Seismic Fragility Curves of RC Buildings Subjected to Aging

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Abstract: A large number of existing reinforced concrete (RC) buildings have surpassed their anticipated service life and show signs of degradation due to aging; this degradation is a function of the construction practices adopted in the past as well as environmental conditions. This paper discusses seismic fragility and the risk assessment of RC structures, emphasizing the impact of corrosion due to concrete aging and the associated deterioration mechanisms. The literature on this topic is critically reviewed, and a methodology for studying the seismic fragility of deteriorated RC buildings is proposed. As a case study, a four-story RC building designed according to contemporary code provisions is examined. The investigation encompasses the derivation of fragility curves, considering critical parameters such as the corrosion rate, the initiation time, and the cover depth. The proposed approach enables the evaluation and quantification of the impact of corrosion mechanisms on the seismic performance of buildings.

Keywords: reinforced concrete; aging; corrosion; fragility; durability; seismic

1. Introduction

Reinforced concrete (RC) has been a widely used structural material for several decades. However, particularly in seismic-prone areas, in recent years, we have seen a growing number of discussions regarding the optimal lifespan of concrete structures. Research shows that the lifespan of RC buildings depends mainly on concrete characteristics and environmental conditions. The most common factors that affect concrete durability are as follows: (i) An intensely alkaline atmospheric environment (pollution); (ii) Intense temperature fluctuations in the environment; and (iii) The proximity to a marine environment. Concrete aging often damages the RC members, as shown in Figure 1. Therefore, it is evident that the long-term durability of an RC structure is characterized by its ability to meet functional, structural, and stability criteria throughout its service life, with a minimal loss of capacity. Due to the high cost of addressing concrete aging, the international community considers concrete durability to be a major problem facing modern societies. The significance of considering the environmental conditions during the design and assessment of RC structures, as well as the possibility of preventive measures, is a topic that should be explicitly addressed in design codes and guidelines.

According to Bertolini et al. [1], the processes that may cause concrete degradation are mechanical, physical, structural, biological, and chemical. Chemical processes, such as attacks by alkali, sulfate, water, and electrochemical (chloride ions [2], carbonation) reactions, may lead to the corrosion of reinforcing steel. Moreover, the carbonation [3–5] of concrete and the penetration of chlorides are two common reasons for reinforcement corrosion [6,7]. Figure 2a shows the impact of chloride ions attacking the rebars [8] in an RC structure, while Figure 2b shows an example of progressive structural deterioration due to concrete...
carbonation [9]. In fact, deterioration encompasses a broader range of factors, including aging, which contribute to structural degradation.

Figure 1. Old building at McAbee Beach, USA, where the effects of aging are evident.

Aging reduces the structural capacity of a building. This is a critical problem, especially in seismic-prone areas. Considering the above, during the capacity assessment of existing RC structures, the impact of corrosion should be taken into consideration. The current study aims to examine the impact of aging and the corresponding deterioration mechanisms with respect to seismic capacity. With the aid of a case study of a four-story RC building designed in accordance with contemporary code provisions, our study involves deriving fragility curves to study the impacts of the most critical problem parameters. This analysis facilitates the assessment and quantification of the influence of structural and environmental parameters on seismic performance, juxtaposed with existing findings in the literature.

Figure 2. Deterioration of RC sections due to (a) chloride-induced and (b) carbonation-induced corrosion of reinforcement.

2. Degradation of Reinforced Concrete Structures
2.1. Damage and Durability

Concrete damage refers to the degradation of a material’s mechanical properties. Although the design of RC structures to modern standards and codes tends to mitigate the problem, the inevitable aging of structures leads to capacity degradation. The durability of concrete depends on several factors, all of which significantly influence its long-term performance. Major parameters include the water–cement ratio, curing methodologies, the mix design, and the quality of constituent materials. Specific properties are influenced by admixtures and air entrainment, whereas the selection and quality of aggregates impact both strength and ductility. Furthermore, construction practices, reinforcement protection, exposure conditions, and temperature control are essential for ensuring durability. Further
durability enhancement can be achieved through crack and shrinkage control, the incorporation of corrosion inhibitors, and the use of sealants. In all, each element in the concrete mix and construction process contributes to the overall resilience of the structure, while structural design plays a pivotal role in ensuring that an RC building can withstand both design actions and environmental challenges during the building’s lifetime.

