Dynamic Modeling of CO2 Absorption Process Using Hollow-Fiber Membrane Contactor in MEA Solution

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Abstract: In this work, a comprehensive mathematical model was developed in order to evaluate the CO2 capture process in a microporous polypropylene hollow-fiber membrane countercurrent contactor, using monoethanolamine (MEA) as the chemical solvent. In terms of CO2 chemical absorption, the developed model showed excellent agreement with the experimental data published in the literature for a wide range of operating conditions (R2 > 0.96), 1–2.7 L/min gas flow rates and 10–30 L/h liquid flow rates. Based on developed model, the effects of the gas flow rate, aqueous liquid absorbents’ flow rate and also inlet CO2 concentration on the removal efficiency of CO2 were determined. The % removal of CO2 increased while increasing the MEA solution flow rate; 81% of CO2 was removed at the high flow rate. The CO2 removal efficiency decreased while increasing the gas flow rate, and the residence time in the hollow-fiber membrane contactors increased when the gas flow rate was lower, reaching 97% at a gas flow rate of 1 L · min−1. However, the effect was more pronounced while operating at high gas flow rates. Additionally, the influence of momentous operational parameters such as the number of fibers and module length on the CO2 separation efficiency was evaluated. On this basis, the developed model was also used to evaluate CO2 capture process in hollow-fiber membrane contactors in a flexible operation scenario (with variation in operating conditions) in order to predict the process parameters (liquid and gaseous flows, composition of the streams, mass transfer area, mass transfer coefficient, etc.).

Keywords: dynamic modeling; CO2 absorption processes; hollow-fiber membrane contactors; flexible operation of carbon capture unit

1. Introduction

The greenhouse effect is the overheating of the Earth’s surface and atmosphere, a phenomenon known as global warming [1]. The principal anthropogenic gas with a greenhouse effect is CO2, representing about 76% of total greenhouse gas emissions [2]. In order to achieve the target that was set at the Paris Climate Agreement [3], to limit the global temperature rise to 1.5 °C, the European goal is to eliminate the greenhouse gas emissions by 2050 [4]. One of the best solutions to reduce the CO2 emissions from the main sources is carbon capture [5].

The post-combustion process is the most feasible method of CO2 capture to implement in existing power plants, consisting in capturing the CO2 from flue gases obtained by burning fossil fuels [6]. The absorption processes for post-combustion CO2 capture are the most commonly applied technologies at the commercial scale, due to their lower costs and high efficiency (over 90% capture efficiency) compared with the other available technologies [7,8]. The absorption may be just physical, where the efficiency is based on the solubility of CO2 in the solvent at the work temperature and pressure, or it can include a chemical reaction to increase the CO2 capture efficiency [7]. Overall, the chemical
absorption is used for CO₂ capture from flue gas with low partial pressure in CO₂, due to the high absorption capacity, even if the CO₂ concentration in gas is low [9]. It is important that the chemical reaction that takes place in the absorber is reversible, so that the cost of the absorbent solution can be minimized by thermal regeneration; taking this into consideration, alkanolamine solutions are the most frequently used solvents [10].

Among all alkanolamines, monoethanolamine (MEA) is the most popular solvent in industrial process of CO₂ capture, due to its fast reaction with CO₂, high absorption capacity, ability to minimize the absorption column dimensions, low price and high water solubility. However, using MEA solutions also brings some disadvantages, such as high corrosion, high viscosity at high concentrations, irreversible reactions with O₂, the solvent lost through vaporization, etc. [7,10,11].

In order to overcome some of the disadvantages of using MEA solutions, a number of other technologies for post-combustion CO₂ capture have been studied. These consist in the use of other liquid solvents, among which are: aqueous ammonia solution [12], aqueous piperazine [13], potassium taurate solvent [14] and semi-aqueous monoethanolamine [15]. However, CO₂ absorption using MEA aqueous solutions remains the most technically and economically mature carbon capture technology with the highest probability of being implemented in large-scale applications in the following years.

The flow diagram for the CO₂ capture process using an MEA aqueous solution is presented in Figure 1.

![Figure 1](image-url)

**Figure 1.** A schematic flowsheet configuration of CO₂ capture using aqueous MEA solution in an absorption-desorption gas-liquid process.

The flue gas from the thermal power plant is pretreated, in order to remove the SO₂ and NOₓ formed by burning fossil fuels, and at the same time is cooled. The SO₂ and NOₓ are acid gases that react with MEA and form very stable compounds, thus reducing the capture efficiency of the solvent [16]. After pretreatment, the flue gas rich in CO₂, enters
the absorption column at its base, where it flows in a countercurrent arrangement with
the aqueous MEA solution entered at the top of the column. The gaseous CO$_2$ is absorbed
in the liquid solution, where it reacts with the MEA, forming a stable compound, which
can be transported in the solution to the stripper column. After the absorption, the gas
treated for CO$_2$ is evacuated safely into the atmosphere. The rich solvent, where the CO$_2$
is chemically bonded to the MEA, is pumped into the cross-heat exchanger, where it is
preheated based on the heat released by the regenerated absorbent solution. After being
preheated, the rich solvent enters the stripper column at the top, where, based on the heat
of the steam in the reboiler, the reverse process occurs: the CO$_2$ is released as gas, and
the MEA solution is regenerated. At the top of the stripper column, the gas flow enters a
condenser where the water and MEA condense, and the mixture is separated in a flash
vessel, with the liquid being sent back to the absorber, and at the top a high-purity gaseous
CO$_2$ is formed. The regenerated MEA solution is pumped to the cross-heat exchanger,
being cooled by the rich solvent. In order to maintain the best possible absorption efficiency,
the lean solvent is cooled to the optimal temperature in another heat exchanger. After
cooling, the regenerated solvent is mixed with the fresh MEA solution in the buffer tank,
and then enters the absorption column.

