Electromagnetic Precursors of Short Gamma-Ray Bursts as Counterparts of Gravitational Waves

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Abstract: Precursor emissions are found in some short gamma-ray bursts (SGRBs). In this paper, we review the theories and observations of the SGRB precursor and discuss its prospect as an electromagnetic counterpart of the gravitational wave event produced by neutron star (NS) mergers. The observed luminosity, spectrum, and duration of precursors are explained by the magnetospheric interaction model during the inspiral or the cocoon/jet shock breakout model during the jet propagation. In general, these two models predict that the precursor will be weaker than the main GRB, but will be of a larger opening angle, which makes it an advantageous gamma-ray counterpart for NS mergers in the local Universe, especially for NS - black hole mergers with very low mass ratios, in which the main GRBs are not expected. The joint observation of the precursor, SGRB, and gravitational wave will help to reveal the jet launch mechanism and post-merger remnant.

Keywords: gamma-ray burst; gravitational wave; neutron stars; magnetosphere; shock breakout

1. Introduction

On 17 August 2017, the Fermi/gamma-ray burst monitor (GBM) was triggered by a short gamma-ray burst (SGRB)-GRB 170817A [1–3]. Independently, the gravitational-wave (GW) event GW170817 produced by the double neutron star (NS) merger was detected by the advanced LIGO and Virgo detectors [4,5]. The joint detection of GW170817/GRB 170817A confirms that at least some SGRBs originate from NS mergers, and herald the multi-messenger astronomy [1–5]. It also enables better localization, which benefited the multi-wavelength follow-up observations. The detection of the associated kilonova, AT 2017gfo, led to the discovery of the host-galaxy NGC 4993 at a distance of ∼40 Mpc, which shed light on the physics of nucleosynthesis [1,6–11].

Joint detection can provide abundant information to study some fundamental physics. Using the GW data alone, constraints on the NS equation of state can be obtained (e.g., [4]). Combining with the electromagnetic (EM) observations, (1) the GW event can be treated as a standard siren to study cosmology [12]; (2) one can also constrain the difference between the speed of gravity and the light speed, test the violation of Lorentz invariance and the equivalence principle [5,13]. It can also be used to study the launching mechanism, structure, composition, and radiation mechanism of GRB jets (e.g., [3,14–23]).

Since the discovery of GW170817/GRB 170817A, many efforts have been put into the follow-up observations of GW events to search for their EM counterparts. No new confident joint detection is observed, except for a sub-threshold event: the sub-threshold GRB (GBM-190816) [20,24] was found to be possibly associated with a sub-threshold NS merger event GW190425 [25]. But in the archived Fermi/GBM data, a small sample of SGRB-like events has been found [26]. In theory, many EM signals are expected for the NS merger. The observation and theory of SGRBs, afterglows, and kilonova were summarized in many reviews [27–32]. However, little attention has been placed on the
pre-merger EM radiation. As a complement, we focused on the precursor emissions of SGRB in this review.

Precursors were initially identified as weak signals in long GRBs (e.g., [33–39]). Later precursors of SGRBs were found in the Swift/Burst Alert Telescope (BAT) data [40]. Within the standard fireball scenario, precursors are suggested to be associated with the transition of the fireball from optically thick to optically thin, leading to photospheric blackbody emissions [29,41–44]. This applies to both long and short GRBs. It is also suggested that a precursor can be generated by the shock breakout (SBO) of a jet or a cocoon. For long GRBs, this links to the SBO from the stellar surface [32,45–50], some research proposed that breakout of a radiation mediated shocks train can naturally generate a band-like spectrum [51,52]. For SGRB, this relates to the SBO from the ejecta produced during the NS merger [32,50,53,54]. Besides, there are two more scenarios proposed only for SGRB precursors. During the inspiral phase of the NS–NS/black hole (BH) binary, the magnetospheric interaction of the binary [55–63], or the crust crack of the NS [64–66] may also generate gamma-ray emissions. As such, precursors of SGRBs may shed light on the physical processes right before or shortly after the merger.

Moreover, the magnetospheric interaction model [62] and the SBO model [32,53,54] predict the precursor, although fainter than the main GRB, would have a much larger opening angle, as the radiation is generated by a mild relativistic component. In this case, the precursor can serve as an independent EM counterpart for GWs, even though the prompt GRB points away from the line of sight. It has been suggested that GRB 170817A can be such a case [32,53,54]. This feature would be greatly appreciated for follow-up observations. Thus, research on precursors is important for multi-messenger astronomy. This review aims to summarize the current understanding of SGRB precursors and discuss the possibility for future observations. In the next section, we review the feasible precursor models. Observations are summarized in Section 3. In Section 4, the discussion and prospects are presented.

