Improvements in CO$_2$ Booster Architectures with Different Economizer Arrangements

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Abstract: CO$_2$ transcritical booster architectures are widely analyzed to be applied in centralized commercial refrigeration plants in consonance with the irrevocable phase-out of HFCs. Most of these analyses show the limitations of CO$_2$ cycles in terms of energy efficiency, especially in warm countries. From the literature, several improvements have been proposed to raise the booster efficiency in high ambient temperatures. The use of economizers is an interesting technique to reduce the temperature after the gas cooler and to improve the energy efficiency of transcritical CO$_2$ cycles. The economizer cools down the high pressure's line of CO$_2$ by evaporating the same refrigerant extracted from another point of the facility. Depending on the extraction point, some configurations are possible. In this work, different booster architectures with economizers have been analyzed and compared. From the results, the combination of the economizer with the additional compressor allows obtaining energy savings of up to 8.5% in warm countries and up to 4% in cold countries with regard to the flash-by-pass arrangement and reduce the volumetric displacement required of the MT compressors by up to 37%.

Keywords: CO$_2$ transcritical booster; economizer; subcooling; commercial refrigeration; integrated mechanical subcooling; variable frequency drive

1. Introduction

The adoption of the F-Gas regulation in 2015 [1] has struck the commercial refrigeration sector harshly, where new limits for the refrigerants used until nowadays were adopted. Accordingly, in centralized refrigeration systems with cooling capacity higher than 40 kW and direct expansion arrangement, the F-Gas demands the use of substances with a GWP100 lower than 150. Since the vast majority of anthropogenic refrigerants with low-GWP are middle-flammable [2], the CO$_2$ is a durable solution to ensure safety conditions, especially in the sales area.

CO$_2$ as refrigerant is used in both transcritical and subcritical conditions depending on the heat rejection conditions. Hence, it can be used as the main refrigerant in transcritical/subcritical refrigerating plants [3], as secondary fluid in CO$_2$ pumped systems [4], or as an additional refrigerant in cascade refrigerating facilities [5,6]. At present, one of the most representative arrangements using this fluid is the booster systems, which have been extended in commercial refrigeration thanks to the complete solution that they provide, covering the services of low and medium temperature [7–9]. At first, this architecture was used mainly in the northern countries of Europe where the ambient temperatures allow working in subcritical conditions most of the time. Later, with the entry into force of the F-Gas, transcritical CO$_2$ booster systems were adopted in the Southern European countries in order to achieve a long-term solution by avoiding the use of fluorinated refrigerants. However, there are important energy differences between the traditional refrigeration systems and the simplest CO$_2$ booster systems [10], which demand the use of new technologies [11] and improvements to

enhance their efficiency [12,13]. These technologies range from the most basic improvements such as the use of a desuperheater [14] to the main advanced systems for CO_2 boosters. Among the advanced improvements, there are the parallel compression [15,16], the dedicated [17] or integrated mechanical subcooling [18], the ejector technology [19] such as the multi-ejector arrangements [20], combinations of these systems [21], flooded evaporators [22], liquid ejectors [23], and the "all-in-one" systems that integrate the A/C and the tap water heating in the same refrigerating plant [24–27]. In addition, there are other improvements applied to the heat rejection zone for high ambient temperatures, such as adiabatic gas coolers [17] or desiccant wheels [28], which are able to increase the efficiency of all facilities, reducing the temperature by increasing the humidity in the heat rejection medium. Some of these technologies are based on the addition an extra heat exchanger named the economizer heat exchanger or subcooler at the exit of the gas cooler. The main function of this element is to reduce the temperature at the exit of the gas cooler just before entering the expansion device, minimizing the vapor quality at the inlet of the evaporators and consequently increasing the cooling capacity of the refrigerating plant [29]. Additionally, these systems allow reducing the optimum heat rejection pressure of the system. Depending on the arrangement used to cool the CO2 through the subcooler, subcooling control can be performed in several ways. This improvement to CO_2 booster architecture is analyzed in detail in this work as well as the use of an additional economizer compression stage with the economizer heat exchanger (integrated mechanical subcooling), which have received little attention on CO_2 booster architectures.

According to the literature, the system with integrated subcooling in booster systems has only been evaluated by Catalan-Gil et al. [18], who performed an energy analysis with respect to the system with dedicated subcooling and parallel compression. However, this system provides high improvements to the basic booster with low-complexity changes in the basic architecture.

Therefore, this work analyzes these improvement systems, evaluating different specific parameters not previously analyzed in CO_2 booster systems, aiming to maximize efficiency by modifying certain parameters, such as those experimentally analyzed by Nebot-Andrés [30] in a single-stage CO_2 refrigeration plant.

In this work, a detailed thermodynamic analysis is presented for several arrangements of an economizer installed in a CO_2 booster system for a typical European supermarket ($\dot{Q}_{LTo}$ = 41 kW at −32 °C $\dot{Q}_{MTo}$ = 140 kW at −6 °C). In order to be close to reality, an accurate parametric compressor model (error less than 0.2% regarding compressors' manufacturing data) has been adopted to take into account the effect of the rotation speed over the efficiencies of the compressors, which has not been considered in booster architectures to the best of the authors' knowledge.

For each arrangement, a wide range of heat rejection temperatures from 0 to 40 °C have been used to determine the optimal operating conditions of the refrigerating plant, including the optimal heat rejection pressure, the optimum subcooling, the required compressor displacement, and its optimal rotation speed. In addition, some relevant parameters that have not been analyzed in other works with booster architectures are studied in detail as well as the importance of controlling the heat rejection pressure and the suction pressure of the additional compressors (EC), as well as the level of subcooling applied. The combined effect of all parameters is reflected in an annual energy consumption study obtained for different European cities and additionally for 282 locations distributed throughout Europe, aiming to clarify the most suitable regions for each system.

2. Booster Architectures

This section is devoted to presenting the main architectures analyzed in this manuscript. All of them are designed to cover two specific cooling demands: 140 kW at medium temperature conditions (approximately −6 °C) and 41 kW at a low-temperature regime (approximately −32 °C). These values are selected according to the field data gathered by Sawalha et al. [31,32] in several supermarkets which revealed a typical load ratio (LR) between medium and low-temperature loads from 3:1 to 3.5:1. The

rest of the parameters considered at each architecture as well as the particular operating limitations for each component are described in Section 3 (Model assumptions).

2.1. Basic Booster (BB)

To determine the degree of improvement reached using the economizer, a typical CO_2 booster arrangement (BB) has been taken as a reference (Figure 1). This base cycle is composed by a rack of compressors at the low-temperature side (LT_C), a desuperheater (DSH) installed at the exit of these compressors, a rack of compressors at the high-temperature side (MT_C), a flash-gas valve (FGv), and an internal heat exchanger (IHX) placed at the exit of the liquid receiver.
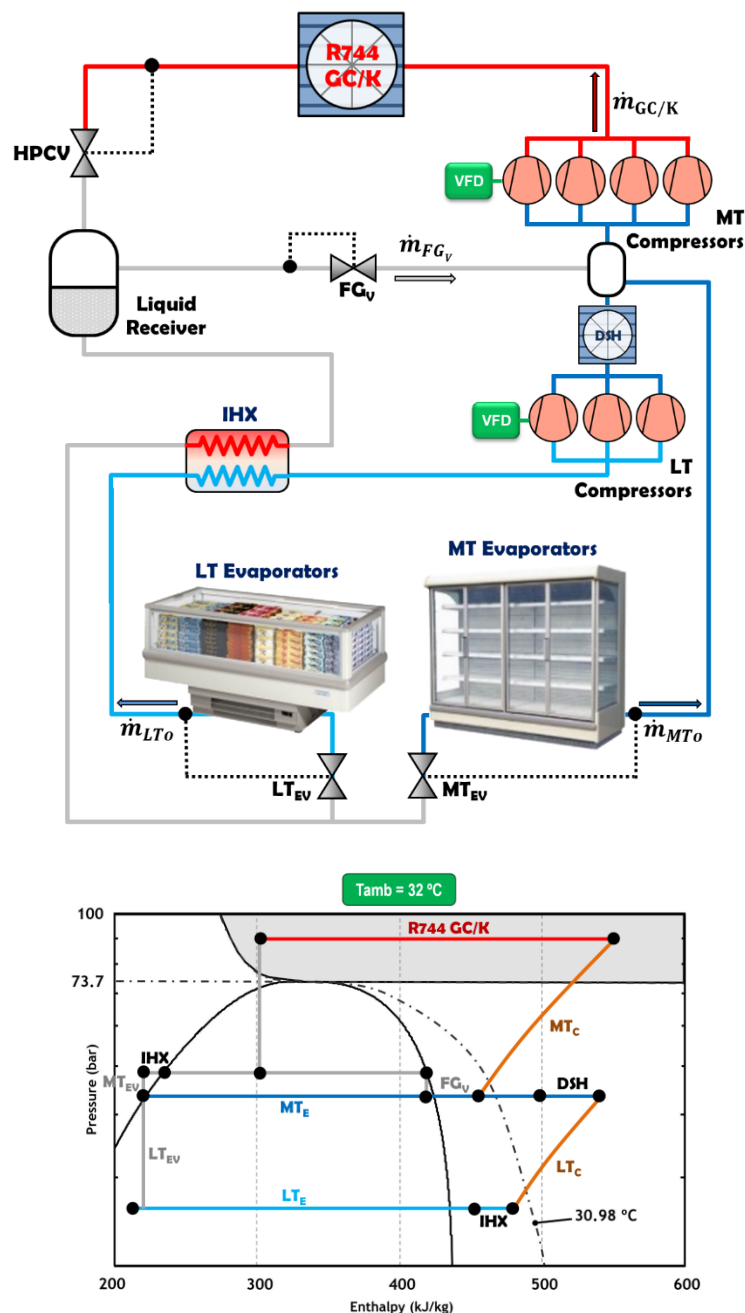

Figure 1. Schematic of the basic booster arrangement (BB) and the P−h diagram for T_{amb} = 32 °C.

The use of the DSH allows reducing the temperature at the inlet of the MT compressors improving their operation and lowering their discharge temperature. In this case, a cross-flow heat exchanger has been used employing ambient air as secondary fluid.

The discharge from the second compressor rack is connected to an air-cross-flow heat exchanger (GC/K), which can operate in a transcritical or subcritical regime depending on the ambient temperature. The heat rejection pressure also depends on the ambient temperature, and it is controlled by a high-pressure control valve (HPCV) that ensures optimal operating conditions [33]. A liquid receiver installed after the HPCV regulates the refrigerant mass distribution as well as feeds the LT_{EV} and MT_{EV} with liquid phase. The use of a flash-gas valve (FG_V) extracts vapor from the liquid receiver, reducing the pressure of the accumulator tank and, consequently, the enthalpy at the inlet of both expansion valves (LT_{EV} and MT_{EV}). The vapor extracted is expanded and injected at the inlet of the MT compressors, which reduces their suction and discharge temperature.

Finally, an IHX is installed at the outlet of the liquid receiver to ensure the liquid phase at the inlet of thermostatic valves (LT_{EV} and MT_{EV}) and to heat up the lubricant oil of the LT compressors [34].

It is important to notice that one compressor of each compression rack is driven by a variable frequency drive (VFD) in order to cover easier the cooling demand with the minimal energy consumption.