The major threat to concrete durability is the corrosion of reinforcement. Corrosion leads to the formation of oxidation products, which, due to their increased volume, can cause concrete cracking. This phenomenon occurs when the protective layer of steel, known as passivation, is disrupted by the alkaline conditions within the concrete in the presence of moisture and oxygen. The corrosion of steel leads to a decrease in the bar’s cross-sectional area as the affected steel becomes rust. Furthermore, corrosion not only diminishes the ductility of steel but also disproportionately weakens its strength, significantly impacting the seismic performance of the structural members. Since the rust has two to six times the volume of steel, it induces cracking by delaminating the protective cover, reducing (or even eliminating) the bond, and exposing the steel rebars to further corrosion. These factors cumulatively reduce the mechanical properties of the steel material. The absence of seismic design codes at the time these buildings were constructed has increased their vulnerability, imposing the need for retrofitting actions.

The process in which the cement paste reacts with atmospheric carbon dioxide is termed concrete carbonation. An example of concrete carbonation in a structural member of a building is shown in Figure 3. As carbon dioxide uses the gaseous phase within the concrete, the level of carbonation intensifies. One immediate outcome of carbonation is the decline in alkalinity of the concrete encasing the reinforcement rebars, with pH values that are dropped below 9. The chlorides exist either as internal components of concrete, e.g., due to the incorporation of aggregates from a site close to the sea, or through the addition of chloride salts as admixtures in the concrete mix. Moreover, the chlorides can originate from the surrounding concrete environment, particularly in coastal areas. The first consequence of exposing reinforced concrete to chlorides is the deterioration of the protective oxide layer that surrounds the reinforcement rebars. This layer is a product of the high alkalinity of the concrete surrounding the reinforcement, and its loss exposes the steel rebars to a corrosive environment, as shown in Figure 4.

In summary, aging results in the degradation of concrete durability through the reduction in both concrete and steel reinforcement properties. Moreover, aging results in a reduction in the effective cross-sectional area of rebars and degrades the mechanical performance of steel rebars (Figure 4b). A loss of the concrete–steel bond is also observed.
2.2. Corrosion Mechanism

The corrosion of RC structures exhibits two phases: the *initiation period* and the *propagation period* [10]. Figure 5 shows the level of structural deterioration as a function of the two phases. Furthermore, Figure 6 shows the impact of reinforcement corrosion on an RC cross-section [11]. The first phase involves the initiation of corrosion, where chloride penetration and/or carbonation of concrete occurs. This period does not harm the concrete or the reinforcement [12]. The reinforcement is de-passivated [1] and the propagation phase starts when the carbonation front reaches the reinforcement, or the chloride concentration at the reinforcement reaches a critical threshold value. This is indicated as point 1 in Figure 5. During the propagation phase, the reinforcing element displays cracks (point 2) leading to spalling (point 3) of the concrete cover. Finally, the loss of the reinforcement cross-section or the bond failure may reduce the load-bearing capacity of structural elements and may lead to the collapse of the structure (point 4). The estimation of the corrosion initiation time and environmental and structural parameters, as well as the effects of the corrosion on the RC structure elements during the propagation phase, are discussed in the following sections.
simplicity in analyses or calculations. However, engineers must recognize its limitations and consider potential variations in corrosion effects when evaluating the performance of a structure over its service life. Starting from the uncorroded phase (Figure 6a), the corrosion builds up, leading to concrete cracking and spalling (Figure 6c,d). More specifically, after the corrosion initiation period, corrosion products appear on the steel surface, corresponding to the line between points 1 and 2 in Figures 5 and 6b. This process results in the reduction of the nominal diameter of the reinforcement steel while the volume of the rebar increases. This phenomenon usually leads to cracking and spalling of the concrete cover (see Figure 6c,d, and points 2 and 3 in Figure 5). Both cracking and spalling reduce the strength of the cover concrete and the bond strength of the two materials. Based on the above, in order to simulate the impact of chloride-induced corrosion, we focus on the following: (i) the reduction in the reinforcing steel’s cross-section along with the reduction in ductility; and (ii) the reduction in the compressive strength of the concrete cover.

**Figure 6.** The effects of reinforcement corrosion on RC cross-section: (a) uncorroded reinforcement, (b) build-up of corrosion products, (c) cracking, and (d) spalling.