2. Precursor Models

Various research studies have shown that a gamma-ray precursor event can be produced prior to the main GRB event. Here, we divide the precursor models into two categories based on their relative time to the merger: pre-merger models and post-merger models. More specifically, in the pre-merger phase, magnetospheric interaction in the NS binary and the crustal failure triggered by tidal interactions could lead to precursor emissions. While during the post-merger phase, it is suggested that the photospheric emission from the fireball and the SBO can also result in precursors.

We summarize the luminosity, spectrum, duration, and opening angle of these pre-cursor models below, which relate to their detectability. To make sure the precursor is detectable at an extra-galactic distance, its luminosity should satisfy $L > 4\pi D^2 S$, where $S$ is the sensitivity of the detector, and $D$ is the distance. Recently, researchers have searched for SGRBs in the local Universe in the Swift catalog and found that the four closest SGRBs could locate at $D \sim 100–200$ Mpc [67]. Thus we adopt $D > 100$ Mpc. For sensitivity, we use the gravitational wave high-energy electromagnetic counterpart all-sky monitor (GECAM) as an example, which has $S \approx 2 \times 10^{-8}$ erg cm$^{-2}$ s$^{-1}$ in $8–2000$ keV [68]. The corresponding lower limit on luminosity is then

$$L \gtrsim 2.4 \times 10^{46} \text{erg s}^{-1}. \quad (1)$$

2.1. Pre-Merger Models

2.1.1. Magnetospheric Interactions of NS–NS/BH Binaries

It has long been suggested that the magnetospheric interactions in compact star binaries can lead to energy dissipation (e.g., [55]). Following [62,69], three cases are considered in this review as shown in Figure 1: case 0 with $B_c < \mu_s a^{-3}$, case 1 with $\mu_s \sim -\mu_c$, and case 2 with $\mu_s \sim \mu_c$, where the subscripts ($s$, $c$) represent the NS and its
companion, respectively. The magnetic dipole moment is \( \mu = BR^3 \), where \( B \) is the surface magnetic field and \( R \) is the radius. We consider the binary to be of a separation \( a \), a mass ratio \( q = M_c/M_* \), and an orbital angular velocity \( \Omega = (GM_*(1+q)/a^3)^{1/2} \). Within this framework, the energy dissipation rate of the NS binary system can be well formulated.

Case 0 can be well understood within the unipolar induction directcurrent (DC) circuit model, i.e., the weakly magnetized NS or non-magnetic BH is moving across the magnetic field lines inside the magnetosphere of the NS. This generates an electromotive force (EMF) \( \mathcal{E} \sim 2R_c|\mathbf{E}| \) on the two poles of the companion, where \( \mathbf{E} = \mathbf{v} \times \mathbf{B}_c/c, \mathbf{v} = (\Omega - \Omega_*) \times a, \) and \( \Omega_* \) is the spin of the NS. This EMF can drive currents along the magnetic field lines, which makes a closed DC circuit. Note this DC circuit may not always be stable [56]. The resistance of the magnetosphere is \( R = 4\pi/c \) [70]. The luminosity can then be estimated as [56],

\[
L_{UI} \approx 1.2 \times 10^{42} M_*(1+q)\mu_{*,30}^2(R_c/10\text{ km})^2(a/30\text{ km})^{-7}\text{ erg/s,}
\]

where the mass \( M_* \) is in units of solar mass \( M_\odot \). Note that, here and below, we adopt the approximation of \( \Omega \gg \Omega_* \), this is appropriate, as we are considering the last few seconds before the merger. Simulations of inspiraling NS–NS/BH binaries indicate that the main features are well captured by this model (e.g., [58,59,61,63,71,72]).

![Figure 1](image_url)

**Figure 1.** We show the schematics of three typical magnetic field configurations in inspiraling NS binaries: case 0 with \( B_c < \mu_* a^{-3} \), case 1 with \( \mu_* \sim -\mu_c \), and case 2 with \( \mu_* \sim \mu_c \). The red winding arrows represent the emitted photons.