2.2. Basic Booster with Economizer (BB+EHX)

In this case, an additional heat exchanger named the economizer or subcooler (EHX) is introduced in the architecture (Figure 2). The EHX cools down the exhaust refrigerant from the GC/K by means of a stream of refrigerant extracted and expanded from the GC/K exit. The expanded fluid has low vapor quality; thus, the cooling capacity to reduce the temperature of the high-pressure stream is greater than that of other cooling systems that reduce the temperature with the vapor extracted from the liquid receiver. The expansion valve used in this case is labeled as ECO_{EV} and its superheating control mode defines two different cycles, as can be shown in Figure 2. The first one (EHX_{OUT} Superheat) controls the superheating degree at the exit of economizer, while the second one (MT_{C_IN} Superheat) minimizes the superheating degree at the inlet of the MT compressors (MT_C). Depending on the control mode adopted, the refrigerant mass flow injected and the degree of subcooling will vary, affecting the pressure of the liquid receiver.
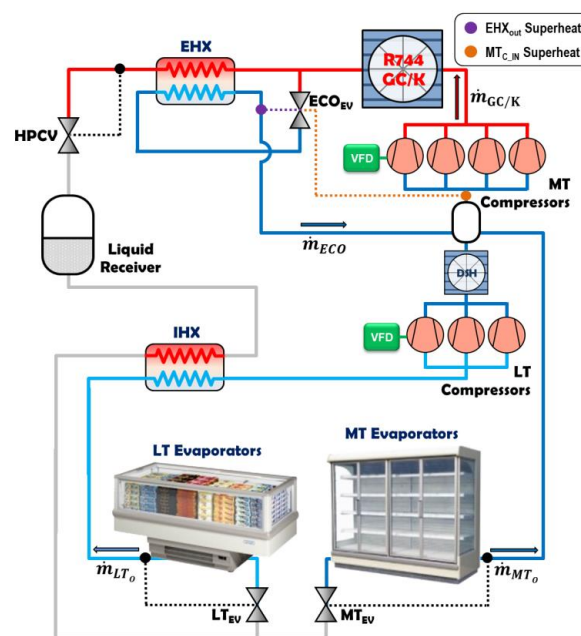

Figure 2. *Cont.*
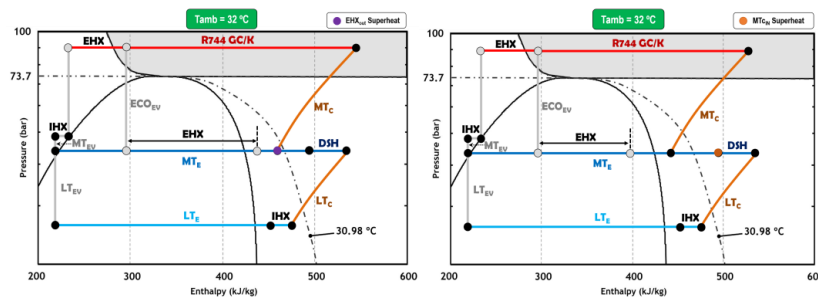
Figure 2. Schematic of a basic booster with economizer and the P−h diagrams for T_{amb} = 32 °C.

From the results obtained in the computational model presented in this work, it has been proved that both configurations have a similar COP, so for the complete analysis of the BB + EHX configuration, only the arrangement that controls the superheating degree at the exit of the economizer (EHX$_{OUT}$ Superheat) has been chosen, because it is easier to implement in a real facility.

2.3. Basic Booster with Economizer and Additional Compression Stage (BB+IMS)

The arrangements shown in Figure 2 can be improved by adding an additional compression stage acting over the stream of refrigerant expanded from the high-pressure level. The purpose of those compressors (EC) is to reduce the mass flow rate driven by the MT compressors, taking advantage of its low compression ratio. As before, Figure 3 presents the possible arrangements of the refrigeration cycle depending on the temperature control of the ECO$_{EV}$ valve. The valve labeled as ELEC$_V$ allows bypassing the EC compressors when they are not used, mainly when their compression ratio is below the manufacturer limits [35] or if the use of the EC compressors does not provide significant energy saving.
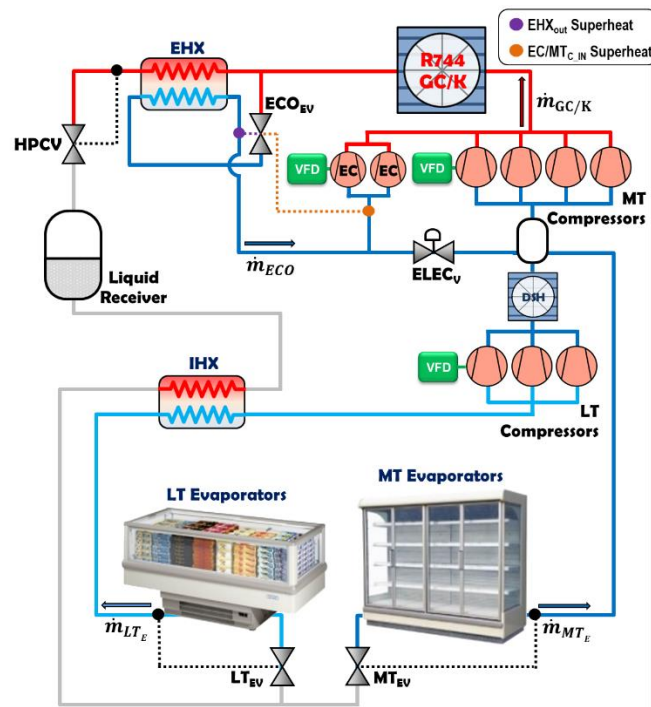

Figure 3. *Cont.*
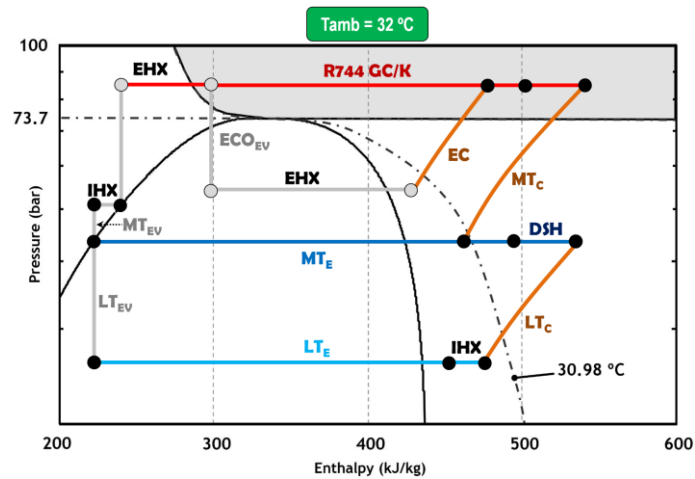
Figure 3. Schematic of a basic booster with IMS and the P−h diagram for T_{amb} = 32 °C.

Similarly to Section 2.2, the configurations depicted in Figure 3 have similar results in terms of COP when the computational model developed in this manuscript is applied. Consequently, the analysis of the BB + IMS configuration will be referred to the configuration that controls the superheating degree at the exit of the economizer (EHX$_{OUT}$ Superheat), as its control is easier to implement.

3. Model Assumptions

This section is dedicated to listing all the model assumptions considered for the theoretical calculation.

3.1. Heat Rejection Conditions

Since all the architectures described before use air as the secondary fluid, the heat rejection conditions depend on the ambient temperature. Hence, for transcritical conditions ($P_{GC/K} \geq 73.75$ bar), the temperature at the exit of the gas cooler has been obtained by means of Equation (1) with the ambient temperature (T_{amb}) and a temperature approach (*ATD*) of 2 K. The low value of *ATD* is based on the high thermal effectiveness of the gas cooler in transcritical conditions [36]. On the other hand, the heat rejection pressure was adjusted to the optimal one with an iterative method from 120 bar to 73.75 bar with small intervals of 0.05 bar.

$$T_{GC_{out}} = T_{amb} + ATD \tag{1}$$

For subcritical conditions ($P_{GC/K} < 73.75$ bar), the temperature approach has fixed to 5K in order to consider the loss of thermal effectiveness when the heat exchanger is operating as a condenser [36]. Additionally, a subcooling degree (*SUB*) of 2 K has been added according to the control strategies described by Danfoss [37] to ensure the proper operation of the facility. With those values, the condensing temperature (T_K) is determined with Equation (2).

$$T_K = T_{amb} + ATD + SUB \tag{2}$$

3.2. Economizer (EHX)

As was stated before, the aim of the economizer (EHX) is to cool down the refrigerant at the exit of the GC/K using a stream of CO_2 expanded with the ECO$_{EV}$. Depending on how the valve is controlled, the cycle arrangement changes as shown in Figures 2 and 3. Notwithstanding, in both cases, the set

point for the superheating control was fixed to 5 K to avoid liquid in the suction line of the compressors. Equations (3)–(7) determine the inlet and outlet temperatures at the economizer.

$$T_{in\_EHX\_HP} = T_{out\_GC/K} \tag{3}$$

$$T_{out\_EHX\_HP} = T_{in\_EHX\_HP} - SUB \tag{4}$$

$$T_{in\_EHX\_LP} \left(BB + EHX \right) = T_{MTo} \tag{5}$$

$$T_{in\_EHX\_LP} \left(BB + IMS \right) = T_{o\_EHX} \tag{6}$$

$$T_{out_{EHX_{LP}}} \left(BB + EHX \text{ and } BB + IMS \right) = T_{in_{EHX_{LP}}} + 5K \tag{7}$$

3.3. Desuperheater (DSH)

The function of the desuperheater is to reduce the temperature of the refrigerant at the discharge line of the LT compressors. To achieve this, a cross-flow heat exchanger has been used employing ambient air as the secondary fluid. Since the discharge temperature of the LT compressors is above the ambient temperature, the use of a desuperheater is always positive, reducing the temperature at the suction port of the MT compressors [38]. Equation (8) allows determining the temperature at the exit of the DSH, assuming a temperature approach (*ATD*) of 5 K regarding the ambient temperature (T_{amb}).

$$T_{DSH_{out}} = T_{amb} + ATD \tag{8}$$

3.4. Service Thermal Loads

For all booster architectures, similar operating conditions have been assumed for the low and medium temperature levels. Taking into account the values reported by Emerson [39], the evaporating levels adopted for medium and low temperature are −6 °C and −32 °C, respectively. The cooling load assumed is 140 kW for the medium temperature level and 41 kW for the low-temperature services, resulting in a load ratio (*LR*) of 3.4.

To make the analysis more realistic, a heat load profile of the evaporators was considered taking into account the opening and closing schedule of a typical supermarket. Thus, it was assumed that the 100% of the heat load is effective from 7:00 to 22:00, while this load falls by up to 50% the rest of time (from 22:00 to 7:00) as considered by Catalán-Gil et al. [13].

3.5. Internal Heat Exchanger (IHX)

Regardless of the arrangement adopted, a suction-to-liquid heat exchanger (IHX) was considered at the exit of the liquid receiver. The presence of the IHX guarantees the absence of any vapor phase at the inlet of the thermostatic valves LT$_{EV}$ and MT$_{EV}$. Moreover, it also introduces a slight subcooling degree that enhances the cooling capacity and a moderate superheating degree which ensures a minimum temperature in the lubricant oil [34]. From Llopis et al. [40], a constant thermal effectiveness of 65% was considered in this work.

3.6. Compressors

To cover the cooling demand assumed in Section 3.4, two compression racks have been used in all systems. According to the thermal loads, the low-temperature rack is composed by three compressors, while the medium-temperature rack has 4. The economizer arrangement has also two additional compressors, whose position is depicted in Figure 3. Depending on the operating conditions, the compressors are switched on or off, guaranteeing the minimal energy consumption.

Each compression rack is equipped with one variable frequency drive (VFD) for one of the compressors to make the adaptation to the thermal load precise. The frequency operation of these compressors varies from 25 to 75 Hz, while the rest of them work with a fixed frequency of 50 Hz.

Taking into account the manufacturer restrictions, we have assumed a minimum compression ratio (t) of 1.5 and a maximum suction pressure of 55 bar in all compressors [35,41].

The mathematical model of the reciprocating compressors has been adjusted from the manufacturer's data [41] using the parameters of volumetric efficiency ($\eta_{volum.}$) and global efficiency (η_{global}). Equations (9) and (10) describe the mathematical model obtained for the compressor efficiencies as a polynomial equation, with the variables of compression ratio (t), specific volume at the suction port (v), and displacement ($\dot{V}_g$). Since this last also depends on the compressor rotation speed, a precise polynomial model has been developed to take into account the effect of the rotation speed over the compressor operation. The maximum relative error obtained from the mathematical adjustment, compared to the manufacturer's data, was lower than 0.2%, so we can assume that the model predictions are in good agreement with the manufacturer data.