### 3. Seismic Fragility Assessment of Structures

Fragility curves are useful tools for assessing the seismic capacity of RC buildings. The fragility of a system is the probability that an engineering demand parameter, $EDP$, exceeds a threshold value, $edp$; it is defined as follows:

$$F_R(IM) = P(EDP > edp | IM)$$

(1)

Engineering demand parameters, $EDPs$, are quantities that characterize the system response, and $IM$ denotes the intensity measure of interest. The $EDPs$ usually considered for the performance assessment of RC buildings include member plastic hinge rotations or the story maximum inter-story drift ratio ($IDR$); both parameters are directly related to the limit state demand. Suitable $IM$s for building structures include peak ground acceleration $PGA$, or, more preferably, spectral acceleration at the fundamental period $S_a(T_1, 5\%)$. For the present study, the $EDP$ and $IM$ adopted are the maximum inter-story drift $IDR$ and the first-mode spectral acceleration $S_a(T_1, 5\%)$.

If the $EDP$ values are known for certain $IM$ levels, and assuming that the data follow the lognormal distribution, the probability of a limit state threshold, $edp$, being surpassed is given by the following expression:

$$P(EDP \leq edp | IM) = \Phi \left[ \frac{\ln(EDP) - \mu_{\lnEDP}}{\sigma_{\lnEDP}} \right]$$

(2)

where $\Phi$ is the standard cumulative distribution function, $\sigma_{\lnEDP}$ is the logarithmic standard deviation of the logarithms of the $EDP$, and $\mu_{\lnEDP}$ is the mean value of the logarithms of the $EDP$. Figure 7 compares the fragility curves, considering either the same mean value or the same standard deviation. Thus, the two solid lines have different mean values but the same standard deviation, while blue lines have the same mean value and different standard deviations.
Figure 7. Definition of fragility curve parameters $\mu_{\ln EDP}$ and $\beta = \sigma_{\ln EDP}$.

3.1. Fragility Analysis Methods

3.1.1. Multiple-Stripe Analysis

The limit state fragility curves of a system can be calculated using different approaches. The incremental dynamic analysis (IDA) method is a common tool. IDA involves subjecting the system to a suite of ground motion records, each scaled to multiple levels of intensity. After incrementally scaling every ground motion, single-record capacity curves are produced in terms of demand versus seismic intensity. IDA has conceptual similarities to the multiple-stripe analysis (MSA) method [13], where instead of scaling up every ground motion, the records are scaled to the same IM level. Since—for every scaling level—the ground motions have the same IM value, the EDP values form a “stripe”, which allows us to directly calculate the median (50% percentile) and the 16% and 84% percentile capacity curves conditional on the IM. Strictly speaking, in IDA, the scaling factors will be different, but stripped data can be easily obtained with interpolation.

3.1.2. Cloud Analysis

If the data are not stripped, then they will form a “cloud”, and the “cloud analysis” method has to be adopted instead. Cloud analysis is a common method when the data are scattered in the $\ln EDP$-$IM$ plane. This occurs when the ground motions are left unscaled, or when they have all been scaled with the same factor. A linear fit provides the mean of the logarithms ($\mu_{\ln EDP}$) and a single constant value for the dispersion $\sigma_{\ln EDP}$. The knowledge of $\mu_{\ln EDP}$ and $\sigma_{\ln EDP}$ facilitates the fragility calculation. More details can be found in the work by Fragiadakis and Diamantopoulos [14].

3.1.3. Maximum Likelihood (MLE) Fitting

A maximum likelihood (MLE) fitting can be also adopted, either when the data are striped or form a cloud in the $EDP$-$IM$ plane. The MLE fitting approach fits the CDF (cumulative distribution function) of a lognormal distribution on the $EDP$-$IM$ data; thus, the fragility function is simply a lognormal CDF of the following form:

$$F_R = P(EDP \geq edp) = \Phi \left( \frac{\log(EDP/\theta_a)}{\beta_a} \right)$$

where $\theta_a$ and $\beta_a$ are the median and dispersion that have to be determined by maximizing the likelihood function.

At discrete IM levels (stripes), the multiple-stripe analysis provides the number of successes $n_{\text{succ}}$, i.e., the number of simulations in which the limit state has been exceeded after $n_{\text{tot}}$ total simulations. Using the binomial distribution on the data of a single stripe, the probability of having exactly $n_{\text{succ}}$ successes after $n_{\text{tot}}$ simulations will be as follows:
\[ P(\text{Success} = n_{\text{suc}}) = \left( \frac{n_{\text{tot}}}{n_{\text{suc}}} \right) P(EDP_{(s)})^{n_{\text{suc}}} (1 - P(EDP_{(s)}))^{n_{\text{tot}} - n_{\text{suc}}} \]  

(4)

