



Article Distributed Cooperative Jamming with Neighborhood Selection Strategy for Unmanned Aerial Vehicle Swarms

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Abstract: In system science, a swarm possesses certain characteristics which the isolated parts and the sum do not have. In order to explore emergence mechanism of a large–scale electromagnetic agents (EAs), a neighborhood selection (NS) strategy–based electromagnetic agent cellular automata (EA–CA) model is proposed in this paper. The model describes the process of agent state transition, in which a neighbor with the smallest state difference in each sector area is selected for state transition. Meanwhile, the evolution rules of the traditional CA are improved, and performance of different evolution strategies are compared. An application scenario in which the emergence of multi–jammers suppresses the radar radiation source is designed to demonstrate the effect of the EA–CA model. Experimental results show that the convergence speed of NS strategy is better than those of the traditional CA evolution rules, and the system achieves effective jamming with the target after emergence. It verifies the effectiveness and prospects of the proposed model in the application of electronic countermeasures (ECM).

Keywords: unmanned aerial vehicle (UAV); electromagnetic agent cellular automata (EA–CA) model; neighborhood selection (NS); electronic countermeasures (ECM)

1. Introduction

The unmanned aerial vehicle (UAV) has gradually gained popularity in the last few years. In the beginning, UAVs were mainly used for military purposes, and now they are increasingly appearing in the fields of industry and academic research. In terms of autonomous flight research of UAVs, [1] proposes the development of a camera-based quadrotor positioning system to finish the process of automated landing. Reference [2] studies the autonomous navigation system for small UAVs suitable for GPS–denied environment, and realizes the collision–free navigation in fully autonomous missions. The state feedback linear quadratic regulator (LQR) controller is applied to the quadrotor UAV to realize the complete autonomy of the control system [3].

Due to limitations of the load and battery capacity of a single UAV, it is difficult to complete some tasks in complex environments. In recent years, UAV swarms have developed rapidly due to their potential huge application value [4]. UAV swarms show the group behavior through the local interaction between individuals, to solve the global collaborative task [5]. Meanwhile, the current trend of electronic countermeasures (ECM) is moving towards intelligent and distributed direction. Compared with traditional centralized ECM, distributed ECM takes advantage of its number and space to achieve better jamming with targets [6]. The background of distributed ECM and the key technical challenges can be referred to in [7]. In [8], the influence of distributed suppression and deception jamming



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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). on radar detection performance is studied. It investigates the jamming effect of a dense UAV swarm on the detection performance of air defense radar. The optimization for the position of each individual through sparse array synthesis is addressed in [9]. However, these studies only demonstrate the effectiveness of distributed ECM, and there is still a lack of corresponding theoretical modeling for analysis on the evolution mechanism of distributed ECM.

The cellular automata (CA) has been used to model the propagation and emergence of cluster behavior in complex systems [10]. The traditional modeling method is based on the differential equations and is studied by deductive reasoning, while the CA model simulates and predicts the overall dynamic process. The CA model has been widely used in many fields such as computer network modeling and communication [11–13]. In the computer field, the side profile flow calculation of sand-like particles in video games is researched in [11]. The CA model can also be used to model computer networks [12]. Reference [13] studies a node scheduling algorithm based on CA, which saves the energy of sensor nodes while ensuring communication coverage. However, there is no literature addressing the application of CA in the field of ECM.

Given these gaps in this research, the main contributions of this paper are summarized as follows:

(a) The process of agent state transition is explored, in which the all selection (AS) strategy of the traditional CA model is improved based on the neighborhood selection (NS) strategy; (b) On the basis of (a), the convergence performance of the model in the four evolution strategies is analyzed; (c) Electromagnetic agents (EA) are UAVs that carry electronic reconnaissance or jamming equipment. By regarding each as a cell, the electromagnetic agent-cellular automata (EA–CA) model is proposed. It is used to simulate the process of cluster jamming in distributed ECM scenarios; (d) By adjusting the parameters of the simulation, the conditions for the system to realize the emergence jamming are analyzed.

The rest of this paper is organized as follows: Section 2 describes the state transition process of CA based on the neighborhood selection-all selection (NS–AS) strategy. The application of the EA–CA model under ECM scenario is introduced in Section 3. In Section 4, the performance of the model and the ECM simulation results are provided to demonstrate the effectiveness of proposed model. Concluding remarks are given in Section 5.

