Article

Improving Machine-Learning Diagnostics with Model-Based Data Augmentation Showcased for a Transformer Fault

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Abstract: Machine-learning diagnostic systems are widely used to detect abnormal conditions in electrical equipment. Training robust and accurate diagnostic systems is challenging because only small databases of abnormal-condition data are available. However, the performance of the diagnostic systems depends on the quantity and quality of the data. The training database can be augmented utilizing data augmentation techniques that generate synthetic data to improve diagnostic performance. However, existing data augmentation techniques are generic methods that do not include additional information in the synthetic data. In this paper, we develop a model-based data augmentation technique integrating computer-implementable electromechanical models. Synthetic normal- and abnormal-condition data are generated with an electromechanical model and a stochastic parameter value sampling method. The model-based data augmentation is showcased to detect an abnormal condition of a distribution transformer. First, the synthetic data are compared with the measurements to verify the synthetic data. Then, ML-based diagnostic systems are created using the model-based data augmentation and are compared with state-of-the-art diagnostic systems. It is shown that using the model-based data augmentation results in an improved accuracy compared to state-of-the-art diagnostic systems. This holds especially true when only a small abnormal-condition database is available.

Keywords: electrical power equipment; small sample size; data augmentation; diagnostics; fault detection; machine learning

1. Introduction

Grid operators are responsible for providing a safe and reliable energy grid. For this purpose, the electrical grid is reinforced to cope with the increasing integration of renewable energies. One approach of grid reinforcement is the installation of diagnostic systems to reduce the cost of preventive maintenance measures and personnel cost, as well as reducing downtimes of electrical equipment. Such diagnostic systems monitor electrical equipment in a continuous or event-driven manner to detect abnormal or fault conditions [1]. In recent years, more and more measurement technology has been installed in the electricity grid [2,3]. This leads to large normal-condition measurement databases and the sporadic measurement of abnormal conditions. The normal- and abnormal-condition measurements enable the use of supervised machine learning (ML) diagnostic systems. Such diagnostic systems have the potential to automatically learn complex relationships between the conditions of electrical equipment and measurements to classify normal and abnormal conditions. To train ML-based diagnostic systems, large databases are necessary [4–8], and the performance of the diagnostic system depends on the quantity and quality of the data [9–13]. Electrical equipment often has a small fault rate [14], leading to only small databases of abnormal conditions for the training of ML models. Therefore, the full
potential of ML-based diagnostic systems is not exploited. One approach to cope with this challenge is using data augmentation methods to augment the training data.

Data augmentation is already widely used for image classification. Images are rotated, cropped, or scaled to generate new images and augment the training data [8]. In signal analysis tasks, the signals are stretched or compressed, and noise is modulated onto the signals [15]. This signal processing has been shown to increase the performance of ML models but could also result in unrealistic signals. Synthetic data can also be generated using generative models, e.g., based on deep learning methods. These generative models offer the advantage of learning complex and multidimensional distribution functions of features and using this knowledge to generate high-quality synthetic data. They have been proven to increase the performance of ML models in the medical sector [8,10,16] and the diagnostic of mechanical equipment [15] and electrical equipment [7] or electrical grids [17]. Generative Adversarial Networks (GANs) are often used as generative models. GANs consist of two multilayer perceptrons (MLPs). The first MLP is trained to classify data whether they are ‘synthetic data’ or ‘measurements’. The second MLP is trained to generate synthetic data and maximize the probability of misclassification of the first MLP. The training is carried out in an iterative manner [18]. Some implementations of GANs also work for tabular data [19–22]. The training of GANs is hard as the required time for training can be very long and the training can be unstable, depending on the optimization algorithm. Another generative model, Restricted-Boltzmann machines, can also be included in deep belief networks. This model resulted in higher accuracy for the detection of faults in transmission lines compared to state-of-the-art approaches [23]. Restricted-Boltzmann machines can be hard to train as it is difficult to calculate the energy gradient function.

However, the existing data augmentation techniques are generic techniques and do not add information about the subsequent diagnostic task to the generated, synthetic data. Such information could be provided by computer-implementable, electromechanical models. The electromechanical models contain information about the functional relationship between the measurement variables and the electrical equipment. Integrating such electromechanical models in data augmentation could improve ML-based diagnostic systems further. Improved diagnostic systems could further reduce maintenance effort, reduce the number of trips and inspections of maintenance personnel due to false alarms, and decrease downtimes of electrical equipment. This could potentially lead to savings for the grid operator.

