Article

Study on the Effects of Selected Factors on the Diagonal Tensile Strength of Oblique Corner Furniture Joints Constructed by Wood Dowel

Wen-Gang Hu 1,2,*, Mengyao Luo 2, Miaomiao Hao 2, Bin Tang 3 and Chuan Wan 3

1 Co-Innovation Center of Efficient Processing and Utilization of Forest Resources, Nanjing Forestry University, Nanjing 210037, China
2 College of Furnishing and Industrial Design, Nanjing Forestry University, Nanjing 210037, China
3 MACIO Home Co., Ltd., Chongqing 401346, China
* Correspondence: hwg@njfu.edu.cn

Abstract: The oblique corner joints (OCJ) of wood-frame furniture doors crack easily during common usage due to external loads or changes in temperature and humidity. Aiming to solve this technology issue, the effects of the selected factors, i.e., material type (MT), diameter of dowel hole (DDH), moisture content of dowel (MCD), and distance between two dowels (DTD), on the diagonal tensile strength of the oblique corner joint (OCJ), were investigated experimentally and optimized based on the response surface method. The results showed that there were two typical mechanical behaviors of OCJs when subjected to diagonal tensile loads, according to load and displacement curves and failure modes. The critical crack strength, $F_c$, and ultimate strength, $F_u$, of samples made of heat-treated alder were smaller than those of samples made of control alder. DDH had a significant effect on $F_c$ but not on $F_u$, while the effect of DTD on both $F_c$ and $F_u$ was significant. The $F_c$ defined in this study was a better indicator for evaluating the crack load resistance of OCJs than $F_u$. The OCJs constructed by double dowels were significantly greater than those of single dowels. The optimal parameters for constructing the OCJs were obtained: MT was the control wood material, DDH was 7.8 mm, double dowels with a DTD of 27 mm, and the MCD should be higher than that of the base material.

Keywords: wood furniture; diagonal tension; wood dowel; structure optimization; heat treatment

1. Introduction

Wood is a natural, environmentally friendly, porous material widely utilized in wood construction and wood products [1–3]. It is the natural properties of wood that seriously influence the quality, appearance, and strength of wood products, such as wood furniture, doors, and windows [4–12].

Many studies have been trying to improve the strength, appearance, and quality of wood products, mainly using the modification method and the structure reinforcement method. The modification method mainly adopted chemical modification [13–15] and heat-treated methods [16–18], which aimed to improve the strength, dimensional stability, and appearance of wood lumber. Meanwhile, modification methods often increase the cost of wood products to a high degree. The structure-reinforced method commonly investigates factors influencing the strength of joints used in wood products and proposes new jointing methods to improve them. Among these studies, the strength of furniture joints, especially mortise-and-tenon joints [19–21] and wood dowel joints [22–26], occupied a large proportion. By contrast, using the structure reinforced method commonly brings less cost than the modification method and is more environmentally friendly.

Commonly, there are three typical jointing forms used in jointing the corner of a wood door: straight (Figure 1a), oblique (Figure 1b), and a combination of straight and oblique (Figure 1c). From the feedback of the market, the oblique jointing forms of wood furniture
doors prevailed most among these three types. In practice, it is the oblique corner joint (OCJ) that cracks easier than the other two types (Figure 1d), which seriously influences the appearance and quality of wood furniture doors. Many furniture enterprises were suffering from this issue and trying to use other joint types instead of the OCJ. However, this means that the appearance of the OCJ must be sacrificed. Obviously, it is tough work to make a trade-off between the prevailing appearance and quality of wood furniture doors, but we have to make a decision.

![Figure 1. Typical jointing methods for corner joints for wood furniture doors are: straight (a), oblique (b), combination of straight and diagonal (c), and typical failure modes of corner joints (d).](image)

Although the heat-treated method was widely used in the wood products industry to improve dimensional stability, the mechanical strengths of wood and wood joints usually decreased [27–29]. Therefore, the strength of wood joints needs to be improved, especially when they are made of heat-treated wood. This is another dilemma that enterprises face when making a trade-off between dimensional stability and strength of joints when using heat-treated wood in the manufacture of the OCJ. However, studies on the crack load resistance of the OCJ were rarely observed, especially considering heat-treated wood and some critical technology parameters of the OCJ.

