



Article Generic and Open-Source Exergy Analysis—Extending the Simulation Framework TESPy

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Abstract: Exergy-based methods support the identification of thermodynamic inefficiencies and the discovery of optimization potentials in thermal engineering applications. Although a large variety of simulation software is available in this field, most do not offer an integrated solution for exergy analysis. While there are commercial products on the market with such capabilities, their access for research and educational purposes is limited. The presented open-source software offers an integrated and fully automated exergy analysis tool for thermal conversion processes. In a first step, physical exergy is implemented, and the tool is then applied to three different example plants to highlight its capabilities and validate the implementation: A solar thermal power plant, a supercritical CO₂ power cycle, and an air refrigeration cycle. The respective models and the results of the analyses are presented briefly. By providing the results in modern data structures, they are easily accessible and postprocessible. Future work will include chemical exergy to enable analyses of applications with conversion of matter. Additionally, the implementation of the exergoeconomic analysis and optimization is envisaged.

Keywords: exergy analysis;simulation; free and open-source software; thermal conversion processes; Python; generic topologies; Grassmann diagram; solar thermal power plant; supercritical carbon dioxide power cycle; air refrigeration cycle

1. Introduction

1.1. Simulation-Based Thermodynamic Analysis

Systems with thermal conversion processes are often complex and require extensive computational efforts to simulate. With the emerging usage of computers in mathematical problem solving, simulation became a powerful and widespread tool in process engineering [1–3]. Its goal is the representation of a process by a mathematical model and its (computer-aided) solution in order to obtain information about the process design and the process performance, cp. [4–6]. While such models can, of course, be solved manually, simulation shows clear advantages, including the following:

- A validated model can be used to answer what-if questions (e.g., in parameter and sensitivity analyses and process design studies) about the behavior of a real-world system [7] and thus to improve understanding of its operation.
- Computers accelerate the speed, increase the quantity, and can improve the quality of calculations [8].
- An extensive, disruptive, or expensive operation of a real-world system can be avoided. Furthermore, scale-ups or novel concepts or components can be examined before they are realized.
- During the cost- and time-limited design cycle of a product, virtual prototypes based on modeling and simulation can be used [9].



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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). Consequently, many authors focused on engineering, technology, and processes simulation and presented comprehensive modeling and simulation methodologies, e.g., [10–12]. Using generalized simulation software instead of specific tools for single instances only, it is possible to solve generic models and enable time-efficient work [13]. For example, Stamatelopoulos [14] presents some fundamentals of calculation and optimization of power plants.

In addition to the engineering and planning of thermal engineering applications, simulation, thermodynamic analysis, and optimization are powerful tools enabled by specialized software. While a large variety of software focusing on steady-state simulation of thermal conversion processes is available, see Table 1, most are proprietary. As stated in a previous publication [15], the financial obligations arising from licensing agreements are significant, despite the discounts that are commonly offered to academic institutions. From our point of view, free and open-source software is therefore particularly suitable for higher education and research.

Although the advantages and disadvantages of usage and development of free and open-source software have already been discussed, e.g., [16–18], we would like to emphasize two benefits of free and open-source software in research. First, collaborative source code development connects international research groups working on similar issues or using similar methods. Their work is available via corresponding repositories and therefore also other scientists are able to contribute and give suggestions (transdisciplinary approach). Second, an increasing number of public funding agencies expect open-access research. The use of proprietary software is not consistent with the requirement of traceability of research results.

Finally, it is necessary to mention that a simple thermodynamic analysis based on energy balances fails to identify the real thermodynamic inefficiencies within a system (see Section 2.2). In consequence, the effective use of energy sources can not be guaranteed. Examples given in [19] reveal the weaknesses of a first-law analysis based on energy balances only (see Equation (1)). An exergy-based analysis should therefore be integrated in a simulation-based thermodynamic analysis.

1.2. Motivation of the Approach

Steady-state (Thermal conversion processes are operated most of the time at steadystate conditions at different loads. Therefore, it is sufficient for most applications to perform a steady-state simulation for system operation at the design and some part-load conditions.) thermal conversion process simulation [6,14,20,21] can be performed in proprietary or open-source frameworks. Specialized software tools use predefined components, property databases, simulation, and optimization subroutines to solve nonlinear equation systems, a programming interface for mathematical-physical relationships, and mostly a graphical user interface [13]. Table 1 gives an overview of available tools. It is limited to software that is still maintained and developed further. Also not considered is any software that requires user-formulated equations to model standard components of thermal engineering systems.

The number of available predefined components varies depending on the orientation and, especially in proprietary software, on the clientele requirements. Usually, it is possible to integrate user-defined components and property functions via an application programming interface (API). The user should be able to model and simulate standardized thermal conversion processes, such as a Rankine cycle (vapor turbine), a Brayton cycle (gas turbine), heat pump or refrigeration machines, or combinations and variants thereof. The majority of available tools do not offer an out-of-the-box exergy analysis [22], although it could easily be integrated [23]. A handful of tools provide values for the specific physical exergy, calculated from enthalpy, entropy, and a user-defined ambient temperature. A comprehensive calculation of specific chemical exergies is usually not implemented. One obstacle is the lack of an internationally accepted standard reference environment to calculate standard chemical exergies. Approaches have been published among others by Szargut et al. [24–28], Ahrents [29,30], Kameyama [31], van Gool [32], Diederichsen [33], Shieh [34], Stepanov [35,36], etc. A discussion of some of these approaches can be found in [37]. Some tools or routines developed in the past to perform exergy-based analyses are closed-source, no longer available, distributed, or further developed, e.g., routines for Aspen Plus [38–44], Aspen Hysys [45], ProSimPlus [46], Sim42 [47], or not assigned to a specific software [48,49]. The computer program THESIS [50] was the first simulation tool with an integrated exergy analysis for chemical and energy engineering. Parts of THESIS are still used for the exergetic and exergoeconomic evaluation of thermal designs in courses offered by the Institute for Energy Engineering at Technische Universität Berlin.

An integrated framework for the simulation and thermodynamic analysis based on exergy destruction, exergy losses, and exergy efficiencies for thermal conversion processes operating above and below the ambient temperature T_0 is unavailable. In case values for specific physical or chemical exergies are completely calculated, users still have to provide exergy balances or definitions for the exergies of product \dot{E}_P and fuel \dot{E}_F . Definitions of these might vary, and they usually are specific to the individual application.

Following a consequent object-oriented program structure, it is possible to implement the tools required for generic exergy analysis by defining exergy balance equations for all classes of components. These balance equations use the physical and chemical exergy values of all mass flows in a system (representing the connections between the components) and the exergy values associated with heat and work.

Consequently, our research aims to consolidate the knowledge of the last decades in the methodology of exergy analysis and to provide this information in the form of a software tool as part of the object-oriented and open-source thermal conversion process simulation software TESPy (Thermal Engineering Systems in Python). In particular, all definitions of exergy efficiencies for the most essential components of thermal conversion systems are compiled. By providing this information not only on written documentation but also within the framework of functional software, these additional valuable functions may support researchers and engineers in using the tool in process development and improvement.

First, the fundamentals of thermal conversion process simulation and exergy analysis are described, followed by the specific implementation of exergy balance equations in the component classes. Subsequently, the structure and procedure of the exergy analysis tool in TESPy are presented. The approach is then applied and validated in three different example applications highlighting the tool's flexibility. The next section summarizes some aspects of the methodologies used. The thermodynamic models, exergy analysis, and their implementation in TESPy are presented. Section 4 contains the example application, including the description of the simulation, the validation, and the results of the exergy analysis. All simulations carried out are given as supplementary material to the present publication. The conclusions are summarized in the last section.