In this paper, we develop a model-based data augmentation using electromechanical models. The aim of the model-based data augmentation is to generate synthetic data and to increase the performance of ML-based diagnostic systems. The model-based data augmentation is showcased for the diagnostic task of detecting an abnormal condition of a secondary distribution transformer. Measurements such as top tank vibration, voltage, and current measurements from the low-voltage side are available for analysis. In the first step of the analysis, the synthetic data generated by the model-based data augmentation are compared to measurements. In the second step, ML-based diagnostic systems are created using model-based data augmentation and are compared with state-of-the-art diagnostic systems.

2. Generation of Synthetic Data and Data Augmentation

Electromechanical models of electrical equipment generate synthetic data. For the variation of the model output to correspond to that of measurements, all variables influencing the model’s output would have to be considered in the electromechanical model. However, electromechanical models typically represent a simplification of the cause–effect relationships so that the variation of the model output does not correspond to that of the measurements. Considering this variation is essential to generate appropriate synthetic normal- and abnormal-condition data. Therefore, the presented model-based data augmentation uses a stochastic approach to sample parameter values of the electromechanical
model [24,25]. The variation of measurements can thus be mapped appropriately. The generated synthetic data can then be integrated into the training process of ML models.

2.1. Model-Based Data Augmentation

The model-based data augmentation consists of three key parts and uses available normal-condition measurements as input [25]:

- An algorithm to parametrize the electrical model. The algorithm fits the model’s parameter to subsets of the available normal-condition measurements. This results in a parameter set of the electromechanical model for each measurement subset and thus a parameter database.
- An algorithm to sample combinations of parameter values from the previously identified parameter database to simulate normal and abnormal conditions.
- An electromechanical model to include additional information about the cause–effect relationships of the electrical equipment.

The electromechanical model is parametrized with the sampled parameter values and is simulated to generate synthetic data.

2.1.1. Establishing the Parameter Database and Generating Synthetic Normal-Condition Data

Input and parameter values are necessary for the simulation of an electromechanical model. Both are sampled with a stochastic approach. The process is shown in Figure 1. In the first step, the probability distributions of the input values are identified from the available normal-condition measurements. In the second step, the normal-condition measurements are divided into subsets. For each subset, the electromechanical model is fitted to the subset to find the optimal parameter values of the parameters of the electromechanical model. This results in parameter value sets \( S_1, \ldots, S_q \). Each parameter value set contains parameter values \( P_1, \ldots, P_m \). These parameter value sets are used to identify a multivariate Gaussian distribution considering the correlation between parameters [25].

For the generation of synthetic normal-condition data, parameter values and input values are sampled from the corresponding and previously identified probability distributions. The electromechanical model is parametrized with these values and simulated. This results in synthetic normal-condition data with input and corresponding output data. This process is repeated until the desired number of normal-condition data is available.

2.1.2. Generating Synthetic Abnormal-Condition Data

For the generation of synthetic abnormal-condition data, parameter values of the electromechanical model are manipulated. Which parameters \( P_{abnormal} \) are used for this should be selected by domain experts so that the manipulation results in realistic abnormal-condition types. It is not possible to derive the statistically meaningful parameter distributions from measurements as it is often the case that only small databases of abnormal-condition measurements are available. Therefore, the idea behind the abnormal-condition generation is sampling parameter values of the electromechanical model outside the main area of the normal condition’s probability distribution. In this paper, Gaussian distributions are fitted to the parameter values from the database of parameter values (Section 2.1.1) for each \( P_{abnormal} \) to represent parameter values for normal conditions. Each Gaussian distribution has a mean value \( \mu_{nc} \) and standard deviation \( \sigma \). To sample parameters outside the main area of these Gaussian distributions, new uniform probability distributions are introduced, representing parameter values for abnormal conditions. In this work, these uniform probability distributions start at \( \mu_{nc} + 5 \sigma \) and end at \( \mu_{nc} + 25 \sigma \). This is illustrated in Figure 2 for different starting points of the probability distribution. Only increasing parameter values are considered because abnormal conditions of transformers lead to an increase of the vibration amplitude [25].
parameter values are considered because abnormal conditions of transformers lead to an increase of the vibration amplitude [25]. For the generation of synthetic abnormal-condition data, parameter values and input values are sampled from the multivariate Gaussian distribution from Section 2.1.1, except for one of the parameters out of $P_{abnormal}$. The value of this parameter is sampled from the introduced uniform probability distribution. The model is parameterized and simulated with the sampled parameter and input values. This results in a data set containing input data and output data representing an abnormal condition. This process can be repeated as often as needed to generate an arbitrary number of synthetic abnormal-condition data.

Figure 1. Illustration of generating the database of parameter values and generating synthetic normal-condition data.