If there are \( k \) stripes, substituting Equation (3) into Equation (4), we obtain the MLE function as follows:

\[ L = \prod_{i=1}^{k} \left( \frac{n_{\text{tot},i}}{n_{\text{suc},i}} \right) \phi \left( \frac{\log(EDP/\theta_a)}{\beta_a} \right)^{n_{\text{suc},i}} \left( 1 - \Phi \left( \frac{\log(EDP/\theta_a)}{\beta_a} \right) \right)^{n_{\text{tot},i} - n_{\text{suc},i}} \]  

(5)

The only unknowns are parameters \( \theta_a \) and \( \beta_a \), which are the values that maximize the likelihood function \( L \) of Equation (5), or preferably, its natural logarithm. This can be easily achieved with a spreadsheet or a simple computer script. Note that the fit is performed on all the data. If the EDP-IM pairs form a cloud, each simulation is assumed as a stripe. Therefore, \( k \) is the number of simulations, \( n_{\text{tot}} \) is equal to one \( (n_{\text{tot}} = 1) \), and \( n_{\text{suc}} \) is equal to one or zero, depending on whether the simulation exceeds the limit state threshold or not. The fragility curves presented in the following sections were obtained by using the above modeling approach.

3.1.4. SPO2IDA Tool

Another approach for the fragility calculation is based on the SPO2IDA (static pushover to incremental dynamic analysis) tool. This tool can be easily extracted from the work of Fragiadakis and Vamvatsikos [15], who proposed a method for estimating the median incremental dynamic analysis (IDA) capacity curve and its fractiles from the backbone of the static pushover. Once the fractile IDAs are known, calculating the fragility curves becomes straightforward; hence, this methodology enables their rapid estimation. The following lines describe the steps of the approach.

Initially, the pushover (backbone) curve of the building is obtained. The pushover curve is then trilinearized using optimum fitting, as discussed in reference [15], in order to define the theoretical “yielding” and “ultimate” displacement. The trilinear force-displacement \( (F-d) \) capacity curve is then converted to the \( F^*/d^* \) curve of the equivalent single-degree-of-freedom (ESDOF) oscillator using the N2 method. The force, \( F^* \), and the displacement, \( d^* \), of the ESDOF are related to the structure’s base shear and roof displacement with the aid of the first mode modal participation factor, \( \Gamma_1 \).

Once the period and the \( F^*/d^* \) curve of the equivalent SDOF system are obtained, the median and the 16th and 84th percentile fractile IDA curves are approximately calculated using the SPO2IDA tool, as discussed in reference [15]. These IDA fractiles of the SPO2IDA tool are provided in normalized \( R-\mu \) coordinates. The strength reduction factor, \( R \), is defined as the ratio \( S_a(T_1,5\%) / S_a^{\text{yield}}(T_1,5\%) \), where \( S_a^{\text{yield}}(T_1,5\%) \) denotes the values of the first spectral acceleration causing the yield point. The ductility, \( \mu \), is the maximum displacement of ESDOF, normalized by the yield displacement.

Assuming appropriate limit state thresholds and the IDR as the engineering demand parameter, the fragility curves are calculated from the IDA curves. More specifically, from the fractile IDA curves, for every IM level, one can calculate the mean, \( \mu_{\text{InEDP}} \), and a standard deviation, \( \sigma_{\text{InEDP}} \), in a straightforward manner, as follows:

\[ \mu_{\text{InEDP}} = \ln \left( S_{a,f,50\%} \right) \]  

(6)

\[ \sigma_{\text{InEDP}} = \ln \left( S_{a,f,50\%} / S_{a,f,16\%} \right) \]  

(7)

where \( (S_{a,f,x\%}) \) is the \( x\% \) fractile of the structural intensity causing exceedance of one limit state. This approach does not provide a lognormal CDF as the fragility curve. However, a CDF can be easily fitted with MLE fitting. This allows the characterization of the fragility curves with the aid of mean and standard deviations (Figure 7).
4. Past Research on the Fragility Assessment of Corroded RC Structures

