Compact Ultra-Wideband Phase Inverter Using Microstrip-CPW-Slotline Transitions

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Abstract: A planar ultra-wideband phase inverter, which consists of a series of transitions between microstrip, coplanar waveguide, and slotline, is designed and implemented. This compact-sized phase inverter can be used to generate wideband 180° phase differential signals, especially at high microwave frequencies up to millimeter-waves. The design is based on the impedance matching and smooth field transformation between the transitional stages. The fabricated transition has dimensions of 7.36 mm × 5.08 mm, and provides ultra-wide frequency bandwidth from 13 GHz to 38 GHz with low insertion loss of better than 2 dB within ±5° phase deviation and with return loss of greater than 10 dB.

Keywords: transition; phase inverter; microstrip line; coplanar waveguide (CPW); slotline; ultra-wideband

1. Introduction

A phase inverter is used to generate 180° phase differential signals, and, especially with the advent of 5th generation mobile communications, wideband phase inverters have become important in modern microwave and millimeter-wave (mm-wave) systems. A series of applications inspired the investigation of generating differential signals for devices such as phase shifters [1], filters [2], hybrid ring couplers [3–5], and recently for antenna arrays [6] and measurement systems.

Recently, various studies have been conducted to design high-performance phase-inverting transitional structures using planar transmission lines such as microstrip line (MSL), coplanar waveguide (CPW), coupled lines, parallel stripline (PSL), slotline (SL), and substrate integrated waveguide (SIW) [7–14]. However, it is quite challenging to design a wideband structure with low insertion loss and good phase balance. Additionally, the structure should be compact in size and easy to be integrated with the system.

A design of a microwave 180° phase shifter was presented in [8] using an MSL-CPW-MSL transition. In this transition, low insertion loss performance from 5.5 GHz to 18 GHz was achieved. In ref. [9], a high-performing mm-wave phase inverter was introduced with a bandwidth of 28%. In order to achieve a wide differential phase bandwidth, a combination of parallel-coupled lines and L-shaped networks was used [10], where line spacing and input/output matching limited the phase inverter bandwidth and performance at high frequencies. In ref. [11], a 180° phase shifter structure using a parallel-coupled line was proposed to improve the bandwidth, but the operating frequency was limited to low microwave frequencies. In ref. [12], an SIW-based phase inverter was proposed with high performance at mm-waves, but the fractional bandwidth was only 42.42%.

Additionally, a pair of transitions from MSL-SL was designed for a 180° phase shifter [13], where the highest operating frequency was limited to 12 GHz due to the...
coupling structure and thickness of the substrate. Furthermore, a pair of ultra-wideband (UWB) transitions for phase inversion applications was reported in [14] by the authors’ group. These transitions comprised various transitions from MSL-CPW to CPW-PSL, and then to PSL-MSL, where the 180° phase shift was achieved up to 25 GHz. The phase inverter performed excellently up to ~25 GHz, but the transition design configuration was not practical to be implemented at mm-wave frequencies.

In this study, a new design method of the planar UWB phase inverter using a series of MSL-CPW-SL transitions is proposed. The proposed transition can be implemented as a simple and compact structure for phase inversion applications at high microwave frequencies up to mm-waves, and it is flexible enough to be integrated with other components or systems.

2. Design of the Phase Inverter

Figure 1 illustrates the proposed phase inverter consisting of three planar transitions, i.e., MSL-to-CPW, CPW-to-SL, and SL-to-MSL transitional structures. In the proposed configuration, the signal line of the MSL is connected through a via to the center signal line of the CPW formed on the bottom of the substrate. The ground plane of the MSL is split into two paths to form the ground planes of the CPW. Two slots of the CPW are converted into two slotlines, and a circular stub terminates each of the slotlines. Additionally, each slotline is converted back to an MSL on the top plane using a via, and the two MSLs are combined to form an MSL.

![Perspective view of the proposed ultra-wideband (UWB) phase inverter consisting of a series of microstrip-coplanar waveguide (CPW)-slot transitions.](image)

The CPW impedance can be adjusted by the slot width and center signal line width, and impedances of the MSL and CPW are kept as 50 Ω in this design. In a CPW, a signal propagates as an unbalanced signal in the even mode of the coupled slotlines of the CPW [15]. This mode of the CPW is then smoothly converted into two slotlines by gradually increasing the width of the center strip of the CPW with an angle of 60°, as shown in Figure 2. The impedance of the slotlines is selected as 82 Ω because it is impractical to design a 50 Ω slotline on a high dielectric substrate using a conventional etching process.

To achieve ultra-wide bandwidth and efficient transformation from SL to MSL, each slotline that is branched out from the CPW at the bottom side is terminated with an inductive circular stub with a diameter of d_v, which acts as a virtual open circuit load [16]. Additionally, each slotline is coupled with the top-side MSL through a via. These two 70 Ω MSLs are then combined with a 40 Ω MSL, which is then tapered to the 50 Ω MSL. The lengths of the CPW, MSLs, and SLs are selected as λg/4, where λg is the guided wavelength of the corresponding line at 15 GHz.