Appendix A includes the main features of the compressors as well as the coefficients used in Equations (9) and (10).

$$
\begin{aligned}
\eta_{volum.} = &\left[\left(Dd3 \cdot \dot{V}_g{}^3 + Dd2 \cdot \dot{V}_g{}^2 + Dd1 \cdot \dot{V}_g + Dd0\right) \cdot v^3 + \left(Dc3 \cdot \dot{V}_g{}^3 + Dc2 \cdot \dot{V}_g{}^2 + Dc1 \cdot \dot{V}_g + Dc0\right) \cdot v^2 \right.\\
&+ \left(Db3 \cdot \dot{V}_g{}^3 + Db2 \cdot \dot{V}_g{}^2 + Db1 \cdot \dot{V}_g + Db0\right) \cdot v + \left(Da3 \cdot \dot{V}_g{}^3 + Da2 \cdot \dot{V}_g{}^2 + Da1 \cdot \dot{V}_g + Da0\right)\Big] \cdot t \\
&+ \left[\left(Cd3 \cdot \dot{V}_g{}^3 + Cd2 \cdot \dot{V}_g{}^2 + Cd1 \cdot \dot{V}_g + Cd0\right) \cdot v^3 + \left(Cc3 \cdot \dot{V}_g{}^3 + Cc2 \cdot \dot{V}_g{}^2 + Cc1 \cdot \dot{V}_g + Cc0\right) \cdot v^2 \right.\\
&+ \left.\left(Cb3 \cdot \dot{V}_g{}^3 + Cb2 \cdot \dot{V}_g{}^2 + Cb1 \cdot \dot{V}_g + Cb0\right) \cdot v + \left(Ca3 \cdot \dot{V}_g{}^3 + Ca2 \cdot \dot{V}_g{}^2 + Ca1 \cdot \dot{V}_g + Ca0\right)\right]
\end{aligned}
\tag{9}
$$

$$
\begin{aligned}
\eta_{global} = &\left[\left(Dd3 \cdot \dot{V}_g{}^3 + Dd2 \cdot \dot{V}_g{}^2 + Dd1 \cdot \dot{V}_g + Dd0\right) \cdot v^3 + \left(Dc3 \cdot \dot{V}_g{}^3 + Dc2 \cdot \dot{V}_g{}^2 + Dc1 \cdot \dot{V}_g + Dc0\right) \cdot v^2 \right.\\
&+ \left(Db3 \cdot \dot{V}_g{}^3 + Db2 \cdot \dot{V}_g{}^2 + Db1 \cdot \dot{V}_g + Db0\right) \cdot v + \left(Da3 \cdot \dot{V}_g{}^3 + Da2 \cdot \dot{V}_g{}^2 + Da1 \cdot \dot{V}_g + Da0\right)\Big] \cdot t^3 \\
&+ \left[\left(Cd3 \cdot \dot{V}_g{}^3 + Cd2 \cdot \dot{V}_g{}^2 + Cd1 \cdot \dot{V}_g + Cd0\right) \cdot v^3 + \left(Cc3 \cdot \dot{V}_g{}^3 + Cc2 \cdot \dot{V}_g{}^2 + Cc1 \cdot \dot{V}_g + Cc0\right) \cdot v^2 \right.\\
&+ \left(Cb3 \cdot \dot{V}_g{}^3 + Cb2 \cdot \dot{V}_g{}^2 + Cb1 \cdot \dot{V}_g + Cb0\right) \cdot v + \left(Ca3 \cdot \dot{V}_g{}^3 + Ca2 \cdot \dot{V}_g{}^2 + Ca1 \cdot \dot{V}_g + Ca0\right)\Big] \cdot t^2 \\
&+ \left[\left(Bd3 \cdot \dot{V}_g{}^3 + Bd2 \cdot \dot{V}_g{}^2 + Bd1 \cdot \dot{V}_g + Bd0\right) * v^3 + \left(Bc3 \cdot \dot{V}_g{}^3 + Bc2 \cdot \dot{V}_g{}^2 + Bc1 \cdot \dot{V}_g + Bc0\right) \cdot v^2 \right.\\
&+ \left(Bb3 \cdot \dot{V}_g{}^3 + Bb2 \cdot \dot{V}_g{}^2 + Bb1 \cdot \dot{V}_g + Bb0\right) \cdot v + \left(Ba3 \cdot \dot{V}_g{}^3 + Ba2 \cdot \dot{V}_g{}^2 + Ba1 \cdot \dot{V}_g + Ba0\right)\Big] \cdot t \\
&+ \left[\left(Ad3 \cdot \dot{V}_g{}^3 + Ad2 \cdot \dot{V}_g{}^2 + Ad1 \cdot \dot{V}_g + Ad0\right) \cdot v^3 + \left(Ac3 \cdot \dot{V}_g{}^3 + Ac2 \cdot \dot{V}_g{}^2 + Ac1 \cdot \dot{V}_g + Ac0\right) \cdot v^2 \right.\\
&+ \left.\left(Ab3 \cdot \dot{V}_g{}^3 + Ab2 \cdot \dot{V}_g{}^2 + Ab1 \cdot \dot{V}_g + Ab0\right) \cdot v + \left(Aa3 \cdot \dot{V}_g{}^3 + Aa2 \cdot \dot{V}_g{}^2 + Aa1 \cdot \dot{V}_g + Aa0\right)\right]
\end{aligned}
\tag{10}
$$

3.7. Expansion Devices

All the expansion devices used in the model have been assumed as isenthalpic with a minimum pressure difference of 3.5 bar between the inlet and the outlet ports [42]. Moreover, the maximum operation pressure (MOP) has been fixed to 120 bar, which corresponds with the maximum operation pressure of the refrigerating plant. For thermostatic valves, the useful superheating was fixed to 5 K in all cases.

3.8. Liquid Receiver Pressure

The pressure of the liquid receiver always depends on the configuration adopted, the heat rejection conditions, and the subcooling introduced after the GC/K heat exchanger. Therefore, the use of economizer or a flash-gas valve (FG_V) reduces the pressure at the liquid receiver. To take into account all these variations, we have assumed a variable liquid receiver pressure with a minimal pressure of 35 bar to comply with the restriction mentioned above of keeping a minimal pressure difference in all expansion devices.

3.9. Additional Considerations

The pressure drops in pipelines, and heat exchangers have been neglected. Similarly, the heat transfer between components and ambient has also been neglected.

3.10. Summary Table

Table 1 summarizes all the assumptions stated before for the analyzed configurations.

Table 1. Assumptions for the computational models. EHX: economizer, GC/K: air-cross-flow heat exchanger, LT: low temperature: MT: high temperature.

		BB	BB+EHX	BB+IMS
GC/K$_{out}$ Temp. [°C]	**Transcritical**		T_{amb} + 2	
	Subcritical		T_{amb} + 5	
Condenser Subcooling (K$_{SUB}$) [K]	**Subcritical**	2	0	
Condensing Temp. [°C]			$T_{amb} + 5 + K_{SUB}$	
EHX$_{pinch}$ [K]	**Transcritical**		2	
	Subcritical		5	
T$_{out}$ EHX HPS [°C]		-	GC/K_{out} *Temp.* $- EHX_{SUB\_opt}$	
T$_{in}$ EHX LPS [°C]		-	*MTo Temp.*	T_{out} *EHX$_{\_HPS}$ -* EHX_{pinch}
T$_{out}$ EHX LPS [°C]		-	*Tin EHX LPS* + 5	
T$_{in}$ MTc [°C]		Variable	Variable	
IHX Thermal Effectiveness [%]	**Transcritical**		65	
DSH$_{out}$ Temp. [°C]	**Subcritical**		T_{amb} + 5	
Liquid Receiver Limit Pressures [bar]			From 35 to 55	
Minimum ΔP (Expansion Valves) [Bar]			3.5	
Maximum Compressor Inlet Pressure [Bar]			55	
Minimum Compression Ratio [-]			1.5	
LT$_o$ Temp. [°C]			-32	
MT$_o$ Temp. [°C]			-6	
LT$_o$, MT$_{o\ R}$ Superheating [K]			5	
Evaporators$_{out}$ Useless Superheating [K]			5	
LT Load [kW]			41	
MT Load [kW]			140	

4. Model Description

To evaluate the maximum COP of all the configurations described in Section 2, a computational model was developed according to the restrictions described in Section 3. The model was programmed using Matlab® and Microsoft® VBA, using the database of RefProp® v.9.1 [43] for determining the thermophysical properties. Figures 4–6 describe the iterative method used by the model to find the maximum COP (COP$_{opt}$) of the facility at each ambient temperature (T_{amb}).
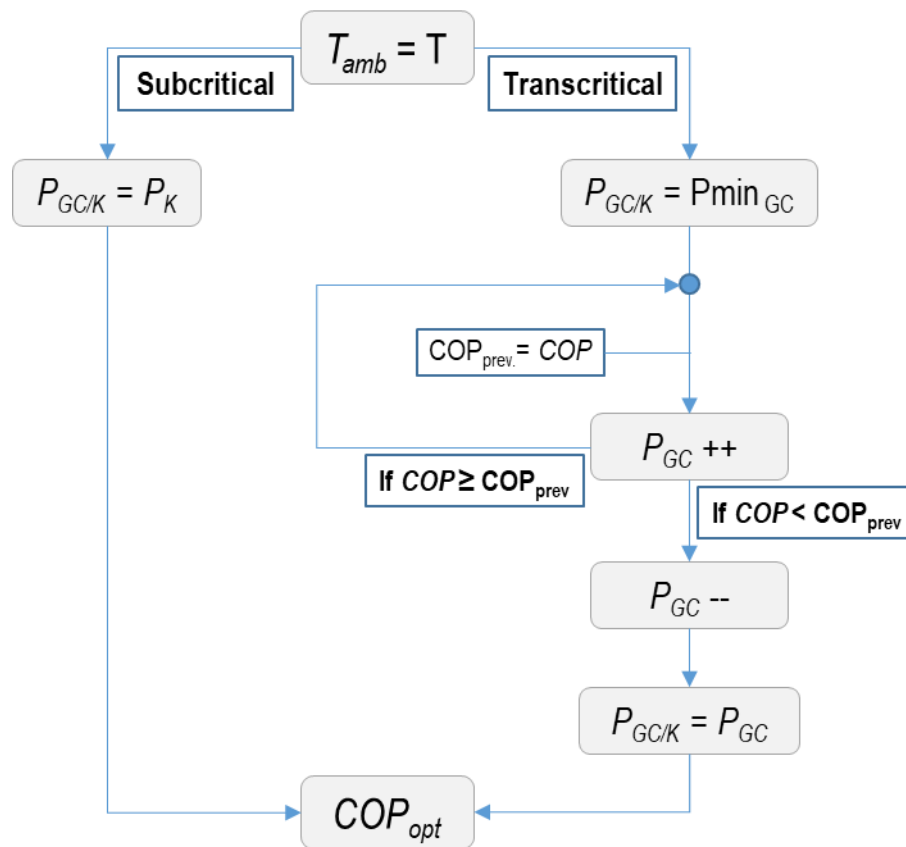
Figure 4. Iterative method for the BB system.

For the Basic Booster arrangement (BB) (Figure 4), the maximum COP is achieved at the optimum GC/K pressure ($P_{GC/K}$) in transcritical conditions. In subcritical conditions, the optimal pressure corresponds to the condensing pressure (P_K) except for the transition zone (near the critical point), where a linear pressure variation with the ambient conditions was considered according to Catalán-Gil et al. [13]. In transcritical operation, the iteration is started with the lowest transcritical pressure ($Pmin_{GC}$ = 74 bar), the COP is obtained with Equation (11), and the GC/K pressure is increased in steps of 0.1 bar (P_{GC} ++). With this pressure, another COP is obtained and compared with the previous one (COP_{prev}). If the current COP is higher, the GC/K pressure is further increased; else, if it is lower, the previous pressure is returned (P_{GC} −−). This will be the optimum pressure that maximizes the COP (COP_{opt}).