For the capacity assessment of reinforced concrete (RC) structures, it is necessary to consistently consider the impact of corrosion, even in the absence of robust assessment methodologies. Numerous studies have aimed to investigate the impact of corrosion on the seismic capacity and fragility of RC buildings, recognizing that aging can significantly reduce structural capacity under a strong earthquake. For instance, Karapetrou et al. [16] investigated the effects of chloride-induced corrosion on the seismic vulnerability of three RC buildings in a marine environment. Similarly, Geng et al. [17] examined the effects of carbonation-induced corrosion on the seismic fragility of RC buildings in an inland atmosphere. In the work by Dizaj et al. [18], the spatial variability of pitting corrosion and the record-to-record variability on the seismic vulnerability of RC frames were investigated. Moreover, Dizaj et al. [19] described the effects of chloride-induced corrosion in terms of mass loss percentage when the studied frame structure was subjected to mainshock-aftershock sequences. Guidelines for modeling the effects of reinforcement corrosion on the mechanical properties of steel and concrete were provided by Dizaj et al. [20]. Finally, Yu et al. [21] summarized the corrosion damage models available for RC structures and investigated their impact on the seismic fragility assessment of RC buildings.

In a more applied context, Yalciner et al. [22] investigated a 50-year-old high school building that had undergone extensive corrosion. The corrosion level was defined, based on specimens extracted from the building, and seismic fragility curves were provided. Furthermore, Karapetrou et al. [23] examined the impact of corrosion on the performance of an existing hospital building by integrating field monitoring data with finite element models. Couto et al. [24] modeled three RC buildings with masonry infills, representing the existing building stock in Portugal. They estimated the impact of reinforcement corrosion for various exposure scenarios. Evangelisti et al. [25] conducted experimental measurements in an old Italian building from the 1960s, which had experienced aging and weathering effects. In a more general process, Tomás et al. [26] proposed new values of behavior modifiers for the seismic vulnerability evaluation of RC buildings, using data from a real earthquake.

The impact of corrosion on buildings designed according to old design codes, with limited or no seismic provisions, has been a notable subject in the literature. For instance, Di Sarno and Pugliese [27] delved into the influence of various seismic intensity measures (IMs) on the seismic capacity of three corroded reinforced concrete (RC) buildings. Furthermore, the same authors [28] explored mainshock-aftershock ground motion sequences and exposure to different levels of corrosion to estimate the seismic fragility of existing RC buildings. In reference [29], the authors discussed the impact of near-field and far-field records on corroded RC frames. All the above studies conclude that reinforcement corrosion is a major parameter that influences the degradation of RC structures and significantly affects their seismic capacity.

In several publications from the above section, the impact of aging was investigated by comparing fragility curves between corroded and uncorroded building models. Quantitative comparisons reveal that the impact of aging may range from negligible to significant, depending on the parameters, such as the cover depth, the corrosion rate, and the limit states, among others. When assuming mean value fragility curves, there are instances where the probability of exceedance remains practically unaffected, as seen in the work of Geng et al. [17]. On the other hand, studies indicate that the increase in fragility, measured by the mean fragility values, can be in the order of 60–65%, as shown in work by Dizaj and Kashani [20]. These substantial differences found in the literature contribute to the complexity of understanding the impact of aging on the structural response, especially in the presence of seismic actions.

In summary, Table 1 shows the influence of aging on the fragility curves of building structures, as obtained from some of the aforementioned studies. The table shows the percentage of the mean value increase of the fragility curve, assuming that the
dispersion is practically not affected. In other words, Table 1 gives the quantity of \( \lambda \) that measures the increase:

\[
\lambda = \frac{|\mu_{\text{pristine}} - \mu_{\text{corroded}}|}{\mu_{\text{pristine}}}
\]  

(8)

It should be noted that Table 1 shows the variation of the fragility curve’s mean value. Due to the fact that different research publications consider different limit states, we summarize three limit states, LS1, LS2, and LS3 (qualitatively); the percentage of increase is calculated following Equation (8).

Table 1. Influence of aging on the mean of the fragility curves (\( \mu_{\text{EDP}} \)) of different RC structures in terms of percentage modification at 40 to 60 years after construction.

<table>
<thead>
<tr>
<th>Paper</th>
<th>t Years</th>
<th>LS1</th>
<th>Min</th>
<th>Max</th>
<th>LS2</th>
<th>Min</th>
<th>Max</th>
<th>LS3</th>
<th>Min</th>
<th>Max</th>
</tr>
</thead>
<tbody>
<tr>
<td>Karapetrou et al. [16]</td>
<td>50</td>
<td>-</td>
<td>-</td>
<td>0.17</td>
<td>0.24</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Dizaj et al. [20]</td>
<td>40</td>
<td>0.15</td>
<td>0.17</td>
<td>0.49</td>
<td>0.52</td>
<td>0.44</td>
<td>0.49</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Yalciner et al. [22]</td>
<td>50</td>
<td>0.25</td>
<td>0.25</td>
<td>0.15</td>
<td>0.15</td>
<td>0.41</td>
<td>0.41</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Couto et al. [24]</td>
<td>40–60</td>
<td>0.11</td>
<td>0.17</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Karapetrou et al. [23]</td>
<td>45</td>
<td>0.013</td>
<td>0.15</td>
<td>0.18</td>
<td>0.36</td>
<td>-</td>
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<td></td>
</tr>
<tr>
<td>Pugliese and DiSarno [29]</td>
<td>50</td>
<td>0.25</td>
<td>0.63</td>
<td>0.28</td>
<td>0.61</td>
<td>0.28</td>
<td>0.55</td>
<td></td>
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</tbody>
</table>