	Solver		Features				Exergy Analysis				
Name ^{Source}	eqOrient. ⁺	seqmod.	Part-Load	Properties	Flowsheeting	e ^{PH}	e ^{CH}	$\dot{E}_{\rm D}$ and $\dot{E}_{\rm L}$	ε_k for $T_j > T_0$	ε_k for $T_j < T_0$	Notes, Remarks
Proprietary, clo	sed-source (with li	icense fee or fre	e of charge)								
Aspen Plus ^a ExerCom ^b	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark	√	\checkmark				focus on chemical engineering exergy routine [51] for ASPEN
Chemcad ^c		\checkmark	\checkmark	\checkmark	\checkmark						focus on chemical engineering
Cycle Tempo ^d	\checkmark		\checkmark	\checkmark	\checkmark	\checkmark		\checkmark	\checkmark		exergy analysis, for systems with $T_i > T_0$
Ebsilon ^e	\checkmark		\checkmark	\checkmark	\checkmark	\checkmark					focus on power plants
EES ^f TAESS ^g	\checkmark			\checkmark				√ ^h			heat transfer and property library Excel exergy cost [52] calc., EES exampl.
IPSEpro ⁱ	\checkmark		\checkmark	\checkmark	\checkmark						conceived for thermal power plants
KPRO ^j	\checkmark		\checkmark	\checkmark	\checkmark						closed-loop calc., no iteration control reg.
Modelon ^k	\checkmark		\checkmark	\checkmark	\checkmark						steady-state and transient simulation
PEPSE ¹	n/a	n/a	\checkmark	\checkmark	\checkmark						steady-state energy balance software
PPSD ^m	\checkmark		\checkmark	\checkmark	\checkmark						focus on steam generators/boilers
ProSimPlus ⁿ	\checkmark		\checkmark	\checkmark	\checkmark						steady-state simulation
Thermoflow ^o		\checkmark									stand-alone mod. for spec. plant categ.
TRNSYS P	n/a	n/a	\checkmark	\checkmark	\checkmark						focus on transient simulation
ValiEnergy ^q	n/a	n/a	\checkmark	\checkmark	\checkmark						Energy performance monitoring sys.
Free and open-	source (free of cha	rge)									
COCO ^r		\checkmark		\checkmark	\checkmark						CAPE-OPEN compliant chem. flowsh.
DWSIM ^s		\checkmark		\checkmark	\checkmark						CAPE-OPEN compliant chem. flowsh.
ThermoCycle t	\checkmark			\checkmark	\checkmark						thermal systems library for Modelica

[†] also known as simultaneous or simultaneous-modular approach; ^a Aspen Plus, AspenTech, aspentech.com/en/products/engineering/aspen-plus; ^b ExerCom, CCS Energie-adies, ccsenergieadvies.nl/en/exercom; ^c Chemcad, Chemstations, chemstations.com/CHEMCAD; ^d Cycle Tempo, Asimptote, asimptote.nl/software/cycle-tempo; ^e Ebsilon Professional, Steag Energy Services, steag-systemtechnologies.com/en/products/ebsilon-professional; ^f Engineering Equation Solver, F-Chart Software, fchartsoftware.com/ees; ^g Thermoeconomic Analysis of Energy Systems Software, UNIZAR-CIRCE, exergoecology.com/taess/download-taess; ^h *E*_P and *E*_F must be defined, values *E*_j must be given from outside; ⁱ IPSEpro, SimTech, simtechnology.com/CMS/index.php/ipsepro; ^j KPRO Kreisprozessrechnung, Fichtner, kpro-fichtner.de/index.php?id=70&L=1; ^k Modelon, Modelon, modelon.com/industries/energy-power-system-simulation-optimization-software; ¹ PEPSE, Scientech, Curtiss-Wright, cwnuclear.com/brands/scientech/information-technologies/pepse/; ^m Power Plant Simulator & Designer, KED, powerplantsimulator.com; ⁿ ProSim/Plus, ProSim, prosim.net/en/product/prosimplus-steady-state-simulation-and-optimization-of-processes; ^o Thermoflow, thermoflow.com; ^p TRNSYS, Thermal Energy System Spec., trnsys.com/; ^q Vali Energy, Belsim, belsim.com/business/solution/vali-energy/; ^r COCO, AmsterCHEM, cocosimulator.org; ^s DWSIM, DWSIM, dwsim.inforside.com.br; ^t ThermoCycle, ThermoCycle, thermocycle.net (all accessed on accessed on 8 April 2022).

2. Methodology

This section shows the general modeling approach for thermal conversion processes introducing different solver concepts. Subsequently, the exergy analysis theory is discussed. The most important equations of the components required for modeling the applications in Section 4 as well as the respective exergy balance equations are presented. Based on these, the implementation of the generic exergy analysis in TESPy is described in Section 3.

2.1. Simulation of Thermal Conversion Processes

Simulation of thermal conversion processes can be performed with different methodological approaches. In general, the behavior of the plant is represented with equations modeling the physical processes in the plant's components. For each component, mass and energy balance equations must be fulfilled. Different approaches to the simulation of such systems, i.e., sequential-modular (SM) approach and equation-oriented (EO) approach, have been developed since the 1970s, and the basic concepts have been extensively discussed [53–55]. They are covered in a variety of textbooks as well, for instance, [6,56,57]. A short overview of these two basic approaches is provided. On top of that, the choice of variables in the EO approach for thermal engineering applications is discussed.

The sequential-modular approach (SM) used, for example, by Aspen Plus or Chemcad (see Table 1), starts at a specific point of the plant and solves the equations of the components one after the other. After determining the change of the fluid's state within a component based on the parameters specified, the result is carried to the next one. While this approach is easy to use and performs quickly for simple and linear plants, generic solutions are more challenging to implement; the calculation routines differ depending on the state at the inlet of a specific component and the parameters specified by the user. Therefore, the order of specifications is restricted or requires iterative solution control. Especially more complex plants with (multiple) recirculations require more solver iterations. Last, the implementation of new components or additional parameters for existing components to an existing software requires the physics applied and an individual solution procedure.

In contrast to the SM strategy, the plant is represented by a full system of equations in the EO approach. It is built from the topology of the plant and the parameters applied and is subsequently solved by an appropriate algorithm, e.g., Newton's method. As the system of equations represents both, the structure and the parameters specified, all equations can be solved simultaneously without additional iterations or slowing down convergence in case of recirculations. Furthermore, the user is free in the specification of topology and parameters as long as the system of equations is well determined with respect to its variables. The main disadvantage is that troubleshooting requires more experience as the solver cannot point out a specific reason for failure. In addition, the solver requires starting values for all variables. An initial guess for generic topologies and generic fluids is challenging to implement and thus might require user inputs. However, running additional simulations based on a converged solution leads to faster convergence.

The EO approach should be favored when modeling generic plants. A combination of both approaches, e.g., by separating mass and energy balance equations from solving equations regarding conversion of matter depending on the convergence state of the system of equations, might improve the convergence stability of EO. However, such additions will not be further investigated since the focus of this publication is on the implementation of a generic exergy analysis.

Last, the variables of the system of equations for the EO approach are an essential factor in determining the formulation of each equation. This approach often requires a numerical calculation of derivatives, e.g., to determine the Jacobian matrix in the Newton algorithm. Thus, the amount of numerically determined derivatives should be minimized for performance reasons. The component parameters of a plant can be calculated once the state of the fluid is fully determined for all inlets and outlets of all components. The state of the pure fluid (or mixture) can be obtained by combining several parameters,

for example, pressure and density, pressure and enthalpy, temperature and entropy, or enthalpy and entropy. The combination of pressure and temperature is unfavorable as additional information is required if a pure fluid is in the two-phase region. Additionally, information on mass flow is required to solve energy balance equations. On top of that, the fluid composition, e.g., mass fraction or mole fraction of the different chemical components, is a crucial variable in case conversion of matter or mixing of different fluids occurs. The changes in kinetic and potential energy can usually be neglected in thermal engineering. Thus, given the general energy balance of a thermodynamic open system in steady-state (Equation (1)), the choice of parameters to describe the state of the fluid falls to enthalpy and pressure.

$$\dot{W} + \dot{Q} = \sum_{out} (\dot{m} \cdot h)_{out} - \sum_{in} (\dot{m} \cdot h)_{in}$$
(1)

2.2. Exergy Analysis

Exergy is an extensive property giving information about the quantity and the thermodynamic quality of any energy carrier within an thermal conversion process. Consequently, only the exergy-based analysis enables comparability in evaluating material and energy flows of an overall plant or specific components [58].

The total exergy rate is the product of mass flow rate and specific exergy, which consists of the sum of physical e^{PH} , chemical e^{CH} , kinetic energy e^{KN} , and potential exergy e^{PT} . Effects associated with nuclear, magnetic, or electric processes are not considered [59].

$$\dot{E} = \dot{m} \left(e^{\rm PH} + e^{\rm CH} + e^{\rm KN} + e^{\rm PT} \right) \tag{2}$$

In the first step of implementing an exergy analysis in TESPy, only physical exergy will be considered.

$$e^{\rm PH} = (h - h_0) - T_0(s - s_0) = e^{\rm T} + e^{\rm M}$$
(3)

Furthermore, it is possible to split physical exergy into thermal and mechanical parts using the following Equations (4) and (5) [60]. In the first step, the fluid's temperature is changed isobarically to the ambient temperature to obtain the thermal exergy. In the second step, the mechanical exergy is obtained by changing the fluid's pressure isothermally to the ambient pressure.

$$e^{1} = (h - h(p, T_{0})) - T_{0}(s - s(p, T_{0}))$$
(4)

$$e^{\mathbf{M}} = (h(p, T_0) - h(p_0, T_0)) - T_0 \cdot (s(p, T_0) - s(p_0, T_0))$$
(5)

Thermal conversion processes are mainly open systems (see Figure 1). In addition to the energy flows of heat and work, there is also an exchange of material flows across the system boundary. The time-related change in the exergy within the overall system corresponds to the difference between all exergy flows entering and leaving the system, minus the exergy destruction caused by irreversibilities.

$$\frac{\mathrm{d}E_{\mathrm{tot}}}{\mathrm{d}t} = \sum_{j} \dot{E}_{\mathrm{q},j} + \sum_{i} \dot{E}_{\mathrm{w},i} + \sum_{in} \dot{E}_{in} - \sum_{out} \dot{E}_{out} - \dot{E}_{\mathrm{D}} \tag{6}$$

In the steady-state operation of a thermal conversion process, Equation (6) can be simplified.

$$0 = \sum_{j} \dot{E}_{q,j} + \sum_{i} \dot{E}_{w,i} + \sum_{in} \dot{E}_{in} - \sum_{out} \dot{E}_{out} - \dot{E}_{D}$$
(7)

The exergy destruction quantifies the thermodynamic inefficiencies associated with a process. These can be caused by chemical reaction, heat transfer, mixing, and friction and occur in every real system. The approach can thus be used to determine the components with the highest exergy destruction and the processes causing them [61].