In the design process of the proposed phase inverter consisting of cascaded transitions, it should be noted that the effective dielectric constant (ε_eff) varies along the position of the transitional structure. The ε_eff, thus the phase shift, changes depending on the field distribution shape of the transition section through the dielectric and air. The ε_eff values at various sections of the transition are calculated using the conventional propagation velocity formula, where the propagation constants are calculated with the help of the electromagnetic (EM) simulator. The calculated ε_eff values are listed in Table 1, where
the used substrate is the Rogers RT/Duroid 6010 with thickness of 10 mil and dielectric constant of 10.2. In this design example, the length of the proposed transition is kept as 290 mil (7.36 mm). The actual length of the transition is longer than that of the MSL (290 mil) due to the bended structures and a via before and after the D-D' section in Figure 2. The phase inversion occurs at the via connection (D-D') between the signal line and ground line. The lengths of the bended structures ($\lambda_{g(slot)/4}$ and $\lambda_{g(ML)/4}$) are slightly adjusted to obtain an equivalent averaged $\varepsilon_{eff}$ between the proposed transition and a straight microstrip line for the best phase inversion pair.

![Figure 2. Layout of the proposed UWB phase inverter. Dimensions: $w_{ms} = 10$, $w_{cpw} = 10$, $w_{slot} = 6$, $l_{ms1} = 80$, $d_{m} = 20$, $l_{cpw} = 90$, $l_{slot} = 40$, $d_{r} = 60$, $d_{via} = 8$, $l_{ms2} = 64$, $\lambda_{g(slot)/4} = 100$, $\lambda_{g(ML)/4} = 80$ (units: mil), $\theta_{1} = 60^\circ$, $\theta_{2} = 45^\circ$.](image)

**Table 1. Effective dielectric constants along the transition.**

<table>
<thead>
<tr>
<th>A-A'</th>
<th>B-B'</th>
<th>C-C'</th>
<th>D-D'</th>
<th>E-E'</th>
<th>F-F'</th>
</tr>
</thead>
<tbody>
<tr>
<td>6.73</td>
<td>4.20</td>
<td>5.09</td>
<td>3.20</td>
<td>6.33</td>
<td>6.73</td>
</tr>
</tbody>
</table>

Figure 3 shows simplified electric field distributions for different cross-sections of the proposed transition. From Figure 3, it is observed that the electric field distribution of the MSL is mostly vertical from the top to the bottom side of the substrate (A-A'), and the field distribution of the CPW on the bottom side is mostly horizontal from center strip to side conductors (C-C'). One via and split ground planes at B-B' help to smoothly convert the field distribution from mostly vertical (A-A') to mostly horizontal (C-C') shapes. Additionally, another via for each slotline converts from a mostly horizontal field of the SL to a mostly vertical field of the MSL (E-E'), at which the phase inversion takes place. Finally, the two MSLs are combined to form a single MSL (F-F').
The cross-section of the finite MSL (E-E’) is represented in Figure 4. Due to the symmetry, the right-hand side of the E-E’ section is considered for the analysis. The electric field distribution is divided by six regions. Each region is analyzed by the conformal mapping to calculate the characteristic impedance of each cross-section. The characteristic impedance and \( \varepsilon_{\text{eff}} \) of the cross-section of the MSL with finite ground plane is calculated by obtained capacitances following the guidelines described by the authors’ group in [17–19].

\[
Z_0 = \frac{120\pi}{\sqrt{\varepsilon_{\text{eff}}(C_1 + C_2 + C_3 + C_4 + C_5 + C_6)} / \varepsilon_0}
\]

\( (1) \)

\[
\varepsilon_{\text{eff}} = \frac{C_1 + C_2 + C_3 + C_4 + C_5 + C_6}{C_1' + C_2' + C_3' + C_4' + C_5' + C_6'}
\]

\( (2) \)

where \( C_1, C_2, C_3, C_4, C_5, \) and \( C_6 \) are the capacitances of each of the six regions, respectively. \( C_1', C_2', C_3', C_4', C_5', \) and \( C_6' \) are the capacitances of the air area in each region.

With the obtained \( \varepsilon_{\text{eff}} \), the total electric lengths of the proposed transition with calculation and simulation are 335° and 337°, respectively, with the phase inversion (D-D’) at 15 GHz. The \( \varepsilon_{\text{eff}} \) value from A-A’ to D-D’ is calculated using the conventional MSL, CPW, and SL analyses [15]. The \( \varepsilon_{\text{eff}} \) value from D-D’ to E-E’ is calculated by using Equation (2). Finally, the \( \varepsilon_{\text{eff}} \) value from E-E’ to F-F’ is calculated using the MSL analysis [15]. The calculated and simulated electric lengths of the reference MSL are 344° and 347° at 15 GHz, respectively. Therefore, the proposed transition can be used as a phase inverter in combination with the same-length MSL.