Table 2 shows the same comparison for structures that were investigated, considering a practically similar corrosion reinforcement level, \( CL (\%) \). The corrosion level, \( CL (\%) \), in terms of area loss, is expressed as follows [28]:

\[
CL(\%) = \frac{A_0 - A_p}{A_0} \times 100
\]  

(9)

where \( A_0 \) is the uncorroded steel bar area, and \( A_p \) is the net cross-sectional area of the corroded rebar. The table provides insight into the influence of aging on the fragility curves of different building structures. There are cases in which the influence of aging is found to be negligible (e.g., 1–2%) and others that confirm that the modification of the mean of the fragility curve can rise to 65%. This increase tends to be smaller for the upper limit states, while for the ultimate limit state (practically close to collapse), the first two papers cited do not provide information.

Table 2. The influence of aging on the fragility curves in terms of percentage modification, considering the evaluation for \( CR = 10\% \).

<table>
<thead>
<tr>
<th>Paper</th>
<th>CL %</th>
<th>LS1</th>
<th>Min</th>
<th>Max</th>
<th>LS2</th>
<th>Min</th>
<th>Max</th>
<th>LS3</th>
<th>Min</th>
<th>Max</th>
</tr>
</thead>
<tbody>
<tr>
<td>Dizaj et al. [18]</td>
<td>10</td>
<td>-</td>
<td>-</td>
<td>0.525</td>
<td>0.526</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>DiSarno &amp; Pugliese [27]</td>
<td>10</td>
<td>0.44</td>
<td>0.448</td>
<td>0.4</td>
<td>0.412</td>
<td>-</td>
<td>-</td>
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<td>-</td>
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<tr>
<td>DiSarno &amp; Pugliese [28]</td>
<td>10</td>
<td>0.368</td>
<td>0.411</td>
<td>0.22</td>
<td>0.276</td>
<td>0</td>
<td>0</td>
<td></td>
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</tr>
</tbody>
</table>

5. Corrosion Modelling

5.1. Initiation Time of Corrosion

Concrete service life models such as DuraCrete [30–32], LIFECON [33], and the fib Bulletin 34 [12] provide probabilistic models in order to estimate the initiation time of chloride and carbonation-induced corrosion on RC structures. In this study, the corrosion model adopted consists of a combination of equations that already exist in the literature. Chloride-induced corrosion is assumed to be a critical source of reinforcement corrosion, considering that a large number of RC structures are exposed to chlorides, i.e., exposure classes XS1, XS2, and XS3, according to EC-2 [34]. The initiation time, \( T_{\text{init}} \), of chloride-induced corrosion can be estimated using the probabilistic model of fib Bulletin 34 [12]:
\[ T_{\text{init}} = \left( \frac{c_d^2}{4 \cdot k_e \cdot k_t \cdot D_{\text{RCM,0}} \cdot (t_0)^n} \cdot \left( \text{erf}^{-1} \left( 1 - \frac{C_{\text{crit}}}{C_S} \right) \right)^{-2} \right)^{\frac{1}{n}} \]  

(10)

where \( c_d \) is the concrete cover depth (mm), \( k_e \) is the environmental transfer variable, which is related to the temperature of the structural element or ambient air, and \( k_t \) is a regression parameter that considers the influence of the test method. \( D_{\text{RCM,0}} \) is the chloride migration coefficient (\( \text{m}^2/\text{s} \)) that depends on the water–cement ratio and the cement type. \( n \) is the aging exponent related to the cement type. Finally, \( C_{\text{crit}} \) is the critical chloride content, which leads to the depassivation of reinforcing steel (wt% / cement); it depends on the type of steel and the electrochemical environment in concrete. \( C_S \) is the chloride content at the concrete surface.