Figure 1. Exergy balance of an open system.

For a single component k within the considered system, each term in Equation (7) can be assigned to the exergetic product or to the exergetic fuel [62]. The exergy destruction within the component is the difference of both terms.

$$\dot{E}_{\mathrm{D},k} = \dot{E}_{\mathrm{F},k} - \dot{E}_{\mathrm{P},k} \tag{8}$$

The exergy efficiency of a component *k* is the ratio [63]:

$$\varepsilon_k = \frac{E_{\mathrm{P},k}}{\dot{E}_{\mathrm{F},k}} \tag{9}$$

The sum of the exergy destruction in all components is equal to the exergy destruction of the total system. In addition, unused flows across the system boundary can be taken into account as exergy loss of the overall system.

$$\dot{E}_{\rm F,tot} = \dot{E}_{\rm P,tot} + \dot{E}_{\rm D,tot} + \dot{E}_{\rm L,tot} \tag{10}$$

Finally, the exergy efficiency of the overall system is defined as:

$$\varepsilon_{\text{tot}} = \frac{\dot{E}_{P,\text{tot}}}{\dot{E}_{F,\text{tot}}} = 1 - \frac{\dot{E}_{D,\text{tot}} + \dot{E}_{L,\text{tot}}}{\dot{E}_{F,\text{tot}}}$$
(11)

Based on the information from the overall system, the exergy destruction ratios for a component can be determined.

$$y_{\mathrm{D},k} = \frac{E_{\mathrm{D},k}}{\dot{E}_{\mathrm{F,tot}}} \tag{12}$$

$$y_{\mathrm{D},k}^* = \frac{E_{\mathrm{D},k}}{\dot{E}_{\mathrm{D,tot}}} \tag{13}$$

Especially for larger systems with many components, it might be reasonable to aggregate several components into functional groups for improved readability of the analysis results. A functional group *G* consists of one or more components of the system, e.g., a steam generator, which composes of an economizer, a steam drum, an evaporator, and a superheater. In contrast to individual components, fuel and product exergy definitions cannot be made for generic functional groups. Therefore, instead of $\dot{E}_{\rm F}$ and $\dot{E}_{\rm P}$, the sum of exergy carried into a functional group $\dot{E}_{\rm in,G}$ and the sum of exergy carried out of a functional group $\dot{E}_{\rm out,G}$ are used. The difference between these two values must then be the total exergy destruction of the functional group $\dot{E}_{{\rm D},G}$. This value must also be equal to the sum of exergy destruction values of all components *g* within that functional group (Equation (14)). Therefore, the exergy destruction ratios of a functional group $y_{{\rm D},G}$ and $y_{{\rm D},G}^*$ can be calculated analogously as shown in Equations (12) and (13).

$$\dot{E}_{\mathrm{D},G} = \sum_{g} \dot{E}_{\mathrm{D},g} \tag{14}$$

2.3. Component-Based Thermodynamic Model

This section will formulate the equations used to model selected components of thermal conversion processes and the corresponding exergy balances. The full set of equations available for each component, as well as other components available in the software with their respective exergy balance equations, are documented in the API documentation [64].

2.3.1. Turbomachinery

All turbomachinery components, i.e., turbines, pumps, fans, and compressors, are considered to be adiabatic components. Therefore, the power transferred \dot{W} can be calculated as the product of mass flow \dot{m} and the change of enthalpy h between inlet (index in) and outlet (index out) of the component.

$$0 = \dot{W} - \dot{m} \cdot (h_{\text{out}} - h_{\text{in}}) \tag{15}$$

The isentropic efficiency is a key figure of adiabatic turbomachinery. For a turbine, it describes the ratio of actual change in enthalpy to the theoretical maximum change in enthalpy of the isentropic process for a given change of pressure. The enthalpy at the outlet of the isentropic process $h_{\text{out,s}}$ is calculated from the outlet pressure and inlet entropy of that process (Equation (17)).

$$0 = \eta_{s,t} \cdot (h_{out,s} - h_{in}) - (h_{out} - h_{in})$$
(16)

$$h_{\text{out,s}} = h(p_{\text{out}}, s(p_{\text{in}}, h_{\text{in}})) \tag{17}$$

The exergy balance of adiabatic expansion, therefore, is defined as follows. Three different cases are distinguished, depending on the ambient temperature in the exergy analysis [65].

$$\dot{E}_{\rm P} = \begin{cases} |W| & T_{\rm in}, T_{\rm out} \ge T_0 \\ |\dot{W}| + \dot{E}_{\rm out}^{\rm T} & T_{\rm in} > T_0 \ge T_{\rm out} \\ |\dot{W}| + \dot{E}_{\rm out}^{\rm T} - \dot{E}_{\rm in}^{\rm T} & T_0 \ge T_{\rm in}, T_{\rm out} \end{cases}$$
(18)

$$\dot{E}_{\rm F} = \begin{cases} \dot{E}_{\rm in}^{\rm PH} - \dot{E}_{\rm out}^{\rm PH} & T_{\rm in}, T_{\rm out} \ge T_0 \\ \dot{E}_{\rm in}^{\rm T} + \dot{E}_{\rm in}^{\rm M} - \dot{E}_{\rm out}^{\rm M} & T_{\rm in} > T_0 \ge T_{\rm out} \\ \dot{E}_{\rm in}^{\rm M} - \dot{E}_{\rm out}^{\rm M} & T_0 \ge T_{\rm in}, T_{\rm out} \end{cases}$$
(19)

Similar concepts apply to compression machines, e.g., pumps and compressors. However, in contrast to expansion, the isentropic efficiency is defined reciprocally.

$$0 = \eta_{s,c} \cdot (h_{out} - h_{in}) - (h_{out,s} - h_{in})$$
(20)

The exergy balance equations are similar to expansion processes as well. The compression machine draws power instead of supplying it.

$$\dot{E}_{P} = \begin{cases} \dot{E}_{out}^{PH} - \dot{E}_{in}^{PH} & T_{in}, T_{out} \ge T_{0} \\ \dot{E}_{out}^{T} + \dot{E}_{out}^{M} - \dot{E}_{in}^{M} & T_{out} > T_{0} \le T_{in} \\ \dot{E}_{out}^{M} - \dot{E}_{in}^{M} & T_{0} \ge T_{in}, T_{out} \end{cases}$$
(21)

$$\dot{E}_{\rm F} = \begin{cases} |\dot{W}| & T_{\rm in}, T_{\rm out} \ge T_0 \\ |\dot{W}| + \dot{E}_{\rm in}^{\rm T} & T_{\rm out} > T_0 \le T_{\rm in} \\ |\dot{W}| + \dot{E}_{\rm in}^{\rm T} - \dot{E}_{\rm out}^{\rm T} & T_0 \ge T_{\rm in}, T_{\rm out} \end{cases}$$
(22)

An essential component of thermal processes is a multistage steam turbine with intermediate steam extraction for feedwater preheating. Such components can be modeled using multiple turbine parts connected to each other with splitters between one part and the next. Therefore, it is assumed that the entire mass flow of steam leaves a turbine part before entering the next one.