The goal of the process is to purify the flue gases, allowing them to be safely released
into the atmosphere, with the highest possible CO$_2$ capture efficiency at a minimum
cost. In order to increase the efficiency of the CO$_2$ absorption process, several types of
absorbers have been studied in order to increase as much as possible the mass transfer
area between the gas and liquid [7,8,17]. At the industrial level, the most commonly used
technology for the absorption process is the packed-bed column, which creates the largest
mass transfer area possible by choosing the best possible packing material [7,8]. However,
the conventional packed-bed columns have many drawbacks, such as liquid channeling,
flooding at high flow rates, unloading at low flow rates, foaming, entrainment, larger
pressure drops and weak heat transfer [18–20]. In order to overcome these disadvantages,
the use of the hollow-fiber membrane contactors (HFMCs) to intensify the process of
CO$_2$ absorption has been intensively investigated. This technology offers a number of
advantages [17,19,21–23]:

- The mass transfer area is considerably higher than in the packed-bed column, due to
  the large number of fibers inside of the HFMC;
- The gas mixture and the liquid solution are not in direct contact, as the membranes
  physically separate them; this avoids some of the problems caused by the contact
  between phases in conventional columns, such as foaming, flooding, channeling
  and entrainment;
- The surface area between the gas and liquid is known and is constant at large flow
  rate variations;
- Because there is no dispersion of gas into the liquid phase, emulsions do not form;
- After the absorption process, there is no need to have a special section for washing the
  losses of the absorbent solution carried over by the gas;
- There is no density difference required between the gas and liquid, compared to
  traditional columns, where the liquid usually flows gravitationally under its own
  weight and gas flows from the bottom up, due to the lower density;
- The solvent holdup is low, an advantageous feature in the case of using high-cost
  absorbent solutions;
- The membrane module is much more compact, due to a large mass transfer area in a
  small volume;
- The membrane systems are modular, allowing the length of the module to be extended
  by simply adding a new module to the existing one, offering the possibility of operating
  in a wide range of gas flow variation.

Additionally, membrane technology has important techno-economic benefits in com-
parison to chemical and physical absorption (for example, decarbonization of integrated
gasification combined cycle power plants) and, “e.g., greater overall net energy efficiency
(up to about one net percentage point), lower specific capital investment costs (down to 9%), lower operational & maintenance costs (down to 10%), lower electricity production costs (down to 7%), lower CO₂ capture costs (down to 50%)” [24].

However, the use of membranes for CO₂ capture also has some disadvantages, including [21]:

- The membrane introduces a new resistance to mass transfer. This resistance is not found in conventional columns; however, it can be minimized by choosing favorable operating conditions;
- The lifetime of the membranes is short, so the cost of replacing them periodically must be considered;
- Over time, due to the watering of the membranes, the absorption efficiency decreases.

In the absorption of CO₂ using an HFMC, the membrane itself functions just as a separator between the gas mixture and the liquid solvent, and does not play any role in actually separating the CO₂ from the flue gases. The actual separation of CO₂ from the gas mixture occurs because of the properties of the solvent. The mass transfer across the membranes pores is carried out by diffusion due to the gradient concentration of CO₂ between the two phases [8]. A schematic representation of the hollow-fiber membrane contactor for CO₂ absorption, with the countercurrent arrangement for the gas mixture and liquid solution flow, is presented in Figure 2.

![Figure 2](image-url)  
**Figure 2.** Schematic representation of the hollow-fiber membrane contactor for CO₂ absorption process [25].
There are two different ways that the fluids can flow into the HFMC: the gas mixture inside the tube and the liquid solution in the shell compartment (Figure 3a), or the liquid in the tube and the gas in the shell (Figure 3b).

![Image of phase flow model inside the HFMC](image)

**Figure 3.** Phase flow model inside the HFMC. (a). Gas mixture—tube and liquid solution—shell, (b). Liquid solution—tube and gas mixture—shell.

In order to provide timely information about the studied system, with a very short response time, and to predict the system’s dynamic behavior under flexible operating conditions, a detailed mathematical model is needed.

Most of the existing mathematical models presented in the literature for CO₂ capture using an HFMC are developed in a stationary mode of operation and use continuity equations to describe the mass transfer of CO₂ from the gas through the membrane into the liquid [26–30]. This paper brings forward a mathematical dynamic model of the carbon capture process in an MEA solution using a hollow-fiber membrane contactor (HFMC). As a novelty, part of the developed model represents the mass transfer coefficients, which are specifically calculated for the investigated system. Even though a simplified model of the CO₂ capture process using an HFMC was used in this work (the variation in the parameters is considered only along the length of the membranes, and the CO₂ mass transfer through the membrane is described by the partial mass transfer coefficients), the simulations results are in concordance with the experimental data presented in the literature [26]. Additionally, the dynamic modeling and simulation of the investigated system represents a key novel element in comparison to the current state of the art.

2. **Dynamic Modeling of CO₂ Absorption in MEA Solutions**

In the process of CO₂ absorption into an aqueous MEA solution using a hollow-fiber membrane contactor, the following processes take place:

- Transport of CO₂ inside the gas phase to the membrane, by convection and diffusion, in the tube side of the HFMC;
- Diffusion of CO₂ inside the membrane pores due to the concentration gradient formed;
- The CO₂ absorption process occurs in the aqueous MEA solution;
Transported CO$_2$ inside the liquid phase, by convection and diffusion and the chemical reaction with MEA.

In order to develop the dynamic mathematic model, the following assumptions are made [26,31]:

- To describe the fluid mechanics inside the HFMC, the plug flow model is applied, with the model parameters being constants on the radial section of the membranes;
- Both phases are considered to behave like ideal mixtures;
- The laminar flow of the gas mixture inside the membranes and the liquid phase in the shell compartment is considered;
- To calculate the CO$_2$ concentration at the gas–liquid interface, Henry’s law is applied;
- The chemical reaction between CO$_2$ and MEA takes place only in the liquid phase;
- The membranes inside the HFMC are considered to operate in non-wetting mode;
- The heat transfer carried out by radiation and conduction is negligible;
- The pressure drop across the HFMC is negligible;
- To calculate the equivalent circular diameter of the liquid absorbent around the fibers, Happel’s approximation is used. In the shell compartment, the effective diameter of the shell can be calculated with the following equation [26]:

$$d_3 = d_2 \cdot \sqrt{\frac{1}{1 - \phi}}$$  \hspace{1cm} (1)