In order to solve this dilemma, we attempted to improve this impossible position from the perspective of structure optimization. Therefore, the main aim of the study was to further investigate the main factors influencing the crack load resistance of the OCJ and propose the optimal connecting parameters of the OCJ for wood furniture doors. The specific work conducted included the following matters: (1) the effect of the selected factors, i.e., material type (MT), moisture content of dowel (MCD), and diameter of dowel hole (DDH), on the diagonal tensile strength of the OCJ; (2) the technology parameters of the OCJ were optimized by the response surface method; (3) the OCJ was further improved by using double dowels, and the effect of distance between two dowels (DTD) on the strength of the OCJ was studied. Finally, improved technology parameters for constructing the OCJ were proposed.

2. Materials and Methods

2.1. Wood Materials

The material type (MT) used in this study was alder (*Alnus cremastogyne* Burk.) and heat-treated alder provided by the MACIO Home Co., Ltd. (Chongqing, China). The main procedures of heat treatment were that (1) the wood sample started heating at 40 °C and increased gradually to 135 °C with an increment of 5 °C equally with a 1.5 h duration for each temperature point; (2) the temperature eventually increased to 140 °C and was kept for 10 h. Therefore, the whole heat-treated cycle was nearly 40 h; (3) and then the wood lumbers were moved out and cooled at the environmental temperature for 12 h; (4) the
wood lumbers were put into a chamber with a constant temperature of 25 °C and humidity of 60% for 10 days. The glue used in constructing the oblique corner joint (OCJ) was PVAc with a solid content of 50%.

2.2. Specimen Preparation

Figure 2 shows the main procedure for preparing samples and the configurations of samples evaluated. The wood furniture door frame was constructed with a wood dowel and “male and female tenon” (MFT) with PVAc glue applied. The main procedure of processing the OCJ was that (1) wood lumbers were cut into members (Figure 2a) of a wood furniture door; (2) the members of the door were constructed by the MFT and a dowel synchronizing with glue (Figure 2b); (3) the wood furniture door frame was constructed firmly and stored in the wood shop until the glue completely dried (Figure 2c); (4) each door frame was cut into four OCJ samples equally, and two load-applied holes were drilled at the end of the members (Figure 2d) for fixing on the universal testing machine.

Figure 2. Procedure for preparing a sample: members of the door (a), constructing method (b), wood furniture door frame (c), corner joint of the door (d).

Figure 3 shows the specific dimensions of the OCJ sample. The dimensions of the L-shape sample measured 250 mm long × 68 mm wide × 22 mm thick, with a hole measuring 20 mm in diameter at the ends of two members at a distance of 40 mm. The wood dowel was made of alder with dimensions of 50 × 8 mm (length × diameter). The dowel hole was a variable in this study; in Figure 3, a male and female tenon (MFT) with a diameter of 8.5 mm (with dowel holes) was presented as an example.

Figure 3. Dimensions of samples: (a) L-shape sample; (b) male and female tenon.

2.3. Experimental Design

A complete $2 \times 3 \times 3$ factorial experiment was designed to investigate the effects of material type (MT) (control and heat-treated alder), moisture content of wood dowel
(MCD) (6.72%, 8.45%, and 12.02%), and diameter of dowel hole (DDH) (7.8 mm, 8 mm, and 8.5 mm) on the diagonal tensile strength of the OCJ. Furthermore, single factorial experiments were designed to further study the effect of dowel number on the strength of OCJs based on the results of the preliminary optimization tests. In preliminary optimization tests, 12 replications were evaluated for each combination; thus, there were 216 total samples tested. In secondary optimization tests, there were 120 samples evaluated, with 12 replications repeated for each combination.