For the generation of synthetic abnormal-condition data, parameter values and input values are sampled from the multivariate Gaussian distribution from Section 2.1.1, except for one of the parameters out of $P_{abnormal}$. The value of this parameter is sampled from the introduced uniform probability distribution. The model is parameterized and simulated with the sampled parameter and input values. This results in a data set containing input data and output data representing an abnormal condition. This process can be repeated as often as needed to generate an arbitrary number of synthetic abnormal-condition data.
2.1.3. Electromechanical Model to Simulate Transformer Vibration

The diagnostic task under investigation utilizes vibration, current, and voltage measurements. Thus, an electromechanical model putting these measurement variables into relation is used for the model-based data augmentation. A base model [26] is modified to consider the individual voltage-dependent magnetostrictions and individual current-dependent electrodynamic forces of the three phases of a distribution transformer. The model calculates the 100 Hz vibration component $A_{100Hz}$ as a function of the individual effective mean voltages $\sigma$ and the individual effective mean currents $i$ across and through phases 1, 2, and 3; see Equation (1). The parameters $a_1$, $a_2$, and $a_3$ and $\beta_1$, $\beta_2$, and $\beta_3$ serve as proportionality factors between vibration and current or voltage as well as damping factors along the propagation path [26].

$$A_{100Hz} = a_1 \cdot i_1^2 + a_2 \cdot i_2^2 + a_3 \cdot i_3^2 + \beta_1 \cdot v_1^2 + \beta_2 \cdot v_2^2 + \beta_3 \cdot v_3^2$$  

(1)

The electromechanical model is fitted to measurements to identify values for the parameters $a_1$, $a_2$, and $a_3$ and $\beta_1$, $\beta_2$, and $\beta_3$ using a least-squares method.

Faults such as mechanical deformation or loosening of the winding or core, insulation degradation of the winding [27,28], and highly unsymmetrical load can lead to an increased vibration amplitude.

2.2. Integration of Synthetic Data into the Training Process

The synthetic data generated by the model-based data augmentation can be integrated into the training process of ML models using two approaches. The first approach augments the training data with the synthetic data. These augmented training data are used for the training of MLPs. The second approach uses synthetic data as a source domain to train MLPs. These models are then retrained with measurements utilizing transfer learning methods.

2.2.1. Augmenting the Training Data

The un-augmented training data consists of normal- and abnormal-condition measurements. Therefore, the model-based data augmentation can be used to generate and augment normal and abnormal conditions or to only augment abnormal conditions [29]. Both methods are analyzed in this work.

Figure 3 illustrates how synthetic data are generated and the constellation of the training data when they are augmented with the synthetic normal- and abnormal-condition data. $n_{DA,nc}$ synthetic normal-condition data and $n_{DA,nc}$ synthetic abnormal-condition data are generated using $n_{M,nc}$ normal-condition measurements utilizing model-based data.
augmentation. The ratio $c_{DA}$ between the number of synthetic data and measurements can be adjusted with Equations (2) and (3). The MLP is trained with the union of the synthetic normal- and abnormal-condition data and the measurements. Such diagnostic systems are denoted by MDA-NC-AC (for model-based data augmentation: normal condition and abnormal condition).

\begin{align*}
    n_{DA,nc} &= n_{M,nc} \times c_{DA} \quad (2) \\
    n_{DA,ac} &= n_{M,ac} \times c_{DA} \quad (3)
\end{align*}

![Diagram](image)

**Figure 3.** Generation of synthetic data and constellation of the training data when synthetic normal- and abnormal-condition data are used to augment the training data [29].

Figure 4 illustrates how synthetic data are generated and the constellation of the training data when it is augmented using only synthetic abnormal-condition data. $n_{DA,ac}$ synthetic abnormal-condition data are generated using $n_{M,nc}$ normal-condition measurements utilizing the model-based data augmentation. The union of the synthetic abnormal-condition data and measurements form the training data. The class balance of the training data can be adjusted to a desired class balance $b$ by limiting the number of synthetic abnormal-condition data added to the training data; see Equation (4). Such diagnostic systems are denoted by MDA-AC (for model-based data augmentation: abnormal condition).

\begin{equation}
    n_{DA,ac} = n_{M,nc} / b - n_{M,ac} \quad (4)
\end{equation}

![Diagram](image)

**Figure 4.** Generation of synthetic data and constellation of the training data when only synthetic abnormal-condition data are used to augment the training data [29].