2.1. Chemical Reaction

The chemical reaction between CO$_2$ and MEA takes place in the liquid phase, in the shell compartment of the hollow-fiber membrane contactor, according to the following reaction equations [32,33]:

$$\text{CO}_2 + 2\text{MEA} \rightleftharpoons \text{MEA}^+ + \text{MEACOO}^-$$ \hspace{1cm} (2)  

$$\text{CO}_2 + \text{H}_2\text{O} \rightleftharpoons \text{H}^+ + \text{HCO}_3^-$$  \hspace{1cm} (3)

The kinetics can be expressed as a second-order reaction, as the first order of each reactant. The reaction rate can be calculated at different temperatures using the following expression [28]:

$$N_R = k \cdot C_{\text{MEA}} \cdot C_{\text{CO}_2}^{\text{l}} = \frac{10^{(10.99 - \frac{2152}{T})}}{1000} \cdot C_{\text{MEA}} \cdot C_{\text{CO}_2}^{\text{l}}$$  \hspace{1cm} (4)

The chemical reaction works as an accelerator of the absorption process; this acceleration is represented in the model through the enhancement factor, $E$, which is calculated with the Kishinevskii correlations [34]:

$$E = 1 + \frac{Ha}{\alpha_1} \cdot [1 - \exp(-0.65 \cdot Ha \cdot \sqrt{\alpha_1})]$$ \hspace{1cm} (5)

$$\alpha_1 = \frac{Ha}{E_{\infty} - 1} + \exp \left[ \frac{0.68}{Ha} - \frac{0.45 \cdot Ha}{E_{\infty} - 1} \right]$$  \hspace{1cm} (6)

$$E_{\infty} = \left( 1 + \frac{1}{b} \cdot \frac{D_B}{D_A} \cdot \frac{C_B}{C_A} \right)^{1/2} \cdot \left( \frac{D_A}{D_B} \right)^{1/2}$$ \hspace{1cm} (7)

where the Hatta module ($Ha$) is calculated with [35]:

$$Ha = \frac{\sqrt{k \cdot C_{\text{MEA}} \cdot D_{\text{CO}_2,l}}}{k_l}$$  \hspace{1cm} (8)
2.2. Balance Equations

The dynamic mathematical model of the CO₂ absorption process using a hollow-fiber membrane contactor consists in the main balance equations presented in Table 1. In addition to the dynamic balance equations and the mass transfer equations, the developed model contains another set of algebraic equations, which calculate the physical-chemical properties of the gas and liquid, such as density, cinematic and dynamic viscosities, specific heat capacities, solubility of CO₂ in the MEA solution, the diffusion coefficients of CO₂ in the gas and liquid phase, etc.

Table 1. Dynamic mathematical model balance equations.

<table>
<thead>
<tr>
<th>Total mass balance</th>
<th>Liquid phase</th>
<th>Gas phase</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\frac{\partial \rho}{\partial t} = -v_L \cdot \frac{\partial \rho}{\partial z} + v_L \cdot \frac{\partial \rho}{\partial z} + \frac{A_L \cdot a \cdot N_{CO_2} \cdot M_{CO_2}}{A_G \cdot a \cdot N_{CO_2} \cdot M_{CO_2}}$</td>
<td>$\frac{\partial \rho}{\partial t} = -v_G \cdot \frac{\partial \rho}{\partial z} - v_G \cdot \frac{\partial \rho}{\partial z}$</td>
</tr>
<tr>
<td>Components’ mass balance</td>
<td>Liquid phase</td>
<td>Gas phase</td>
</tr>
<tr>
<td></td>
<td>$\frac{\partial C}{\partial t} = -v_L \cdot \frac{\partial C}{\partial z} + a \cdot \frac{\partial C}{\partial z} - 2 \cdot N_R$</td>
<td>$\frac{\partial C}{\partial t} = -v_G \cdot \frac{\partial C}{\partial z} + a \cdot \frac{\partial C}{\partial z}$</td>
</tr>
<tr>
<td>Heat balance</td>
<td>Liquid phase</td>
<td>Gas phase</td>
</tr>
<tr>
<td></td>
<td>$\frac{\partial T}{\partial t} = \frac{\partial}{\partial z} \left( \rho C_L \cdot \frac{\partial T}{\partial z} \right) + \frac{\partial}{\partial t} \left( \rho C_L \cdot \frac{\partial T}{\partial t} \right) - \frac{\partial H_{L} \cdot N_{G}}{\partial t \cdot \rho L \cdot c_p L} - \frac{\partial H_{G} \cdot N_{L}}{\partial t \cdot \rho G \cdot c_p G}$</td>
<td>$\frac{\partial T}{\partial t} = \frac{\partial}{\partial z} \left( \rho C_G \cdot \frac{\partial T}{\partial z} \right) + \frac{\partial}{\partial t} \left( \rho C_G \cdot \frac{\partial T}{\partial t} \right) - \frac{\partial H_{G} \cdot N_{L}}{\partial t \cdot \rho L \cdot c_p L} - \frac{\partial H_{L} \cdot N_{G}}{\partial t \cdot \rho G \cdot c_p G}$</td>
</tr>
</tbody>
</table>

$L, G$ represent the liquid and gas phase; $z, t$ represent the space and time dependence of variables.

2.3. Mass Transfer Model

The CO₂ mass transfer flow across the gas–liquid interface is described by the two-film model, and is proportional to the enhancement factor, $E$, the overall mass transfer coefficients of CO₂ inside the gas, $K_G$, and liquid phase, $K_L$, and the CO₂ concentration gradient between the two phases [36–38].

$$N_{CO_2} = E \cdot K_G \cdot \left( C_{CO_2}^{G,e} - C_{CO_2}^{G,e} \right) = E \cdot K_L \cdot \left( C_{CO_2}^{L,e} - C_{CO_2}^{L,e} \right)$$  \hspace{1cm} (16)

where $C_{CO_2}^{G,e}$ and $C_{CO_2}^{L,e}$ are the equilibrium CO₂ concentration in the liquid and gas phase, calculated using Henry’s law:

$$C_{CO_2}^{G,e} = H_{CO_2} \cdot C_{CO_2}^L$$  \hspace{1cm} (17)

$$C_{CO_2}^{L,e} = \frac{C_{CO_2}^G}{H_{CO_2}}$$  \hspace{1cm} (18)