2.4. Testing Method

Figure 4 shows the setup for measuring the diagonal tensile strength of the OCJ of a furniture door using a universal testing machine (WDW-30 Kn, Tianchen, China) synchronized with a camera to record the crack of the OCJ. The loading speed was set at 10 mm/min until the joint completely failed. The critical crack load and ultimate load of OCJs were recorded when the OCJ initially cracked and completely failed, respectively. In addition, the moisture content (MC) and density of the OCJ samples were measured according to ASTM D4442 [30] and ASTM D2395 [31].

![Figure 4. Setup for measuring the diagonal tensile strength of the oblique corner joint.](image)

2.5. Statistical Analysis

The effects of MT, MCD, and DDH on the diagonal tensile strength of OCJs were statistically analyzed using the analysis of variance (ANOVA) and generalized linear model (GLM) procedures. Mean comparisons using the chi-square statistic testing multiple comparison procedure were performed based on SPSS (22, IBM, USA) if any significant factors were observed. The optimal parameters for constructing OCJs were analyzed based on the response surface method using Design Expert (Version 12, Stat-Ease, Inc., Minneapolis, MN, USA). All statistical analyses were performed at the 5% significance level.

3. Results and Discussion

3.1. Density and Moisture Content

The density and moisture content (MC) of control alder and heat-treated alder are shown in Table 1. It can be found that the MC of control samples reduced significantly compared with heat-treated samples, which was consistent with the results of previous
Table 1. Density and moisture content of wood evaluated in this study.

<table>
<thead>
<tr>
<th>Material Type</th>
<th>Density (g/cm$^3$)</th>
<th>MC %</th>
</tr>
</thead>
<tbody>
<tr>
<td>Control</td>
<td>0.74 (2.5)</td>
<td>9.69 (2.4)</td>
</tr>
<tr>
<td>Heat-treated</td>
<td>0.68 (5.5)</td>
<td>9.22 (2.7)</td>
</tr>
</tbody>
</table>

Note: The values in parenthesis are COV in percentage.

3.2. Typical Mechanical Behaviors of Oblique Corner Joints

Figure 5 shows the load-displacement curves of all 216 tested samples in each group. To further characterize the mechanical behavior of the OCJs, each load-displacement curve was plotted in Origin software and analyzed based on the changes in stiffness (slope). Meanwhile, the critical load points and corresponding values were extracted.

Figure 5. Load-displacement curves of all tested oblique corner joint samples.

There were two typical mechanical behaviors of oblique corner joints (OCJ) when subjected to the diagonal tensile load. Figure 6 shows these two typical load and displacement curves, named Mode A and Mode B, with their corresponding failure processes at critical load points. Meanwhile, these two typical failure modes were further analyzed and discussed as follows:

In the case of Mode A (Figure 6a), the load and displacement curve included two linear stages divided by the first proportional limit load point ($F_{p1}$) and the second proportional limit load point ($F_{p2}$). According to the recording video and observations of sample failure processes, the critical crack load of the OCJ was defined as the load corresponding to the intersection of the tangential lines of the first elastic portion and the second elastic portion in the load and displacement curve and named as critical crack strength, $F_c$. Figure 6(a1–a3) shows the status of the sample corresponding to the critical load points of $F_c$, $F_u$, and complete failure of OCJs, respectively. In addition, the final failure of Mode A resulted from the fracture of a single dowel.
By contrast, Figure 6b shows the other typical mechanical behavior of OCJs, named Mode B. It was obvious that there was a slide of displacement in the load and displacement curve. Therefore, the turning point, $F_c$, was defined as the critical crack strength of the OCJ. Figure 6(b1–b3) shows the status of the OCJ corresponding to the critical load points of $F_c$, $F_u$, and complete failure, respectively. Compared with Mode A, the final failure of Mode B resulted from the withdrawal of the single dowel. There were 159 samples fractured in failure Mode A, and 57 samples failed in failure Mode A, which suggested that most samples failed resulting from the fracture of dowels and a minority fractured because of the withdrawal of dowels. Meanwhile, the number of sample fractures in failure Mode A was greater than those in failure Mode B for each tested group, which indicated that manufacturing technology was relatively stable.