2.3.2. Heat Exchangers

Heat exchangers do only transfer heat. Heat losses to the ambient are neglected. The heat provided by the hot side (index 1) of a heat exchanger is therefore fully transferred to the fluid on the cold side (index 2) (Equation (23)). The heat transferred \dot{Q} is calculated using Equation (24).

$$0 = \dot{m}_{\text{in},1} \cdot (h_{\text{out},1} - h_{\text{in},1}) - \dot{m}_{\text{in},2} \cdot (h_{\text{out},2} - h_{\text{in},2})$$
(23)

$$0 = \dot{Q} - \dot{m}_{\text{in},1} \cdot (h_{\text{out},1} - h_{\text{in},1}) \tag{24}$$

Regarding the exergy balance of heat exchangers, it is necessary to distinguish six cases. Five cases are illustrated in Figure 2. The sixth variant is denoted as a purely "dissipative" heat exchanger regarding exergy, as the hot side of the heat exchanger is cooled toward T_0 while the cold side is heated towards T_0 , but T_0 is not crossed. While this type of heat exchanger has no exergetic product, it might be necessary to implement such a component for economic or technical reasons.

$$\dot{E}_{\rm F} = \begin{cases} \dot{E}_{\rm out,2}^{\rm T} - \dot{E}_{\rm in,2}^{\rm T} & ({\rm a}) \ T_{\rm in,1}, \ T_{\rm in,2}, \ T_{\rm out,1}, \ T_{\rm out,2} \ge T_{\rm 0} \\ \dot{E}_{\rm out,2}^{\rm T} & ({\rm b}) \ T_{\rm in,1}, \ T_{\rm out,1}, \ T_{\rm out,2} \ge T_{\rm 0} > T_{\rm in,2} \\ \dot{E}_{\rm out,1}^{\rm T} + \dot{E}_{\rm out,2}^{\rm T} & ({\rm c}) \ T_{\rm in,1}, \ T_{\rm out,2} > T_{\rm 0} \ge T_{\rm in,2}, \ T_{\rm out,1} \\ \dot{E}_{\rm out,1}^{\rm T} & ({\rm d}) \ T_{\rm in,1} > T_{\rm 0} \ge T_{\rm in,2}, \ T_{\rm out,1}, \ T_{\rm out,2} \\ \dot{E}_{\rm out,1}^{\rm T} - \dot{E}_{\rm in,1}^{\rm T} & ({\rm e}) \ T_{\rm 0} \ge T_{\rm in,1}, \ T_{\rm out,2} \\ not \ defined & ({\rm f}) \ T_{\rm in,1}, \ T_{\rm out,1} > T_{\rm 0} \ge T_{\rm in,2}, \ T_{\rm out,1}, \ T_{\rm out,2} \\ not \ defined & ({\rm f}) \ T_{\rm in,1}, \ T_{\rm out,1} > T_{\rm 0} \ge T_{\rm in,2}, \ T_{\rm out,1} \\ \dot{E}_{\rm in,1}^{\rm PH} - \dot{E}_{\rm out,1}^{\rm PH} + \dot{E}_{\rm in,2}^{\rm PH} - \dot{E}_{\rm out,2} \\ \dot{E}_{\rm in,1}^{\rm PH} - \dot{E}_{\rm out,1}^{\rm OH} + \dot{E}_{\rm out,2}^{\rm M} & ({\rm a}) \ T_{\rm in,1}, \ T_{\rm out,2}, \ T_{\rm 0} \ge T_{\rm in,2}, \ T_{\rm 0} \\ \dot{E}_{\rm in,1}^{\rm PH} - \dot{E}_{\rm out,1}^{\rm PH} - \dot{E}_{\rm out,2} \\ \dot{E}_{\rm in,1}^{\rm PH} - \dot{E}_{\rm out,2}^{\rm PH} - \dot{E}_{\rm out,2} & ({\rm b}) \ T_{\rm in,1}, \ T_{\rm out,2}, \ T_{\rm 0} \ge T_{\rm in,2}, \ T_{\rm 0} \\ \dot{E}_{\rm in,1}^{\rm PH} - \dot{E}_{\rm out,1}^{\rm PH} - \dot{E}_{\rm out,2} \\ \dot{E}_{\rm in,1}^{\rm PH} - \dot{E}_{\rm out,2}^{\rm PH} - \dot{E}_{\rm out,2} & ({\rm c}) \ T_{\rm in,1}, \ T_{\rm out,2} \ge T_{\rm 0} \ge T_{\rm in,2}, \ T_{\rm 0} \\ \dot{E}_{\rm in,1}^{\rm PH} + \dot{E}_{\rm in,2}^{\rm PH} - \dot{E}_{\rm out,2}^{\rm PH} \\ \dot{E}_{\rm in,2}^{\rm PH} - \dot{E}_{\rm out,2}^{\rm PH} - \dot{E}_{\rm out,2}^{\rm PH} & ({\rm d}) \ T_{\rm in,1}, \ T_{\rm 0} \ge T_{\rm in,2}, \ T_{\rm 0} \\ \dot{E}_{\rm in,1}^{\rm PH} - \dot{E}_{\rm out,2}^{\rm PH} + \dot{E}_{\rm in,1}^{\rm PH} - \dot{E}_{\rm out,1}^{\rm PH} \\ \dot{E}_{\rm in,2}^{\rm PH} - \dot{E}_{\rm out,2}^{\rm PH} + \dot{E}_{\rm in,1}^{\rm PH} - \dot{E}_{\rm out,1}^{\rm PH} \\ \dot{E}_{\rm in,2}^{\rm PH} - \dot{E}_{\rm out,2}^{\rm PH} + \dot{E}_{\rm in,2}^{\rm PH} - \dot{E}_{\rm out,2}^{\rm PH} \\ \dot{E}_{\rm in,2}^{\rm PH} - \dot{E}_{\rm out,2}^{\rm PH} + \dot{E}_{\rm in,2}^{\rm PH} - \dot{E}_{\rm out,2}^{\rm PH} \\ \dot{E}_{\rm in,1}^{\rm PH} - \dot{E}_{\rm out,2}^{\rm PH} + \dot{E}_{\rm in,2}^{\rm PH} - \dot{E}_{\rm out,2}^{\rm P$$



Figure 2. Illustration of use cases for heat exchangers. Not illustrated: variant f.

In addition to the energy and exergy balances, essential parameters for the design of heat exchangers are the terminal temperature difference values defining the temperature difference between the fluid on the hot side and the fluid on the cold side when entering and leaving the component. In TESPy, all heat exchangers implemented are countercurrent heat exchangers. The hot side inlet temperature difference ΔT_{in} describes the temperature difference of the fluid entering the hot side to the fluid leaving on the cold side (Equation (27)). Similarly, the hot side outlet temperature difference ΔT_{out} is the temperature difference of the fluid leaving the component on the hot side to the fluid entering on the cold side in Equation (28).

$$0 = \Delta T_{\rm in} - T(p_{\rm in,1}, h_{\rm in,1}) + T(p_{\rm out,2}, h_{\rm out,2})$$
(27)

$$0 = \Delta T_{\text{out}} - T(p_{\text{out},1}, h_{\text{out},1}) + T(p_{\text{in},2}, h_{\text{in},2})$$
(28)

For condensers, i.e., heat exchangers with the purpose of condensing a fluid, there are two modifications applied. The condensing fluid on the hot side of the heat exchanger leaves the component as saturated liquid, i.e., the vapor mass fraction x equals zero (Equation (29)). The hot side inlet temperature difference is often referred to as terminal temperature difference, which uses the saturation temperature at the hot side inlet instead of the actual temperature in case the fluid enters the component as superheated vapor (Equation (30)). This is done because the enthalpy difference during desuperheating is much lower than during condensation. This also ensures that the cold side temperature can never be higher than the temperature of the condensing fluid in the model.

$$0 = h_{\text{out},1} - h(p_{\text{out},1}, x = 0)$$
(29)

$$0 = \Delta T_{\rm in} - T_{\rm sat}(p_{\rm in,1}) + T_{\rm out,2} \tag{30}$$

Last, the approach point temperature difference (Equation (31)) is an essential parameter. It describes the temperature difference to the boiling point ΔT_{ap} of the working fluid for some heat exchangers, e.g., feedwater preheaters. In the economizer, it describes the temperature difference between vaporization temperature in the steam drum and the final preheating temperature and is thus crucial in the design to avoid evaporation in the economizer.

$$0 = T_{\text{sat}}(p) - \Delta T_{\text{ap}} - T_{\text{ap}}$$
(31)

2.3.3. Energy Balance Closing Components

In many applications, it might be useful to have a component closing the energy balance for the overall system, e.g., the solar field of a solar thermal power plant, as it effectively serves as energy input without necessarily needing information about the secondary side of the component. Therefore, the energy balance (Equation (32)) is applied. Other examples for this component might be heat losses in pipelines or solar-thermal collectors.