2.2.2. Generating a Source Domain for Transfer Learning

Transfer learning is normally used to transfer already existing ML models trained on huge databases (source domain) to other tasks or domains. However, such ML models are not available for the diagnostics of electrical equipment. Therefore, a source domain is created with synthetic data generated by the model-based data augmentation using the available normal-condition measurements. The source domain contains synthetic normal- and abnormal condition data. MLPs are trained with this source domain and learn the cause–effect relationships and information provided by the synthetic data during the training process. These MLPs are then transferred to the available normal- and
abnormal-condition measurements using transfer learning methods. Retraining the MLPs with measurements offers the potential to reduce the impact of inaccuracies of the electromechanical model or the simulation on the diagnostic system. Generally, knowledge learned in the first training process is preserved in the MLP. The process is shown in Figure 5. Two methods of transfer learning are considered in this paper: fine-tuning (FT) and feature extraction (FE) [30].

![Figure 5](image-url)

**Figure 5.** Training of MLPs with synthetic data and transferring MLPs to measurements using transfer learning [30].

The first layers of an MLP mostly represent general knowledge, while the back layers contain specific knowledge [31,32]. The last layers perform the classification into different classes and do not contain or contain only very little information about the features. The structure of the classification part can be one fully connected layer or multiple layers.

The idea behind fine-tuning is that the structure and knowledge of already trained MLPs are useful for a new domain when adapted. Therefore, this MLP is used as a base model. This model is transferred to the new domain, in the case of this paper to measurements, by retraining the output layer with the measurements (fine-tuning) [31,32]. The parameters of the other layers are frozen during this training process (fine-tuning) [31,32]. Such diagnostic systems are denoted by *MDA-FT*.

![Figure 6](image-url)

**Figure 6.** Transfer learning using fine-tuning [30,31].

The second transfer learning method utilized in this paper is feature extraction. The classic use case of feature extraction is transferring an MLP to a new task. This is completed by reusing the part of the MLP where information about features is stored and changing the part of the MLP responsible for the classification, as shown in Figure 7. The part responsible for the classification is removed from the MLP, and a new classification structure is added. The added structure is retrained with new data while the parameters of the rest of the MLP remain unchanged [31,32]. Such diagnostic systems are denoted by *MDA-FE*. 

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[30] Fine tune

[31] Fine tune

[32] Fine tune
In this paper, diagnostic systems utilizing feature extraction are trained with synthetic data and the diagnostic task to classify between normal condition, abnormal condition 1, abnormal condition 2, etc. This MLP is then transferred to measurements with a binary diagnostic task—normal condition or abnormal condition.

3. MLP Structure and Benchmark Diagnostic Systems

To test whether the model-based data augmentation improves the performance of diagnostic systems, diagnostic systems created utilizing the model-based data augmentation are benchmarked with state-of-the-art diagnostic systems. The state-of-the-art diagnostic systems include a model-based diagnostic system, a diagnostic system based on kernel density estimation, an MLP classifier, and an MLP classifier combined with state-of-the-art data augmentation. All MLPs have the same structure.

3.1. Structure of the Multilayer Perceptrons

All diagnostic systems utilizing MLPs use MLPs with identical structures and hyperparameters to achieve comparability between the systems. The chosen structure and hyperparameters do not claim to be the optimal choice for the given diagnostic task.

The MLPs are implemented with $l$ layers. Each hidden layer has $n$ nodes. The input layer has seven nodes, one for each normalized feature (100 Hz amplitude of the vibration signal, current phase 1, 2, 3, and voltage phase 1, 2, 3). The output layer contains one node for the binary classification task of normal condition or abnormal condition. The number of nodes in the last layer is equal to the number of synthetic abnormal-condition fault types only in the case of the pre-training of MLPs utilizing feature extraction. The activation functions are randomized leaky rectified linear units [33]. The parameters of the MLPs are optimized with an Adam optimization function [34], and the MLPs are implemented and trained utilizing PyTorch [35].

3.2. Model-Based Diagnostic System

Model-based diagnostic systems are widely used as they do not require abnormal-condition measurements [36–41]. They use an electromechanical model or an ML model as a predictor for a variable in normal conditions. If a measurement with input data should be analyzed for an abnormal condition, the residuum between the predictor for the given input data and the actual measurement is calculated. If the residuum exceeds a threshold predefined by an expert, an abnormal condition is assumed.

In this paper, a parametrized vibration model from Section 2.1.3 is used as the predictor for the normal condition. The threshold is set to the threshold that maximizes the diagnostic accuracy for the available measurements to simulate a domain expert setting the optimal threshold. The diagnostic system is illustrated in Figure 8, where $\theta$ denotes the vibration amplitude of the 100 Hz component, $R$ is the residuum, $v$ is the voltage, $i$ is the current, and $\alpha$ and $\beta$ are the parameters of the vibration model. This diagnostic system is denoted by $\text{Res}$. 