It is noteworthy that the critical crack strength, $F_c$, and ultimate strength, $F_u$, of Mode A were nearly the same as those of Mode B. Furthermore, when the external load reached the point of $F_u$, the corner joint cracked. Therefore, it seemed that $F_u$ could not be a good indicator for evaluating the crack load resistance of the OCJ. By contrast, $F_c$ was the turning point of the elastic stiffness of the OCJ, which could reflect the crack load resistance better.

3.3. Diagonal Tensile Strength of Oblique Corner Joints

Table 2 shows the results of the analysis of variance (ANOVA) for the diagonal strength of the OCJs on three factors, which indicates that the diameter of the dowel hole (DDH) has the main effect on $F_c$. The interaction effects of moisture content of dowel (MCD) and material type (MT) and those of MCD and DDH have significant effects on $F_c$. By contrast, there was no main effect on $F_u$, but the interaction effects of MCD and MT and MT and DDH on $F_u$ were statistically significant. The above ANOVA results indicated that $F_c$ was more sensitive than $F_u$ to the factors evaluated. In order to further analyze the results, multiple comparisons of diagonal tensile strengths for OCJs were conducted.
Table 2. Summaries of ANOVA results for critical crack strength and ultimate strength of oblique corner joints constructed by one dowel through a generalized linear model on three factors.

<table>
<thead>
<tr>
<th>Factor</th>
<th>( p )-Value</th>
<th>( F_c )</th>
<th>( F_u )</th>
</tr>
</thead>
<tbody>
<tr>
<td>MCD</td>
<td>0.298</td>
<td></td>
<td>0.529</td>
</tr>
<tr>
<td>MT</td>
<td>0.300</td>
<td></td>
<td>0.177</td>
</tr>
<tr>
<td>DDH</td>
<td>&lt;0.001 *</td>
<td></td>
<td>0.499</td>
</tr>
<tr>
<td>MCD ( \times ) MT</td>
<td>0.012 *</td>
<td></td>
<td>0.009 *</td>
</tr>
<tr>
<td>MCD ( \times ) DDH</td>
<td>0.003 *</td>
<td></td>
<td>0.116</td>
</tr>
<tr>
<td>MT ( \times ) DDH</td>
<td>0.299</td>
<td></td>
<td>0.021 *</td>
</tr>
<tr>
<td>MCD ( \times ) MT ( \times ) DDH</td>
<td>0.460</td>
<td></td>
<td>0.160</td>
</tr>
</tbody>
</table>

* means the factor has significant effects at the 5% significance level.

Table 3 shows the mean values of  \( F_c \) for all combinations of the three factors evaluated. For control samples,  \( F_c \) increased with the increase in MCD. However, for heat-treated samples, this trend was not identical to the control samples: (1)  \( F_c \) increased with the increment of MCD when the DDH was 7.8 mm (interference fit); (2)  \( F_c \) decreased with the increase of MCD when the DDH was 8 mm (snug fit); and (3)  \( F_c \) got its maximum value at the MCD of 8.45% when the DDH was 8.5 mm (clearance fit).

Table 3. Summaries of critical crack strength (\( F_c \)) of oblique corner joints and their comparisons for diameter of dowel hole within each combination of material type and moisture content.

<table>
<thead>
<tr>
<th>Material Type</th>
<th>MCD (%)</th>
<th>( F_c ) (N)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>8.5 mm</td>
</tr>
<tr>
<td>Control</td>
<td>6.72</td>
<td>681.8(7.0)Aa</td>
</tr>
<tr>
<td></td>
<td>8.45</td>
<td>662.5(8.4)ABa</td>
</tr>
<tr>
<td></td>
<td>12.02</td>
<td>704.1(14.7)Ba</td>
</tr>
<tr>
<td></td>
<td>6.72</td>
<td>687.0(8.3)Aa</td>
</tr>
<tr>
<td>Heat-treated</td>
<td>8.45</td>
<td>728.6(10.5)ABa</td>
</tr>
<tr>
<td></td>
<td>12.02</td>
<td>659.3(14.3)Bb</td>
</tr>
</tbody>
</table>

Note: The mean values in the same row not followed by a common upper-case letter are significantly different from one another at the 5% significance level. The mean values in the same column not followed by a common lower-case letter are significantly different from one another at the 5% significance level. The values in the parenthesis are coefficients of variance (COV).