In order to determine the CO₂ mass transfer flow across the gas–liquid interface, we need to estimate the overall mass transfer coefficients inside the liquid and gas phase. The coefficients are calculated based on the mass transfer partial coefficients, the HFMC dimensions and Henry’s coefficient of CO₂ in the MEA solution [29]:

$$\frac{1}{K_L \cdot d_2} = \frac{1}{k_{CO_2,j} \cdot d_2} + \frac{1}{k_{CO_2,m} \cdot H_{CO_2} \cdot d_m} + \frac{1}{k_{CO_2,g} \cdot H_{CO_2} \cdot d_1}$$  \hspace{1cm} (19)

$$\frac{1}{K_G \cdot d_2} = \frac{H_{CO_2}}{k_{CO_2,j} \cdot d_2} + \frac{1}{k_{CO_2,m} \cdot H_{CO_2} \cdot d_m} + \frac{1}{k_{CO_2,g} \cdot H_{CO_2} \cdot d_1}$$  \hspace{1cm} (20)
where \(d_1, d_2\) and \(d_{lm}\) are the inside, outside and logarithmic diameter of the membrane. To calculate Henry’s coefficient of CO\(_2\) in the MEA solution, the following analogy is used [39]:

\[
H_{CO_2,MEA} = H_{N_2O,MEA} \cdot \frac{H_{CO_2,H_2O}}{H_{N_2O,H_2O}}
\]

(21)

\[
H_{N_2O,MEA} = 1.207 \times 10^5 \cdot \exp \left( -\frac{1136.5}{T} \right)
\]

(22)

\[
H_{CO_2,H_2O} = 2.82 \times 10^6 \cdot \exp \left( -\frac{2044}{T} \right)
\]

(23)

\[
H_{N_2O,H_2O} = 8.55 \times 10^6 \cdot \exp \left( -\frac{2284}{T} \right)
\]

(24)

In order to develop the model, the partial mass transfer coefficients of CO\(_2\) inside the gas phase, through the membrane pores and inside the liquid phase \((k_{CO_2,g}, k_{CO_2,m} \text{ and } k_{CO_2,l})\), need to be calculated. The following expressions of the coefficients, specific to the studied system, are presented in the literature.

### 2.3.1. The Partial Mass Transfer Coefficient of CO\(_2\) Inside the Gas Phase—\(k_{CO_2,g}\)

The gas, rich in CO\(_2\), flows through the tube side of the membranes, where the mass transfer is carried out by the convection mechanism, due to the movement of the gas mixture along the length of the membranes, and by the diffusion mechanism, due to the CO\(_2\) concentration gradient obtained by the absorption process in the liquid phase.

The Yang and Cussler correlation is used to predict the value of the partial mass transfer coefficient of CO\(_2\) inside the gas phase [40]:

\[
Sh = \frac{k_{CO_2,g} \cdot d_1}{D_{CO_2,g}} = 1.25 \cdot \left( \frac{Re \cdot d_h}{L} \right)^{0.93} \cdot Sc^{0.33}
\]

(25)

The hydraulic diameter \((d_h)\) depends on the inner diameter of the HFMC module \((d_{mod})\) and number of membranes \((n)\), and is calculated with the following expression [39]:

\[
d_h = \frac{d_{mod}^2 - n \cdot d_2^2}{d_{mod} + n \cdot d_2^2}
\]

(26)

### 2.3.2. The Partial Mass Transfer Coefficient of CO\(_2\) through the Membrane—\(k_{CO_2,m}\)

The membranes inside the HFMC introduce further resistance at the CO\(_2\) mass transfer stage, a resistance that does not occur in the traditional systems for CO\(_2\) absorption, such as packed-bed absorption columns. The mass transfer across the membrane is carried out by diffusion.

According with the experimental data used to validate the model, the operating condition of the membranes inside the HFMC is considered non-wetted [26].

The partial mass transfer coefficient of CO\(_2\) through the non-wetted membrane can be calculated, using the membrane parameters (porosity, thickness and tortuosity), by the following equation [41]:

\[
k_{CO_2,m} = \frac{D_{CO_2,g,m} \cdot \varepsilon}{d \cdot \tau}
\]

(27)

The membrane tortuosity is calculated, based on the membrane porosity, with the following equation [26]:

\[
\tau = \frac{(2 - \varepsilon)^2}{\varepsilon}
\]

(28)
The CO₂ diffusion coefficient inside the membrane pores can be calculated based on the Knudsen \( D_{\text{CO}_2,Kn} \) and the molecular \( D_{\text{CO}_2,M} \) diffusion coefficients, with the following equations [26,42,43]:

\[
\frac{1}{D_{\text{CO}_2,g,m}} = \frac{1}{D_{\text{CO}_2,M}} + \frac{1}{D_{\text{CO}_2,Kn}} \tag{29}
\]

\[
D_{\text{CO}_2,M} = 1200 \cdot \frac{R \cdot T \cdot \mu_M}{M_{\text{CO}_2} \cdot P \cdot \Omega_D \cdot \mu_{\text{CO}_2}} \tag{30}
\]

\[
D_{\text{CO}_2,Kn} = \frac{d_p}{3} \cdot \sqrt{\frac{8 \cdot R \cdot T}{\pi \cdot M_{\text{CO}_2}}} \tag{31}
\]

2.3.3. The Partial Mass Transfer Coefficient of CO₂ Inside the Liquid Phase—\( k_{\text{CO}_2,l} \)

The MEA solution flows through the shell side of the HFMC, where the mass transfer is carried out by the convection mechanism, due to the movement of the liquid mixture along the length of the membranes, and by the diffusion mechanism, due to the CO₂ concentration gradient obtained by the absorption process and the chemical reaction with MEA.