Regarding the Basic Booster with economizer arrangement (BB+EHX), the optimum COP depends not only on the GC pressure, but also on the refrigerant mass flow expanded by the expansion valve (ECO_{EV}) used to produce the subcooling at the EHX; thus, the iteration method (Figure 5) is similar to the previous one but adding another iteration to obtain the optimum subcooling.
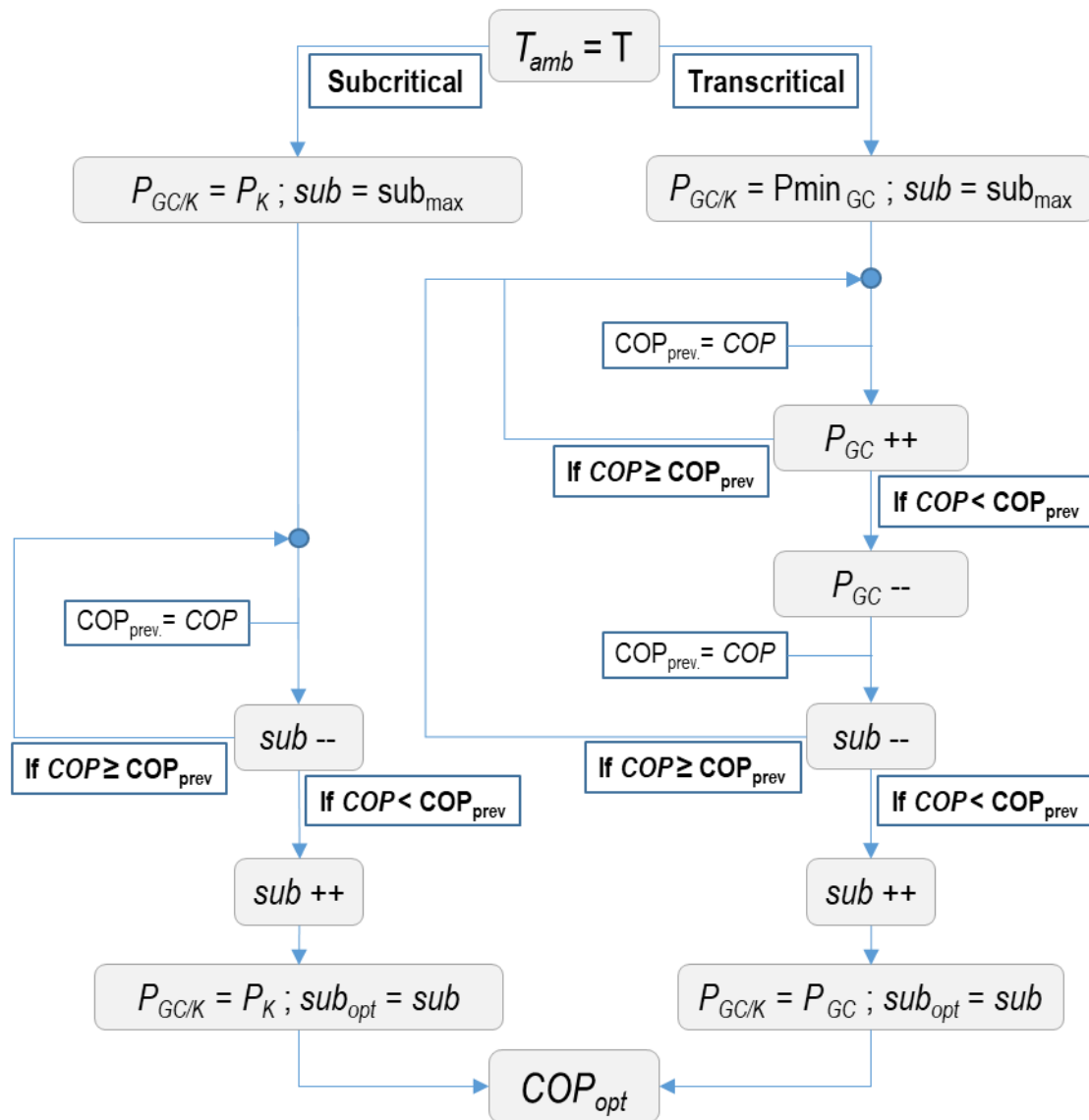
Figure 5. Iterative method for the BB+EHX system.

Hence, two iterative tested loops have been used in this arrangement. The first one determines the optimal heat GC/K pressure, while the second one is focused on determining the optimal subcooling degree which is achieved by varying the mass flow rate expanded by the ECO_{EV}. The subcooling degree is changing in steps of 0.1 K (sub ++, sub −−).

Finally, the last configuration (BB+IMS) introduces an additional compressor (EC) to act over the refrigerant evaporated in the EHX. The presence of this component means that the inlet pressure of the EC needs to be controlled by the computational model (Figure 6) in order to obtain the maximum COP of the facility. Taking into account the restrictions explained in Section 3, the maximum value for this pressure is 55 bar, and the minimum one must ensure a minimum pressure ratio of 1.5 in the EC. Accordingly, an extra iterative loop has been programmed acting over the previous programmed loops. Similar to the previous method, the optimum subcooling degree depends on the GC/K pressure and the mass flow rate but, in this case, it also depends on the suction pressure of the additional compressors (P_{IN} EC).
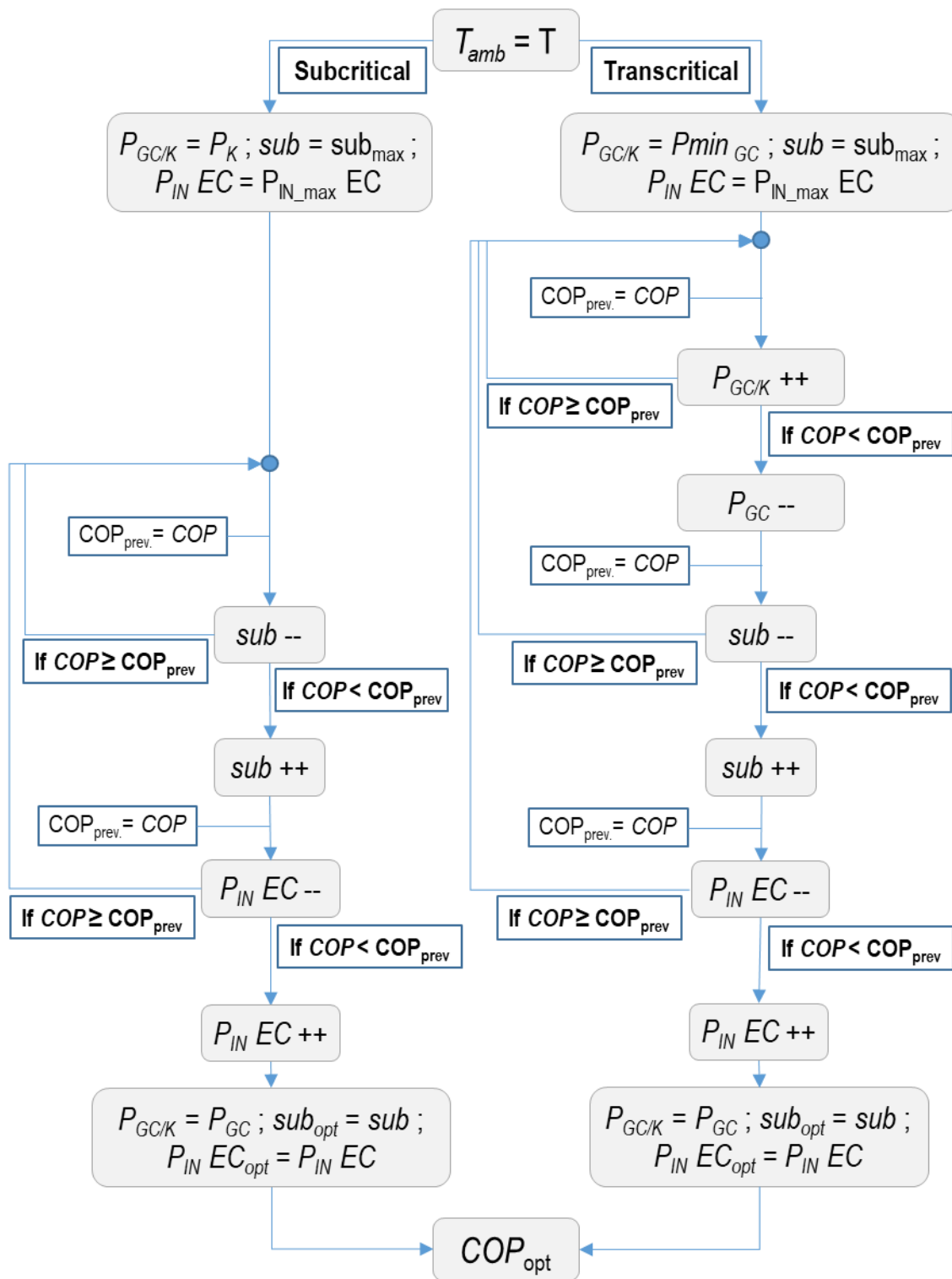
$$T_{amb} = T$$

Subcritical　　　　　　　　　　　　　　**Transcritical**

$P_{GC/K} = P_K$; $sub = sub_{max}$; $P_{IN} EC = P_{IN\_max} EC$

$P_{GC/K} = Pmin_{GC}$; $sub = sub_{max}$; $P_{IN} EC = P_{IN\_max} EC$

$COP_{prev.} = COP$

$P_{GC/K}$ ++

If $COP \geq COP_{prev}$　　　　**If** $COP < COP_{prev}$

P_{GC} --

$COP_{prev.} = COP$

$COP_{prev.} = COP$

sub --　　　　　　　　　　　　　　sub --

If $COP \geq COP_{prev}$　　**If** $COP < COP_{prev}$　　　　　　**If** $COP \geq COP_{prev}$　　**If** $COP < COP_{prev}$

sub ++　　　　　　　　　　　　　　sub ++

$COP_{prev.} = COP$　　　　　　　　　　　　　$COP_{prev.} = COP$

$P_{IN} EC$ --　　　　　　　　　　　$P_{IN} EC$ --

If $COP \geq COP_{prev}$　　**If** $COP < COP_{prev}$　　　　**If** $COP \geq COP_{prev}$　　**If** $COP < COP_{prev}$

$P_{IN} EC$ ++　　　　　　　　　　　$P_{IN} EC$ ++

$P_{GC/K} = P_{GC}$; $sub_{opt} = sub$; $P_{IN} EC_{opt} = P_{IN} EC$

$P_{GC/K} = P_{GC}$; $sub_{opt} = sub$; $P_{IN} EC_{opt} = P_{IN} EC$

COP_{opt}

Figure 6. Iterative method for the BB+IMS.

5. Results and Discussion

In this section, the computational model results are presented and discussed in a wide range of ambient temperatures from 0 to 40 °C. The results are used to determine the annual energy consumption in different European cities in order to justify which is the best configuration.

5.1. Operating Modes

Taking into account the restrictions summarized in Section 3 and the best-performing conditions of the systems, Figure 7 presents the operation modes of each configuration according to the ambient temperature.
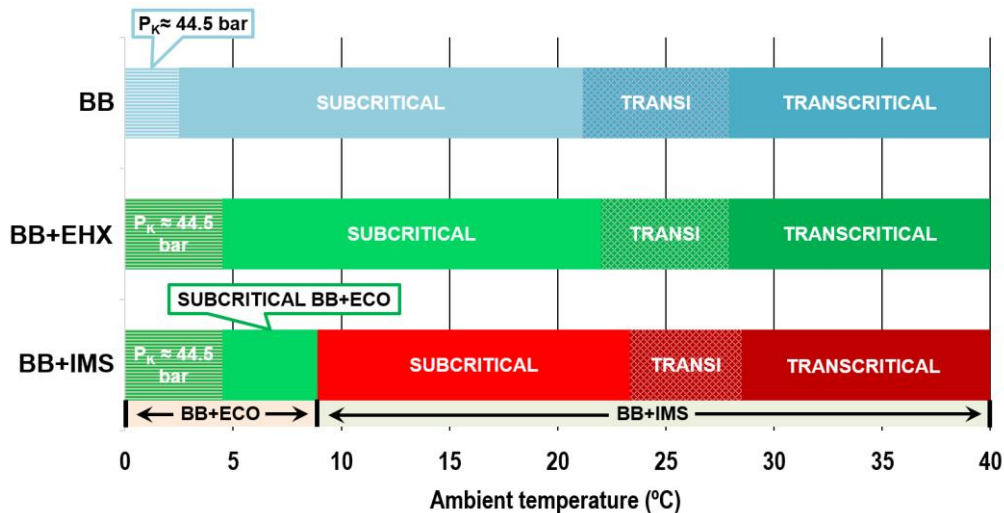

Figure 7. Operation mode of the analyzed configurations.

It must be highlighted that in each arrangement at least three operative modes can be achieved: transcritical operation, subcritical operation, and transition mode, which corresponds to the change from transcritical to subcritical and vice versa.

For the Basic Booster system (BB), the transcritical operating mode is achieved for ambient temperatures above 27.9 °C, while subcritical is recommended for below 21.2 °C. The range from 27.9 °C to 21.2 °C corresponds to the transition zone where the pressure is reduced progressively from 73.75 °C bar to the corresponding condensing one for 21.2 °C. It is important to outline that floating condensing is limited from 21.2 °C to 2.5 °C in subcritical operation. For ambient temperatures below 2.5 °C, the system is forced to keep the same condensing pressure in order to ensure a minimum compression ratio of 1.5 in the MT_C rack.

Regarding the configuration with economizer (BB+EHX), the temperature limits vary only for the subcritical operating mode. Thus, the floating condensing is limited from 22 °C to 4.5 °C, while the transient zone is delimited from 27.9 °C to 22 °C. The presence of the economizer reduces the temperature at the inlet of the expansion device and also the condensing temperature in subcritical conditions. As a consequence, the minimum ambient temperature for floating condensing (when MT_C compression rate = 1.5) is higher than the basic cycle.

Finally, the inclusion of an additional compressor in the system (BB+IMS) modifies not only the subcritical limits but also the transcritical ones. Thus, this system works in transcritical operation for ambient temperatures above 28.5 °C and in subcriticial operation from 23.4 °C to 8.9 °C. Below 8.9 °C, the BB+EHX configuration is preferred because it works more efficiently.