The other cases are more complicated. During the shrinking of the orbit, the magnetospheres of NSs would interact with each other, dissipating the orbital kinetic energy. The location of the interaction is around \( r_i = a/(1 + e^{1/3}) \), where \( \mu_c r_i^{-3} = \mu_c (a - r_i)^{-3} \).
and $\epsilon = \mu_c / \mu_s$. If the magnetic field lines from two stars are anti-parallel with each other (Case 1), magnetic reconnection is expected. After the reconnection, the magnetic field lines would connect the two stars directly, leading to the formation of a DC circuit, such as in Case 0 driven by the EMF with an electric field $E \approx a \Omega B_\text{c} c^{-1}$. We find that the energy dissipation rate from the DC circuit is generally larger than that in the magnetic reconnection in the last few seconds before the merger, and it can be formulated as [62],

$$L_{\text{u,UL}} \approx 3.8 \times 10^{44} (R_\text{c} / 10 \text{ km})^{-3} (\epsilon^{5/3} + \epsilon^2) \mu_{30}^2 (a / 30 \text{ km})^{-2} \text{ erg/s}.$$  \hspace{1cm} (3)

If the magnetic field lines are parallel with each other (Case 2), the field lines would experience compressing at $r_i$, and the compression location would rotate around the main star at an angular speed $\Omega - \Omega_c$. When the compression location moves away, the compressed field lines will relax. This alternate compression and relaxation would lead to an electric field $E \sim \mu_s r_i^{-2} \Omega c^{-1}$ and an energy dissipation rate [62],

$$L_p \approx 1.8 \times 10^{44} (0.19 / \eta - 0.08)(1 + \epsilon^{1/3})^3 (1 + \epsilon) \mu_{30}^2 (a / 30 \text{ km})^{-9/2} \text{ erg/s},$$  \hspace{1cm} (4)

where $\eta r_i$ is the width of the compression region.

It can be found that the energy dissipation rate increases non-linearly with time. Comparing with Equation (1), we found that it would be detectable only in the last few milliseconds to seconds depending on the magnetic field and distance to the observer. In general, Case 1 would have the highest energy dissipation rate, while Case 0 would have the lowest. We noticed that, for real cases, the magnetic axis may have an inclination angle with respect to the orbital axis, and in these cases, the energy dissipation rate would lie in between the above scenarios. As the poloidal field is the dominant component, we ignored the contribution of the toroidal magnetic field, which are caused by the revolution of the binary system and are observed in many simulations (e.g., [58,59,61,63,71,72]).

The opening angle of the radiation depends on the actual magnetic configuration and the orbital phase. In all cases, the generated acceleration electric field is not parallel to the $B$ field. The radiation process would then be dominated by the synchrotron radiation [62]. Based on the threshold (Equation (1)), the magnetic field should be $B > 10^{13} \text{ G}$. While in such a high magnetic field, the high-energy photon will be absorbed, leading to a synchrotron-pair cascade. Using Monte-Carlo simulations, we find the spectral energy distribution (SED) can be well described by a cutoff-power law, with a photon index around $-2/3$ and peak energy at $\lesssim \text{MeV}$ [62,73]. This could be understood as the synchrotron radiation by the mildly relativistic electrons with $\gamma \lesssim 10$, as high-energy photons emitted by higher-energy electrons will be absorbed to produce pairs. Therefore, the radiation cone will be of half opening-angle $\sim 1 / \gamma = \mathcal{O}(0.1)$, and this radiation cone is rotating with an angular speed at $\Omega - \Omega_c$. Note that the magnetospheric interaction can create more open field lines than the isolated NSs, we would expect the outer gap acceleration to operate at around $r_i$, and so the curvature radiation may dominate after the electrons/positrons, losing their perpendicular moment. Overall, in these cases, the radiation opening angle will be much larger than that of jetted GRBs [62]. This can also be seen from the Poynting flux direction from magneto-hydrodynamics simulations (e.g., [57,58]).