![Figure 7. Transfer learning using feature extraction [30,31].](image-url)
The transformer is a 20° kV/630 kVA transformer with an on-load tap changer on the low-voltage side. The transformer is equipped with sensors to measure the current through and the voltage across each phase on the low-voltage side and a vibration sensor positioned at the tank. The 100 Hz amplitude is extracted from the vibration measurements. The sensors take hourly measurements. In total, measurements of approximately 13 months are available. The absolute load of the transformer for the period under review is shown in Figure 9. At the beginning of the measurement campaign, the transformer operates in an abnormal condition.
for approximately 42 days as the on-load tab changer is faulty due to a bad surge arrester in the auxiliary circuit. The transformer is then switched off, the surge arrester is replaced, and the transformer switched on again after 119 more days. Since then, the transformer has operated in normal condition. The measurement campaign resulted in 5614 labeled normal-condition measurements and 1009 labeled abnormal-condition measurements.

Figure 9. Absolute load of the transformer.

The faulty on-load tap changer leads to an unsymmetrical voltage output of the transformer and increased vibration. Figure 10 shows one of the malfunctioning parameters during the fault: the unsymmetrical voltage. The figure displays the transformer voltage of phase L1, phase L2, and phase L2 for the period under review. During the fault, the voltage of phases L1, L2, and L3 are not symmetrical and have a mean voltage of 233.2 V (L1-N), 230.8 V (L2-N), and 227.8 V (L3-N), respectively. After the repair, the phase imbalance is drastically reduced. The mean voltage is 230.8 V (L1-N), 231.3 V (L2-N), and 231.9 V (L3-N), respectively.

Figure 10. Voltage of the transformer for the period under review.

The difference in the vibration amplitude of the normal-condition measurements (meas. NC) and the abnormal-condition measurements (meas. AC) can be seen in the box plots in Figure 11. The abnormal condition results in higher vibration amplitudes. The distribution of the abnormal-condition measurements has a median of 0.024 m/s² and reaches amplitudes up to 0.046 m/s², whereas the distribution of the normal-condition measurements has a median of 0.014 m/s², and the maximum occurring value is 0.019 m/s².
4.1. Analysis of Synthetic Normal-Condition Data Generated by the Model-based Data Augmentation

Synthetic data are generated with the model-based data augmentation using all 5614 normal-condition measurements as input data. The results in this section form the foundation of the results shown in Section 4.2 and are also discussed in [25].

4.1.1. Synthetic Normal-Condition Data

A total of 10,000 synthetic normal-condition data are generated utilizing the model-based data augmentation. The distribution of the resulting synthetic 100 Hz amplitude (synth. NC) and the normal-condition measurements (meas. NC) is shown as box plots in Figure 12. The synthetic data’s mean deviates $-1.19\%$ from the measurements. The 25%- and 75%-quantile deviates by $-8.59\%$ and $5.93\%$ only. This shows that the model-based data augmentation is capable of generating realistic, synthetic, normal-condition data.

Figure 11. Box plots of the normal- and fault-condition measurements.

The recorded measurements are used to analyze the model-based data augmentation. First, the synthetic data generated by the model-based data augmentation are compared with the measurements. Then, diagnostic systems utilizing the model-based data augmentation are benchmarked with state-of-the-art diagnostic systems.

4.1.2. Synthetic Abnormal-Condition Data

Synthetic abnormal-condition data are sequentially generated by using the parameters of the electromechanical model $\alpha_1$, $\alpha_2$, and $\alpha_3$ and $\beta_1$, $\beta_2$, and $\beta_3$ as parameters to simulate abnormal conditions. For each of these parameters, 10,000 synthetic abnormal-condition data are generated. The distribution of the synthetic data (synth. NC and Synth. AC) and the measurements, including the 1009 abnormal-condition measurements (meas. AC), are shown in Figure 13a. Table 1 shows the percental deviation of characteristic box plot values from the corresponding values of the abnormal-condition measurement. The deviation of the median of the abnormal-condition measurement from the normal-condition measurements is 65.70%. The whiskers of the synthetic abnormal-condition data show a deviation

Figure 12. Box plots of the synthetic normal-condition data and normal-condition measurements [25].
from the median of the abnormal-condition measurements of up to 6475.00%. Even negative vibration amplitudes are generated. With smaller start points and endpoints of the introduced abnormal distribution, realistic abnormal condition data cannot be generated with $\beta_1$, $\beta_2$, and $\beta_3$. This is an indicator that for a realistic abnormal condition simulation with $\beta$, the correlation between the parameters needs to be considered. Figure 13b shows the distribution of the data without the synthetic abnormal-condition data generated with $\beta_1$, $\beta_2$, and $\beta_3$. The synthetic data generated with $\alpha_1$, $\alpha_2$, and $\alpha_3$ show a distribution similar to the abnormal-condition measurements but is shifted to smaller vibration amplitudes. The median of the synthetic abnormal-condition data deviates from the median of the abnormal-condition measurements by a maximum of $-23.82\%$. The 25% quantile only deviates by up to $-17.44\%$ from the 25% quantile of the measurements. The results show that the model-based data augmentation generates realistic synthetic data for independent parameters when properly parametrized.