Graetz-Lévêque propose the following equation to predict the partial mass transfer coefficient of CO₂ inside the liquid phase [21]:

\[
Sh = \frac{k_{\text{CO}_2,l} \cdot d_e}{D_{\text{CO}_2,l}} = 1.62 \cdot \left( \frac{d_p^2 \cdot v_L}{D_{\text{CO}_2,l} \cdot L} \right)^{1/3} \tag{32}
\]

The mass transfer coefficients were calculated and compared with those presented in the literature, and similar values were obtained \( k_{\text{CO}_2,g} = 5.2 \times 10^{-3} \text{ m.s}^{-1} \), \( k_{\text{CO}_2,m} = 5.3 \times 10^{-3} \text{ m.s}^{-1} \) and \( k_{\text{CO}_2,l} = 2.2 \times 10^{-4} \text{ m.s}^{-1} \) [26,39,40].

3. Results and Discussions

The hollow-fiber membrane contactor dimensions and properties used in the development process of the model and to validate it are presented in Table 2.

<table>
<thead>
<tr>
<th>Parameter (Unit)</th>
<th>Symbol</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Inner fiber diameter (m)</td>
<td>( d_1 )</td>
<td>3.5 \times 10^{-4}</td>
</tr>
<tr>
<td>Outer fiber diameter (m)</td>
<td>( d_2 )</td>
<td>4 \times 10^{-4}</td>
</tr>
<tr>
<td>Module inner diameter (m)</td>
<td>( d_{\text{mod}} )</td>
<td>1.512 \times 10^{-3}</td>
</tr>
<tr>
<td>Module length (m)</td>
<td>( L )</td>
<td>0.27</td>
</tr>
<tr>
<td>Average pore diameter (µm)</td>
<td>( d_p )</td>
<td>0.1</td>
</tr>
<tr>
<td>Membrane porosity (–)</td>
<td>( \varepsilon )</td>
<td>0.17</td>
</tr>
<tr>
<td>Voidage (–)</td>
<td>( \varphi )</td>
<td>0.93</td>
</tr>
<tr>
<td>Tortuosity (–)</td>
<td>( \tau )</td>
<td>19.7</td>
</tr>
<tr>
<td>Number of fibers (–)</td>
<td>( n )</td>
<td>510</td>
</tr>
<tr>
<td>Membrane thickness (m)</td>
<td>( \delta )</td>
<td>2.5 \times 10^{-5}</td>
</tr>
</tbody>
</table>

Table 2. Polypropylene HFMC module properties [26].

The operating conditions of the hollow-fiber membrane contactor for the CO₂ absorption process in an aqueous MEA solution used in the simulations are presented in Table 3.

Using the HFMC properties and the operating conditions presented in Tables 2 and 3, as well as the physical properties of the gas and liquid phase, the developed dynamic mathematical model presented in Section 2 was implemented in MATLAB/Simulink. The partial differential equations, which describe the mass and energy variations in the time and space of the parameters, presented in Table 1, were transformed into total differential equations using a numerical method for discretization.
Table 3. Operating conditions of HFMC [26].

<table>
<thead>
<tr>
<th>Parameter (Unit)</th>
<th>Symbol</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pressure (bar)</td>
<td>$P$</td>
<td>1</td>
</tr>
<tr>
<td>Temperature (K)</td>
<td>$T$</td>
<td>298.15</td>
</tr>
<tr>
<td>Liquid flow rate (L · h$^{-1}$)</td>
<td>$Q_L$</td>
<td>10 − 30</td>
</tr>
<tr>
<td>Gas flow rate (L · min$^{-1}$)</td>
<td>$Q_G$</td>
<td>1 − 2.75</td>
</tr>
<tr>
<td>Gas composition (—)</td>
<td>$y_{CO_2}$, $y_{CH_4}$</td>
<td>0.1, 0.9</td>
</tr>
<tr>
<td>MEA concentration (wt%)</td>
<td>$C_{MEA}$</td>
<td>5</td>
</tr>
</tbody>
</table>

The available experimental data from the literature, which were used to validate the mathematical model [26], consider a CO$_2$/CH$_4$ gas mixture to be purified by CO$_2$ absorption using an HFMC; however, the same developed mathematical model could also be used to evaluate the CO$_2$ removal efficiency of the HFMC from flue gases.

A block flow diagram representing the used algorithm is presented in Figure 4.

3.1. Model Validation

In order to confirm that the model gives correct information about the CO$_2$ absorption process using an HFMC in an MEA solution, the simulation results were compared with experimental data published in the literature [26] (Figures 5 and 6). The validation of the...
model was realized via evaluating the CO₂ removal efficiency of the HFMC at different gas and liquid flow rates, being calculated with the following equation:

\[
\text{CO}_2 \text{ removal efficiency (\%) } = \frac{C_{\text{CO}_2,\text{in}} - C_{\text{CO}_2,\text{out}}}{C_{\text{CO}_2,\text{in}}} \cdot 100
\]  

(33)

**Figure 5.** CO₂ removal efficiency at different gas flow rates, \(Q_L = 25 \text{ L} \cdot \text{h}^{-1}\).

**Figure 6.** CO₂ removal efficiency at different liquid flow rates, \(Q_G = 2 \text{ L} \cdot \text{min}^{-1}\).

The CO₂ removal efficiency at different gas flow rates, evaluated at a constant liquid flow rate (25 L · h⁻¹), is represented in Figure 5. When the gas flow rate was lower, the residence time in the HFMC increased, and the CO₂ removal efficiency was substantially higher, reaching 97% at a gas flow rate of 1 L · min⁻¹. When the gas flow rate was increased to 2.75 L · min⁻¹, the CO₂ removal efficiency considerably decreased to 66%.
The simulation results and experimental data in terms of CO₂ removal efficiency for a wide range of liquid flow rates, keeping the gas flow rate constant at 2 L · min⁻¹, are represented in Figure 6. When the liquid flow rate was increased from 10 L · h⁻¹ to 30 L · h⁻¹, the removal efficiency increased, as we expected, from 64% to 81%.

As shown in Figures 5 and 6, the developed model gives a good approximation of the CO₂ absorption process using an HFMC; compared to the experimental data, the correlation coefficient obtained is R² > 0.96. It can be concluded that the developed model of the CO₂ absorption process, in an MEA solution, using a hollow-fiber membrane contactor, provides a good approximation of the system, and can be further used to predict the behavior of the system in a wide range of operating conditions.