Therefore, in this work, the corrosion effects on structural elements are considered through three parameters: (i) the reduction in the diameter of the reinforcement rebars, (ii) the reduction in the cover compressive strength, and (iii) the reduction in ductility through the reduction in steel elongation at maximum load.

5.2. Reduction of Rebar Diameter and Ductility

During the propagation phase of chloride-induced corrosion, the diameter \( D(t) \) and the rebar area \( A(t) \) are calculated as follows [35]:

\[ D(t) = D_i - i_{\text{corr}}(t - T_{\text{init}}) \]  

(11)

\[ A(t) = \begin{cases} 
  n_{\text{bars}}D_i^2\pi/4 & t \leq T_{\text{init}} \\
  n_{\text{bars}}(D(t))^2\pi/4 & t > T_{\text{init}} 
\end{cases} \]  

(12)

where \( n_{\text{bars}} \) is the number of reinforcement rebars, \( D_i \) is the initial diameter of the rebar, and \( i_{\text{corr}} \) is the corrosion rate. The corrosion rate is expressed as current density in \( \mu\text{A/cm}^2 \), where \( v_{\text{corr}} \) (mm/year) \( \approx 0.0116i_{\text{corr}}(\mu\text{A/cm}^2) \), and it is affected by the availability of oxygen and water at the steel surface; therefore, it is related to environmental factors, the concrete quality, and the cover depth. The factor 0.0116 is a conversion factor of \( \mu\text{A/cm}^2 \) into mm/year for steel material [36]. The reduction in the ductility of reinforcement steel is taken into account through the reduction in steel elongation at maximum load. The experimental results provided by Rodriguez and Andrade [37] are used to assess the reduction in the ultimate steel deformation, \( \epsilon_{\text{su}} \). This reduction varies between 30% and 50%, while the loss of the reinforcement’s cross-sectional area varies from 15% to 28%, respectively. Thus, we use linear interpolation when the reinforcement’s cross-sectional reduction is between 15% and 28%, while for values smaller than 15%, we assume that the increase is linear. In other words, if the loss is 22.5%, then the \( \epsilon_{\text{su}} \) reduction is 40%; if the loss is 7.5%, the reduction is 15%.

5.3. Reduction in the Concrete Cover Compressive Strength

The reduced concrete cover’s compressive strength, \( f_{\text{c}}^* \), is calculated according to the model by Coronelli and Gambarova [38]:

\[ f_{\text{c}}^* = \frac{f_c}{1 + K \frac{\epsilon_{\text{CO}}}{\epsilon_1}} \]  

(13)

where \( K \) is a coefficient related to the rebar diameter and roughness and is equal to 0.1 for medium-diameter ribbed rebars. \( \epsilon_{\text{CO}} \) is the strain at peak compressive stress, \( f_c \), and \( \epsilon_1 \) is the average tensile strain of the cracked concrete, which is calculated as follows [38]:

\[ \epsilon_1 = \frac{b_f - b_0}{b_0} \]  

(14)
In Equation (14), $b_0$ is the initial section width before the corrosion initiation and $b_f$ is the increased section width due to rust expansion and corrosion cracking. An approximation of the increase of the section is obtained as follows [38]:

$$b_f - b_0 = n_{bars} w_{cr}$$ (15)

where $n_{bars}$ is the number of rebars under compression and $w_{cr}$ is the total crack width for a given corrosion intensity level, given as follows [38]:

$$w_{cr} = \sum_{i} u_{i,corr} = 2\pi (v_{rs} - 1)d_c$$ (16)

In Equation (16), $u_{i,corr}$ is the opening of each single corrosion crack, $v_{rs}$ is the ratio of the volumetric expansion of the rust products with respect to the initial material (e.g., equal to 2, as proposed by Simioni [39]) and $d_c$ is the depth of the corrosion attack equal to the reduction in the rebar radius.

6. Case Study

6.1. Four-Story RC Building under Corrosion

The four-story RC building shown in Figure 8 is considered as the case study. The structure is a modern building designed for Eurocode 2 and Eurocode 8, assuming ductility class high (DCH). The cross-section of the side columns of the first two stories is $40 \times 40$ cm and of the internal columns is $45 \times 45$ cm. On the third story, the side columns have a cross-section of $35 \times 35$ cm, while the internal columns are $40 \times 40$ cm. The columns of the top story have a cross-section of $35 \times 35$ cm and the cross-section of the beams is $30 \times 60$ cm for all stories. The column reinforced is $8 \varnothing 16$ mm, apart from the $45 \times 45$ cm cross-section that was reinforced with $8 \varnothing 20$ mm. The reinforcement of the beams is $3 \varnothing 12$ mm and $3 \varnothing 14$ mm, at the span and the supports, respectively.

