} + 1 \right) \tag{14}$$

- $|h_{UK}|^2 \leq |h_{UL}|^2$

$$R_{UL}^{t1} = \frac{1}{2} \log_2 \left( 1 + \frac{\alpha_k P_t |h_{UL}|^2}{h_{UL} |h_{UL}|^2 + 1} \right) \tag{15}$$

By introducing $\kappa \in \{0, 1\}$ as the interference cancellation parameter, the received data rate at UAV in Phase 1 can be summarized as:

$$R_{UL}^{t1} = \log_2 \left( 1 + \frac{\alpha_k P_t |h_{UL}|^2}{\kappa \alpha_k P_t |h_{UL}|^2 + 1} \right) = \begin{cases} \log_2 \left( 1 + \frac{\alpha_k P_t |h_{UL}|^2}{\kappa \alpha_k P_t |h_{UL}|^2 + 1} \right) & \kappa = 0, |h_{UL}|^2 \leq |h_{UL}|^2 \\ \log_2 \left( 1 + \frac{\alpha_k P_t |h_{UL}|^2}{\alpha_k P_t |h_{UL}|^2 + 1} \right) & \kappa = 1, |h_{UL}|^2 \leq |h_{UL}|^2 \end{cases} \tag{16}$$

2. Phase-2 ($t_2$)

In phase 2, both MCU and UAV transmit symbols $x_2$ and $y_1$ simultaneously to onshore BS with powers $\beta_k P_t$ and $\beta_k P_t$, where $\beta_k, \beta_k'$ are the power allocation coefficient in phase 2 and $\beta_k + \beta_k' = 1$. Thus, received data at onshore BS can be represented as:

$$y_{BLK'}^2 = |h_{UB}| \sqrt{P_k^2 x_2^2} + |h_{BK'}| \sqrt{P_k^2 x_2^2} + w \tag{17}$$

Since $|h_{UB}|^2 \leq |h_{BK'}|^2$, the achievable data rates of the UAV relay and MCU are presented, respectively, by:

$$R_{UB}^{t2} = \frac{1}{2} \log_2 \left( 1 + \frac{\beta_k P_t |h_{UB}|^2}{\sigma^2} \right) = \frac{1}{2} \log_2 \left( 1 + \beta_k P_t |h_{UB}|^2 \right) \tag{18}$$

$$R_{BK'}^{t2} = \frac{1}{2} \log_2 \left( 1 + \frac{\beta_k' P_t |h_{BK'}|^2}{\beta_k P_t |h_{UB}|^2 + \sigma^2} \right) = \frac{1}{2} \log_2 \left( 1 + \frac{\beta_k' P_t |h_{BK'}|^2}{\beta_k P_t |h_{UB}|^2 + 1} \right) \tag{19}$$

3. Sum Capacity

Using Equations (13) and (19), the sum capacity of the $k'th$ MCU is given as:

$$R_{k'} = R_{BK'}^{t2} + R_{BK'}^{t2} \tag{20}$$

On the other hand, the end-to-end capacity of a two-hop cooperative link is the minimum one of the two hops. Thus, according to Equations (16) and (18), the capacity of MRU is obtained as:

$$R_k = \min \left( R_{UL}^{t1}, R_{UB}^{t2} \right) \tag{21}$$
2.2. Problem Formulation

It is assumed that the UAV fights with a fixed altitude, which means \( h_k \) is constant. Since the transmission duration and fighting trajectory for each relay mission is predetermined, the propulsion energy and hovering energy required for the UAV is also considered before. The UAV transmit power minimization problem has formulated constraints on maritime users’ minimum rate requirements, maritime maximum users’ transmit power thresholds and UAV power budget, which can be summarized as:

\[
(P1) \quad \min_{\alpha, \beta, (x_k, y_k)} P_{UAV} \\
\text{s.t.} \; C1 : P_{UAV} \leq \frac{P_{\text{UB}}}{\delta}, \forall k \\
C2 : a_k \geq 0, a_{k'} \geq 0, \beta_k \geq 0, \beta_{k'} \geq 0, \forall k, k' \\
C3 : a_k + a_{k'} = 1, \beta_k + \beta_{k'} = 1, \forall k, k' \\
C4 : \min \left( R_{Uk}^{1}, R_{UB}^{2} \right) \geq \bar{R}_k, \forall k \\
C5 : R_{Uk}^{1} \geq \bar{R}_k, \forall k' \\
C6 : R_{UB}^{2} \geq \bar{R}_k, \forall k'
\]

where \( P_{UAV} = \sum_{k \in K, k'} \beta_k \rho_k \) denotes the total transmitted energy consumption of UAV during mission execution. \( \alpha = [a_1, \ldots, a_k, \ldots, a_K] \) and \( \beta = [\beta_1, \ldots, \beta_k, \ldots, \beta_K] \) denote power coefficient vectors of \( K \) NOMA pairs. \( \hat{P}_{UB} \) denotes the transmit power budget of UAV. C1 guarantees the power supplied by UAV is not exceeding its transmit power budget. C2 and C3 are the power allocation coefficient constraints. C4–C6 can guarantee the minimum rate requirements of two types of maritime users. To solve (P1), we first introduce \( K \) slack variables \( \eta_k = \min \left( \frac{R_{Uk}^{1}, R_{UB}^{2}}{R_k} \right), \forall k \) into the objective function such that it is reformulated as:

\[
(P2) \quad \min_{\alpha, \beta, (x_k, y_k), \eta} P_{UAV} \\
\text{s.t.} \; C7 : R_{Uk}^{1} \geq \eta_k, \forall k \\
C8 : R_{UB}^{2} \geq \eta_k, \forall k \\
C1 - C6
\]

where \( \eta = [\eta_1, \ldots, \eta_k, \ldots, \eta_K] \) denotes the slack variables vector of \( R_k \). Thus, (P2) can be transformed as:

\[
(P3) \quad \min_{\alpha, \beta, (x_k, y_k), \eta} P_{UAV} \\
\text{s.t.} \; C4' : a_k \geq \frac{\lambda_k |g_{k'}|^2 + \lambda_k \left| g_{k'} \right|^2}{|h_{UK}|^2 + \lambda_k \left| g_{k'} \right|^2}, \beta_k \geq \frac{\lambda_k}{\rho_k |h_{UB}|^2} \\
C5' : a_k \leq \frac{|h_{k'}|^2 - \lambda_k}{|h_{k'}|^2} \\
C6' : \beta_k \leq \frac{|h_{k'}|^2 - \lambda_k}{\lambda_k |h_{UB}|^2 + |h_{k'}|^2} \\
C1 - 3, C7 - 8
\]

where \( \lambda_k = \left( 2^{2\beta_k} - 1 \right) \) and \( \lambda_k' = \left( 2^{2\beta_k'} - 1 \right) \). (P3) is still challenging to solve since C7 and C8 are non-convex to \( \alpha \) and \( \beta \). For the UAV placement optimization problem, there are two sorts of optimization approaches, namely the deterministic optimization method and stochastic optimization method [25]. The BCD approach is a computationally-efficient deterministic approach that can be used to solve joint UAV placement and resource allocation problem by iteratively optimizing two block variables in turn [26]. Therefore, we introduce
the BCD optimization method to decouple the original problem into a power allocation problem and optimal UAV placement and optimize two block variables alternately.

3. Proposed Optimization Solution

3.1. Power Minimization

With the given optimum UAV hovering placement, the power minimization problem can be transformed as:

\[
\begin{align*}
(P4) \quad \min_{\alpha, \beta, \eta} & P_{ULAV} \\
\text{s.t.} & \quad C7: R_{ULk}^1 = \frac{1}{2} \log_2 \left( 1 + \frac{\alpha_k \rho_t |h_{UK}|^2}{\kappa (1 - \alpha_k)} |h_{UK'}|^2 + 1 \right) \geq \eta_k, \forall k \\
& \quad C8: R_{UB}^2 = \log_2 \left( 1 + \beta_k \rho_t |h_{UB}|^2 \right) \geq \eta_k, \forall k \\
& \quad C1 - C3, C4', C5', C6'
\end{align*}
\]