![Graphs showing distribution of measurements and synthetic data](image)

**Figure 13.** (a) Distribution of the measurements and synthetic data. (b) Distribution of the measurements and synthetic data except synthetic abnormal-condition data created with $\beta_1$, $\beta_2$, and $\beta_3$ [25].

**Table 1.** Percentage deviation of characteristic values of the box plots from the corresponding box plot values of the abnormal-condition measurements [25].

<table>
<thead>
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<th>Data</th>
<th>Median</th>
<th>25% Quantil</th>
<th>75% Quantil</th>
<th>Upper Whisker</th>
<th>Lower Whisker</th>
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<td>$-37.96%$</td>
<td>$-51.24%$</td>
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<td>$5737.78%$</td>
<td>$2600.50%$</td>
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4.2. Analysis of the Diagnostic Performance of MLPs Created with Model-Based Data Augmentation

Data augmentation methods are often applied when only limited databases are available. Therefore, the model-based data augmentation is analyzed by limiting and successively increasing the number of abnormal-condition measurements in the training data; the number of normal-condition measurements is kept constant. This limitation is carried out to simulate how the ML models would perform if only small abnormal-condition databases were available. Diagnostic systems are created with the limited training data and then tested with test data. The test data contains 80% of the available measurements. Each diagnostic system is trained multiple times for each number of abnormal-condition measurements in the training data with a different constellation of abnormal-condition measurements. The performance on the test data is averaged for each number of abnormal-condition measurements in the training data—similar to cross-validation. The process is illustrated for four abnormal-condition measurements in the training data in Figure 14.

![Figure 14](image.png)

**Figure 14.** Illustration of the testing process for 4 abnormal-condition measurements in the training data.

By successively increasing the number of abnormal-condition measurements in the training data, learning curves can be generated for each diagnostic system. Learning curves plot the performance of a diagnostic system against the number of abnormal-condition measurements in the training data. During the data-limitation process, the class balance between the number of normal-condition measurements and abnormal-condition measurements is kept constant to change only one influence on the performance, the number of abnormal conditions in the training data, at once. The MDA-AC and GAN-AC diagnostic systems allow adding synthetic abnormal-condition data until a pre-defined class balance is met. For the rest of the diagnostic systems, a constant class balance is realized by upsampling the abnormal-condition measurements to a pre-defined value. Upsampling adds data duplicates without adding new information in the form of unseen data to the training data.
The performance of the diagnostic systems is evaluated using accuracy; see Equation (5). TP are true positive, TN are true negative, FP are false positive, and FN are false negative diagnoses.

\[
\text{accuracy} = \frac{TP + TN}{TP + FP + TN + FN} \tag{5}
\]

Section 4.1.2 shows that the model-based data augmentation does not simulate abnormal conditions with the parameters $\beta_1$, $\beta_2$, and $\beta_3$ properly. Therefore, synthetic abnormal-condition data are simulated with the parameters $\alpha_1$, $\alpha_2$, and $\alpha_3$ in the following. When an abnormal condition is simulated with one of these parameters, the other parameters are sampled from the normal-condition distribution.

4.2.1. Learning Curves of Diagnostic Systems Created with the Model-Based Data Augmentation and State-of-the-Art Diagnostic Systems

In the first step of the analysis, the MLPs of the diagnostic systems have $l = 5$ layers, and each hidden layer has $n = 200$ neurons. Figure 15 shows the learning curves of the state-of-the-art diagnostic systems. The diagnostic systems Res and KD have a constant accuracy (96.6% and 95.0%), as abnormal-condition measurements are not required to create these systems. The accuracy of the MLP-based diagnostic systems MLP-Std and GAN-AC is greater than the Res and KD diagnostic systems when only three and four abnormal-condition measurements are in the training data. The GAN-NC-AC diagnostic systems are inferior to the MLP-Std and GAN-AC diagnostic systems. The GAN-AC diagnostic systems are superior to the MLP-Std systems for <25 abnormal-condition measurements in the training data. The MLP-Std and GAN-AC systems converge for a similar accuracy.

![Figure 15. Learning curves of the state-of-the-art diagnostic systems [30].](image)

Figure 16 shows the learning curves of the diagnostic systems created with the model-based data augmentation using the approaches presented in Section 2.2 and the learning curve of the state-of-the-art diagnostic systems. The state-of-the-art diagnostic systems are represented by the maximal envelope curve of the diagnostic systems from Figure 15 (SoA systems). For the analysis, $c_{DA}$ is set to $c_{DA} = 0.5$. 