3. Implementation and Measurements

The proposed phase inverter consisting of a series of transitions is fabricated on the Rogers RT/Duroid 6010 substrate (thickness of 10 mil, dielectric constant of 10.2, and tangent loss of 0.0023). Figure 5 shows the top and bottom views of the fabricated
The proposed phase inverter consists of a series of transitions fabricated on the Rogowski LT/DT/Duroid 6010 substrate (thickness of 10 mil, dielectric constant of 10.2, and tangent loss of 0.0023). Figure 5 shows the top and bottom views of the fabricated phase inverting transition with the reference microstrip line. The dimensions are 290 mil \times 200 mil (7.36 mm \times 5.08 mm).

The simulation of the proposed transition was performed with a 3D EM simulator (CST Microwave Studio). For the measurements, an Anritsu MS4644B vector network analyzer (VNA) with a universal test fixture was used. The short-open-load-through (SOLT) calibration method was adopted for the VNA calibration. The measured and simulated results of the planar ultra-wideband phase inverter are shown in Figure 6. The insertion loss of the fabricated phase inverter is better than 2 dB from 8 GHz to 39 GHz, and the maximum insertion loss is 0.9 dB at the frequencies below 30 GHz. The return loss of the fabricated phase inverter is greater than 10 dB over the frequency range from 8 GHz to 39 GHz. Some minor discrepancies between the simulated and measured results at the high frequency might have occurred due to fabrication inaccuracy and the high loss tangent of the substrate. It may be challenging to design the proposed transition for frequencies higher than 40 GHz since the substrate used in the design example is lossy at high frequencies. However, at above 40 GHz, the proposed transition can be designed on low-loss tangent substrates, still achieving good performance with further miniaturization. Figure 7 shows the phase difference between the proposed fabricated phase inverter and a reference 50 \Omega microstrip line. The phase difference is observed to be less than \pm 5° over the wide range of frequencies from 13 GHz to 38 GHz.

Figure 5. Fabricated UWB phase inverter: (a) top view, (b) bottom view, (c) top view of the reference microstrip line. The dimensions are 290 mil \times 200 mil (7.36 mm \times 5.08 mm).

Figure 6. Measured and simulated S-parameters of the fabricated phase inverter.
The performance comparison of the proposed phase inverter transition as compared with recently reported ones is summarized in Table 2. It can be noted that the proposed phase inverter provides obvious advantages of the operating frequency range with low insertion loss, design flexibility, good phase balance, and compact size. However, the main advantage of the proposed phase inverter is its application in the mm-wave band.

### Table 2. Performance comparison between reported 180° phase inverters.

<table>
<thead>
<tr>
<th>Ref.</th>
<th>Max PD (°)</th>
<th>IL (dB)</th>
<th>RL (dB)</th>
<th>BW (%)</th>
<th>FR (GHz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>[5]</td>
<td>±25</td>
<td>N/A</td>
<td>&gt;10</td>
<td>120</td>
<td>1–4</td>
</tr>
<tr>
<td>[9]</td>
<td>±4.6</td>
<td>&lt;1.48</td>
<td>&gt;10</td>
<td>28.01</td>
<td>24.4–32.35</td>
</tr>
<tr>
<td>[10]</td>
<td>±8</td>
<td>&lt;1.3</td>
<td>&gt;10</td>
<td>100</td>
<td>1–3</td>
</tr>
<tr>
<td>[11]</td>
<td>5</td>
<td>&lt;0.5</td>
<td>&gt;15</td>
<td>83.9</td>
<td>1.14–2.79</td>
</tr>
<tr>
<td>[12]</td>
<td>±2.9</td>
<td>&lt;2.66</td>
<td>&gt;12.7</td>
<td>42.42</td>
<td>26–40</td>
</tr>
<tr>
<td>[13]</td>
<td>±3.6</td>
<td>&lt;2.1</td>
<td>&gt;10</td>
<td>142.8</td>
<td>2–12</td>
</tr>
<tr>
<td>[14]</td>
<td>±5</td>
<td>&lt;1.8</td>
<td>&gt;10</td>
<td>169</td>
<td>2.1–25</td>
</tr>
<tr>
<td>TW</td>
<td>±5</td>
<td>&lt;2</td>
<td>&gt;10</td>
<td>98.04</td>
<td>13–38</td>
</tr>
</tbody>
</table>

PD: phase deviation, IL: insertion loss, RL: return loss, BW: bandwidth, FR: operating frequency range

4. Conclusions

A new design method of the planar UWB phase inverter consisting of cascaded microstrip-CPW-slotline transitions is described. The design is based on the impedance matching and smooth field transformation. The proposed phase inverter provides ultra-wide bandwidth and good phase balance with compact size and design flexibility at higher microwave frequencies up to mm-waves. The implemented phase inverter has an insertion loss of less than 2 dB and good phase balance in the frequency range of 13 GHz to 38 GHz.

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