### 2.1.2. NS Crust Crack Model

During the inspiral of the NS binary, tidal interactions can distort the NS, inducing ellipticities. Once the ellipticity becomes large enough that after the crystalline structure of the NS crust cannot respond linearly, a crust failure may be induced [40,64]. It has been suggested that the crust breaking strain is around $0.1$ [74], which corresponds to a critical ellipticity of $\epsilon_c \approx \delta R / R \approx 4 \times 10^{-6}$, where $R + \delta R$ is the elongated NS radius. This can be easily reached by the tidally-induced f-mode oscillation in the last seconds before the merger [65] (see also Figure 3 of Reference [75]). Recent works show that the g-mode can also lead to the breaking of the NS crust [66].
If the energy is dissipated into heat, the crust can be heated up to $T_c = E_{cc}/C \approx 27.2 E_{cc,46}^{1/2}$ keV with $C \approx 10^{20} T_c$ erg/K [76] and $E_{cc} = E_{cc,46} 10^{46}$ erg. The corresponding thermal luminosity from the crust surface with $R_\ast \approx 10^6$ cm is then [69],

$$L_{cc} \approx 4\pi R_\ast^2 a_S T_c^4 \sim 4.5 \times 10^{42} E_{cc,46}^2 \text{erg s}^{-1}, \quad (5)$$

where $a_S$ is the Stefan–Boltzmann constant. This is too faint to be observed at an extra-galactic distance.

It has also been proposed that, if the NS is highly magnetized, i.e., being a magnetar with $B \gg 10^{13}$ G, the crust failure may trigger a violent reconstruction of magnetic fields, leading to a magnetar-giant-flare-like event (e.g., [40,66]). However, it should be noted that for magnetar giant flares, the crust failure is believed to be caused by the sudden rearrangement of magnetic field [77]. It is unclear whether a crust failure could lead to the amplification and rearrangement of magnetar magnetic field. Nevertheless, in this case, the luminosity may be estimated as

$$L_{\text{Flare}} = E_{cc}/t_f = 10^{46} E_{cc,46}/t_f \text{ erg s}^{-1}, \quad (6)$$

where $t_f$ is the duration of the flare. The SED and opening angle in this case would be similar to observed giant flares.

### 2.2. Post-Merger Models

Within the standard fireball model for GRBs, a photospheric blackbody precursor can be produced when the fireball changes from optically thick regime to optically thin (see Section 7.3.3 of Reference [29], and references therein). The luminosity is determined by the transition radius. However, it has been found that, to fit the observation, the fireball Lorentz factor should be $\sim 30$, much smaller than the expected value (>100) [40,69]. Therefore, this is unlikely to be responsible for the precursors, and we mainly focus on the SBO model for post-merger models.

#### SBO Model

Both NS–NS and NS–BH mergers can launch relativistic jets. As the relativistic jet propagates through the sub-relativistic expanding merger ejecta, a high-pressure bubble would be generated, which engulfs the jet and affects its propagation. This will lead to the formation of a jet-cocoon system, which is a structured relativistic outflow with a wide-angle. A successful SGRB jet is expected to penetrate through this ejecta and produce gamma-rays by the internal dissipation processes within the jet. It has been proposed that when the shock driven by a mildly relativistic cocoon breaks out of the ejecta, gamma-ray emission would also be produced [53,54]. This process differs significantly from what occurs in ordinary SGRBs.

For a low-power and short-duration jet, it may not penetrate through the ejecta, and the jet is choked. Both successful jet and choked jet can drive an at least mildly relativistic SBO from the expanding merger ejecta [53]. The SBO of the relativistic jet or the mildly relativistic cocoon from the sub-relativistic expanding merger ejecta could release a tiny fraction, e.g., $\sim 10^{-4}$, of the total kinetic energy of the outflow into gamma-ray.

Two key physical parameters, the final Lorentz factor of the breakout layer $\Gamma_{\text{SBO}}$ and the radius of the SBO $R_{\text{SBO}}$, determine the main properties of the observed emissions. The SBO occurring in a sub-relativistic expanding ejecta is very different from that occurring in a static stellar envelope. The shock velocity in the lab frame would determine the boost of the emission to the observer, and the shock velocity in the ejecta frame would determine the strength of the shock. The SBO from the breakout layer would have an optical depth $\tau \sim c/v_{sh}'$, where $v_{sh}'$ is the shock velocity seen in the ejecta frame. The shock quantities...
seen in the unshocked merger ejecta frame are marked with a prime. The mass of the
breakout layer can be estimated to be

$$M_{\text{SBO}} \sim \frac{4\pi R_{\text{SBO}}^2}{\kappa \beta_{\text{SBO}}^2} = 4 \times 10^{-8} M_\odot \beta_{\text{SBO}}^{-1} \left( \frac{R_{\text{SBO}}}{10^{12} \text{ cm}} \right)^2 \left( \frac{\kappa}{0.16 \text{ cm}^2 \text{ g}^{-1}} \right)^{-1},$$

where the opacity $\kappa = 0.16 \text{ cm}^2 \text{ g}^{-1}$ is expected for fully ionized heavy elements, $\beta_{\text{SBO}} = v_{\text{sh}}'/c$.