where C8 is non-convex inequality constraint since \( \log_2 \left( 1 + \beta_k \rho_t |h_{UB}|^2 \right) \) is concave. C7 can be transformed as:

\[
\begin{align*}
R_{ULk}^1 &= \log_2 \left( \alpha_k \rho_t \left( |h_{UK}|^2 - \kappa |h_{UK'}|^2 \right) + \rho_t |g_{UK'}|^2 + 1 \right) \\
& \quad - \log_2 \left( \kappa (1 - \alpha_k) \rho_t |h_{UK'}|^2 + 1 \right) \\
& \geq 2 \eta_k, \forall k
\end{align*}
\]

which is a non-convex inequality constraint since \( \log_2 \left( \alpha_k \rho_t \left( |h_{UK}|^2 - \kappa |h_{UK'}|^2 \right) + \rho_t |g_{UK'}|^2 + 1 \right) \) is concave and \( - \log_2 \left( \kappa (1 - \alpha_k) \rho_t |h_{UK'}|^2 + 1 \right) \) is convex. To tackle the non-convexity of C7 and C8, we introduce the successive convex approximation (SCA) method. By giving any local point \( \bar{\alpha}_k \), the upper bound of \( R_{ULk}^1 \) can be obtained as:

\[
R_{ULk}^{1(\text{upper})} = \log_2 \left( \alpha_k \rho_t \left( |h_{UK}|^2 - \kappa |h_{UK'}|^2 \right) + \kappa \rho_t |h_{UK'}|^2 + 1 \right) \\
- \log_2 \left( \kappa (1 - \alpha_k) \rho_t |h_{UK'}|^2 + 1 \right) \\
+ \frac{\rho_t \left( |h_{UK}|^2 - \kappa |h_{UK'}|^2 \right) (\alpha_k - \bar{\alpha}_k)}{\ln 2 \left( \alpha_k \rho_t \left( |h_{UK}|^2 - \kappa |h_{UK'}|^2 \right) + \kappa \rho_t |h_{UK'}|^2 + 1 \right)}
\]

Similarly, the left-side of C8 is concave with respect to \( \beta_k \). Given any local point \( \bar{\beta}_k \), the upper bound of \( R_{UB}^2 \) is obtained as:

\[
R_{UB}^{2(\text{upper})} = \log_2 \left( 1 + \beta_k \rho_t |h_{UB}|^2 \right) + \frac{\rho_t |h_{UB}|^2}{\ln 2 \left( 1 + \beta_k \rho_t |h_{UB}|^2 \right)} (\beta_k - \bar{\beta}_k)
\]

Then, \((P4)\) can be approximated by:

\[
\begin{align*}
(P5) \quad \min_{\alpha, \beta, \eta} & P_{ULAV} \\
\text{s.t.} & \quad C7': \eta_k \leq R_{ULk}^{1(\text{upper})} \\
& \quad C8': \eta_k \leq R_{UB}^{2(\text{upper})} \\
& \quad C1 - C3, C4' - C6'
\end{align*}
\]

\((P5)\) is convex with respect to \( \alpha, \beta \) and \( \eta \), which can be solved by the interior point method.
3.2. UAV Placement Optimization

With the given power allocation coefficients, (P1) can be rewritten as:

\[
\begin{align*}
\text{(P6) } & \min_{(x_u, y_u) \in K_u} \sum_{k \in K} \beta_k p_i \\
\text{s.t. } & C6" : \log_2 \left( 1 + \frac{\beta_k p_i h_{BU}}{\beta_k p_i \varphi_{UB}^2 + (d_{UB})^{c_k}} \right) \geq 2 R_k', \forall k \\
& C7" : \log_2 \left( 1 + \frac{\alpha_k p_i \varphi_{UK}^2 (d_{UK})^{c_k'}}{(d_{UK})^{c_k}} \right) \geq 2 \eta_k, \forall k \\
& C8" : \log_2 \left( 1 + \frac{\beta_k p_i \varphi_{UB}^2}{(d_{UB})^{c_k}} \right) \geq 2 \eta_k, \forall k
\end{align*}
\]