Comparing the  \( F_c \) between control and heat-treated OCJ samples, the maximum value of  \( F_c \) was obtained with the combination of control alder with a MCD of 12.02% and a DDH of 7.8 mm. Concerning the DDH, the whole trend was that  \( F_c \) increased with the decrease of the DDH, which indicated that interference fit can improve the  \( F_c \) of the OCJ of a furniture door.

Table 4 shows the results of the ultimate strength,  \( F_u \), of OCJs for all combinations of factors evaluated. For control samples,  \( F_u \) increased with the increment of MCD, but for heat-treated samples, the trend varied among different DDHs, especially for MCD of 12.02%. Concerning the MT, the  \( F_u \) of control samples was higher than those of heat-treated samples from the whole trend, which was identical to previous studies on other joints [22–26]. For DDH, the clearance fit seemed more suitable than other fits.
Table 4. Summary of ultimate strength ($F_u$) of oblique corner joints and their comparisons for diameter of dowel hole within each combination of material type and moisture content.

<table>
<thead>
<tr>
<th>Material Type</th>
<th>MCD (%)</th>
<th>$F_u$ (N) 8.5 mm</th>
<th>8 mm</th>
<th>7.8 mm</th>
</tr>
</thead>
<tbody>
<tr>
<td>Control</td>
<td>6.72</td>
<td>947.6(5.5)Aab</td>
<td>850.3(9.4)Bb</td>
<td>966.7(6.4)Aa</td>
</tr>
<tr>
<td></td>
<td>8.45</td>
<td>972.0(11.3)Aab</td>
<td>933.0(12.5)ABa</td>
<td>901.6(9.9)Ba</td>
</tr>
<tr>
<td></td>
<td>12.02</td>
<td>1011.4(10.3)Aa</td>
<td>952.3 (10.0)Aa</td>
<td>974.6(9.2)Aa</td>
</tr>
<tr>
<td>Heat-treated</td>
<td>6.72</td>
<td>924.8(11.5)Abc</td>
<td>948.3(8.6)Aa</td>
<td>916.5(12.2)Aa</td>
</tr>
<tr>
<td></td>
<td>8.45</td>
<td>957.2(12.8)Aab</td>
<td>973.2(12.5)Aa</td>
<td>916.3(11.9)Aa</td>
</tr>
<tr>
<td></td>
<td>12.02</td>
<td>858.1(17.2)Bc</td>
<td>898.8(13.2)ABab</td>
<td>953.0(9.7)Aa</td>
</tr>
</tbody>
</table>

Note: The mean values in the same row not followed by a common upper-case letter are significantly different from one another at the 5% significance level. The values in the parenthesis are coefficients of variance (COV).

3.4. Preliminary Optimization of Oblique Corner Joints

3.4.1. Critical Crack Strength ($F_c$)

The optimization analysis procedure was conducted using the response surface method to get the optimal parameters used in constructing the OCJ. Figure 7 shows correlations of $F_c$ related to MCD and DDH, which indicate that high MCD and small DDH benefit the $F_c$ of OCJs made of both control alder and heat-treated alder. Specifically, Equations (1) and (2) show the relationships between $F_c$, MCD, and DDH for control alder and heat-treated alder, respectively.

$$F_{c1} = 22326D + 11098M - 2723DM - 1364D^2 + 7.8M^2 + 166D^2M - 0.7DM^2 - 90430 \quad R^2 = 0.842$$  \hspace{1cm} (1)

$$F_{c2} = 11468D + 7816M - 1961DM - 718.6D^2 + 32.9M^2 + 123.9D^2M - 4.6DM^2 - 45277 \quad R^2 = 0.96$$  \hspace{1cm} (2)

where $F_{c1}$ and $F_{c2}$ are critical crack strengths of control alder and heat-treated alder corner joints in N. $D$ and $M$ are the diameter of the dowel hole in mm and moisture content in percentage.