If the shock is fast enough (e.g., $v_{\text{sh}}' > 0.5c$), the radiation temperature behind the
shock reaches $\sim 50 \text{ keV}$ at which pair production becomes important [49]. In this case, the mean photon energy is in the $\gamma$-ray regime. The observed energy from the breakout layer $E_{\text{SBO}}$ can be roughly estimated by the internal energy of the shocked breakout layer and boosted to the observer frame as [32,50]

$$E_{\text{SBO}} \sim M_{\text{SBO}} c^2 \Gamma_{\text{SBO}} \left( \frac{\Gamma_{\text{SBO}}'}{5} - 1 \right)^{-1} \simeq 7 \times 10^{46} \text{ erg} \left( \Gamma_{\text{SBO}} 5 \right)^{-2}. (8)$$

In the case of a spherical breakout, the difference between the light travel time of
photons emitted along the line of sight determines the duration of the breakout signal

$$\tau_{\text{SBO}} \sim \frac{R_{\text{SBO}}}{2c \Gamma_{\text{SBO}}^2} = 0.67 \text{ s} \left( \frac{R_{\text{SBO}}}{10^{12} \text{ cm}} \right) \left( \frac{\Gamma_{\text{SBO}}}{5} \right)^{-2}. (9)$$

The bolometric luminosity of an SBO could then be roughly estimated as [69]

$$L_{\text{SBO}} \sim \frac{E_{\text{SBO}}}{\tau_{\text{SBO}}} = \zeta E_{K,\text{iso}} \tau_{\text{SBO}}^{-1}. (10)$$

where $E_{K,\text{iso}}$ is the total kinetic energy of the outflow, and $\zeta$ is the fraction of the total explosion energy emitted in $\gamma$-rays.

In the framework of the SBO scenario, three SBO parameters: the breakout radius $R_{\text{SBO}}$, the ejecta Lorentz factor $\gamma_{\text{ej,SBO}}$, and the shock Lorentz factor $\gamma_{\text{SBO}}$, are related with
three main observables: the total observed isotropic equivalent energy $E_{\text{SBO}}$, the duration $\tau_{\text{SBO}}$, and the breakout temperature $T_{\text{SBO}}$. The SBO temperature $T_{\text{SBO}}$ is roughly the immediate downstream temperature of the breakout layer, as observed in the observer frame. The rest-frame temperature at the time that the photons are released is $\sim 50 \text{ keV}$, the observed temperature of SBO can be estimated as

$$T_{\text{SBO}} \sim 50 \Gamma_{\text{SBO}} \text{ keV}. (11)$$

The three breakout observed quantities, $\tau_{\text{SBO}}, E_{\text{SBO}},$ and $T_{\text{SBO}}$, satisfy a closure rela-
tion [32,49]

$$\tau_{\text{SBO}} \sim 20 \text{ s} \left( \frac{E_{\text{SBO}}}{10^{46} \text{ erg}} \right)^{1/2} \left( \frac{T_{\text{SBO}}}{50 \text{ keV}} \right)^{-9/4}. (12)$$

This closure relation can be used to see if the detected $\gamma$-ray flash is consistent with
a relativistic SBO origin. It is worth noting that this relation is strongly dependent on
the breakout temperature $T_{\text{SBO}}$, which is difficult to determine precisely because the SBO spectrum could deviate from a blackbody spectrum.

There are three generic properties of a relativistic SBO from a moving ejecta: (1) the
light curve is smooth; (2) only a tiny fraction of the total energy would be emitted at the
SBO stage; (3) the spectrum shows a hard to soft evolution [49,53]. Thus for precursors
produced by SBO, the observed energies could be orders of magnitude lower, but depend
on the viewing angle of the jet. Note, interestingly, all of these properties are observed in
GRB 170817A. Therefore, a mildly relativistic cocoon shock breaking out from the merger
ejecta provides a natural explanation of the observational properties of GRB 170817A.
### 3. Observational Results

Searching SGRB precursors has been performed in various space observatories, such as INTEGRAL [78], *Swift* [40,79], and *Fermi* /GBM [69,79]. Detecting weak signals before SGRBs will be subject to instrumental biases (the energy range and sensitivity). For example, although *Fermi* /GBM covers a broad energy range (∼8 keV–40 MeV), *Swift* /BAT has a higher sensitive in the 15–150 keV band. Thus *Swift* will be stronger to detect soft weak precursors, consistent with observations.