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The results show that the MDA-NC-AC and MDA-FE diagnostic systems are inferior to the MDA-FT, MDA-AC, and SoA Systems as they have a smaller accuracy for the considered numbers of abnormal-condition measurements. The MDA-FT and MDA-AC diagnostic systems achieve higher diagnostic accuracies than the SoA Systems. The MDA-AC diagnostic systems improve the accuracy, especially for small numbers of abnormal-condition measurements in the training data. The MDA-FT diagnostic systems have, for ≤8 abnormal-condition measurements in the training data, worse accuracy than the MDA-AC diagnostic systems. For >8 abnormal-condition measurements in the training data, the accuracy of the MDA-FT diagnostic systems is, on average, 0.06% greater than the accuracy of the MDA-AC systems.

The results indicate that the model-based data augmentation improves the accuracy of diagnostic systems compared with state-of-the-art diagnostic systems when MDA-FT or MDA-AC systems are used. These diagnostic systems are further analyzed.

4.2.2. Influence of the Number of Layers on Accuracy

In this section, it is analyzed how diagnostic systems utilizing the model-based data augmentation perform compared with state-of-the-art systems for varying numbers of layers. A similar analysis as in Section 4.2.1 is conducted, but the MDA-FT, MDA-AC, and state-of-the-art diagnostic systems are trained with a number of layers varied from \( l = 3 \) layers to \( l = 7 \) layers in steps of 1. The number of neurons per hidden layer is \( h_l = 200 \).

Figure 17 shows the difference in accuracy between MDA-FT and MDA-AC diagnostic systems and SoA Systems with the corresponding number of layers as a function of the number of abnormal-condition measurements in the training data and the number of layers. Table 2 lists the averaged accuracy difference between the listed diagnostic systems and the SoA Systems for the analyzed number of layers. The results show that the MDA-AC and MDA-FT diagnostic systems achieve greater accuracy than the SoA Systems for all analyzed number of layers, except the MDA-FT system with \( l = 6 \) layers. The accuracy of the MDA-FT system with \( l = 6 \) layers for ≤17 abnormal-condition measurements in the training data is 0.36% smaller on average than the accuracy of the SoA Systems. For ≥17 abnormal-condition measurements in the training data, the MDA-FT system with \( l = 6 \) layers improves the diagnostic performance by 0.11% on average. The accuracy of the MDA-AC diagnostic systems is, especially for ≤14 abnormal-condition measurements in the training data, larger than the SoA Systems, on average 0.61%. For >14 abnormal-condition measurements in the training data, the accuracy difference compared to the SoA Systems is 0.10% on average. The MDA-FT diagnostic systems outperform the MDA-AC
diagnostic systems for >14 abnormal-condition measurements with an accuracy difference compared to the SoA Systems of 0.11%.

![Figure 17. Differences in accuracy between the MDA-FT, MDA-AC, and the SoA Systems.](image)

**Table 2.** Averaged difference in accuracy between the MDA-FT, MDA-AC, and the SoA Systems.

<table>
<thead>
<tr>
<th>Diagnostic System</th>
<th>( l = 3 )</th>
<th>( l = 4 )</th>
<th>( l = 5 )</th>
<th>( l = 6 )</th>
<th>( l = 7 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>MDA-FT</td>
<td>0.15</td>
<td>0.14</td>
<td>0.19</td>
<td>-0.02</td>
<td>0.11</td>
</tr>
<tr>
<td>MDA-AC</td>
<td>0.12</td>
<td>0.14</td>
<td>0.17</td>
<td>0.17</td>
<td>0.17</td>
</tr>
</tbody>
</table>

The results show that the model-based data augmentation combined with MDA-FT and MDA-AC generally improves the accuracy compared to state-of-the-art diagnostic systems for the analyzed number of layers. An improvement of 0.61% results in 53 less misclassifications per year per equipment for hourly measurements. Thus the improvement has a great impact on number of triggered equipment inspections of the equipment owner.

4.2.3. Influence of the Number of Neurons Per Hidden Layer on the Accuracy

In this section, it is analyzed how the diagnostic systems utilizing the model-based data augmentation perform compared with the state-of-the-art systems for varying the numbers of neurons per hidden layer. A similar analysis as in Section 4.2.1 is conducted, but the MDA-FT, MDA-AC, and state-of-the-art diagnostic systems are trained with a number of neurons per hidden layer varied from \( n = 50 \) neurons to \( n = 300 \) neurons in steps of 25. The number of layers is \( l = 5 \).