2. The EA-CA Model

2.1. Mechanism of EA-CA

The definition of CA is described based on the set theory as follows: Denote the dimension of the cell space as d, the neighbor radius of the cell as r, and time as t. The cell state is a value in the finite state set S, and Z is a set of integers in one dimension. In distributed ECM scenarios, two-dimensional CA [14] are commonly used for modeling. The state of a cell at the next moment is determined by the current states of its neighboring cells. Thus, the state value of a cell at t can be summarized as

$$S_{i,j}^{t} = f(S_{i,j}^{t-1}, S_{i-1,j}^{t-1}, S_{i+1,j}^{t-1}, S_{i-1,j-1}^{t-1}, S_{i-1,j+1}^{t-1}, S_{i,j-1}^{t-1}, S_{i,j+1}^{t-1}, S_{i+1,j+1}^{t-1}, S_{i+1,j-1}^{t-1})$$
(1)

Let G(V, E, A) represent the diagram of communication topology structure of the CA model. The elements in the set V = 1, 2, ..., n are used to mark the corresponding n agent members in turn, and the state of agent i is denoted by $x_i(t)$. The set of communication edges between members is represented by $E = \{(i, j) : i, j \in V, i \neq j\}$.

According to the rules of CA, the consensus algorithm [15] of the system can be defined as

$$\dot{x}_{i}(t) = -\sum_{i,j \in E} a_{ij}(t) \left(x_{j}(t) - x_{i}(t) \right)$$
(2)

where a_{ij} is an element of the adjacency matrix $A(t) = [a_{ij}(t)]$ at $t \ge 0$. The weight assigned to the edge of the graph *G* is defined as

$$(i,j) \in E \iff a_{ij} > 0, (i,j) \notin E \iff a_{ij} = 0, a_{ii} = 0$$
(3)

Then, the adjacency matrix A represents the communication network between all agents in the system. Given that G is an undirected graph, the degree of the agent i is

$$d(i) = d_{in}(i) = d_{out}(i) = \sum_{j=1}^{n} a_{ji}$$
(4)

and the degree matrix can be denoted by $D = \text{diag}\{d(i), i \in V\}$; the elements of D can be written as

$$d_i = \begin{cases} \sum_{j=1}^n a_{ji}, i = j\\ 0, i \neq j \end{cases}.$$
(5)

Combining Formulas (3) and (5), the Laplacian matrix of the figure G can be obtained by L = D - A. The element of *L*, l_{ij} , is given by

$$L = [l_{ij}](i, j = 1, 2..., n) = \begin{cases} \sum_{j=1}^{n} a_{ij}, i = j \\ -a_{ij}, i \neq j \end{cases}.$$
 (6)

The consensus algorithm of the system based on CA can be written in matrix form $\dot{x} = -Lx$, $x = [x_1, x_2, ..., x_n]$. It can be seen from the evolutionary rules of CA that the state of each agent is determined by the states of its neighbors. Therefore, when $t \to \infty$ and $|x_i(t) - x_j(t)| \to 0$, the system achieves global consistency, i.e., the states of all agents converge to a common value.

2.2. The NS–AS Strategy

The traditional CA model adopts the AS strategy, i.e., the state of agent is determined by the states of all its neighboring agents. This makes the system more computationallyconsumed and difficult to converge, while using the NS strategy can increase the convergence speed of the system and improve the stability of the system [16,17]. In the NS strategy, neighboring agents are divided into several communication sectors. In order to benefit the system convergence and enhance the system consistency, the neighbor agents with the smallest state difference in each communication sector are selected to construct the backbone network topology. In the network topology, all candidate neighbor agents of agent *i* participate in the calculation of the state update for agent *i*. Thus, the state transition equation is given by

$$x_i(t+1) = x_i(t) + u_i(t)$$
(7)

where $u_i(t)$ represents the control input. Supposing a neighborhood member *j* with the smallest state difference between the communication area and that of the agent *i*, the agent *i* selects the agent *j* for collaborative cooperation and adds it to the candidate set. Then, $u_i(t)$ can be written as