In the pioneer research, precursors are searched by visual inspection in binned light curves with a certain fixed bin width (e.g., [33]). Later, wavelet analysis is introduced to analyze such binned light curves [34,40]. Recently, the Bayesian block algorithm [80] has been widely applied in both the binned light curve and the time-tagged event data [69,79,81]. Yet in the Bayesian block algorithm, the false alarm probability is adopted; thus, additional analysis is required to obtain the significance of the precursor [69,79]. By applying these methods, precursors are found in both long GRBs and SGRBs, and the detection rate of precursor is higher in long GRBs (e.g., [35,81]).

For SGRBs, the fraction of precursor events is less than 0.4% for INTEGRAL [78], and is ∼8–10% for *Swift* /BAT [40]. For the combined *Swift* and *Fermi* /GBM sample, the fraction is found to be 2.7% [79]. Applying the Bayesian block algorithm in the *Fermi* /GBM sample alone, we found a fraction of 3.0% SGRBs are associated with precursor activities [69], while only a fraction of 1.2% is found in Reference [81]. The major difference in the detection fraction may arise from the selection criteria for the precursors. The precursor events provided in Reference [69] are found of the signal-to-noise ratio (SNR) ≳ 4.5σ, where the SNR is obtained in the optimized energy range for the precursor. Thus, we adopt this precursor sample for *Fermi* /GBM in the following analysis. In Table 1, we list the SGRBs with precursors detected by *Fermi* /GBM [69] and/or *Swift* /BAT [40,79], where we show the duration of the precursor (τ\textsubscript{pre}), waiting time (τ\textsubscript{wt}), and the main SGRB (τ\textsubscript{GRB}).

The GRB duration is usually described as τ\textsubscript{GRB} ≈ R\textsubscript{GRB} (1 + z) / (2Γ\textsuperscript{2}c), where R\textsubscript{GRB} is the jet dissipation radius, Γ is the bulk Lorentz factor at R\textsubscript{GRB}, and z is the redshift of...
the source. For the magnetospheric interaction model, the waiting time consists of the jet launch time ($\Delta_{\text{jet}}$) and the jet propagation time ($\Delta_{\text{GRB}} \sim t_{\text{GRB}}$). For the SBO model, the waiting time relates to the jet propagation from the SBO radius to the jet dissipation radius, i.e., $\tau_{\text{wt}} = (R_{\text{GRB}} - R_{\text{SBO}})/(1 + z)/(2(\Gamma z))$. For the cases with $\Delta_{\text{jet}} \ll \Delta_{\text{GRB}}$ and $R_{\text{SBO}} \ll R_{\text{GRB}}$, we would expect $\tau_{\text{wt}} \sim t_{\text{GRB}}$. Yet there is an exception case for magnetospheric interaction model, in which the NS merger remnant is a stable NS (SNS) formed after the spin-down of the initially-formed uniform-rotation-supported supramassive NS with $\Delta_{\text{wt}} > t_{\text{GRB}}$ [19,86]. Note that for the SBO model, one can constrain the ratio of the radii $R_{\text{SBO}}/R_{\text{GRB}} \approx 1 - \tau_{\text{wt}}/t_{\text{GRB}}$ from observations.

Previous results based on Fermi/GBM events have indicated that $\tau_{\text{wt}} \sim t_{\text{GRB}}$ can be generally satisfied [69]; here, in Figure 2, we show the updated $\tau_{\text{wt}} - t_{\text{GRB}}$ diagram, which includes both Fermi/GBM and Swift/BAT events. The fitting of the data (red line) shows that $\tau_{\text{wt}} \approx 1.9 t_{\text{GRB}}$, largely consistent with theories and previous results [69]. However, note here that the fitting errors are not provided, as the errors of the data points are not available for the Swift events [40,79]. However, there are two outliers, GRB090510 (the first precursor event) and GRB191221802, with $\tau_{\text{wt}} \gg t_{\text{GRB}}$. This might suggest that SNSs are formed in these two events.