$$0 = \dot{Q} - \dot{m} \cdot (h_{\text{out}} - h_{\text{in}}) \tag{32}$$

The exergy balance is related to the exergy balance of the heat exchanger but needs to distinguish between heat input and heat output:

$$\dot{E}_{P} = \begin{cases} \begin{cases} \text{not defined} & \text{if dissipative} \\ \dot{E}_{\text{in}}^{T} - \dot{E}_{\text{out}}^{T} & \text{else} \\ \dot{E}_{\text{out}}^{T} & T_{\text{in}} \ge T_{0} > T_{\text{out}} \\ \dot{E}_{\text{out}}^{T} - \dot{E}_{\text{in}}^{T} & T_{0} \ge T_{\text{in}}, T_{\text{out}} \\ \dot{E}_{\text{out}}^{T} - \dot{E}_{\text{in}}^{T} & T_{0} \ge T_{\text{in}}, T_{\text{out}} \\ \dot{E}_{\text{out}}^{T} - \dot{E}_{\text{in}}^{T} & T_{\text{out}} > T_{0} \\ \dot{E}_{\text{in}}^{T} + \dot{E}_{\text{out}}^{T} & T_{\text{out}} > T_{0} \ge T_{\text{in}} \\ \dot{E}_{\text{in}}^{T} - \dot{E}_{\text{out}}^{T} + \dot{E}_{\text{out}}^{M} - \dot{E}_{\text{in}}^{M} + T_{0} \ge T_{\text{in}}, T_{\text{out}} \\ \end{cases} \end{cases}$$
(33)

$$\dot{E}_{F} = \begin{cases} \dot{E}_{in}^{PH} - \dot{E}_{out}^{PH} & T_{in}, T_{out} \ge T_{0} \\ \dot{E}_{in}^{T} + \dot{E}_{in}^{M} + \dot{E}_{out}^{T} - \dot{E}_{out}^{M} & T_{in} \ge T_{0} > T_{out} & \dot{Q} < 0 \\ \dot{E}_{out}^{T} - \dot{E}_{in}^{T} + \dot{E}_{in}^{M} - \dot{E}_{out}^{M} + & T_{0} \ge T_{in}, T_{out} \\ \dot{E}_{out}^{T} - \dot{E}_{in}^{T} & T_{in}, T_{out} \ge T_{0} \\ \dot{E}_{in}^{T} + \dot{E}_{in}^{M} - \dot{E}_{out}^{M} & T_{out} > T_{0} \ge T_{in} & \dot{Q} > 0 \\ \dot{E}_{in}^{T} - \dot{E}_{out}^{T} & T_{0} \ge T_{in}, T_{out} \end{cases}$$
(34)

2.3.4. Merge Points

Another important component is the merge in which two or more different incoming streams (indexed *i*) are mixed with no transport of heat or power to the surroundings. Therefore, the energy balance equation can be deducted.

$$0 = \sum_{i} (\dot{m}_{\text{in},i} \cdot h_{\text{in},i}) - \dot{m}_{\text{out}} \cdot h_{\text{out}} \quad \forall \quad i \in \text{inlets}$$
(35)

The exergy balance equations are defined with the analogous approach of the heat exchanger exergy balance equations. For a mixing temperature T_{out} higher than the ambient temperature, the product is heating the colder fluids. For a mixing temperature below the ambient temperature level, the product is cooling the hotter fluids. In addition, a distinction must be made in case an incoming stream is heated starting below the ambient temperature or cooled starting above the ambient temperature. In these cases, only change of exergy starting at the ambient temperature is accounted for in the product exergy (Equation (36)). The fuel exergy is then defined analogously (Equation (37)). If the temperature of the mixed stream is at ambient temperature, the component is considered a dissipative one. In the current version of the software TESPy, it is assumed that all mixed streams have the same chemical composition. Therefore, chemical exergies are not considered. Equations (36) and (37) cover all possible cases. It should be noted, however, that some of them are thermodynamically not meaningful.

$$\dot{E}_{P} = \begin{cases}
\begin{cases}
\sum_{i} \dot{m}_{i} \cdot \left(e_{out}^{PH} - e_{in,i}^{PH}\right) & T_{in,i} < T_{out} \& T_{in,i} \ge T_{0} \\
\sum_{i} \dot{m}_{i} \cdot e_{out}^{PH} & T_{in,i} < T_{out} \& T_{in,i} < T_{0}
\end{cases}$$

$$for defined & T_{out} = T_{0} \\
for defined & T_{out} = T_{0} \\
\sum_{i} \dot{m}_{i} \cdot e_{out}^{PH} & T_{in,i} > T_{out} \& T_{in,i} \ge T_{0} \\
\sum_{i} \dot{m}_{i} \cdot \left(e_{out}^{PH} - e_{in,i}^{PH}\right) & T_{in,i} > T_{out} \& T_{in,i} < T_{0}
\end{cases}$$

$$\dot{E}_{F} = \begin{cases}
\begin{cases}
\sum_{i} \dot{m}_{i} \cdot \left(e_{in,i}^{PH} - e_{out}^{PH}\right) & T_{in,i} > T_{out} \\
\sum_{i} \dot{E}_{in,i}^{PH} & T_{in,i} < T_{out} \& T_{in,i} < T_{0}
\end{cases}$$

$$\dot{E}_{F} = \begin{cases}
\begin{cases}
\sum_{i} \dot{m}_{i} \cdot \left(e_{in,i}^{PH} - e_{out}^{PH}\right) & T_{in,i} > T_{out} \\
\sum_{i} \dot{E}_{in,i}^{PH} & T_{in,i} < T_{out} \& T_{in,i} < T_{0}
\end{cases}$$

$$\dot{E}_{I} = \begin{cases}
\begin{cases}
\sum_{i} \dot{E}_{in,i}^{PH} & T_{in,i} > T_{out} \& T_{in,i} < T_{0}
\end{cases}$$

$$\dot{E}_{I} = \begin{cases}
\begin{cases}
\sum_{i} \dot{E}_{in,i}^{PH} & T_{in,i} > T_{out} \& T_{in,i} > T_{0}
\end{cases}$$

$$\dot{E}_{I} = \begin{cases}
\begin{cases}
\sum_{i} \dot{E}_{in,i}^{PH} & T_{in,i} > T_{out} \& T_{in,i} > T_{0}
\end{cases}$$

$$\dot{E}_{I} = \begin{cases}
\begin{cases}
\sum_{i} \dot{E}_{in,i}^{PH} & T_{in,i} > T_{out} \& T_{in,i} > T_{0}
\end{cases}$$

$$\dot{E}_{I} = f_{In,i}^{PH} & T_{In,i} < T_{0}
\end{cases}$$

$$\dot{E}_{I} = \begin{cases}
\begin{cases}
\sum_{i} \dot{E}_{in,i}^{PH} & T_{in,i} > T_{out} \& T_{in,i} > T_{0}
\end{cases}$$

$$\dot{E}_{I} = f_{In,i}^{PH} & T_{In,i} < T_{0}
\end{cases}$$

$$\dot{E}_{I} = f_{In,i}^{PH} & T_{In,i} < T_{0}$$

$$\dot{E}_{I} = f_{In}^{PH} & T_{In,i} < T_{0}$$

$$\dot{E}_{In}^{PH} & T_{In,i} <$$

2.3.5. Steam Drum

A drum is implemented to separate saturated liquid from saturated vapor in the evaporation process. The drum's energy balance is similar to that of a merge point with two streams leaving the device. Additional constraints are applied, i.e., the saturated liquid state at the first outlet stream and the saturated vapor state at the second outlet stream. Note that blowdown is not be considered in this modeling approach.

$$0 = \sum_{i} (\dot{m}_{\text{in},i} \cdot h_{\text{in},i}) - \sum_{j} (\dot{m}_{\text{out},j} \cdot h_{\text{out},j})$$
(38)

$$0 = h_{\text{out},1} - h'(p_{\text{out},1}) 0 = h_{\text{out},2} - h''(p_{\text{out},2})$$
(39)

It is usually not meaningful to define an exergy efficiency just for a steam drum alone, since this component is part of an evaporator.

2.3.6. Motors and Generators

The turbines of the plant power a generator, whereas pumps and fans require an electrical motor to be powered. Assuming an efficiency for the generator $\eta_{el,m}$, its electrical power output of a generator $\dot{W}_{el,gen}$ is calculated according to Equation (40). The turbine power \dot{W} (Equation (15)) is multiplied with the efficiency factor $\eta_{el,m}$ considering mechanical and electrical losses.

$$\dot{W}_{\rm el.gen} = \dot{W} \cdot \eta_{\rm el.m} \tag{40}$$

Analogously, in Equation (41), the electrical power input for a motor $W_{el,mot}$ is determined.

$$\dot{W}_{\rm el,mot} = \frac{W}{\eta_{\rm el,m}} \tag{41}$$

3. Implementation of the Exergy Analysis in TESPy

Here, the implementation of a generic exergy analysis is presented. The software TESPy is designed to simulate the steady-state operation of thermal conversion processes, such as thermal power plants, heat pumps, or pipeline networks at the component level. The software models typical units (e.g., turbines, pumps, heat exchangers), thus allowing the user to build generic plant models [66]. An introduction to Python fundamentals is given in [67].

Figure 3 shows an overview of the structure of TESPy. Each simulation model is based inside the network class. The class automatically builds a system of nonlinear equations representing the plant's topology and the boundary conditions specified, for instance, cooling water temperature or turbine isentropic efficiency. The topology is derived from the connections between the system's components. Therefore, the connection class holds the topological information by connecting a source component with a target component and the fluid property data, i.e., mass flow, pressure, enthalpy, and mass fraction. In addition, it is possible to connect pure energy streams, e.g., the power of a turbine or the power of a pump, by the use of energy busses (class bus). Conversion losses can be considered with constant efficiency values.