3.2. Steady-State Profiles

Based on the simulation results, the variation in the parameters over the module length was predicted for different operating condition scenarios. As we expected, in the gas–liquid absorption process, both parameters, gas flow rate (blue line in Figure 7) and CO₂ concentration, (red line in Figure 7), decreased over the module length in the gas phase, due to the CO₂ absorption into the liquid solvent. At the same time, the CO₂ removal efficiency increased over the length of the module due to the absorption of CO₂, and the concentration of MEA in the liquid phase decreased, due to the chemical reaction with the absorbed CO₂ (Figure 8). The liquid solvent flows in the shell compartment of the HFMC, in a countercurrent with the gas mixture. The CO₂ concentration inside the gas phase decreased from the initial 10% vol. to nearly 1% vol.

3.2.1. Influence of the Number of Membranes on the CO₂ Removal Efficiency

When increasing the number of fibers inside the HFMC, the mass transfer area between the gas and liquid significantly increased, having a positive effect on the absorption efficiency. The effect of the number of fibers inside the HFMC on the CO₂ removal efficiency for different gas flow rates, at a constant liquid flow rate (25 L · h⁻¹), is represented in Figure 9. Additionally, different liquid flow rates, holding the gas flow rate constant at 2 L · min⁻¹, are represented in Figure 10. At a gas flow rate of 1 L · min⁻¹, the CO₂ removal efficiency increased from 35% at 150 fibers inside the HFMC to nearly 99% at 700 fibers. The positive increase in the absorption efficiency was consistent at different gas flow rates when the number of fibers inside the HFMC was increased, as shown in Figure 9. The positive
effect of more fibers inside the module can also be noticed in the case of changing the liquid
flow rate (increasing the CO\textsubscript{2} removal efficiency from 20\% at 150 fibers to 90\% at 700 fibers,
in the case of a 2 L\text{·}min\textsuperscript{-1} gas flow rate), with the results being presented in Figure 10. It
needs to be considered, for an industrial scale up, that when increasing the liquid flow
rate, the energy consumption with amine regeneration will increase, and furthermore, the
replacement cost for a large number of fibers is high (the lifetime of the membranes is
short). Thus, a compromise must be considered between the liquid flow rate and number
of fibers used to achieve the desired CO\textsubscript{2} removal efficiency.

Figure 8. CO\textsubscript{2} removal efficiency and MEA concentration in liquid phase over the module length,
\(Q_L = 25\text{ L·h}^{-1}\).

Figure 9. Effect of the number of fibers on the CO\textsubscript{2} removal efficiency at different gas flow rates,
\(Q_G = \text{2 L·min}^{-1}\).

Figure 10. Effect of the number of fibers on the CO\textsubscript{2} removal efficiency at different liquid flow rates,
\(Q_G = \text{3 L·min}^{-1}\).
3.2.2. Influence of the Module Length on the CO\textsubscript{2} Removal Efficiency

In determining the optimal operating conditions, the length of the module could be easily modified, in comparison with the number of fibers inside the HFMC, due to the membrane modularity, offering the possibility of extending the module by simply adding a new one, continuing the existing one \[21\].

The effect of the module length on the CO\textsubscript{2} removal efficiency, for different gas flow rates (from 1 to 3 L \cdot \text{min}^{-1}) and liquid flow rates (from 10 to 30 L \cdot \text{h}^{-1}), is presented in Figures 11 and 12.

![Figure 11](image)

**Figure 11.** Effect of the module length on the CO\textsubscript{2} removal efficiency at different gas flow rates, \(Q_G = 25 \text{ L} \cdot \text{h}^{-1}\).
The effect of the module length on the CO$_2$ removal efficiency, for different gas flow rates (from 1 to 3 L·min$^{-1}$) and liquid flow rates (from 10 to 30 L·h$^{-1}$), is presented in Figures 11 and 12.

As we expected, by increasing the length of the HFMC, the CO$_2$ removal efficiency was increased, due to the increase in the residence time in the module, resulting in a higher surface area between the gas and liquid.

Initially, a small increase in the length of the module showed a significant increase in the CO$_2$ removal efficiency, at a liquid flow rate of 1.5 L·min$^{-1}$. The CO$_2$ removal efficiency was increased from 62% at 0.1 m to nearly 90% at 0.3 m of the module length. When the length of the module continued to increase, the CO$_2$ removal efficiency reached the value of nearly 98% at a module length of 0.8 m. As seen in Figure 11, the CO$_2$ removal efficiency was increased by 28% (from 62% to 90%) with the addition of 0.2 m in fiber length (from 0.1 to 0.3 m), and after the addition of another 0.5 m (from 0.3 to 0.8 m), the CO$_2$ removal efficiency increased by only 8% (from 90% to 98%). This can be explained by the fact that the CO$_2$ concentration gradient is higher on the inlet side of the system, and when the gas advances into the HFMC, the CO$_2$ partial pressure in the gas phase decreases, due to the absorption in the liquid phase; as a result, the overall process velocity also decreases, requiring a longer contact time between the phases to obtain an increase in the efficiency of removing the CO$_2$ from the gas.

The same effect was observed when the liquid flow rate was changed (Figure 12). At a liquid flow rate of 25 L·h$^{-1}$, the CO$_2$ removal efficiency increased from 50%, at a module length of 0.1 m, to nearly 95% at a module length of 0.8 m.

It can be concluded that the length of the HFMC is an important factor in the efficiency of the absorption process; when increasing the length, leading to an increase in the contact time between the two phases, the impact of the CO$_2$ removal efficiency is positive. However, it should be considered that a CO$_2$ removal efficiency value greater than 90% requires longer fiber lengths, which leads to a higher operation/capital cost.

3.3. Dynamic Behavior

3.3.1. The System Response at Step Signal on the Gas Flow Rate

Due to the dynamic production process of electricity by power plants, the flow rate of the flue gases and the concentration in CO$_2$ change over time [16]. It is important to predict the HFMC system’s response to these variations; thus, the application of step and ramp signals was considered.
In the first evaluated scenario, increasing and decreasing the inlet flue gas flow rates by 20% (from 2 L · min⁻¹), as a step function, was considered (Figure 13). The system response to the step function is represented in Figures 14 and 15.