$$u_{i}(t) = \alpha \left(\sum_{u=1}^{m} \left(x_{\min(i^{u})}(t) - x_{i}(t) \right) + \sum_{ii \in P_{i}(t), ii \notin A_{i}(t)} \left(x_{ii}(t) - x_{i}(t) \right) \right)$$
(8)

where α is the adjustment factor of the model, *m* represents the number of communication sector, i^u represents the neighbor agents set of agent *i* in the *u*th sector, and $x_{min(i^u)}(t)$ is the state of the agent with smallest difference from the state of agent *i* among its neighboring agents in the *u*th sector at time *t*. In the above, $P_i(t)$ and $A_i(t)$ represent the set of

neighborhood members of agent *i* and the set of agents from the smallest state difference in each sector, respectively.

As the NS strategy only selects the neighbor agent with the smallest difference in each sector to participate in the update calculation, a small sum of state difference is obtained. The step of each update of the agent is small, which causes the system to converge too slowly. Therefore, in order to improve the convergence speed of the system, the system switches to the NS–AS strategy. When the system is fully connected, the number of neighbor agents of agent *i* is n - 1, and all agents within communication range are select to participate in state evolution. The algorithm process of the NS–AS strategy is shown in Algorithm 1.

Algorithm 1: The NS-AS Strategy Algorithm				
The NS-AS strategy for <i>n</i> agents:				
1: Initialize the network topology and $x_i(t), i \in 1, 2N$				
2: for agent $i=1$ to N				
3: if the network is not fully connected				
4: Adopt the NS steategy				
5: Divide the agents into several communication sectors.				
6: Calculate the rotation angle set $\beta = rotate_array(min(std(N_n)))$				
7: for $j = 1$ to m				
8: Selects the neighbor agent $\min(i^u) = \operatorname{argmin} x_{i^u}(t) - x_i(t) $,				
add the agent into candidate set $u_i(t)$, update $x_i(t)$;				
9: $\exists ii, ii \in P_i(t), ii \notin A_i(t)$, add agent ii into candidate set $u_i(t)$;				
10: Acooording to candidate set $u_i(t)$, update $x_i(t)$.				
11: end for				
12: else				
13: Switch to AS strategy				
14: Select all agents in the neighborhood, update $x_i(t)$				
15: end for				

By calculating the standard deviation of the number of agents in each sector, the angle of the rotating sector can be adjusted. In Algorithm 1, *rotate_array* represents the list of rotation angles to be searched, which cannot exceed the angle of each sector. N_n represents the number of agents in each sector and N_c denotes the number of communication sector.

Combining Formulas (11) and (12), the state information of agent can be set as

$$\forall i, N_i(t) < n - 1:$$

$$x_i(t+1) = x_i(t) + \alpha 1 \{ \sum_{u=1}^{n} x_{\min(i^u)}(t) - x_i(t) + \sum_{ii \in P_i(t), ii \notin A_i(t)} (x_{ii}(t) - x_i(t)) \};$$

$$(9)$$

$$\forall i, N_i(t) = n - 1:$$

$$x_i(t+1) = x_i(t) + \alpha 2 \sum_{j \in N_i(t)} (x_j(t) - x_i(t)).$$
 (10)

where N_i represents the number of neighbor agents of agent *i*, and $\alpha 1$ and $\alpha 2$ represent the adjustment factor in different condition, respectively.

3. Signal Model of ECM

The EA–CA model can be used to simulate the process of agent state transition in ECM application scenarios. The jamming consistency to radiation sources can be achieved through the information interaction between agents [18]. In order to realize the distributed

noise suppression jamming with the radar [7], each jammer is regarded as an electromagnetic agent that transmits jamming noise that drowns the echo of a radar-detected target.

The radar detection equation without jamming can be written as [19]

$$P_{\rm r} = \frac{P_t G_t G_r(\theta_t) \delta \lambda^2 K_I K_C}{(4\pi)^3 R^4 L_s} \tag{11}$$

where P_t and G_t correspond to the transmitting power and the gain of the transmitting antenna, respectively. $G_r(\theta_t)$ is the gain of the radar antenna in the target direction, δ is the radar cross section, λ is the wavelength of signal, and K_I and K_C represent the pulse accumulation correction factor and the pulse compression correction factor, respectively. In the above, R is the distance between radar and target. L_s is the signal transmission loss in clear air; Appendix A the definition of mathematical symbols, Appendix B gives the specific calculation process.