The system of equations is solved numerically with the multidimensional Newton-Raphson algorithm for the system's variables, which are mass flow, pressure, enthalpy, and fluid mass fraction on every connection. As mass flow and fluid property data are available for all connections after a converged simulation is obtained, all remaining variables of a stream, e.g., pressure or temperature, and all component parameters, can be determined with the fluid property module. The module holds all functions to calculate required fluid properties, including calculation of physical exergy using CoolProp [68]. The online documentation provides extensive information on the component models and fluid property calculations applied in the software.

Figure 4 illustrates the procedure of the exergy analysis implemented in TESPy. The user defines the busses of the TESPy network, which hold information on fuel and product exergy and exergy loss. These are passed together with the network to create an instance of the class ExergyAnalysis (see also Figure 3). Subsequently, the exergy analysis is carried out using data of the ambient state, i.e., pressure and temperature. In the first step, physical exergy, including thermal and mechanical exergy (see Equations (5) and (4)) of all fluid streams, is calculated for the connection objects of the network. In the second step, the exergy balance of all components (see Section 2.3) is evaluated.

Based on the exergy balances of the components, the exergy balances of the busses corresponding to the plant's total fuel and product exergy and exergy loss are evaluated. Furthermore, the balance equations for internal massless exergy transfer, e.g., a feed pump that is directly driven by a respective turbine, are calculated. The individual conversion factor of each component as part of a bus object is applied to the exergy flow, analogously to the definition of generator and motor power in Equations (40) and (41). The exergy destruction within each component and their corresponding bus (if any) is summed to calculate the network's total exergy destruction $\dot{E}_{D,tot}$. As all elements of the overall network exergy balance are now known (Equation (10)), a consistency check can be carried out, where the deviation ΔE of total fuel exergy $\dot{E}_{F,tot}$ from the sum of total product exergy $\dot{E}_{P,tot}$, exergy loss $\dot{E}_{L,tot}$, and exergy destruction $\dot{E}_{D,tot}$ must be equal to zero. To account for rounding errors, the absolute value of $\Delta \dot{E}$ should be smaller than a threshold value of 0.001 W. When running the exergy analysis on a converged simulation, this condition must be true. If it is not, some exergy streams in the overall system have not correctly been accounted for in the exergy analysis setup.



Figure 3. Simplified structure of the TESPy package and the embedding of the exergy analysis.



Figure 4. Simplified flowchart of the exergy analysis in TESPy.

Finally, all exergy balance data of the components and their respective busses, including exergy efficiency as well as exergy destruction and exergy loss ratio, are provided to the user as pandas DataFrames [69], which can easily be exported to any tabular format. Furthermore, the physical exergy values of all connections are accessible in a DataFrame.

In addition, during the setup of the system's components, the user can assign each component to a functional group, as described in Section 2.2. A DataFrame is then provided for all functional groups, including their information on the inflow $E_{in,G}$ and outflow of exergy $E_{out,G}$, the total exergy destruction as well as the exergy destruction ratios according to their definitions in Equations (7) and (12)-(14). If a component is not assigned to any functional group, it will form a functional group by itself. With these data, a graphical representation of exergy flows between the different functional groups of the system in a Grassmann diagram [70] is enabled. For this purpose, the data is provided as expected by the Python library plotly for its Sankey class [71]. The functional groups, including individual components, that form their own functional group, are the nodes of the Grassmann diagram. The edges represent the exergy flows. The values are shown in a true-to-scale manner by the width of the edges. The exergy flows of the overall system across the system boundary (see Equation (10)) are each represented by their respective color. Exergy flows associated with a mass flow of a fluid, a heat rate, or work rate within the system boundary are marked with a unique color. The software provides default color codes; however, the user can specify the colors as desired. For more information, please visit the respective section of the online documentation [64]. The diagram is provided in an interactive format, showing additional information when hovering over nodes and edges. The displayed data can be modified according to the user's requirements following the API of plotly.

Given the exergy streams crossing the system's boundaries are well defined by the user, changing any values in the process's specifications or even modifying the plant's topology

does not require any changes regarding the exergy analysis setup. The analysis can be performed again easily. The online documentation of TESPy provides several examples on the usage and implementation of the exergy analysis as well.

4. Example Applications

Exergy analyses are carried out for three different applications to demonstrate the new feature in TESPy. The Python scripts, the result reports, and the model validation are available via zenodo.

- The so-called "Solar Energy Generating System VI" (SEGS) [72], see Section 4.1
- Supercritical CO₂ power cycle [73], see Section 4.2
- Refrigeration machine using air as working fluid [74], see Section 4.3

Subsequently, the examples are briefly presented with the respective results generated by the exergy analysis tool. The SEGS model is validated using the proprietary software Ebsilon. The other two examples have originally been published in [75,76]. These contain all data necessary to set up and evaluate the TESPy simulation. Therefore, the respective TESPy models are compared to results from these publications instead of using Ebsilon. The versions used are TESPy v0.6.0 [77] and Ebsilon 14.03.01.

4.1. Solar Energy Generating System

The SEGS in Southern California, USA, has been chosen as a real application. A complete set of parameters and performance data is available in References [78,79] for this concentrating solar power (CSP) plant.

4.1.1. Process Simulation and Validation

SEGS consists of three major subsystems: the solar field, the power cycle, and the cooling water system. The TESPy model corresponds to the layout shown in Figure 5.



Figure 5. Flow chart of SEGS implemented in TESPy.

In the first subsystem, a eutectic mixture of diphenyl oxide and biphenyl, commercially known as Therminol VP-1 [80], circulates as the heat transferring fluid (HTF). The heat rate from the solar field is transferred through the heat exchangers of the steam generator and the reheater to the power cycle. In the steam generator, the HTF is split into two parallel heat exchanger trains. Each consists of a superheater, evaporator, and economizer. The division into two parallel streams also applies to the reheater. For simplicity, the two trains are modeled as a single one in both cases. A field pump ensures the circulation of the HTF. The solar field is modeled as simple heat input. The exact layout of the solar field does not influence the overall analysis.

The steam turbine drives the generator to provide electricity. The steam turbine is divided into a high-pressure and a low-pressure turbine. In between, reheating is used. The turbine sections are split into two and five parts to extract steam for preheating, respectively. The power plant has three low-pressure and two high-pressure preheaters and a feedwater tank (deaerator).

An induced draft cooling tower is used for recooling. Therefore, a cooling water cycle is modeled, transporting the heat rate from the power cycle via a heat exchanger to the ambient air. A fan provides the necessary mass flow rate of air.

The example covers the design state in full-load steady-state conditions and pure solar mode. Table 2 summarizes selected process and component parameters. For a complete set of input parameters, see model documentation in [72].

The isentropic efficiencies of the turbines are taken from [81], which are derived them from the stated properties for every stream in [78]. Due to inconsistencies in the primary data, a reasonable isentropic efficiency for the fourth low-pressure turbine stage of 88% was assumed.

Regarding the preheaters, the pressure drop on the hot side is neglected. The pressure drop on the cold side has been calculated by using the stated properties for every stream in [78]. This procedure has also been applied to the steam generator and reheater. The temperature difference for the approach point in the steam generator is assumed to be 2 K, and the pinch point temperature difference is at 5 K. Regarding the temperature specifications of the preheaters and the steam generator, the assumptions listed in Table 2 have been applied.

Parameter	Symbol	Unit	Value
HTF temperature	T ₇₀	°C	390
HTF mass flow ratio	$\dot{m}_{76} / \dot{m}_{70}$	-	0.13
Steam temperatures	T_1, T_7	°C	371, 371
Steam pressures	<i>p</i> ₁ , <i>p</i> ₇	bar	100, 17.1
Steam mass flow	\dot{m}_1	kg/s	38.97
Condensation pressure	p_{17}	bar	0.08
Pumps, efficiencies	$\eta_{\rm is}, \eta_{\rm el,m}$	%	70.0, 95.0
Generator, efficiency	$\eta_{\rm el,m}$	%	97.0
Air fan, efficiency	η_{is}	%	60.0
Preheaters, upper temperature difference	$\Delta T_{t,u}$	К	5
Subcoolers, lower temperature difference	$\Delta T_{\rm t,l}$	K	10

Table 2. SEGS—Parameters of the overall process and components [78,82].

Pressure losses during the condensation on the hot side of the condenser are neglected. For the cooling system, the parasitic power requirement is at 0.91 MW [78]. Therefore, an air cooling tower is implemented to cool the water in an intermediate cycle for the main condenser of the power plant. With the assumptions made in the simulation, the parasitic power requirements for the cooling system add up to 0.92 MW.

In addition to the TESPy model, an identical model has been built with the industrial standard software Ebsilon. As TESPy's thermodynamic library for fluid property calcula-

tion CoolProp [68] is available for Ebsilon as well, it is used in both models. The library contains Therminol VP-1 as an incompressible liquid, the air is calculated as pseudopure fluid with the Helmholtz equation of state (HEOS) back-end, and for water, the IAPWS-95 formulation is implemented. The results obtained from both models are identical.