where,

\[
\begin{align*}
\varphi_{UB} &= 10^{-\frac{A_{UB} + X_{UB}}{30}} \cdot (d_0)^{2 c_k} \left( \sqrt{\frac{S_{UB}}{1 + S_{UB}}} + \sqrt{\frac{1}{1 + S_{UB}} \varsigma_{UB}} \right) \\
\varphi_{UK} &= 10^{-\frac{A_{UK} + X_{UK}}{20}} \cdot (d_0)^{\frac{c_k}{2}} \left( \sqrt{\frac{S_{UK}}{1 + S_{UK}}} + \sqrt{\frac{1}{1 + S_{UK}} \varsigma_{UK}} \right), \\
\varphi_{UK'} &= 10^{-\frac{A_{UK'} + X_{UK'}}{20}} \cdot (d_0)^{\frac{c_k'}{2}} \left( \sqrt{\frac{S_{UK'}}{1 + S_{UK'}}} + \sqrt{\frac{1}{1 + S_{UK'}} \varsigma_{UK'}} \right).
\end{align*}
\]

(P6) is non-convex for its three non-convex constraints. By the SCA method, C6" is transformed into:

\[
\log_2 \left( \beta_k p_i \varphi_{UB}^2 + (d_{UB})^{c_k} \right) - \frac{\xi_{UB} (d_{\epsilon_x, \epsilon_y})^{(c_k - 1)} (\epsilon_x - c_B)^T (\epsilon_x - c_B)}{\ln 2 (\beta_k p_i \varphi_{UB}^2 + (d_{\epsilon_x, \epsilon_y})^{c_k})} \geq 2 R_k' \tag{34}
\]

By introducing a slack variable \( Z_1 \), C6" are equivalent to the following two constraints as:

\[
\begin{align*}
\log(Z_1) - \log_2 \left( \beta_k p_i \varphi_{UB}^2 + (d_{UB})^{c_k} \right) &\geq 2 R_k' \\
\log_2 \left( \beta_k p_i \varphi_{UB}^2 + (d_{UB})^{c_k} + \beta_k p_i h_{BU}^2 (d_{UB})^{c_k} \right) &\geq Z_1 \tag{35}
\end{align*}
\]

Then, we approximate the above equations by their lower bounds. The item \(-\log_2 \left( \beta_k p_i \varphi_{UB}^2 + (d_{UB})^{c_k} \right) \) in Equation (35) is convex with respect to \((d_{UB})^{c_k} \) and convex with respect to \( c_k \). Thus, given any \( c_u = (\xi_{x_u}, \eta_u) \), where \( h_u \) is constant. Thus, given any \( c_u = (\xi_{x_u}, \eta_u) \), Equation (35) can be approximated by their lower bound as:

\[
\log(Z_1) - \log_2 \left( \beta_k p_i \varphi_{UB}^2 + (d_{\epsilon_x, \epsilon_y})^{c_k} \right) - \frac{\xi_{UB} (d_{\epsilon_x, \epsilon_y})^{(c_k - 1)} (\epsilon_x - c_B)^T (\epsilon_x - c_B)}{\ln 2 (\beta_k p_i \varphi_{UB}^2 + (d_{\epsilon_x, \epsilon_y})^{c_k})} \geq 2 R_k' \tag{36}
\]

\[
\begin{align*}
\beta_k p_i \varphi_{UB}^2 + (1 + \beta_k p_i h_{BU}^2 (d_{UB})^{c_k}) &\left( (d_{\epsilon_x, \epsilon_y})^{c_k} + (d_{\epsilon_x, \epsilon_y})^{(c_k - 1)} (\epsilon_x - c_B)^T (\epsilon_x - c_B) \right) \geq Z_1 \tag{37}
\end{align*}
\]