The noise power of the system contains the thermal noise power of the receiver and the jamming noise power. The thermal noise power can be written as $P_{rn} = kT_0B_rF_n$, where k is Boltzmann constant, and T_0 is the standard room temperature. B_r is radar receiver bandwidth, and F_n is noise figure.

The jamming signal power of n jammers received by the radar is represented as follows [20]

$$P_{rj} = \sum_{i=1}^{n} \frac{P_j G_j G_r(\theta_j) \lambda^2}{(4\pi)^2 R_j^2 L_j} \cdot \frac{B_r}{B_j}$$
(12)

where P_j and G_j represent the jammer power and gain. $G_r(\theta_j)$ is the gain of radar antenna in the direction of jammer, and R_j denotes the distance and loss of the jammer, of which B_r and B_j stand for the bandwidth of receiver and jammer, respectively.

The total noise power of the system is given by $P_n = P_{rn} + P_{rj}$ [6]. The total signal-noise ratio (SNR) of the system can be expressed as follows:

$$\left(\frac{S}{N}\right)_{S} = \frac{P_{\rm r}}{P_{\rm n}} = \frac{P_{\rm t}G_{\rm r}(\theta_{\rm t})\delta\lambda^{2}K_{\rm I}K_{\rm C}}{(4\pi)^{3}R^{4}L_{\rm s}\left(kT_{0}B_{\rm r}F_{\rm n} + P_{\rm rj}\right)}$$
(13)

In practice, it draws more attention to SNR or detection probability of the radar receiver. For a radar receiver, $(SNR)_{o \min}$ is the minimum output SNR [21]. The minimum detectable signal power is

$$S_{i\min} = kT_0 B_r F_n (SNR)_{o\min} \tag{14}$$

The detection probability is related to false alarm probability P_{fa} , output SNR $(SNR)_o$, and the type of target fluctuation. The detection probability of a non-undulating target [22] can be calculated approximately by

$$P_d = 0.5 erfc(\sqrt{-ln(P_{fa})} - \sqrt{(SNR)_o + 0.5}).$$
(15)

where erfc() represents the complementary error function.

4. Simulation Results Analysis

4.1. Performance Analysis of the EA–CA Model

The EA–CA model is evaluated in a simulated scenario. The initial topology in the EA–CA model is connected. When an EA detects the radiation source, it transmits the information to its neighboring agents and the neighborhood agents transform their states from the reconnaissance state to the jamming state. The evolution process of the EA state information in different strategies is shown in Figure 1. The color keys in the figure indicate the evolution of each agent state. In the ECM scenarios, state Y represents the state of agent with the initial state being reconnaissance state. When the radiation source is detected, the agent state evolutes to the jamming state with the increase of reconnaissance information. The performances of different evolution strategies are determined by final convergence

or divergence. It can be seen that when the AS strategy is adopted, the communication topology of the EA–CA model is not always connected during the evolution process, and the system will converge to multiple local centers. The NS strategy 1 represents dividing the neighboring agent into several sectors. The NS strategy 2 is based on the NS strategy 1, by adjusting the angle of the sectors to make the individuals of each sector evenly distributed. When using the NS strategy 1, the communication area of each agent is divided into several sectors, and the communication topology is always connected during the evolution process. The EA–CA model converges to a small area quickly, then to achieve the consensus at a very slow speed. When the NS strategy 2 is adopted, the number of agents in each sector is evenly distributed, and its convergence speed is faster than the NS strategy 1. When the communication topology of the model has not reached full connectivity, the system adopts NS strategy 2, and the convergence speed at this time is closed to the NS strategy 2. When the communication topology of the model reaches full connectivity, it switches to AS strategy; the convergence speed at this time is faster than NS strategy 2.

The influence of different parameters, such as the number of communication sectors, the communication radius of agent, the number of agents, and the different adjustment factors on the convergence speed of the system are also analyzed.



Figure 1. The evolution process of EA–CA model state information in different strategies.

4.1.1. The Number of Communication Sector

The evolutions of state using NA–AS strategy with the different number of communication sectors are shown in Figure 2. The number of agents in the candidate set decreases when the number of sectors is too small, which leads to the system converge to multiple local centers. If the number of sectors is set too large, though the convergence speed can be improved, the computational cost increases.