5.2. Compressors Sizing and Operation

As described in Section 3, each compression stage has a compressor with variable frequency drive (VFD) to achieve the desired volumetric displacement without abrupt changes. Figures 8–10 present the volumetric displacement of the compressors used for each configuration.
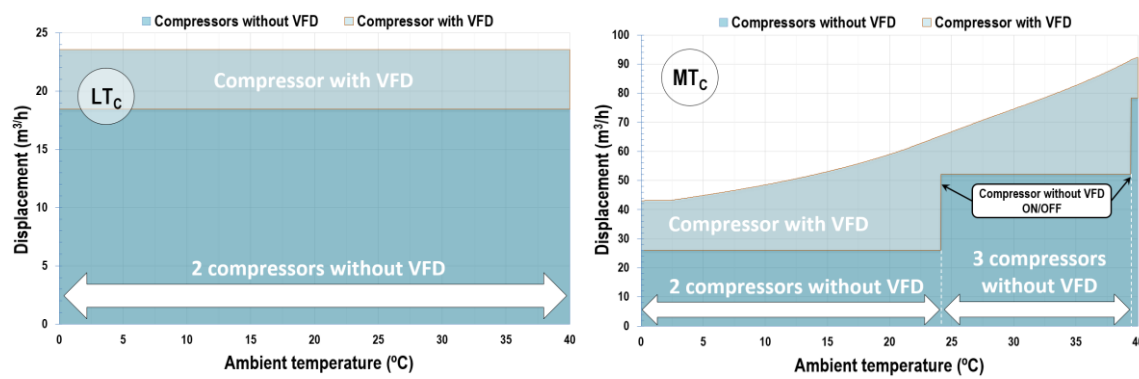
Figure 8. BB compressors operation. A rack of compressors at the low-temperature side (LT$_C$, left) and a rack of compressors at the high-temperature side (MT$_C$, right).
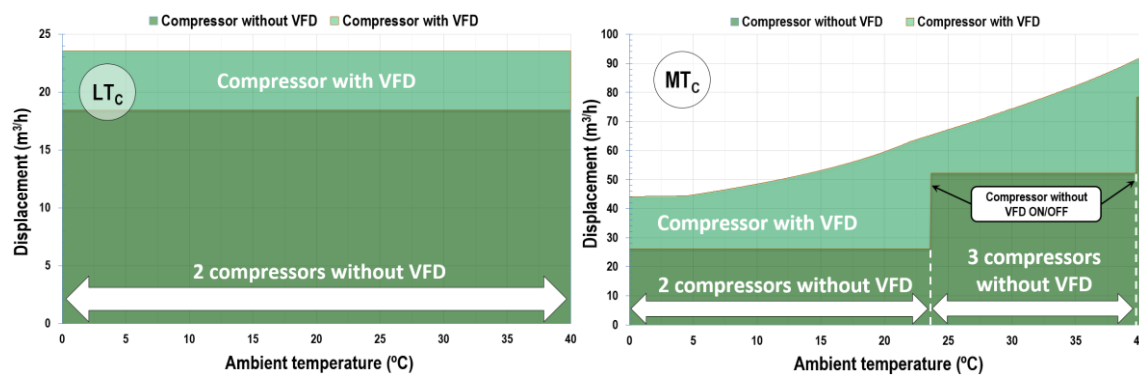

Figure 9. BB+EHX compressors operation. LT$_C$ (left) and MT$_C$ (right).

Figure 8 refers to the BB configuration. The LT stage uses two compressors with a displacement of 9.22 m^3/h at their nominal frequency (without VFD at 50 Hz) and one compressor with VFD operating with a displacement of 5.1 m^3/h at about 32 Hz. These compressors have the same operation for all the heat rejection conditions, since the pressure of the receiver is kept constant at 35 bar. That means a constant cooling capacity in LT$_O$ as well as the mass flow rate.

Regarding the medium temperature compressors (MT$_C$), the volumetric requirements of the MT$_C$ are not constants. Thus, for ambient temperatures from 0 °C to 24.1 °C, the system operates with one MT$_C$ at nominal conditions (26.12 m^3/h at 50 Hz) and one compressor with VFD operating from 16.95 to 39.18 m^3/h (38.3–75 Hz). When the ambient temperature ranges between 24.1 °C and 39.4 °C, another compressor at its nominal conditions is switched on, and the compressor with VFD reduces its frequency to 25 Hz (13.06 m^3/h). Finally, for ambient temperatures above 39.4 °C, a fourth compressor without VFD is switched on.

Figure 9 shows the displacement of the low and medium-temperature compressors of the BB+EHX system. This system cools the refrigerant after the GC/K, and the pressure of the receiver changes depending on the subcooling degree in the EHX. The optimal subcooling allows the receiver pressure to be close to the previous system (35 bar) for all ambient temperature. So, the graphs of Figure 9 are quite similar to Figure 8. The main difference is depicted in the temperature limits that are stated at 23.6 °C and 37.75 °C.
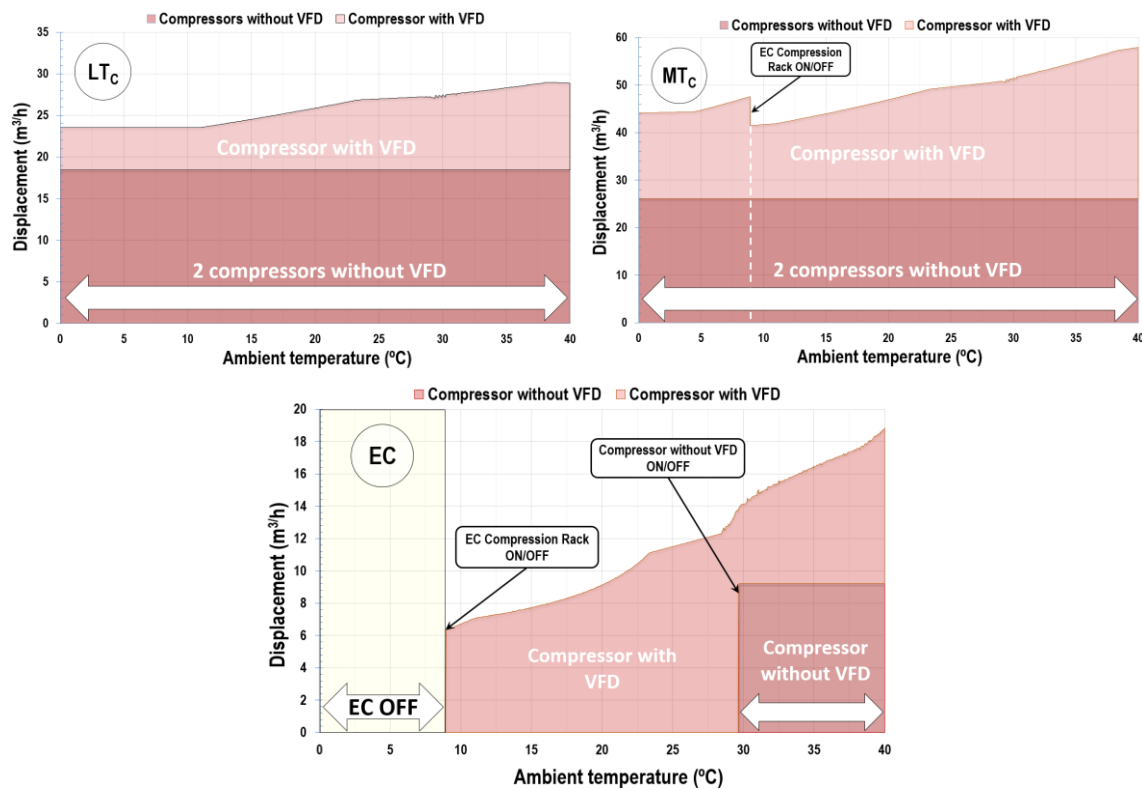
Figure 10. BB+IMS compressors operation. LT_C (left), MT_C (right), and EC (center).

Figure 10 shows the volumetric displacement of the compressors for BB+IMS. In this case, the system works slightly different than the previous ones. For LT_C, the system works with three compressors: two at their nominal frequency and one with VFD. In this case, the compressor with VFD keeps its frequency constant from 0 to 11 °C because the receiver optimum pressure remains constant at 35 bar. However, for above ambient temperature, this compressor changes its frequency from 32 to 56.9 Hz (5.1–10.5 m^3/h) due to the variation of the pressure in the liquid receiver (Figure 11).

For MT_C, the system works with one compressor at its nominal frequency and one with VFD for all the rejection temperatures analyzed. In this case, the displacement of the MT_C rack has been significantly reduced compared to previous systems. For ambient temperatures below 8.9 °C, the system works as BB+EHX due to the better energy efficiency (EC is switched off). For ambient temperatures above (8.9–40 °C), the system works as BB+IMS. In this range of temperatures, the compressor with VFD changes its frequency from 29.2 °C to 60.7 Hz (15.3 m^3/h to 31.8 m^3/h).

Finally, the EC rack operates from 8.9 °C to 29.5 °C with a VFD compressor running from 34.6 Hz to 75 Hz (6.3–13.6 m^3/h) and from 29.5 °C with an additional compressor running at nominal conditions.

Focusing on the medium-temperature compressor rack (MTc), which is the one that most affects the efficiency of a CO_2 booster facility (they are the most energy-consuming compressors), it can be seen from the above figures that the introduction of the EHX without additional compression does not reduce the displacement needed in the MTc; however, the reduction of the volumetric displacement required in MTc, with the introduction of the EHX with additional compression, is drastically reduced (over 37%), at the cost of a reduced increase in the volumetric displacement of the additional compression stage.
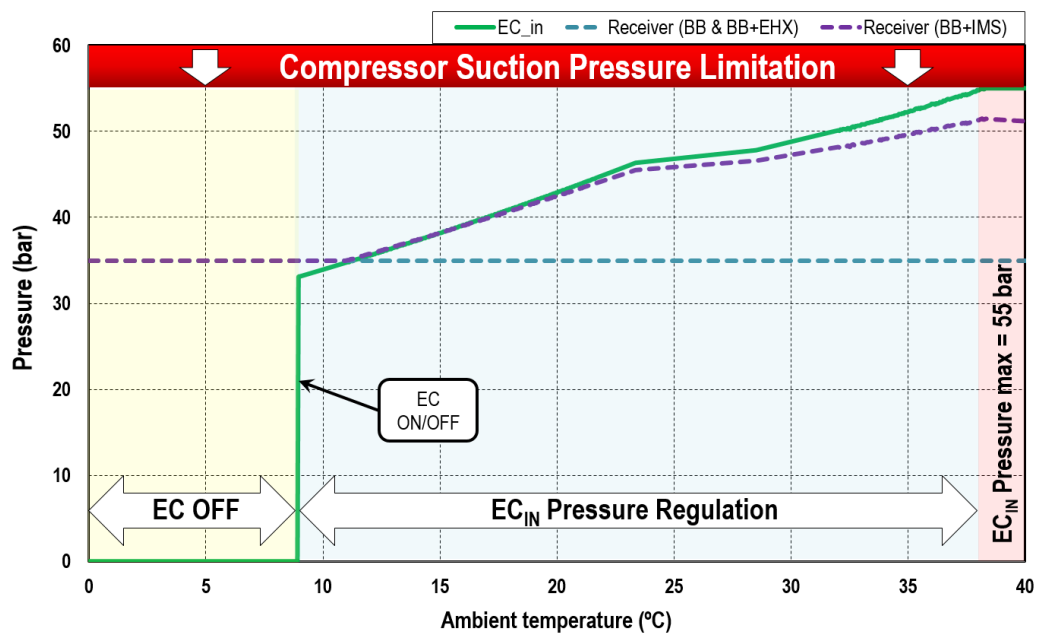
Figure 11. Optimal additional compressor (EC) suction pressure for BB+IMS and receiver pressure in all systems.

5.3. Optimal EC Suction Pressure

To achieve the higher COP at the BB+IMS system, the suction pressure of the EC compressors has been optimized. This value is related with the subcooling degree at the economizer. Figure 11 shows the variation of the suction pressure with the ambient temperature taking into account the restrictions considered in Section 3. Accordingly, three different operation zones can be identified. For temperatures higher than 38.2 °C, the suction pressure is kept at 55 bar, which is the maximum value recommended by the compressor's manufacturer. From 38.2 °C to 8.9 °C, the suction pressure proportionally decreases to 33.1 bar with ambient temperature and a slight change in the transition from transcritical to subcritical (23.4–28.5 °C). Finally, below 8.9 °C, it is not worth using the EC compressors, since their use penalizes the refrigeration facility's COP (Section 5.6).