4.1.2. Results of the Exergy Analysis

The exergy-based analysis is carried out for the specifications used in the model validation. The ambient temperature T_0 is 25 °C; the ambient pressure p_0 is 1.013 bar.

Table 3 shows the exergy balance of the overall process for SEGS. The product exergy corresponds to net power output. If the energy rate absorbed by the parabolic trough collectors is specified as the exergetic fuel, this results in an exergy efficiency ε_{tot} of 66.7% for the overall process. The real thermodynamic losses at the solar field, i.e., the difference between the exergy of the incident global radiation and the exergy associated with the absorbed heat rate, are thus not taken into account. The overall exergy loss $\dot{E}_{L,tot}$ is the release of the cooling air to the environment. Compared to the overall exergy destruction, the overall exergy loss is significantly smaller since the temperature of the released air, and thus the physical exergy of the material flow, is low.

Table 3. SEGS—Results of the exergy analysis, overall process. All values given in MW.

Ė _{F,tot}	Ė _{P,tot}	Ė _{D,tot}	Ė _{L,tot}
47.63	31.77	15.37	0.49

The power plant simulation model consists of a large number of individual components. For a better understanding of the causes of exergy destruction, components were accumulated into functional groups. Results are presented in Table 4. Based on these results, the Grassmann diagram feature of TESPy can be used to create Figure 6, which illustrates the flow of exergy through the functional groups.

It can be seen that the low-pressure turbine (LPT) and the cooling water system (CW) account for almost 50% of the overall exergy destruction rate. Especially the low value of isentropic efficiency of the low-pressure turbine causes a high share of exergy destruction. For the cooling water system, only the condensate is reused within the plant, which is close to the ambient state. Therefore, most of the exergy is destroyed or lost to the ambient state. Other quantitatively relevant contributions to the overall exergy destruction rate occur in the steam generator (SG) and the high-pressure turbine (HPT). All other functional groups account for less than 10% each, summing up to approx 24% in total.

Table 4. SEGS—Results of the exergy analysis, functional groups. If not given, dimension of data is MW.

Functional Group G	Ė _{in,G}	Ė _{out,G}	Ė _{D,G}	$y_{{ m D},G}(\%)$	$y^{*}_{{ m D},G}$ (%)
Low-pressure turbine (LPT)	36.01	31.94	4.07	8.6	26.5
Cooling water system (CW)	4.09	0.59	3.50	7.3	22.8
Steam generator (SG)	107.46	104.94	2.52	5.3	16.4
High-pressure turbine (HPT)	46.66	45.06	1.60	3.4	10.4
Reheater (RH)	43.64	42.41	1.23	2.6	8.0
Solar field (SF)	114.09	112.89	1.20	2.5	7.8
Low-pressure preheater (LPP)	5.25	4.51	0.74	1.6	4.8
High-pressure preheater (HPP)	10.13	9.79	0.33	0.7	2.2
Feedwater pump (FWP)	5.26	5.07	0.18	0.4	1.2



Figure 6. Machine-generated Grassmann diagram based on functional groups of SEGS. The value of the exergy flows are shown in a true-to-scale manner by the width of the edges.

4.2. Supercritical Carbon Dioxide Power Cycle

As a second example, the variant c) of the supercritical CO_2 (s CO_2) power cycles reported by Penkuhn and Tsatsaronis [75] has been implemented and analyzed using TESPy as all necessary input data, and the results of the exergy-based analysis are available.

4.2.1. Process Simulation and Validation

The investigated cycle is the recompression, recuperated cycle, with two compressors and one turbine. The working fluid is heated and routed to the turbine. After expansion, two recuperators are used to preheat the compressed CO_2 . After exiting the recuperators, one part of the fluid is cooled and compressed before entering the cold side of the recuperator 1. The remaining CO_2 is compressed without entering the cooler and mixed into the reheated CO_2 stream from the first compressor and then routed through the recuperator 2 before entering the heater. The model created in TESPy corresponds to the layout shown in Figure 7.



Figure 7. Flow chart of sCO₂ power cycle implemented in TESPy.

In contrast to the original study, the exergy balances of the heater and the cooler are modeled without knowledge of the temperature profile of the non-CO₂ side (see Section 2.3.3). The cooler is considered a dissipative component. Thus, the plant will not have exergy losses. Furthermore, the distribution of the mass flow through compressor 1 and compressor 2 is assumed to be a result of the temperature values observed at the merge point between the recuperators. The compressor 2 and recuperator 1 outlet temperatures T_{11} and T_{12} are thus specified to be equal (but unknown prior to the calculation) values. Table 5 summarizes selected process and component parameters. For a complete set of input parameters, see model documentation [73].

Parameter	Symbol	Unit	Value
Turbine inlet temperature	T_5	°C	600
Turbine inlet pressure	p_5	bar	250
Compressor inlet pressures	p_1, p_{10}	bar	75,75
Compressors, efficiencies	$\eta_{\rm is}, \eta_{\rm el.m}$	%	85.0, 95.1
Turbine, efficiencies	$\eta_{\rm is}, \eta_{\rm el,m}$	%	90.0, 98.0
Recuperators, lower temperature difference	$\Delta T_{\rm t,l}$	К	5

Table 5. sCO₂ power cycle—Parameters of the overall process and components [75].

In this example, HEOS back-end of CoolProp was used as well. Although the data from the original source are based on the REFPROP database and calculation, the relative deviation between both libraries is less than 10^{-9} for enthalpy values and 10^{-12} for entropy values. Consequently, the results agree except for numerical deviations without impacting real-life operation. The highest deviation in thermodynamic properties is observed in the turbine outlet temperature T_5 with 0.2 K. All other (nonspecified) temperature values are within less than 0.1 K compared to the original data. Therefore, a deviation can be observed in the physical exergy of the streams. Considering the overall cycle efficiency η_{th} , a relative deviation of about 0.1% occurs.

4.2.2. Results of the Exergy Analysis

The exergy-based analysis is carried out for an ambient temperature T_0 of 25 °C and an ambient pressure p_0 of 1.013 bar. The results of the analysis are summarized in Tables 6 and 7. Since the number of components in this application is low, the component results are reported instead of the functional group results. The net power generation of the process is associated with the product exergy $\dot{E}_{P,tot}$. If the exergy rate supplied to the process associated with the heat rate is considered as fuel exergy $\dot{E}_{F,tot}$, the overall exergy efficiency ε_{tot} is 64.6%. Figure 8 illustrates the exergy flow rates within the process.

Table 6. sCO₂ power cycle—Results of the exergy analysis, overall process. All values given in MW.

Ė _{F,tot}	Ė _{P,tot}	Ė _{D,tot}	Ė _{L,tot}
154.93	100.00	54.93	0.00

Component k	$\dot{E}_{\mathrm{F},k}$	Ė _{P,k}	$\dot{E}_{\mathrm{D},k}$	ε _k (%)	$y_{{ m D},k}$ (%)	$y^{*}_{{ m D},k}$ (%)
Compressor 1	47.49	40.20	7.29	84.6	4.7	13.3
Compressor 2	37.58	32.81	4.76	87.3	3.1	8.7
Heater	154.93	154.09	0.84	99.5	0.5	1.5
Recuperator 1	73.81	69.93	3.87	94.8	2.5	7.1
Recuperator 2	139.19	135.43	3.76	97.3	2.4	6.8
Turbine	197.19	185.07	12.12	93.9	7.8	22.1
Water cooler	22.28	nan	22.28	nan	14.4	40.6

Table 7. sCO₂ power cycle—Results of the exergy analysis, components. If not given, dimension of data is MW.

The highest share of the overall exergy destruction rate can be observed in the cooler. The exergy destruction rate of the rotating equipment—compressors and turbine—amounts to a cumulative 24 MW. The heater has the smallest share in the total exergy destruction rate, as per definition in Equations (33) and (34) only the pressure losses account for the exergy destruction rate in this type of heat exchanger. Note that the difference in the definition of the heater's exergy balance is the reason why a high relative deviation in

the exergy destruction values between the results of this paper and the original study (approx. -70%) is observed.



Figure 8. Machine-generated Grassmann diagram based on functional groups of sCO₂ power cycle. The value of the exergy flows are shown in a true-to-scale manner by the width of the edges.

4.3. Air Refrigeration Cycle

The third example focuses on a refrigeration cycle using air as working fluid originally presented by Morosuk and Tsatsaronis [76].

4.3.1. Process Simulation and Validation

The process consists of a four-component refrigeration cycle with compressor, heater, cooler, and turbine. The compressor and turbine are on a single shaft, and an inverter is included in the original analysis to account for conversion losses of the electrical power input to mechanical power of the shaft driving the compressor, as seen in Figure 9. The cycle is applied to cool air. The heat sink is water at ambient conditions.