Figure 2. The evolution performance with the number of different sectors.

4.1.2. The Communication Radius of the Agent

Figure 3 shows the evolutions of state using NA–AS strategy with different communication radius. It can be seen that the number of candidate agents is positively correlated with the size of communication radius, so the convergence speed of the system increases accordingly. The number of neighbor agents decreases when the communication radius is too small, which causes divergence.

4.1.3. The Number of the Agents

The evolutions of state using NA–AS strategy with the different number of agents are observed in Figure 4. The system converge speed is related with the density of agents, the system diverges to multiple statuses when the number of agents is small. However, a large number of agents leads to the increase of the computation cost, resulting in a slow converge speed.



Figure 3. The evolution performance with different communication radius.







Figure 4. The evolution performance with the different number of agents.

4.1.4. The Adjustment Factor

Figure 5 shows the effect of different adjustment factors on the system convergence performance. Adjustment factor denotes the step–step process of the agent state change. The unreasonable adjustment factor set may cause the modeled divergence.



Figure 5. The evolution performance with different α .

4.2. ECM Simulation Results

4.2.1. ECM Simulated Scenario

An ECM simulated scenario is shown in Figure 6. Each UAV carries reconnaissance and jamming payloads. When the radar radiation source is detected, it will perform jamming, covering the target. The relevant parameters with their values are shown in Table 1.



Figure 6. The ECM scenario based on UAV swarm.

Table 1. Simulation parameters with their values.

Parameter	Definition	Value
F _r	The radar center frequency	3.1 GHz
T_r	The pulse width	20 μs
B_w	The chirp bandwidth	30 MHz
B_r	The bandwidth of receiver	100 MHz
G _r	The antenna gain of radar in the jammer direction	38.5 dB
B _i	The bandwidth of jammer	50 MHz
P_i	The jammer transmitting power	3 W
$\dot{G_i}$	The jammer transmitting antenna gain	20 dB
L_j	The comprehensive loss of jammer	5 dB

The jamming pattern of this paper is noise convolutional jamming signal. The jamming signal S_j is formed by the convolution of the received radar signal S_r and the Gaussian white noise signal S_n . The jamming signal can be represented as follows:

$$S_j = conv(S_r, S_n) \tag{16}$$

$$S_r = exp(j\pi Kt^2) \tag{17}$$

where exp() is the exponential function with the constant *e* as the base, and $K = B_w/T_r$ is the frequency modulation slope.

The time domain and frequency domain of jamming signal are shown in Figure 7.



Figure 7. Time domain and frequency domain of the jamming signal.

4.2.2. The Performance Analysis of Different Evolution Strategies

Figure 8 shows the radar detection power map of a single radar interfered with by multiple jammers. When the main lobe of the radar antenna points to the direction of jammer distribution, multiple jammers effectively suppress the radar exposure area.



Figure 8. Radar detection power map.

In order to verify the influence of the number of jammers on the performance of the radar, the relationship between the number of UAVs and the signal-to-noise ratio of the system is shown in Figure 9. As the evolution process progresses, the number of UAVs in jamming state gradually increases, and the signal-to-noise ratio of the system decreases accordingly.



Figure 9. The influence of the number of jammers on the system SNR.

The curve of the radar target detection probability with different number of jammers is shown in Figure 10. The detection probabilities under various jammer transmit power are compared. In an actual scenario, the number of jammers and the jamming power should be considered comprehensively. The experimental results show that to optimally allocate jamming resources, the number of jammers and the interference power can be adjusted according to actual application requirements.



Figure 10. The curve of the radar target detection probability.

Figure 11 shows the influence of different evolution strategies on the radar detection probability. It can be seen that as the evolution progresses, the number of UAVs in the jamming state gradually increases, and the radar detection probability gradually decreases. From the previous analysis results, the AS strategy and NS strategy 1 converge to multiple local centers with only certain individuals evolving to the interference state. Due to the lack of sufficient interference power, these two strategies cannot effectively interfere with the radar. On the contrary, both NS strategy 2 and NS–AS strategy can eventually achieve effective interference with the radar. Meanwhile, as the convergence speed of the NS–AS strategy is faster than the NS strategy 2, it achieves effective interference faster.