**Figure 13.** Step signal for intel flue gas scenario (increase/decrease).

**Figure 14.** CO₂ concentration in gas (on the left, represented by solid lines) and CO₂ removal efficiency (on the right, represented by the dashed lines) over the module length (increase/decrease scenarios of gas flow rate).
As shown in Figure 14, when the gas flow was increased, the concentration of CO\(_2\) in the gas phase increased along the module length, and the absorption efficiency decreased by approximately 8%. The effect can be explained by the decrease in the residence time in the absorber. The system reacts oppositely when the gas flow rate decreased by 20%, with the absorption efficiency increasing by approximately 9%.

Because of the increase in the gas flow rate, the quantity of CO\(_2\) absorbed increased, which led to a decrease in the MEA concentration (Figure 15), and the opposite effect occurred when the gas flow rate decreased.

3.3.2. The System Response at Ramp/Oscillatory Signal on the Gas Flow Rate

In order to be able to analyze the performance of the absorption system in a flexible scenario, an oscillatory change in the flue gas flow, over time, was considered (in Figure 16). This scenario was created to reproduce the variations in the flue gas flow, due to the increase and decrease in energy demand for the 24 h period (during the day, the energy demand is higher than at night) [44]. A simulation time of 75 h was considered to be able to represent three full cycles of 24 h. The variation in the gas flow rate was increased by 25% during the day, compared to the nominal value of \(Q_g = 1.5 \text{ L} \cdot \text{min}^{-1}\), and a decrease with the same value occurred during the night. The increase and the decrease in the gas flow rate was achieved in the form of a ramp signal for a period of 3 h. The response of the system shows that when the gas flow rate increases by 25%, the CO\(_2\) removal efficiency decreases by approximately 7%, and the CO\(_2\) concentration in gas released into the atmosphere increases from 0.42 mol \cdot m\(^{-3}\) to 0.7 mol \cdot m\(^{-3}\).
increase and decrease in energy demand for the 24 h period (during the day and at part-load or even shut down during the night). Therefore, the developed dynamic model was used to simulate the transient behavior of the CO₂ absorption system due to an oscillatory change in the flue gas flow. In a flexible operation scenario of an absorption system, it was observed that the CO₂ removal efficiency changed by approximately 7% during 24 h period.

The developed model could be used to evaluate the CO₂ capture process in hollow-fiber membrane contactors for wide range of operating conditions in order to predict with accuracy the process parameters (liquid and gaseous flows, composition of the streams, mass transfer coefficient, etc.).

4. Conclusions

A complex mathematical model for CO₂ capture in MEA solutions, using a hollow-fiber membrane contactor, has been developed. The mass transfer coefficients were calculated and compared with those presented in the literature, and similar values were obtained. For a wide range of gas and liquid flow rates, the simulation results were compared with experimental data published in the literature. In terms of CO₂ removal efficiency, a good correlation was observed ($R^2 > 0.96$).

Based on the developed model, the effect of the number and length of the fibers on CO₂ removal efficiency was evaluated. By increasing the number of fibers inside the HFMC, the mass transfer area between the gas and liquid was significantly increased, having a positive effect on the CO₂ absorption efficiency. The CO₂ removal efficiency increased from 20% at 150 fibers to 98% at 700 fibers due to the change in the gas flow rate (1 to 3 L·min⁻¹) and liquid flow rate (10 to 30 L·h⁻¹). The length of the HFMC is an important factor in the efficiency of the absorption process. The increased fiber module length led to an increase in the contact time between the two phases with a positive impact on the CO₂ removal efficiency. However, it should be considered that a CO₂ removal efficiency greater than 90% requires longer fiber lengths, which leads to higher operational/capital costs, due to the fact that the lifetime of the membranes is not too long.

Usually, the power plant is operated at full capacity during the day and at part-load or even shut down during the night. Therefore, the developed dynamic model was used to simulate the transient behavior of the CO₂ absorption system due to an oscillatory change in the flue gas flow. In a flexible operation scenario of an absorption system, it was observed that the CO₂ removal efficiency changed by approximately 7% during 24 h period.

The developed model could be used to evaluate the CO₂ capture process in hollow-fiber membrane contactors for wide range of operating conditions in order to predict with accuracy the process parameters (liquid and gaseous flows, composition of the streams, mass transfer coefficient, etc.).

Author Contributions: Conceptualization, A.-C.B., A.-M.C., S.D. and C.D.; Investigation, A.-C.B., A.-M.C. and S.D.; Resources, C.-C.C.; Supervision, A.-M.C. and C.-C.C.; Validation, A.-C.B.; Visualization, S.D. and C.-C.C.; Writing—original draft, A.-C.B. and A.-M.C.; Writing—review & editing, A.-C.B., A.-M.C., C.D. and C.-C.C. All authors have read and agreed to the published version of the manuscript.

Funding: The research leading to these results received funding from the NO Grants 2014–2021, under project contract no. 13/2020 and from a grant from the Romanian Ministry of Education and Research, CCCDI—UEFISCDI, project number PN-III-P4-ID-PCE-2020-0632, within PNCDI III.

Informed Consent Statement: Not applicable.

Conflicts of Interest: The authors declare no conflict of interest.
### Nomenclature