Table 8 summarizes selected process and component parameters. For a complete set of input parameters, see model documentation [74]. The input data match the original data from [76]. However, due to the architecture of the TESPy solver and the exergy analysis feature, losses on a single shaft with respect to the residual power $\dot{W}_{cmp} + \dot{W}_{tur}$ cannot be accounted in the same way as in the original study. Therefore, the residual power is first determined without accounting for losses.

$$\frac{\dot{W}_{\rm cmp} + \dot{W}_{\rm tur}}{\eta_{\rm el, original}} = \frac{\dot{W}_{\rm cmp}}{\eta_{\rm el, m}} + \dot{W}_{\rm tur} \cdot \eta_{\rm el, m}$$
(42)

In a second step, equal efficiencies $\eta_{el,m}$ for both, the turbine's generator and the compressor's motor, are applied to the power bus to match the efficiency specifications of the original study $\eta_{el,original} = 0.9$ (see Equation (42)). This results in an efficiency $\eta_{el,m}$ of 96.2%.



Figure 9. Flow chart of the air refrigeration cycle implemented in TESPy.

Parameter	Symbol	Unit	Value
	-		
Compressor inlet temperature	T_1	°C	-30
Compressor inlet pressure	p_1	bar	1
Turbine inlet temperature	T_3	°C	35
Turbine inlet pressure	p_3	bar	5
Ambient air temperatures	T_{21}, T_{22}	°C	25,40
Refrigeration temperatures	T_{11}, T_{12}	°C	-10, -20
Compressor/turbine efficiencies	η_{is} , $\eta_{\mathrm{el,m}}$	%	80.0, 96.2

Table 8. Air refrigeration cycle—Parameters of the overall process and components [76].

For the original analysis, the used fluid property back-end is not documented. In the TESPy model, the HEOS for pseudopure dry air is applied using CoolProp. Deviations in the outlet temperature of the compressor and the turbine of 0.04% and -0.18%, respectively, can be observed. A relatively high deviation is found in the enthalpy difference at the cooling side heat exchanger with about 2%. For the other components, the maximum deviation is at the heat sink heat exchanger with about 0.6% and 0.55% on the secondary stream of the cooling heat exchanger. Due to the 2% deviation, the cycle's mass flows calculated with the TESPy model deviate by the same value as the governing equation for mass flow is the heat transferred at that heat exchanger (see Equation (23)).

4.3.2. Results of the Exergy Analysis

The ambient state is not explicitly reported in the original study but can be derived from the exergy tables. The ambient temperature T_0 is 25 °C; the ambient pressure is 1.0 bar.

Overall, the specific thermal exergy data of the streams are consistent with the reported data from literature. The mechanical exergy matches for all streams, as all pressure values are identical. The deviations in the thermodynamic properties, including the exergy values between the original paper and the calculations reported here, are lower than 2.1% and are caused by the different fluid properties functions used in each calculation. Since the inverter is treated separately in the original study, high deviations are observed in the compressor and turbine exergy analysis results.

The results of the exergy analysis are presented in Tables 9 and 10. The total product exergy is associated with the exergy rate required to cool the air. The total fuel exergy represents the power input. This results in an overall exergy efficiency of 3.5%.

The compressor, the turbine, and the heat sink heat exchanger have the highest shares of the overall exergy destruction rate, with 92.5%. This includes the mechanical losses on the shaft, which account for 10.7% of the overall exergy destruction rate. The heat sink heat exchanger has the smallest share of the overall exergy destruction rate. Figure 10 illustrates the exergy flow rates within the process.



Figure 10. Machine-generated Grassmann diagram for the refrigeration cycle. The value of the exergy flows are shown in a true-to-scale manner by the width of the edges.

Ė _{F,tot}	Ė _{P,tot}	Ė _{D,tot}	$\dot{E}_{ m L,tot}$
439.80	15.51	412.22	12.07

Table 9. Air refrigeration cycle—Results of the exergy analysis, overall process. All values given in kW.

Table 10. Air refrigeration cycle—Results of the exergy analysis, components. If not given, dimension of data is kW.

Component k	$\dot{E}_{\mathrm{F},k}$	Ė _{P,k}	$\dot{E}_{\mathrm{D},k}$	ε_k (%)	$y_{{ m D},k}$ (%)	$y^{*}_{{ m D},k}$ (%)
Compressor	815.29	674.08	141.21	82.7	32.1	34.3
Cooling heat exchanger	46.30	15.51	30.79	33.5	7.0	7.5
Heat sink heat exchanger	107.31	12.07	95.24	11.2	21.7	23.1
Turbine	549.60	404.62	144.98	73.6	33.0	35.2

5. Conclusions

Exergy-based analyses are powerful tools for the thermodynamic and thermoeconomic investigation of thermal conversion processes. Available simulation and analysis software, proprietary as well as free and open-source, do not provide a fully integrated solution for such analyses. Considering that such analysis requires knowledge of the topological structure of a process and the results from a respective simulation, it is evident that exergy-based analyses should be integrated as automatic analyses following the solution of the system of equations of the simulation.

For the first time, open-source software can perform a generic exergy analysis for thermal conversion processes. The automated exergy analysis allows evaluation for processes above, below, and with a transition at T_0 . The study provides exergy efficiencies for all possible application cases for all basic unit operations of thermal process engineering (for the heat exchanger, for example, see Equations (25) and (26)). Furthermore, Grassman diagrams can be generated.

The paper discussed the approach, summarized the equations and definitions used, and validated the results with three example applications. The contributions of our research can be summarized as follows.

- A complete set of exergy balance equations, including definitions of fuel and product exergy, for the most important components in thermal conversion processes is implemented.
- The paper presents a generic and reproducible workflow. It allows researchers to perform exergy analyses based on any thermodynamic application modeled by the software.
- The thermodynamic models and the results of the exergy analysis have been validated based on published research.
- Due to the fully integrated solution, changes in topology or parameter specifications
 of an existing model do not require changes in the exergy analysis setup.
- Providing the results in modern data structures enables further investigation or integration of external algorithms, e.g., exergy-based optimization procedures. For instance, refs. [83,84] published implementations of optimization procedures using first law analysis with TESPy.
- Updating and evaluating exergy analyses of published research is possible.

While the exergy analysis in the presented research as well as the software implementation do cover a wide range of thermal engineering applications, two important use cases for exergy analysis have not yet been considered, in addition to the inclusion of calculation of chemical exergies. These are:

- Analysis of processes with conversion of matter, such as gas turbine power plants or power-to-gas facilities.
- Provision of exergoeconomical analysis tools.

The next step in the further development of the software is the implementation of chemical exergy. Due to the modular structure, this step means to integrate the methods of chemical exergy calculation for every stream of matter and to update the exergy balance equations of the components to account for the change in chemical exergy. For the implementation of the exergoeconomic analysis, additional functionalities have to be added to the component classes to define cost balances and auxiliary equations.

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Nomenclature

Abbreviat	ions
API	Application programming interface
CMP	Compressors
CON	Condenser
CSP	Concentrating solar power
СР	Condensate pump
СТ	Cooling tower
CW	Cooling water
CWP	Cooling water pump
ECO	Economizer
EO	Equation-oriented
EV	Evaporator
DR	Drum
FP	Field pump
FWP	Feed water pump
FWT	Feed water tank
HEOS	Helmholtz equation of state
HPP	High-pressure preheater
HPT	High-pressure turbine
HTF	Heat-transfer fluid
IAPWS	International Association for the Properties of Water and Steam
LPP	Low-pressure preheater
LPT	Low-pressure turbine
NIST	National Institute of Standards and Technology
REC	Recuperators
RH	Reheater
sCO ₂	supercritical CO ₂
SH	Superheater
SEGS	Solar Energy Generating System
SG	Steam generator
SM	Sequential-modular
sub	Subcooler

TESPy Thermal Engineering Systems in Python

Latin symbols	
'n	Mass flow, kg/s
С	Flow velocity, m/s
Ė	Exergy flow, W
8	Gravity, m/s ²
ĥ	Specific enthalpy, J/kg
р	Pressure, bar
, Ż	Heat flow, W
S	Specific Entropy, J/kgK
Т	Temperature, °C
Ŵ	Power, W
x	Steam mass fraction, -
y	Exergy destruction ratio, -
z	Height, m
Greek symbols	<u> </u>
η	Energetic efficiency
Δ	Difference
ε	Exergetic efficiency
Subscripts and	superscripts
0	Reference state
ар	Approach point
ĊH	Chemical
cmp	Compressor
D	Destruction
el	Electrical
F	Fuel
g	gth component of functional group
gen	Generator
G	Functional group
in	Inlet
k	kth component
KN	Kinetic
L	Loss
m	Mechanical
М	Mechanical
min	Minimum
mot	Motor
out	Outlet
Р	Product
PH	Physical
PT	Potential
S	Isentropic
sat	At saturation
Т	Thermal
tot	Total
tur	Turbine

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