Figure 11. The influence of different evolution strategies on the radar detection probability.

When radar performs the searching and tracking task, it usually uses pulse compression technology to improve the target detection capabilities. The effect of a few jammers on the radar pulse compression output is described in Figure 12. It can be seen that as the evolution process progresses, the number of UAVs in the jamming state gradually increases, and the radar detection probability gradually decreases. The target echo is detected normally when the SNR is large in Figure 12a. However, with the constant transition of the agent state, more agents are transformed into the jamming state. As can be seen in Figure 12b, the target echo submerges into background noise with the jamming power increasing. It verifies the effectiveness of the interference signal by comparing the results of pulse pressure output under different signal-to-noise ratios.



Figure 12. Target detection results after radar pulse compression.

5. Conclusions

In this paper, an EA-CA model based on NS strategy was proposed, and the effectiveness of the model was verified in an ECM scenario. Firstly, the process of the agent state transition was analyzed based on the CA method. Then, four state evolution strategies were studied, and the convergence performances of different parameters on the system were compared. Finally, the radar detection performance under different evolution strategies was simulated in distributed cooperative jamming scenarios. By comparing the detection probability of the system under different evolution strategies and the results of pulse compression output under different SNRs, the effectiveness of the interference signal was verified. It can be concluded that the system achieves convergence and jamming quickly with an improved stability when the NA-AS strategy is adopted. However, the UAV communication is often limited by real-time transmission bandwidth. It is necessary to establish a suitable communication mechanism. Meanwhile, when multiple radiation sources appear in the actual environment, the UAV swarm needs to self-organize to sense the radiation sources and allocate interference resources. We will carry out the related research in future work.

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Abbreviations

The following abbreviations are used in this manuscript:

- UAV Unmanned aerial vehicle
- LQR Linear quadratic regulator
- EA Electromagnetic agent
- CA Cellular automata
- AS All selection
- NS Neighborhood selection
- ECM Electronic countermeasure
- SNR Signal-noise ratio

Appendix A

Table A1. The definition of mathematical symbols.

Mathematical Symbol	Definition
G	The communication topology diagram of the CA model
E	The set of communication edges between members
D	The degree matrix
A(t)	The adjacency matrix
L	The Laplacian matrix of the figure G
$x_i(t)$	The state of agent <i>i</i>
$u_i(t)$	The candidate set of the agent <i>i</i>
α	The adjustment factor of the model
N_n	The number of agents in each sector
N_c	The number of communication sector
P_r	The radar receiving power
P_t	The radar transmitting power
G_t	The gain of the radar transmitting antenna
$G_r(\theta_t)$	The gain of the radar antenna in the target direction
σ	The radar cross section
λ	The wavelength of radar signal
K _I	The pulse accumulation correction factor
K _C	The pulse compression correction factor
R	The distance between radar and target
L_s	The loss of system
P _{rj}	The interference power received by the radar

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Mathematical Symbol	Definition
P_i	The jammer transmitting power
Ġ _i	The jammer transmitting antenna gain
L_i	The comprehensive loss of jammer
F _r	The radar center frequency
T_r	The pulse width
B_w	The chrip bandwidth
B_r	The bandwidth of receiver
B_{i}	The bandwidth of jammer
$\dot{P_{rn}}$	The thermal noise power
P_n	The total noise power of the system
T_0	The standard room temperature
F_n	The noise figure
P_{fa}	The false alarm probability
$\dot{P_d}$	The target detection probability
$S_{i\min}$	The minimum detectable signal power

Appendix **B**

Appendix B.1. The Clear Air Atmosphere Attenuation

The calculation process of the electromagnetic wave propagation attenuation model is as follows:

$$L_s = \gamma_0 r_0 + \gamma_w r_w \tag{A1}$$

where γ_0 and γ_w represent the ground attenuation rates of oxygen and water vapor. r_0 and r_w are the equivalent path lengths of oxygen and water vapor, respectively.