5.4. EHX Operation

This section discusses the different parameters related to the EHX, such as the subcooling degree, heat load, and efficiency.

5.4.1. Subcooling Degree

As was stated in Section 4, there is an optimal subcooling degree that maximizes the COP of the refrigeration facility [18]. The subcooling degree has been varied from 0 K to a maximum value that ensures a liquid receiver pressure above 35 bar or a minimum enthalpy of about 200 kJ/kg (h_{sat_liq} at 35 bar). The results from model are depicted in Figures 12 and 13. Figure 12 shows the subcooling degree versus the ambient temperature for the two economizer arrangements, while Figure 13 graphically shows the subcooling area depending on the configuration adopted.
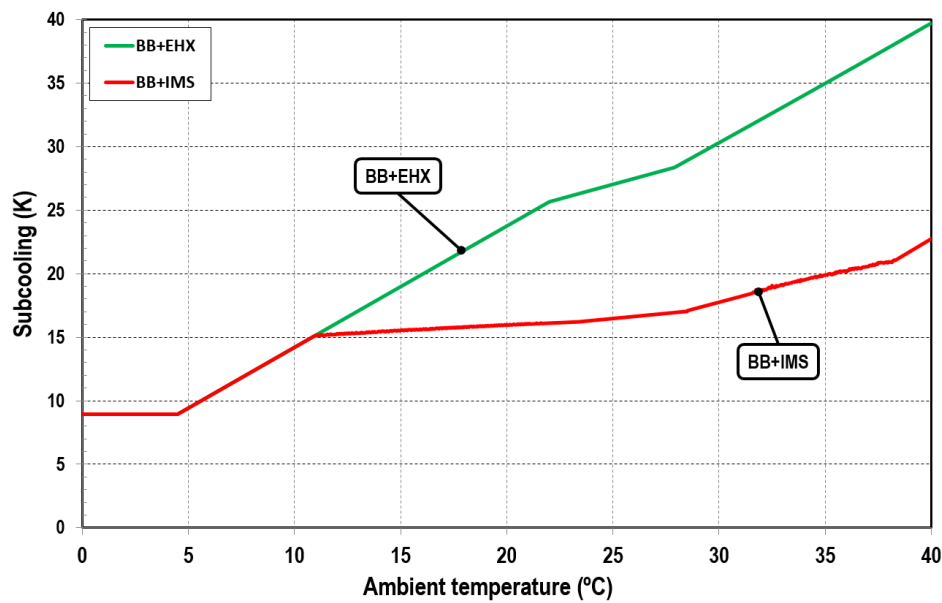
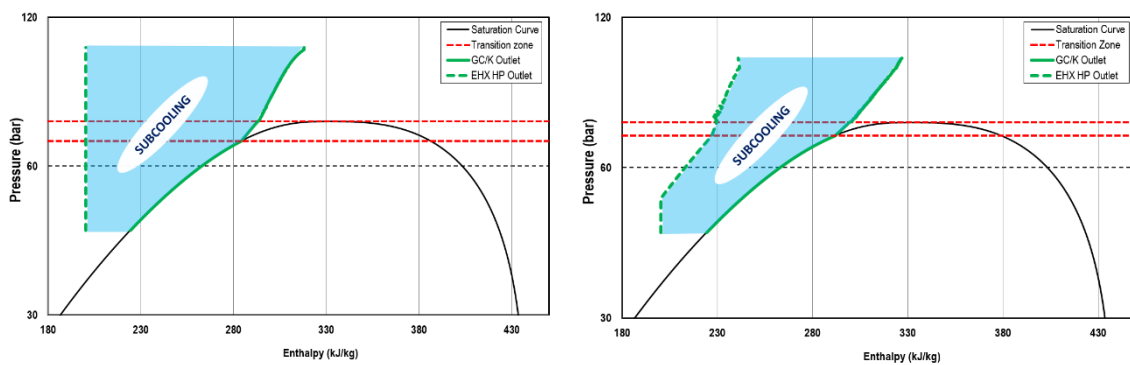**Figure 12.** Economizer optimum subcooling degree.

Figure 13. Subcooling area for the configurations of BB+EHX (left) and BB+IMS (right).

The degree of subcooling is related to the heat rejection pressure, the suction pressure of the additional compressors EC (refrigerant evaporating pressure in the EHX), the refrigerant mass flow in the heat rejection line, and the considered superheat in the EHX (low-pressure side in the heat exchanger), so the subcooling applied will depend on the values of the above parameters.

Taking into account Figures 12 and 13, it can be noticed that the optimum subcooling degree always decreases with the ambient temperature, reaching a minimum value of 9 K for ambient temperatures below 4.5 °C. Notwithstanding, depending on the arrangement, this subcooling degree varies significantly (Figure 12). Thus, the inclusion of an extra compressor entails a significant reduction of the required optimum subcooling degree from ambient temperatures higher than 11.3 °C. The maximum difference is reached at 40 °C, where the BB+EHX system needs a subcooling degree of 40 K, while the configuration of BB+IMS only requires 22.5 K. For ambient temperatures below 11.3 °C, both arrangements require the same subcooling degree due to the pressure limitation of the liquid receiver.

As shown in the graphs that relate the EC compression rate with the GC/K pressure (EC suction pressure can be obtained), relating to the COP of the BB+IMS (Figure 16), the suction pressure control of the EC is an important term for maximizing the COP of the BB+IMS system. This can also be seen in Figure 16, which shows the COP variation of the system with the variation of the heat rejection pressure and the compression rate of the EC compressor (it depends on the EC suction pressure).

5.4.2. Load and Efficiency

The important variation of temperatures stated in Figure 12 denotes a remarkable variation of the economizer cooling capacity, whose dependence on ambient temperature is depicted in Figure 14.
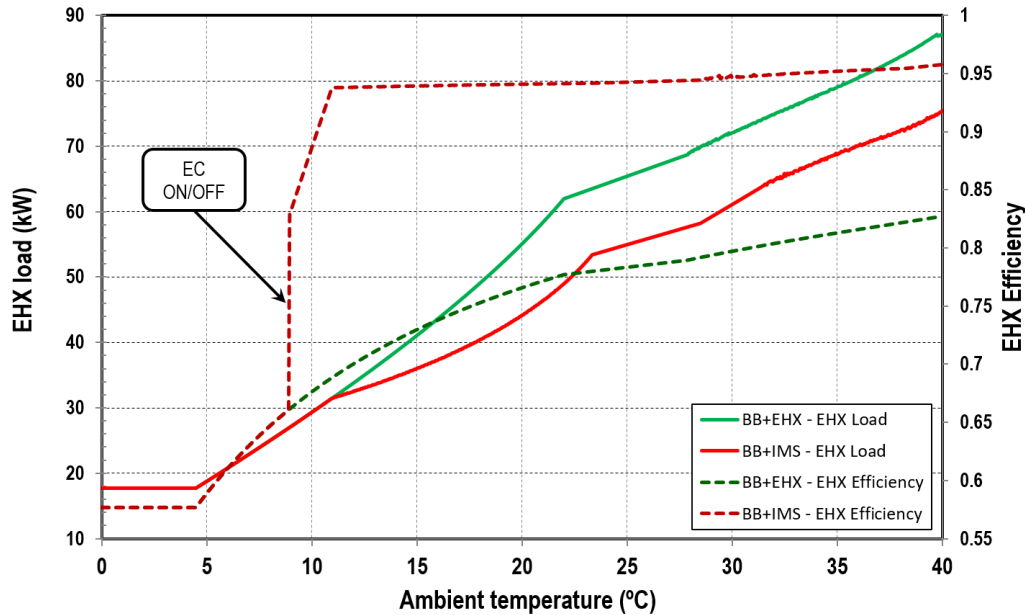

Figure 14. Economizer's cooling capacity vs. ambient temperature.

The heat exchange capacity in the EHX depends mainly on the conditions of the refrigerant at the inlets and outlets, but also on the refrigerant mass flow rate. The refrigerant mass flow expanded to produce subcooling in the EHX changes depending on the required cooling load by controlling the superheat at the output of the EHX. Therefore, this cooling capacity variation is possible by controlling the superheat of the EHX expansion valve in both systems. Accordingly, depending on the location, the heat transfer area of the economizer needed must be adjusted. Additionally, the efficiency achieved in the economizer (EHX) for system with an additional compression stage (BB+IMS) is greater than the system without EC (BB+EHX), which occurs whenever the EC compressors are turned on.

5.5. COP

The COP of the facility can be obtained by using the Equation (11), which depends on the cooling loads and the total power consumption by the compressors. The latter is calculated with the Equation (12) as a function of the mass flow rate, the specific compression work, and the global effectiveness from Equation (10).

$$COP = \frac{Q_{OLT} + Q_{OMT}}{Pc_{LTc \ (VFD)} + Pc_{LTc} + Pc_{MTc \ (VFD)} + Pc_{MTc} + Pc_{EC \ (VFD)} + Pc_{EC}} \tag{11}$$

$$Pc_i = \frac{\dot{m}c_i \left(h_{out_i} - h_{in_i} \right)}{\eta_{global_i}} \tag{12}$$

The results from Equation (11) are presented in Figure 15, where the positive effect of the economizer is evident when it is installed in the refrigeration facility, especially when the EC compressor is used. Only when the ambient temperature is below 2.6 °C does the basic cycle achieve the best results in terms of COP. Additionally, Table 2 presents the variation of COP with regard to the base cycle.
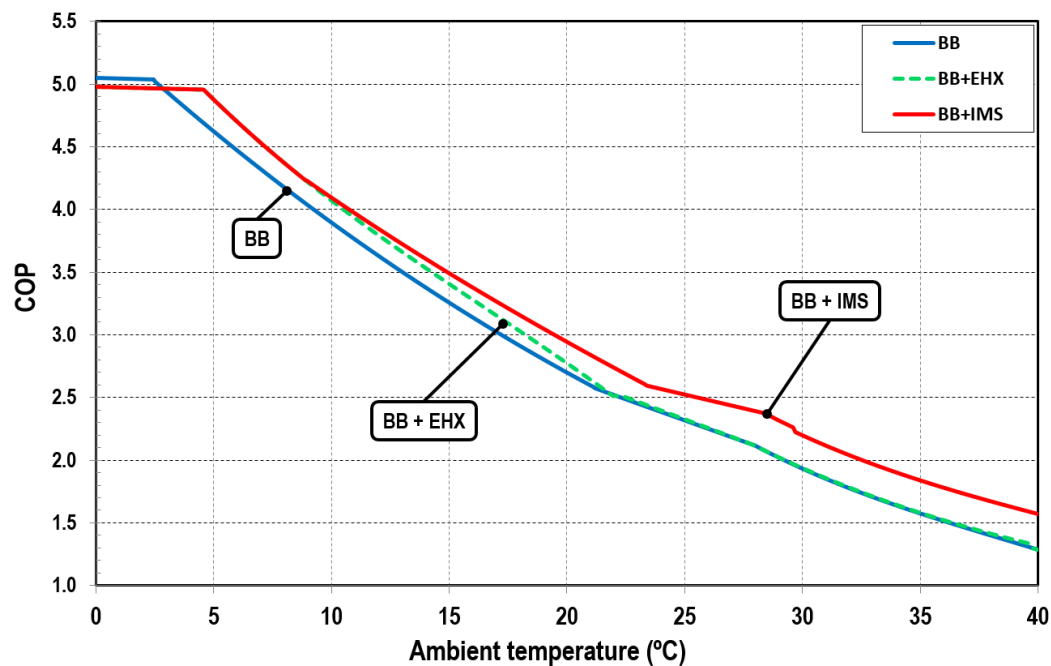
Figure 15. COP vs. ambient temperature.

Table 2. COP variation with regard to the basic cycle.

SYSTEM	Ambient Temperature (°C)								
	0	**5**	**10**	**15**	**20**	**25**	**30**	**35**	**40**
BB+EHX	−1.43%	5.47%	4.47%	4.53%	2.74%	0.31%	0.14%	0.19%	−0.2%
BB+IMS	−1.43%	5.47%	5.06%	7.14%	9.01%	8.77%	13.66%	16.63%	21.94%

Focusing on both improved systems, it is evident that the implementation of an additional compressor enhances the COP of the base system in a wide range of ambient temperatures (from 2.6 °C onwards). This makes this configuration very interesting in almost all European climates.

In order to maximize the COP of CO_2 booster systems operating in transcritical, different parameters can be modified depending on the booster configuration.

In this case, the heat rejection pressure is changed for the BB system as described in Figure 4. In the BB+EHX configuration, the pressure of the GC/K is also changed and depending on the mass flow rate through the EHX, certain subcooling is applied to the high-pressure mass flow (Figure 5). Finally, the BB+IMS adds another parameter, so that in addition to controlling the GC/K pressure, the EC suction pressure must be controlled as shown in Figure 6 and thus a certain subcooling after the GC/K is applied to the high-pressure mass flow.