Figure 18 shows the difference in accuracy between MDA-FT, MDA-AC diagnostic systems, and SoA Systems with the corresponding number of neurons per hidden layer as a function of the number of abnormal-condition measurements in the training data and the number of neurons per hidden layer. Table 3 lists the averaged accuracy difference between the listed diagnostic systems and the SoA Systems for the analyzed number of neurons per hidden layer. The accuracy of the MDA-AC and MDA-FT diagnostic systems are 0.15% and 0.13% higher on average than the SoA Systems, respectively. Only the MDA-FT diagnostic systems with \( n = 250 \) neurons result in a smaller averaged accuracy than the SoA Systems with a difference of -0.01%. For <17 abnormal-condition measurements in the training...
data, the MDA-AC diagnostic systems are superior to the MDA-FT diagnostic systems. The difference in accuracy to the SoA Systems is 0.21% for MDA-FT and 0.56% for the MDA-AC diagnostic systems for <17 abnormal-condition measurements in the training data. For \( \geq 17 \) normal-condition measurements in the training data, no clear statement can be made as to which of the systems, MDA-FT or MDA-AC, is better, as it depends on the number of neurons per hidden layer. The MDA-AC diagnostic systems have a 0.09% and the MDA-FT diagnostic systems have a 0.1% higher accuracy than the SoA Systems averaged over all numbers of neurons per hidden layer.

![Figure 18. Differences in accuracy between the MDA-FT, MDA-AC, and the SoA Systems.](image)

The results show that the model-based data augmentation combined with MDA-FT and MDA-AC generally improves the accuracy compared to state-of-the-art diagnostic systems for the analyzed number of neurons per hidden layer.

### Table 3. Averaged difference in accuracy between the MDA-FT, MDA-AC, and the SoA Systems.

<table>
<thead>
<tr>
<th>Diagnostic System</th>
<th>( n = 50 )</th>
<th>( n = 75 )</th>
<th>( n = 100 )</th>
<th>( n = 125 )</th>
<th>( n = 150 )</th>
<th>( n = 175 )</th>
<th>( n = 200 )</th>
<th>( n = 225 )</th>
<th>( n = 250 )</th>
<th>( n = 275 )</th>
<th>( n = 300 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>MDA-FT</td>
<td>0.2</td>
<td>0.25</td>
<td>0.12</td>
<td>0</td>
<td>0.14</td>
<td>0.1</td>
<td>0.19</td>
<td>0.13</td>
<td>-0.01</td>
<td>0.05</td>
<td>0.13</td>
</tr>
<tr>
<td>MDA-AC</td>
<td>0.07</td>
<td>0.13</td>
<td>0.16</td>
<td>0.18</td>
<td>0.17</td>
<td>0.17</td>
<td>0.17</td>
<td>0.16</td>
<td>0.14</td>
<td>0.17</td>
<td>0.16</td>
</tr>
</tbody>
</table>

5. Conclusions

Within this paper, we proposed a new model-based data augmentation method to improve the performance of ML-based diagnostic systems by including synthetic data in the training process. The synthetic data are generated utilizing an electromechanical model and a parameter value sampling. Such data are then compared with measurements. The results show that the model-based data augmentation is capable of generating realistic synthetic normal- and abnormal-condition data. Two approaches on how to include these synthetic data into the training process are proposed: augmenting the training data and generating a source domain for transfer learning. Each approach has two types of execution. Diagnostic systems utilizing the model-based data augmentation are trained and compared
with state-of-the-art diagnostic systems. The latter includes a model-based diagnostic system, a diagnostic system based on kernel density estimation, an MLP classifier, and an MLP classifier combined with state-of-the-art data augmentation. Including the model-based data augmentation into the training process of ML-based diagnostic systems results in increased accuracy for the MDA-AC and MDA-FT diagnostic systems compared with state-of-the-art diagnostic systems for the analyzed diagnostic task. This holds especially true for the MDA-AC diagnostic systems only if a small number of abnormal-condition measurements are available for the training—this is often the case for power engineering use cases. The average accuracy improvement for <13 abnormal-condition measurements in the training data is 0.68% compared with state-of-the-art diagnostic systems. This corresponds to a reduction of 60 misclassifications per year for hourly measurements of one piece of equipment. For ≥60 abnormal conditions in the training data, the increase in accuracy is smaller. The increase in accuracy compared with state-of-the-art diagnostic systems is, on average, 0.13% for MDA-FT and 0.09% for MDA-AC diagnostic systems. The MDA-AC diagnostic systems should be used only if very few abnormal-condition measurements are available for the training and MDA-FT systems when more abnormal-condition measurements are available for training.

In this paper, the model-based data augmentation is verified for one diagnostic task. The model-based data augmentation should be tested for other diagnostic tasks to identify possible limits.

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**References**