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
</tr>
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<tbody>
<tr>
<td>$a_e$</td>
<td>effective mass transfer area [$m^2/m^3$]</td>
</tr>
<tr>
<td>$A_G, A_L$</td>
<td>tube (G) and shell (L) transversal section area [$m^2$]</td>
</tr>
<tr>
<td>$b$</td>
<td>MEA stoichiometric coefficient ($b = 2$)</td>
</tr>
<tr>
<td>$C_{CO_2}, C_{LCO_2}$</td>
<td>$CO_2$ molar concentration in gas and liquid phase [$kmol/m^3$]</td>
</tr>
<tr>
<td>$C_{GCO_2}, C_{LCO_2}$</td>
<td>equilibrium $CO_2$ molar concentration in gas and liquid phase [$kmol/m^3$]</td>
</tr>
<tr>
<td>$C_{MEA}, C_B$</td>
<td>MEA molar concentration in liquid phase [$kmol/m^3$]</td>
</tr>
<tr>
<td>$C_i$</td>
<td>$CO_2$ molar concentration at the gas–liquid interface [$kmol/m^3$]</td>
</tr>
<tr>
<td>$C_{MEA}, C_{BMEA}$</td>
<td>molar concentration in liquid phase [$kmol/m^3$]</td>
</tr>
<tr>
<td>$C_{GCO_2}, C_{LCO_2}$</td>
<td>$CO_2$ molar concentration in gas and liquid phase [$kmol/m^3$]</td>
</tr>
<tr>
<td>$d_1$</td>
<td>inner fiber diameter of membrane [m]</td>
</tr>
<tr>
<td>$d_2$</td>
<td>outer fiber diameter of membrane [m]</td>
</tr>
<tr>
<td>$d_3$</td>
<td>effective diameter of shell [m]</td>
</tr>
<tr>
<td>$d_h$</td>
<td>hydraulic diameters of HFMC [m]</td>
</tr>
<tr>
<td>$d_{lm}$</td>
<td>logarithmic mean diameter of membrane [m]</td>
</tr>
<tr>
<td>$d_{mod}$</td>
<td>module inner diameter [m]</td>
</tr>
<tr>
<td>$d_p$</td>
<td>average pore diameter [m]</td>
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<tr>
<td>$d_e$</td>
<td>average inner diameter of shell [m]</td>
</tr>
<tr>
<td>$D_{CO_2,G}, D_{CO_2,L}$</td>
<td>diffusion coefficient of $CO_2$ in gas and liquid phase [$m^2/s$]</td>
</tr>
<tr>
<td>$D_{CO_2,G,m}$</td>
<td>diffusion coefficient of $CO_2$ in membrane pores [$m^2/s$]</td>
</tr>
<tr>
<td>$D_{CO_2,Kn}, D_{CO_2,M}$</td>
<td>Knudsen and molecular $CO_2$ diffusion coefficient [$m^2/s$]</td>
</tr>
<tr>
<td>$D_{A,G}, D_{B}$</td>
<td>diffusion coefficient of $CO_2$ and MEA in liquid phase [$m^2/s$]</td>
</tr>
<tr>
<td>$E$</td>
<td>enhancement factor [-]</td>
</tr>
<tr>
<td>$F_G, F_L$</td>
<td>gas and liquid flow rate [$m^3/s$]</td>
</tr>
<tr>
<td>$h$</td>
<td>heat transfer coefficient [W/m$^2$ K]</td>
</tr>
<tr>
<td>$Ha$</td>
<td>Hatta module [-]</td>
</tr>
<tr>
<td>$H_{CO_2}, H_{CO_2,MEA}$</td>
<td>Henry’s coefficient of $CO_2$ in the MEA solution [-]</td>
</tr>
<tr>
<td>$k$</td>
<td>reaction rate constant [$m^3/kmol s$]</td>
</tr>
<tr>
<td>$k_{CO_2,G}$</td>
<td>partial mass transfer coefficient of $CO_2$ inside the gas phase [m/s]</td>
</tr>
<tr>
<td>$k_{CO_2,m}$</td>
<td>partial mass transfer coefficient of $CO_2$ through the membrane [m/s]</td>
</tr>
<tr>
<td>$k_{CO_2,L}, k_I$</td>
<td>partial mass transfer coefficient of $CO_2$ inside the liquid phase [m/s]</td>
</tr>
<tr>
<td>$K_{G}, K_{L}$</td>
<td>overall mass transfer coefficient of $CO_2$ inside the gas and liquid phase [m/s]</td>
</tr>
<tr>
<td>$L$</td>
<td>module length [m]</td>
</tr>
<tr>
<td>$M_{CO_2}$</td>
<td>$CO_2$ molecular weight [kg/kmol]</td>
</tr>
<tr>
<td>$N_{CO_2}$</td>
<td>$CO_2$ molar flow across the gas–liquid interface [$kmol/m^3 s$]</td>
</tr>
<tr>
<td>$N_R$</td>
<td>reaction rate of $CO_2$ and MEA [$kmol/m^3 s$]</td>
</tr>
<tr>
<td>$n$</td>
<td>number of fibers [-]</td>
</tr>
<tr>
<td>$P$</td>
<td>pressure [atm]</td>
</tr>
<tr>
<td>$Re$</td>
<td>Reynolds number [-]</td>
</tr>
<tr>
<td>$Q_{G}, Q_{L}$</td>
<td>gas and liquid flow rate [L/min], [L/h]</td>
</tr>
<tr>
<td>$Sc$</td>
<td>Schmidt number [-]</td>
</tr>
<tr>
<td>$Sh$</td>
<td>Sherwood number [-]</td>
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<tr>
<td>$T_{G}, T_{L}$</td>
<td>liquid and gas temperature [K]</td>
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<tr>
<td>$v_{G}, v_{L}$</td>
<td>gas and liquid velocity [m/s]</td>
</tr>
<tr>
<td>$y_{CO_2,0}, y_{CH_4,0}$</td>
<td>inlet $CO_2$ and $CH_4$ molar fraction in gas phase [-]</td>
</tr>
<tr>
<td>MT</td>
<td>mass transfer</td>
</tr>
<tr>
<td>PMT, GMT</td>
<td>partial and global mass transfer</td>
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### Greek Symbols

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Definition</th>
</tr>
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<tbody>
<tr>
<td>$\Delta H_r$</td>
<td>reaction heat [kJ/kmol]</td>
</tr>
<tr>
<td>$\delta$</td>
<td>membrane thickness [m]</td>
</tr>
<tr>
<td>$\varepsilon$</td>
<td>membrane porosity [-]</td>
</tr>
<tr>
<td>$\mu_{CO_2}$</td>
<td>dynamic viscosity of $CO_2$ [Pa s]</td>
</tr>
<tr>
<td>$\nu_{L}$</td>
<td>kinematic viscosity of liquid phase [$m^2/s$]</td>
</tr>
<tr>
<td>$\rho_{G}, \rho_{L}$</td>
<td>gas and liquid density [kg/m$^3$]</td>
</tr>
<tr>
<td>$\tau$</td>
<td>membrane tortuosity [-]</td>
</tr>
<tr>
<td>$\Omega_{\mu}, \Omega_D$</td>
<td>viscosity and diffusion collision integrals [-]</td>
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