In this case, depending on the chosen values of these parameters, the COP of the facility will change as experimentally analyzed by Nebot-Andrés et al. [30]. Figure 16 shows how the variation of these parameters affects the COP of the most complex system (BB+IMS) for two heat rejection temperatures (30 °C and 40 °C).
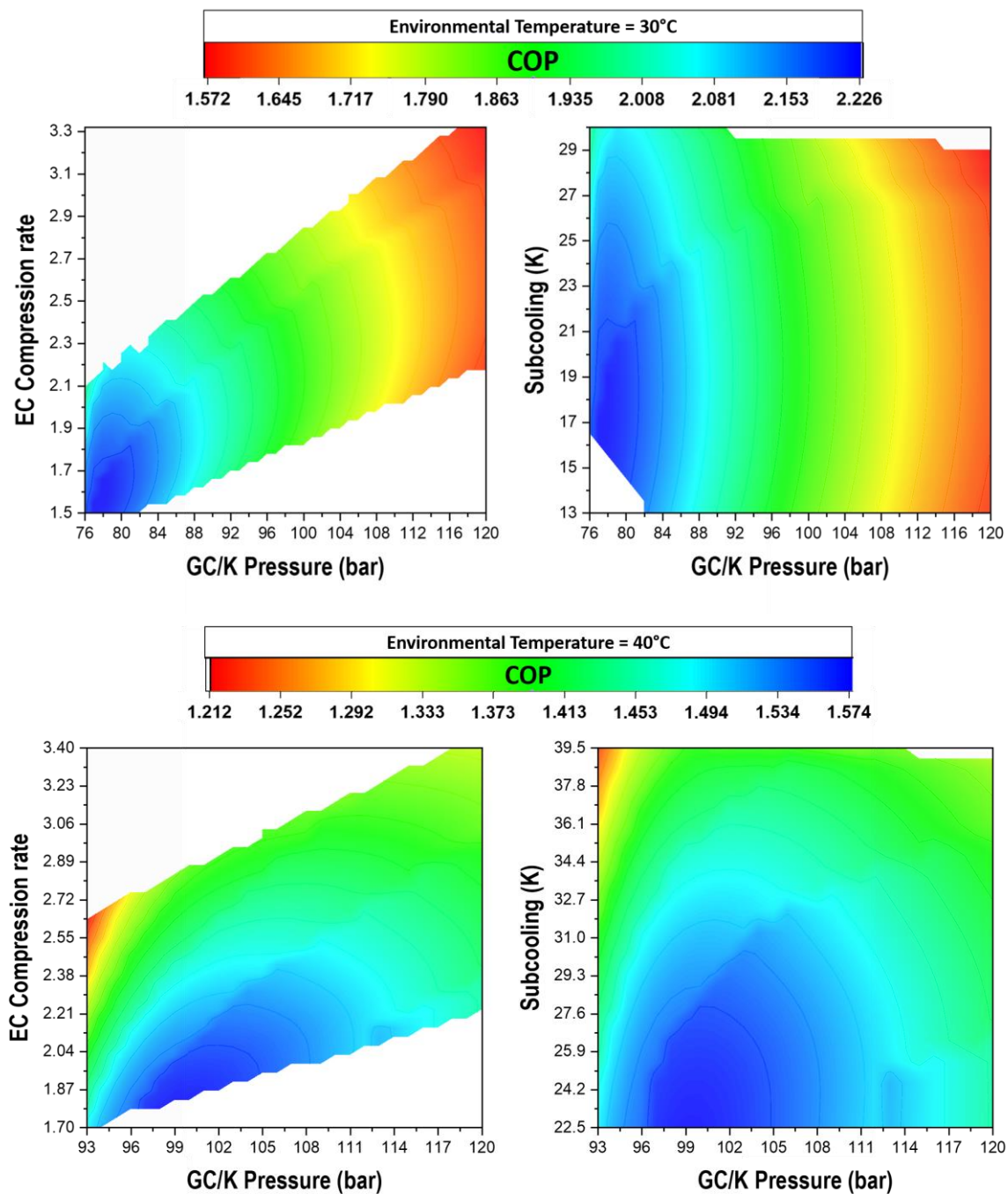
Figure 16. COP variation depending on GC/K pressure and EC compression ratio (left) or subcooling (right) for the BB+IMS.

As shown in the graphs that relate the EC compression rate with the GC/K pressure (EC suction pressure can be obtained), relating to the COP of the BB+IMS (Figure 16 left), the suction pressure control of the EC is an important term for maximizing the COP of the BB+IMS system.

The graphs on the left show the relationship between the EC compression rate, GC/K pressure, and COP, while the graphs on the right show the relationship between subcooling, GC/K pressure, and COP. For ambient temperature of 30 °C, the maximum COP (2.22) is achieved at the GC/K pressure of 77 bar, a subcooling of 17.5 K, and an EC compression rate of 1.54 (corresponds to 51.3 bar at EC suction port); nonetheless, for an ambient temperature of 40 °C, the maximum COP of 1.57 is achieved at the GC/K pressure of 100.1 bar, a subcooling of 22.5 K, and an EC compression rate of 1.82

(corresponds to 55 bar at the EC suction port). These results show that the compressors used in the EC rack must have the capacity to work at low compression rates and high suction pressures.

It has been calculated that for ambient temperatures below 23.4 °C, the optimum COP is achieved at an EC compression rate below 1.5 (minimum recommended by the manufacturer), and for rejection temperatures above 38.2 °C (Figure 11), the maximum COP is achieved at an EC suction pressure above 55 bar (maximum recommended by the manufacturer). Therefore, with compressors designed to operate efficiently at lower compression rates and higher suction pressures than the above operating limitations, the results for this system would be even better.

5.6. Annual Energy Consumption

To sum up the positive effect of the economizer, this section presents the annual energy consumption of the analyzed configurations in several European cities with different temperature profiles. A heat load factor (LF) of 100% from 7:00 to 22:00 and 50% from 22:00 to 7:00 is assumed for all the days of the year at optimum operating conditions. The average hourly temperature for each month was obtained with the EnergyPlus tool [44], excluding the effect of the relative humidity. The annual energy consumption (AEC) for each location is calculated using Equation (13) and depicted in Figure 17. Figure 18 presents the energy consumption reduction with regard to the basic booster system obtained by Equation (14). For a load factor of 50%, the cooling load is reduced, and thus the volumetric requirements of the compressors is reduced as well. This reduction changes the COP of the system due to the variation of the efficiency of the compressor with variable frequency drive and the influence on the total energy consumption, despite the load reduction.

$$AEC(\text{kWh}) = \sum_{m=1}^{12} \sum_{H=1}^{24} \frac{Qo_{LT} + Qo_{MT}}{COP_{m,H}} \cdot \frac{LF}{100} \cdot D_m \tag{13}$$

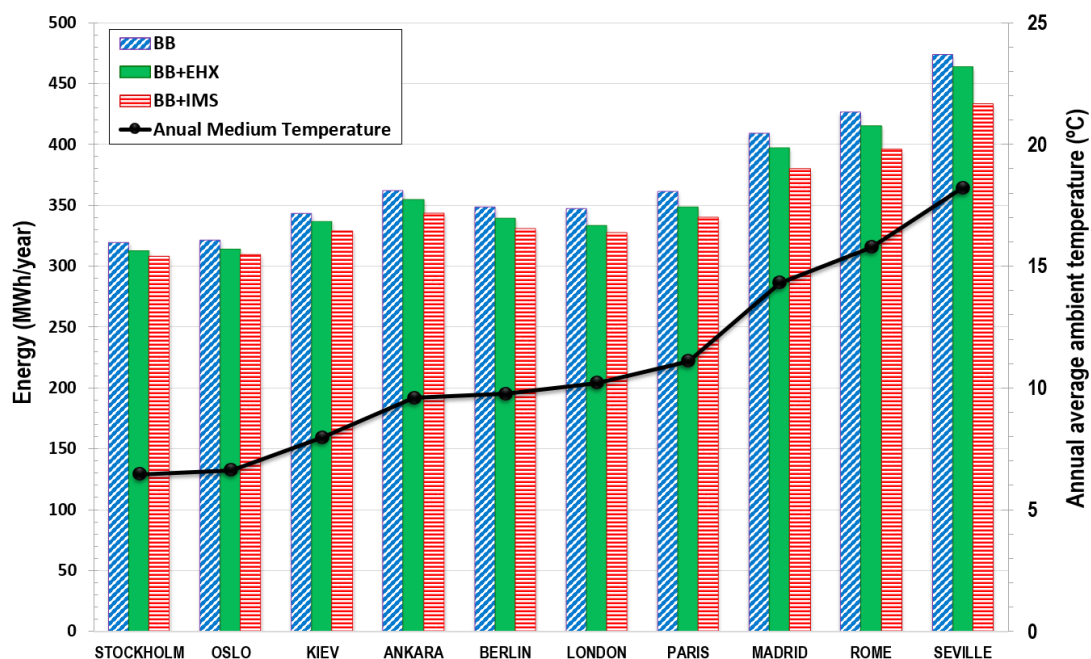$$\Delta E_i(\%) = \frac{E_i - E_{CC}}{E_{CC}} \cdot 100 \tag{14}$$

Figure 17. Annual energy consumption of the analyzed booster architectures.

Figure 18. Energy consumption reduction with regard to the basic booster system.

From Figures 17 and 18, it is evident that the use of the economizer always reduces the energy consumption of the refrigerating plant. However, this reduction depends on the configuration and the location. Thus, if the architecture implemented is that described in Figure 2 (BB+EHX), the savings made range between 1.95% and 4%. However, if the architecture installed contains the extra compressor described in Figure 3 (BB+IMS), the reductions vary from 3.6% to 8.5% at the same operating conditions.

To extend the analysis to more locations in Europe, a contour map of the energy consumption improvements of the systems regarding BB are presented in Figure 19, BB+EHX (left) and BB+IMS (right). The yellow dots represent the cities considered in Figure 19.

Figure 19. Annual energy benefit of the BB+EHX and BB+IMS in relation to BB in Europe (%).

In relation to the BB+EHX configuration, the system offers greater energy improvements for locations with cool temperatures as Northern France, Belgium, Netherlands, Ireland, or the United Kingdom. However, BB+IMS offers major energy improvements for all countries in Europe, but the best results are obtained for locations with higher ambient temperatures such as Spain, Italy, France, and Greece.

6. Conclusions

This work analyzes two subcooling systems to improve the efficiency of the CO_2 booster architectures. The analysis has been made for a medium-sized supermarket in different European cities with cooling loads of 41 kW and 140 kW for low and medium-temperature services, respectively. Real constraints in the operation of the systems have been taken into account as well as the performance data of the compressors provided by manufacturer, including the effect of the frequency variation in compressors.

Regarding the operating mode of the systems, the most important data are those of the basic booster with economizer and additional compression stage (BB+IMS), as the use of this additional compression stage (EC) is more beneficial for ambient temperatures above 8.9 °C regarding a basic booster with an economizer (BB+EHX).

The analysis of the compressors' sizing and their operation reveals, on the one hand, that the basic booster (BB) and BB+EHX similarly operate in the low-temperature compression rack (LTC) for all the rejection temperatures analyzed and for the medium-temperature compression rack (MTC). On the other hand, the BB+IMS system operates with two compressors at their nominal frequency and one with VFD in LTC with changes in frequency from 32 to 56.9 Hz depending on the rejection temperature. For MT_C, the great difference regarding the previous systems is that BB+IMS needs compressors with lower volumetric displacement. This reduction directly affects by lowering the power consumption of the compressors, and thus the efficiency of the facility increases. With respect to the additional compression stage of the BB+IMS, the system only uses the compressor with VFD at rejection temperatures from 8.9 to 29.5 °C (34.6 to 75 Hz), adding another compressor at its nominal frequency (50 Hz) for higher ambient temperatures.

With respect to the optimal pressure at the suction port for the EC stage, it changes from 33.1 to 55 bar to achieve the optimum COP at temperatures from 8.9 to 38.2 °C, limiting the maximum EC suction pressure to 55 bar for rejection temperatures above 38.2 °C.

The economized systems provide a degree of subcooling to the refrigerant after the GC/K. This subcooling is different depending on the system and the ambient temperature. The optimum subcooling for BB+EHX changes from 9 to 40 K for rejection temperatures from 0 to 40 °C. However, the introduction of an additional compression rack (BB+IMS) significantly reduces the optimum subcooling up to a maximum of 22.5 K and is more consistent over a wide range of temperatures.