**Table 1.** The durations of the precursor ($\tau_{\text{pre}}$), waiting time ($\tau_{\text{wt}}$), and the main SGRB ($t_{\text{GRB}}$) are taken from [69] for Fermi/GBM detected bursts, and from [40,79] for Swift detected bursts (marked with ‘*’). * For the events only detected by Fermi/GBM, their names are provided following the Fermi GBM Burst Catalog. The redshift is 0.287 for GRB060502B, and GRB090510 for 0.903.

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<td>0.03 ± 0.01</td>
<td>0.08 ± 0.01</td>
</tr>
<tr>
<td>GRB160804180</td>
<td>0.16 ± 0.02</td>
<td>0.17 ± 0.02</td>
<td>0.26 ± 0.02</td>
</tr>
<tr>
<td>GRB170709334</td>
<td>0.46 ± 0.01</td>
<td>0.17 ± 0.07</td>
<td>0.15 ± 0.07</td>
</tr>
<tr>
<td>GRB170802638</td>
<td>0.15 ± 0.17</td>
<td>1.85 ± 0.14</td>
<td>0.33 ± 0.04</td>
</tr>
<tr>
<td>GRB180511437</td>
<td>2.80 ± 1.38</td>
<td>12.72 ± 1.80</td>
<td>3.33 ± 0.18</td>
</tr>
<tr>
<td>GRB181126A</td>
<td>0.73 ± 0.18</td>
<td>0.85 ± 0.40</td>
<td>0.46 ± 0.11</td>
</tr>
<tr>
<td>GRB191221802</td>
<td>0.03 ± 0.59</td>
<td>19.36 ± 1.24</td>
<td>0.37 ± 0.26</td>
</tr>
</tbody>
</table>
4. Discussion and Prospects

Precursors have been detected for a small fraction of SGRBs. Here, we briefly review the models for precursors, mainly focusing on the magnetospheric interaction model and the SBO model, while the crust crack model and the fireball photospheric radiation model are found to be less likely based on current observations [69]. We focused on the explanation of the major physical processes in these models. To directly compare with observations, we estimated the luminosity, spectrum, duration, and opening angle for these models.

For the magnetospheric interaction model, the precursor will be produced simultaneously with GWs. A cutoff-power-law spectrum is expected with a photon index $\sim -2/3$ and a cutoff at MeV. Moreover, fast radio bursts (FRBs) are suggested to be produced during the magnetospheric interaction (e.g., [60,63]). It should be noted that for NS–BH binaries with mass ratio $<0.2$, the NS would be swallowed by the BH without producing a GRB and, thus, only the precursor is available.

While for the SBO model, the precursor is produced after the merger, but before the main GRB. Although GRB 170817A was classified as an SGRB, with a duration $\approx 0.5$ s, it was fainter than the faintest SGRB previously detected by roughly three orders of magnitude, with the isotropic equivalent energy of $E_{\gamma,iso} = 3 \times 10^{46}$ erg. The delay time between the GW signal and the $\gamma$-rays, $\tau_{GW,\gamma} = 1.7$ s. The peak energy of the observed integrated spectrum is $E_p = 185 \pm 62$ eV [2,3]. The breakout layer parameter that could produce the observables of GRB 170817A are $R_{SBO} \approx 6 \times 10^{11}$ cm and $\Gamma_{SBO} \approx 4$. SBO emissions from the jet-cocoon system seems to provide a natural explanation for this observed event because of the low radiation efficiency and the wide emission angle. However, the event rate for cocoon-SBO-induced GRBs should be very small, considering that most GRBs are observed at cosmological distances [87].

Compared with the main GRBs, we found that precursors are usually much weaker, but with a larger opening angle. Thus, for the NS mergers that occurred within several hundred Mpc, the detection of precursors is very likely. This will greatly benefit the search for gamma-ray counterparts of GW events and FRBs, which can be well tested by the current and near-future observatories, e.g., Fermi/GBM and Swift/BAT, GECAM [68], and the space-based multi-band astronomical variable objects monitor (SVOM) [88]. Furthermore, the time delay between precursors and GRBs or GW can be used to constrain the jet launch mechanism and post-merger remnant [19,69]. For the magnetospheric interaction model,
photon splitting could be important, and it might significantly change the polarization state of emitted photons \[89,90\]. This can also be tested by the future gamma-ray polarimeter detector POLAR-2 [91].

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**References**