where \( d_{\epsilon_x, \epsilon_y} = \| \epsilon_x - c_B \| \). Apparently, the left-side of Equations (36) and (37) are concave with respect to \( c_u = (\epsilon_x, \epsilon_y) \), \( \eta_k \) and \( Z_1 \). Similarly, the non-convex constraints C7" and C8" are approximated by their lower bounds:

\[
\begin{align*}
\log(Z_2) - \log_2 \left( \alpha_k p_i \varphi_{UK}^2 (d_{UK})^{c_k'} + (d_{UK})^{c_k'} \right) &\geq 2 \eta_k \tag{38}
\end{align*}
\]
Drones 2022, 6, 304

ς(U, c_k) = \left( 1 + \frac{(\tilde{c}_u - c_k)^T (c_u - \tilde{c}_u)}{d_{\tilde{c}_u, c_k}} \right) \geq Z_2

where \( d_{\tilde{c}_u, c_k} = \|c_u - c_k\|_2 d_{\tilde{c}_u, c_k'} = \|c_u - c_k'\|_2 \).

\[
\log(Z_3) - \log_2((d_{\tilde{c}_u, c_B})^{UB}) - \frac{\xi_{UB} (d_{\tilde{c}_u, c_B})^{UB - 1} (c_u - c_B)^T (c_u - \tilde{c}_u)}{\ln 2 (d_{\tilde{c}_u, c_B})^{UB}} \geq 2\eta_k
\]

(40)

\[
\beta_k \rho \eta_k (d_{\tilde{c}_u, c_B})^{UB} + (d_{\tilde{c}_u, c_B})^{UB} + (d_{\tilde{c}_u, c_B})^{UB - 1} (c_u - c_B)^T (c_u - \tilde{c}_u) \geq Z_3
\]

(41)

where \( Z_2 \) and \( Z_3 \) are the slack variable introduced to C7” and C8”, respectively, and \( \tilde{c}_u \) is the local point of the UAV coordinate obtained in the last iteration. Thus, the optimum solution of (P6) is always lower bounded by:

\[
(P7) \min_{\tilde{c}_u, q} \sum_{k \in K_r} \beta_k \rho_k
\]

s.t. (36), (37), (38), (39), (40), (41), \( \forall k, k' \)

3.3. Iterative Algorithm

Based on the solutions to the two sub-problems, we propose an iterative algorithm for (P2) by using the BCD method, which is guaranteed to cover a sub-optimum [27] (In [27]; its BCD-based algorithm contains an additional feasibility checking to guarantee the feasibility of its proposed optimization problem), as summarized in Algorithm 1. Different from [27], the optimal results are acquired in feasible sets obtained in Equation (29) and Equation (42) by Algorithm 1 without additional feasibility checking. \( q \) and \( \epsilon \) are denoted as the number of iteration times and the algorithm convergence factor.

Algorithm 1 BCD Method for Joint Placement and Power Optimization

\[
\begin{align*}
\text{Initialize } & \mathbf{a}^{(0)}, \mathbf{\beta}^{(0)}, \mathbf{\eta}^{(0)} \text{ and } c_u \text{ let } q = 0, \epsilon = 10^{-5} \\
\text{repeat} & \\
\quad \text{Solve (P5) for given } \left\{ c_u^{(q)} \right\}, \text{ and denote the optimal solution as } \left\{ \mathbf{a}^{(q+1)}, \mathbf{\beta}^{(q+1)}, \mathbf{\eta}^{(q+1)} \right\} \\
\quad \text{Solve (P7) for given } \left\{ \mathbf{a}^{(q+1)}, \mathbf{\beta}^{(q+1)}, \mathbf{\eta}^{(q+1)} \right\}, \text{ and denote the optimal solution as } \left\{ c_u^{(q+1)} \right\} \\
\quad \text{Update } q = q + 1 \\
\text{until } & \sum_{k \in K_r} \beta_k^{(q+1)} - \sum_{k \in K_r} \beta_k^{(q)} \geq \epsilon
\end{align*}
\]