Focusing on COP results, the higher improvement is obtained by the BB+IMS system in all ranges of ambient temperatures above 2.6 °C with a maximum improvement regarding a BB of 22%. Moreover, BB+EHX improves the COP with respect to BB for ambient temperatures from 2.6 to 21 °C up to 5.5%. The optimum COP points obtained in the BB+IMS are achieved at low compression rates in the additional compression stage (EC) for all the heat rejection temperatures analyzed and high suction pressures in the EC for high rejection temperatures.

Both improved systems provide a reduction in energy consumption in all the cities analyzed. BB+EHX reduce the annual energy consumption from 1.95% to 4%, offering greater energy improvements for locations with cool temperatures as Northern France, Belgium, Netherlands, Ireland, or the United Kingdom. However, the best results for all the countries in Europe have been obtained by the BB+IMS, which achieve reductions in energy from 3.5% to 8.5%, being more beneficial for cities with higher annual medium temperature such as Spain, Italy, France, and Greece.

It has been concluded that the BB+EHX system improves the COP of the basic one from 2.6 to 21 °C. Notwithstanding, the BB+IMS provides higher energy improvements for all ambient temperatures above 2.6 °C without adding a large complexity to the system.

Conflicts of Interest: The authors declare that no part of manuscript has been published previously and that it will not be published elsewhere including electronically in the same form, in English or in any other languages without the written consent of the copyright-holder. Publication is approved by authors and by responsible authorities where the work was carried out. Authors declare that there is non additional conflict of interest.

Nomenclature

AEC	annual energy consumption (kWh)
ATD	ambient temperature difference
BB	Basic Booster
CC	comparative cycle
COP	coefficient of performance
D	number of days
DSH	desuperheater
E	energy
EC	economizer compressor
ECO	economizer
EHX	economizer heat exchanger
ELEC	electric
FG	Flash gas
GC/K	gas cooler/condenser
H	number of hours
HFC	hydrofluorocarbon
HPS	high-pressure side
HPCV	high-pressure control valve
IMS	integrated mechanical subcooling
IHX	internal heat exchanger
K_{sub}	condenser subcooling (K)
LF	load factor
LT	low temperature
LPS	low-pressure side
LR	load ratio
$\dot{m}$	mass flow (kg·s-1)
M	number of months
MT	medium temperature
P	pressure (bar)
$\dot{Q}$	cooling load (kW)
SH	useful superheating (K)
SHC	superheat control
SUB	subcooling (K)
t	compression ratio
T	temperature (°C)
v	specific volume ($m^3 \cdot kg^{-1}$)
VFD	variable frequency drive
$\dot{V}_g$	compressor swept volume ($m^3 \cdot s^{-1}$)
$\dot{W}_{elec}$	power consumption (W)
Greek Symbols	
Δ	variation (increment or decrement)
ε	relative error (%)/thermal effectiveness
η_V	volumetric efficiency
η_G	global efficiency

Subscripts

amb	ambient
C	compressor
CO_2	carbon dioxide
EV	expansion valve
GC	gas cooler
in	inlet/in
K	condenser
LT	low temperature
m	month
max	maximum
MT	medium temperature
o	evaporator
out	out/outlet
opt	optimum
prev	previous
SUB	subcooling degree
sub_opt	optimum subcooling
V	valve

Appendix A Compressor coefficients

The coefficients used for modelling each compressor are detailed in this appendix. These data have been obtained from the real operating curves of the compressors in transcritical and subcritical operation.

Using these coefficients with Equations (9) and (10), we can obtain the global and volumetric efficiency of each compressor for the entire operating range.

COMPRESSORS — SUBCRITICAL OPERATION

MODEL BITZER 4JTC-15K — VG (m³/h): 9.21 — NOMENCLATURE EC — NUMBER OF COMPRESSORS 2

	CONSTANTS FOR ηV			
	3	2	1	0
Dd	0.154317	-5.14552	66.27658	508.5627
Dc	-0.04389	1.463619	-18.8521	-144.658
Db	0.001839	-0.06131	0.789737	6.059918
Da	-3.9E-05	0.001302	-0.01677	-0.12867
Cd	0.119499	-3.98457	51.32302	393.819
Cc	0.050164	-1.67267	21.54478	165.3204
Cb	-0.00268	0.089432	-1.15193	-8.83913
Ca	0.000236	-0.00788	0.101556	0.779277

	CONSTANTS FOR ηG			
	3	2	1	0
Dd	-16963.1	561474	-6498275	-9128614
Dc	600.5089	-19877.7	230084.9	322924.3
Db	-7.14769	236.6128	-2739.2	-3840.4
Da	0.028702	-0.95019	11.00189	15.40603
Cd	70760.94	-2341888	27096449	38141884
Cc	-2520.53	83424.04	-965390	-1357437
Cb	30.24837	-1001.23	11588.36	16273.51
Ca	-0.12289	4.067927	-47.092	-66.0341
Bd	-96696.6	3199771	-3.7E+07	-5.2E+07
Bc	3467.908	-114765	1327633	1871194
Bb	-42.0093	1390.355	-16087.5	-22638.4
Ba	0.173103	-5.72959	66.30998	93.16515
Ad	43239.59	-1430562	16538548	23417462
Ac	-1562.37	51694.86	-597770	-845067
Ab	19.12744	-632.952	7321.088	10329.51
Aa	-0.07987	2.643226	-30.5804	-43.0699

MODEL BITZER 6FTC-50K — VG (m³/h): 26.12 — NOMENCLATURE MTc — NUMBER OF COMPRESSORS 4

	CONSTANTS FOR ηV			
	3	2	1	0
Dd	-0.10974	10.37729	-379.063	-8248.84
Dc	0.00572	-0.54086	19.75644	429.9222
Db	-8.1E-05	0.007673	-0.28029	-6.09946
Da	-3.6E-07	3.44E-05	-0.00126	-0.02732
Cd	-0.04202	3.973008	-145.127	-3158.12
Cc	-0.00028	0.026151	-0.95524	-20.787
Cb	2.66E-05	-0.00251	0.091765	1.996914
Ca	8.68E-06	-0.00082	0.029965	0.652075

	CONSTANTS FOR ηG			
	3	2	1	0
Dd	-82.8692	7787.059	-256244	-1002283
Dc	3.870038	-363.672	11968.03	46784.31
Db	-0.06103	5.734783	-188.739	-737.362
Da	0.000326	-0.03067	1.009535	3.94222
Cd	373.927	-35134.1	1155903	4528283
Cc	-17.6623	1659.629	-54607.5	-213742
Cb	0.282842	-26.5783	874.6055	3420.506
Ca	-0.00155	0.145285	-4.78109	-18.6882
Bd	-543.428	51052.81	-1679035	-6595055
Bc	26.01441	-2444.13	80397.36	315372.9
Bb	-0.42471	39.9058	-1312.87	-5143.61
Ba	0.00239	-0.22457	7.387851	28.9462
Ad	252.3578	-23701.8	779026.5	3074031
Ac	-12.2637	1151.971	-37874.4	-149118
Ab	0.205096	-19.2677	633.6539	2489.585
Aa	-0.00119	0.111463	-3.66545	-14.4042

MODEL BITZER 2DSL-5K — VG (m³/h): 9.22 — NOMENCLATURE LTc — NUMBER OF COMPRESSORS 3

	CONSTANTS FOR ηV			
	3	2	1	0
Dd	-9.92198	290.221	-3210.58	-35420
Dc	0.842936	-23.6294	254.8379	3057.207
Db	-0.02394	0.629939	-6.48553	-85.0291
Da	0.000213	-0.00495	0.04531	0.682397
Cd	32.69335	-1039.16	11980.87	107193.4
Cc	-2.82929	88.48107	-1012.94	-9492.24
Cb	0.081514	-2.48298	28.00868	274.1534
Ca	-0.00067	0.018495	-0.19185	-1.74767

	CONSTANTS FOR ηG			
	3	2	1	0
Dd	-33.6329	1363.69	-16510.3	-27431
Dc	3.478327	-140.831	1703.534	2777.689
Db	-0.12094	4.889453	-59.0891	-94.543
Da	0.001425	-0.05749	0.693899	1.083527
Cd	154.1276	-6333.58	77162.42	148464.1
Cc	-16.4454	673.2255	-8186.03	-15193.9
Cb	0.589313	-24.0414	291.8064	524.6849
Ca	-0.00719	0.292132	-3.53834	-6.12976
Bd	-195.393	8195.849	-99570.6	-266566
Bc	22.412	-930.979	11291.28	27402.66
Bb	-0.85354	35.19162	-426.271	-955.79
Ba	0.011095	-0.4541	5.493327	11.3367
Ad	45.09291	-1945.22	20581.65	171463.8
Ac	-7.07303	295.516	-3307.59	-17405.2
Ab	0.323541	-13.3307	153.294	603.262
Aa	-0.00461	0.188427	-2.20169	-6.98557

Figure A1. *Cont.*

COMPRESSORS — TRANSCRITICAL OPERATION

MODEL BITZER 4JTC-15K — VG (m³/h): 9.21 — NOMENCLATURE EC — NUMBER OF COMPRESSORS 2

	CONSTANTS FOR η_V					CONSTANTS FOR η_G			
---	3	2	1	0	---	3	2	1	0
Dd	-26.6284	636.9889	-4674.82	15942.35	Dd	-184.018	6161.381	-71897.1	-115367
Dc	1.208065	-28.5814	203.9179	-841.863	Dc	6.99786	-234.569	2740.237	4472.621
Db	-0.01626	0.372143	-2.42565	15.88986	Db	-0.0892	2.996865	-35.0967	-58.9916
Da	4.2E-05	-0.00067	-0.00151	-0.15842	Da	0.000378	-0.01277	0.15063	0.268951
Cd	-1.31902	116.4402	-1964.33	-16218	Cd	1205.131	-40199.5	466845.8	685898.9
Cc	-0.73314	14.42215	-62.1413	1158.819	Cc	-46.728	1559.087	-18099.5	-26791.1
Cb	0.016235	-0.3288	1.455776	-27.3967	Cb	0.612419	-20.4486	237.4028	357.1413
Ca	0.000131	-0.00546	0.084772	0.853195	Ca	-0.00268	0.090005	-1.04956	-1.66838
					Bd	-2480.68	82498.89	-958011	-1344457
					Bc	98.19582	-3263.37	37832.71	52963.69
					Bb	-1.33141	44.19523	-510.804	-711.664
					Ba	0.006067	-0.20189	2.335535	3.422341
					Ad	1569.533	-52344.2	612803.6	870629.9
					Ac	-63.346	2108.146	-24628.6	-34876.3
					Ab	0.898045	-29.7461	344.796	470.8401
					Aa	-0.00397	0.131507	-1.51885	-2.13673

MODEL BITZER 6FTC-50K — VG (m³/h): 26.12 — NOMENCLATURE MTc — NUMBER OF COMPRESSORS 4

	CONSTANTS FOR η_V					CONSTANTS FOR η_G			
---	3	2	1	0	---	3	2	1	0
Dd	-0.08584	8.117429	-296.515	-6452.49	Dd	-2.41684	229.1071	-7554.56	-29436.1
Dc	0.004365	-0.41279	15.07854	328.1258	Dc	0.116816	-11.074	364.8771	1434.054
Db	-5.1E-05	0.00479	-0.17498	-3.80773	Db	-0.00191	0.18075	-5.95052	-23.6056
Da	-6.2E-07	5.82E-05	-0.00212	-0.04624	Da	1.05E-05	-0.001	0.032875	0.132538
Cd	-0.03473	3.283804	-119.951	-2610.27	Cd	17.5984	-1665.75	55030.62	206179.2
Cc	-0.00086	0.080937	-2.95649	-64.3365	Cc	-0.86604	81.95387	-2704.19	-10256.2
Cb	2.61E-05	-0.00247	0.090261	1.964181	Cb	0.014482	-1.37016	45.14283	173.4189
Ca	8.84E-06	-0.00084	0.030527	0.6643	Ca	-8.3E-05	0.007822	-0.25712	-1.00923
					Bd	-39.7559	3762.065	-124820	-445575
					Bc	1.99913	-189.081	6262.482	22778.49
					Bb	-0.03448	3.259463	-107.697	-398.965
					Ba	0.000205	-0.01935	0.636344	2.448808
					Ad	27.22254	-2578.75	86161.74	286182
					Ac	-1.40234	132.7692	-4427.39	-15206.5
					Ab	0.025198	-2.38298	79.18258	280.0777
					Aa	-0.00014	0.013522	-0.44653	-1.65474

Figure A1. Compressor coefficients.

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