![Figure 7](image1.png)

Figure 7. Correlations of critical crack strength of alder (a) and heat-treated alder (b) relating to moisture content of the dowel and diameter of the dowel hole.

3.4.2. Ultimate Strength ($F_u$)

Figure 8 shows the correlations of $F_u$ with MCD and DDH. By contrast with $F_c$, the trend of maximum $F_u$ in OCJs made of control alder was different from those made of...
heat-treated alder and \( F_c \). The specific relationships between \( F_{u1} \), MCD, and DDH of control alder and heat-treated alder were Equations (3) and (4), respectively.

\[
F_{u1} = 101130 - 23933D - 8617M + 1958DM + 1425.7D^2 + 65.5M^2 - 110.4D^2M - 7.9DM^2 \quad R^2 = 0.799 \tag{3}
\]

\[
F_{u2} = 17677D + 57948M - 1587.DM - 1125.8D^2 + 88M^2 + 108.5D^2M - 11.3DM^2 - 6854.9 \quad R^2 = 0.94 \tag{4}
\]

where \( F_{u1} \) and \( F_{u2} \) are the ultimate strengths of OCJs made of alder and heat-treated alder in N. \( D \) and \( M \) are the diameter of the dowel hole in mm and the moisture content of the dowel in percentage, respectively.

**Figure 8.** Correlations of the ultimate strength of alder (a) and heat-treated alder (b) relating to moisture content and the diameter of the dowel hole.

The above analysis suggested that the optimal parameters of OCJ made of alder and heat-treated alder were nearly the same for \( F_c \). However, the optimal parameters of OCJs for \( F_{u1} \) varied from MT and were different from those of \( F_c \), which indicated that \( F_c \) was a more stable indicator to evaluate the crack load resistance of OCJs.

### 3.5. Secondary Optimization of Oblique Corner Joints

In order to further improve the crack load resistance of the OCJ, we tried to use double dowels to construct the samples, and the effect of distance between two dowels (DTD) and material type (MT) was investigated experimentally. Figure 9 shows the layouts of two dowels in the OCJs with DTDs of 22 mm, 27 mm, and 32 mm. Meanwhile, OCJs constructed with a single dowel and without a dowel were also tested for comparison. According to the preliminary optimization result of \( F_c \), the optimal parameters applied in secondary optimization were that DDH was 7.8 mm, the MCD of the dowel was nearly 12%, and the glue applied was PVAc.

**Figure 9.** Configurations of oblique corner joints constructed by double dowels with different distances: 22 mm (a), 27 mm (b), and 32 mm (c).
Table 5 shows that the DTD has a significant effect on $F_c$ and $F_u$, but the effect of MT and the interaction of DTD × MT are not significant at the 5% significance level. Therefore, further comparisons of $F_c$ and $F_u$ of the OCJs with different DTDs were conducted.

Table 5. Summaries of ANOVA results for critical crack strength and ultimate strength of oblique corner joints constructed by two dowels through a generalized linear model on two factors.

<table>
<thead>
<tr>
<th>Factor</th>
<th>$F_c$</th>
<th>$p$-Value</th>
<th>$F_u$</th>
<th>$p$-Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>DTD</td>
<td>4.03</td>
<td>0.012 *</td>
<td>41.53</td>
<td>&lt;0.001 *</td>
</tr>
<tr>
<td>MT</td>
<td>1.54</td>
<td>0.22</td>
<td>2.93</td>
<td>0.09</td>
</tr>
<tr>
<td>DTD × MT</td>
<td>0.98</td>
<td>0.408</td>
<td>1.37</td>
<td>0.26</td>
</tr>
</tbody>
</table>

* means the factor has significant effects at the 5% significance level.