The flowchart of Algorithm 1 is present in Figure 2, which shows the iterative procedure of the proposed optimization solution of joint UAV placement and power optimization. In this paper, we introduce the BCD method to alternately solve the power allocation problem and UAV optimal placement problem by convex optimization. Firstly, initial values \( \left\{ \mathbf{a}^{(0)}, \mathbf{\beta}^{(0)}, \mathbf{\eta}^{(0)} \right\} \) and \( \left\{ c_u^{(0)} \right\} \) are given and the BCD method is applied to optimize the variables block with the other variables block fixed. Then, we repeat the iteration until the UAV transmitted power minimization is obtained due to its convergence. Finally, the optimal power allocation \( \left\{ \mathbf{a}^{(*)}, \mathbf{\beta}^{(*)}, \mathbf{\eta}^{(*)} \right\} \) and UAV position coordinates \( \left\{ c_u^{(*)} \right\} \) can be derived. In addition, Algorithm 1 yields a suboptimal solution, due to the optimal solution obtained by two suboptimal problems.
4. Numerical Results and Discussion

In this section, we simulate a maritime IoT UAV-relaying network with $K$ pairs of maritime users. The coordinates of onshore BS are $(0, 0, 150)$. The onshore BS coverage is a circle with 200 m as radius. $K$ MCUs are randomly located along the coastline within the onshore BS service area. $K$ MRUs are randomly located in a square area of $200 \times 200$ m$^2$ with coordinates $(0, 400, 0)$. The constant altitude of UAV is set as $h_u = 150$ m. Set UAV power budget $P_{Ul} = 4$ W, $\delta^2 = -108$ dBm, the carrier frequency $f_c = 5$ MHz, $d_0 = 1$ m, light speed $c = 3 \times 10^8$ m/s. The parameters of the channel models in maritime propagation environment can be obtain by [22]. The simulation parameters are given in Table 1.
Table 1. Simulation parameters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$c_B$</td>
<td>Coordination of onshore BS</td>
<td>(0, 150, 0)</td>
</tr>
<tr>
<td>$h_u$</td>
<td>Flight altitude of UAV</td>
<td>150 m</td>
</tr>
<tr>
<td>$d_0$</td>
<td>Reference distance</td>
<td>1 m</td>
</tr>
<tr>
<td>$f_c$</td>
<td>Carrier frequency</td>
<td>5 MHz</td>
</tr>
<tr>
<td>$\sigma^2$</td>
<td>Background noise</td>
<td>-108 dBm</td>
</tr>
<tr>
<td>$c$</td>
<td>Light speed</td>
<td>$3 \times 10^8$ m/s</td>
</tr>
<tr>
<td>$P_k$</td>
<td>UAV transmit power budget</td>
<td>4 W</td>
</tr>
<tr>
<td>$A_{UL}$</td>
<td>A2S link path loss exponent</td>
<td>116.7</td>
</tr>
<tr>
<td>$\delta X_U$</td>
<td>standard deviation of $X_U$</td>
<td>0.1</td>
</tr>
<tr>
<td>$S_U$</td>
<td>A2S link Rician factor</td>
<td>30</td>
</tr>
<tr>
<td>$A_{UB}$</td>
<td>A2A linkpath loss exponent</td>
<td>46.4</td>
</tr>
<tr>
<td>$\delta X_{UB}$</td>
<td>standard deviation of $X_{UB}$</td>
<td>15</td>
</tr>
<tr>
<td>$S_{UB}$</td>
<td>A2A link Rician factor</td>
<td>10</td>
</tr>
</tbody>
</table>