Suppose the path elevation angle is θ , and the smaller and larger heights of the radiating source antenna and the reconnaissance receiver antenna are h_1 and h_2 , respectively. r_0 and r_w can be calculated as follows:

$$r_{0} = \begin{cases} \frac{h_{0}(e^{-\frac{h_{1}}{h_{0}}} - e^{-\frac{h_{1}}{h_{0}}})}{\sin\theta}, 10^{\circ} \le \theta \le 90^{\circ} \\ \frac{\sqrt{a_{e}h_{0}}[F(\chi_{1})e^{-\frac{h_{1}}{h_{0}}} - F(\chi_{2})e^{-\frac{h_{2}}{h_{0}}}]}{\cos\theta}, 0^{\circ} \le \theta < 10^{\circ} \end{cases}$$

$$r_{w} = \begin{cases} \frac{h_{w}(1 - e^{-\frac{h_{1}-h_{2}}{h_{w}}})}{\sin\theta}, 10^{\circ} \le \theta \le 90^{\circ} \\ \frac{\sqrt{a_{e}h_{0}}[F(\chi_{1}') - F(\chi_{2}')e^{-\frac{h_{1}-h_{2}}{h_{w}}}]}{den}, 0^{\circ} \le \theta < 10^{\circ} \end{cases}$$
(A2)
(A3)

where h_0 and h_w are the equivalent heights of oxygen and water vapor. a_e is the equivalent radius of the Earth. h_0 and h_w can be calculated as follows:

$$aah_0 = \begin{cases} 6, f \le 63GHz \\ 6 + \frac{40}{(f - 118.7)^2 + 1}, 63GHz < f \le 350GHz \end{cases}$$
(A4)

$$h_w = h_{w0} \left[1 + \frac{3}{(f - 22.2)^2 + 5} + \frac{5}{(f - 183.3)^2 + 6} + \frac{2.5}{(f - 325.4)^2 + 4}\right], f < 350 GHz$$
(A5)

where h_{w0} is the water vapor coefficient, and the value is 1.6 for sunny days and 2.1 for rainy days.

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The calculation equation of $F(\chi)$ can be represented as follows:

$$F(\chi) = \frac{1}{0.661\chi + 0.339\sqrt{\chi^2 + 5.51}}$$
(A6)

$$\chi_i = \cos\theta [\sin\theta \tan^2\theta \sqrt{\frac{a_e}{h_0} + \sqrt{\frac{a_e}{h_0}}} \sin^2\theta + \frac{2h_i}{h_0} + \frac{h_i^2}{2a_eh_0}], (i = 1, 2)$$
(A7)

$$\chi_{i}^{'} = \cos\theta[\sin\theta \tan^{2}\theta\sqrt{\frac{a_{e}}{h_{w}} + \sqrt{\frac{a_{e}}{h_{w}}}}\sin^{2}\theta + \frac{2h_{i}}{h_{w}} + \frac{h_{i}^{2}}{2a_{e}h_{w}}], (i = 1, 2)$$
(A8)

Appendix B.2. Multipath Propagation Factor

In the process of calculating the multipath effect in the electromagnetic wave transmission process, it is first necessary to establish a vertical profile model of the actual ground on the transmission path from the radiation source to the reconnaissance receiver, and then analyze the possible arrival of the reconnaissance receiver antenna according to the electromagnetic wave reflection model. The radiation source reflects the signal. Finally, according to the electromagnetic characteristics of the reflecting surface and the transmission path, the reflection intensity and phase lag of the reflected signal are calculated, and then the composite signal of the direct wave and the reflected wave at the reconnaissance receiver is obtained. The calculation equation of multipath propagation factor is as follows:

$$F = f_d |\sqrt{1 + x_2 + 2x\cos\alpha}| \tag{A9}$$

where $x = \frac{\rho_0 \rho_s D f_r}{f_d}$ is the generalized reflection coefficient. ρ_0 and ρ_s represent the electromagnetic reflection coefficient and roughness factor of the reflecting surface. D is the divergence factor of the reflecting surface. f_d and f_r represent the value of the amplitude of the pattern coefficient on the direct path and the reflected path, respectively. $\alpha = \frac{2\pi\delta}{\lambda} + \varphi + \beta_r - \beta_d$ is the total phase difference between direct wave and reflected wave. σ is the path length difference between the direct wave and the reflected wave. φ is the phase angle of reflection coefficient. β_r and β_d represent the phase of the reflected and direct directions of the pattern factor.

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