Table 6 summarizes the mean values of $F_c$ for OCJs constructed without a dowel, with a single dowel, and with double dowels with different DTDs. It can be found that the $F_c$ of OCJs constructed by double dowels was significantly greater than those of single dowels, followed by those without dowels, regardless of MT. Meanwhile, the $F_c$ of OCJs constructed with double dowels with a distance of 27 mm was greater than that of OCJs constructed with DTDs of 22 mm and 32 mm.

Table 6. Mean comparisons of critical crack strength ($F_c$) of an oblique corner joint constructed without a dowel, with a single dowel, and with double dowels with different distances.

<table>
<thead>
<tr>
<th>Material Type</th>
<th>Without Dowel</th>
<th>Single Dowel</th>
<th>Distance between Double Dowel (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$F_c$</td>
<td>$F_u$</td>
<td>22</td>
</tr>
<tr>
<td>Control</td>
<td>595.4(10.8)C</td>
<td>635(8.0)B</td>
<td>724(9.0)A</td>
</tr>
<tr>
<td>Heat-treated</td>
<td>601.6(16.7)C</td>
<td>718(13.6)B</td>
<td>745(10.8)AB</td>
</tr>
</tbody>
</table>

Note: The values in the same row not followed by a common letter are significantly different from one another at the 5% significance level. The values in parentheses are the coefficients of variance.

Table 7 summarizes the mean values of $F_u$ of OCJs constructed without a dowel, with a single dowel, and with double dowels with different DTDs, which suggests that the OCJs constructed with double dowels with a DTD of 27 mm were significantly greater than those of others. Figure 10 shows the typical failure modes of the OCJs assembled with different numbers of dowels, which further validates that the double dowel can improve the $F_c$ and $F_u$ of OCJs [22,23].

Table 7. Mean comparison of ultimate strength ($F_u$) of corner joints constructed by single dowel and double dowels with different distances.

<table>
<thead>
<tr>
<th>Material Type</th>
<th>Without Dowel</th>
<th>Single Dowel</th>
<th>Distance between Double Dowel (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$F_c$</td>
<td>$F_u$</td>
<td>22</td>
</tr>
<tr>
<td>Control</td>
<td>595.4(10.8)C</td>
<td>635(8.0)B</td>
<td>724(9.0)A</td>
</tr>
<tr>
<td>Heat-treated</td>
<td>601.6(16.7)C</td>
<td>718(13.6)B</td>
<td>745(10.8)AB</td>
</tr>
</tbody>
</table>

Note: The values in the same row not followed by a common letter are significantly different from one another at the 5% significance level. The values in the parenthesis are coefficients of variance (COV).
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4. Conclusions
This study focused on the oblique corner joint (OCJ) cracks in wood furniture door products. The effects of the selected factors on the strength of the OCJ were investigated and optimized. The following conclusions were drawn:

(1) Two typical mechanical behaviors of OCJs were characterized through camera tracking and mechanical analysis of the load-displacement curve, and their corresponding failure modes were observed.

(2) The critical crack strength, $F_c$, defined in this study was a better indicator to evaluate the crack load resistance of the OCJ since it is more sensitive to the crack load resistance and stable than the ultimate strength, $F_u$, of the OCJ.

(3) The analysis of variance results showed the diameter of the dowel hole (DDH) had a significant effect on $F_c$, and there were interaction effects on factors evaluated on $F_c$ and $F_u$ of OCJs. Samples made of control alder performed better than heat-treated alder on both $F_c$ and $F_u$ of OCJs.

(4) Optimal parameters for constructing the OCJs were obtained and indicated that the OCJ should be made of control alder constructed by double dowels with a distance of 27 mm and that the moisture content of the dowel should be higher than that of the base material.

Figure 10. Failure modes of an oblique corner joint constructed without a dowel (a), with a single dowel (b), and with double dowels (c).
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