Figure 3 shows the optimized horizontal locations of UAV with different transmit power budget. Both the $K = 4$ NOMA pair scenario and $K = 6$ NOMA pair scenario are discussed in this part. We set the minimum rate requirement $R_k = R_U = 0.5$ bps/Hz. The optimized UAV locations with a NOMA pair total transmit power $P_t = 1$ W, 1.5 W and 2 W are marked with colored star markers. It shows that there exists an optimal hovering position, which achieves the tradeoff between UAV transmit power minimization and MRU’s minimum rate requirements. It can be seen in Figure 3 that with higher maritime user pair total transmit power, the UAV should hover closer to the onshore BS to enjoyed better A2A channels. Then, the UAV relay consumes less energy. Moreover, with the number of MRUs increasing, the UAV should hover closer to the onshore BS to serve more MRUs within its power budget. Figure 4 illustrates the power allocation results of UAV for each MRU data ferrying with various NOMA pair’s total transmitted power, according to the optimal position in Figure 3. It is indicated that UAV consumes less power for hovering closer to onshore BS and enjoying a better A2A link. Furthermore, at the same hovering position, UAV allocates more power for the MRU that is closer to relay data since UAV receives a higher MRU rate with better A2S channel condition.

Figure 3. Horizontal locations of UAV with different NOMA total power pairs $P_t$. 

Figure 4. Power allocation results of UAV for each MRU data ferrying with various NOMA pair’s total transmitted power and hovering position.
Figure 4. Power allocation of UAV to BS for each MRU with different NOMA total power pairs $P_t$.

Figure 5 demonstrates that the required UAV transmits power with various NOMA total transmitted power pairs $P_t$ in the $K = 4$ NOMA pairs scenario. We set the same dMCU rate requirement as the MRUs. Specifically, randomly searched UAV placement scheme (In the randomly searched UAV placement scheme, the UAV coordinates are obtained after several times randomly searching in the feasible region. The number of searching times is predetermined. This scheme is also used as a benchmark in [8,18].) is employed as a benchmark with 10 times random search. The proposed optimized power allocation is applied as a power allocation scheme. It shows in Figure 5 that UAV requires more total transmitted power by increasing MRU’s rate requirement. With the increasing of $P_t$, the required UAV’s transmitted power decreases. It is shown that, compared with a randomly searched location scheme, the UAV transmit power decreases over 7% with $\bar{R}_k = 0.45 \text{ bps/Hz}$, over 3% with $\bar{R}_k = 0.5 \text{ bps/Hz}$, and over 3% with $\bar{R}_k = 0.55 \text{ bps/Hz}$, respectively. Furthermore, it is illustrated that our proposed optimal algorithm outperforms the benchmark scheme.

Figure 5. UAV transmit power with different NOMA pair total power $P_t$. 
The impact of the MRU rate requirements to the required UAV transmitted power is evaluated in Figure 6 with a NOMA pair total transmitted power $P_t = 1$ W. The 1.5 W and 2 W $K = 4$ NOMA pair scenario is discussed in this part. We set the same MCU rate requirement as the MRUs. It shows that more UAV transmitted power is required by the increasing MRU rate requirement with more transmitted power to guarantee higher data rate requirements. It is shown that compared with randomly searched location scheme, the UAV transmit power decrease over 2% with $P_t = 1$ W, over 4% with $P_t = 1.5$ W and 7% with $P_t = 2$ W, respectively. It is worth noting that the curve of UAV transmitted power grows smoothly with higher rate requirements compared to lower rate requirements. The reason is that with the increasing user rate requirement, more transmitted power is allocated to MCU to guarantee its minimum rate requirement, which has no extra channel gain due to its fixed position, whereas the MRU can obtain a better data rate with better A2A channel condition.

![Figure 6. UAV transmitted power with different MRU rate requirements $R_k$.](image_url)

5. Conclusions

In this paper, a UAV was utilized as a relay to help offshore maritime users connect with onshore BS. The UP-NOMA scheme was proposed to increase system spectrum efficiency. The optimal UAV hovering placement and transmitted power allocation were jointly optimized to minimize the total transmitted power consumption of the UAV relay energy with constraints of the minimum maritime user rate requirements and transmitters’ power budgets. The SCA method was applied to deal with the non-convexity of the proposed optimization problem and the BCD method was employed to generate an iterative algorithm for successively optimizing two sub-problems. Numerical results indicate that the proposed algorithm outperformed the benchmark algorithm and shed light on the potential for exploiting the energy-limited aerial relay in IoT systems.

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