![Figure 8. The four-story case study building.](image)

The building examined is located in Greece, and the national codes and annexes have been considered. It features a 2D frame structure designed with a behavior factor equal to 4, under the actions of a 475-year return period. The frame was modeled using OpenSees [40] software, assuming lumped masses at every story. The considered story mass equals 60t for every story, apart from the top, where it is assumed equal to 50t. The materials specified for the design are as follows: C20/25 for concrete and B500C for the reinforcement. A similar version of the building was discussed in work by Fragiadakis and Diamantopoulos [14], where further details are available. The building’s model was implemented in OpenSees using force-based fiber elements, employing Concrete04 and ReinforcingSteel materials for the concrete and steel fibers, respectively. Confined concrete strength is
considered, while second-order ($P$-$\Delta$) effects are explicitly taken into consideration in the numerical simulations.

Modal analysis was initially performed; the first eigenperiod of the uncorroded building was equal to $T_1 = 0.50$ s, with a high mass modal participation factor, indicating that the building is first mode-dominated. We should note that for the corroded cases, the fundamental period is always different, usually larger since the structure becomes more flexible. The latter can be seen from the pushover curves, as discussed in the next subsection. Furthermore, several works that evaluate the changes in the dynamic characteristics can be found in the literature, e.g., Ditommaso et al. [41] and Cataldo et al. [42].

The methodology described in Section 3 has been applied to both the corroded and uncorroded building models, and the corresponding seismic fragility curves were obtained.

The corrosion assumptions for the case study considered are as follows: (i) marine environment, (ii) atmospheric zone as the environment of the structure, (iii) ambient air temperature equal to 20 $^\circ$C, (iv) cement type CEM I used in the concrete mix, and (v) the water to cement ratio equal to 0.5, i.e., $w/c = 0.5$. These assumptions determine the parameters of the corrosion model adopted. More specifically, the statistical distribution, mean, and coefficient of variation (COV) of these five parameters are presented in Table 3. The parameters considered concern the effects of environmental and structural factors on the initiation of chloride-induced corrosion. Their definitions are based on the environmental conditions assumed and the characteristics of the structure considered.

Table 3. Statistical properties of the parameters that affect chloride-induced corrosion.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Mean</th>
<th>COV</th>
<th>Distribution</th>
</tr>
</thead>
<tbody>
<tr>
<td>$k_e$</td>
<td>0.676</td>
<td>0.17</td>
<td>Gamma</td>
</tr>
<tr>
<td>$k_t$</td>
<td>1.25</td>
<td>0.28</td>
<td>Normal</td>
</tr>
<tr>
<td>$D_{RCM,0}$ (m$^2$/s)</td>
<td>$1.58 \times 10^{-11}$</td>
<td>0.2</td>
<td>Normal</td>
</tr>
<tr>
<td>$t_0$ (years)</td>
<td>0.0767</td>
<td>-</td>
<td>Deterministic</td>
</tr>
<tr>
<td>$n$</td>
<td>0.362</td>
<td>0.677</td>
<td>Beta</td>
</tr>
<tr>
<td>$C_{crit}$ (wt% cement)</td>
<td>0.6</td>
<td>0.25</td>
<td>Beta</td>
</tr>
<tr>
<td>$C_S$ (wt% cement)</td>
<td>1.2825</td>
<td>0.35</td>
<td>Normal</td>
</tr>
</tbody>
</table>

The evaluation of chloride-induced corrosion effects through fragility analysis requires defining the parameters that mostly affect the initiation of corrosion and its propagation. For this purpose, the initiation time, $T_{init}$, should be calculated according to Equation (10). For all corroded realizations of the building, the reduced concrete cover strength and reduced reinforcement material properties should be determined by following Equations (12) and (13). This modification affects the member capacities, i.e., the beam and column moment-rotation, $M$-$\theta$ relationships, thus correspondingly reducing the global capacity.

The corrosion initiation time $T_{init}$ is calculated using Equation (10) for three cover depth $c_d$ values. Following modern design standards, the minimum cover value $c_d$ is 35 mm, while values 25 mm and 45 mm are also considered here for investigation purposes. The corresponding mean values of the corrosion initiation time $T_{init}$ are estimated to be equal to 7.34, 21.08, and 46.34, respectively.

6.2. Numerical Results

The seismic performance of the building was assessed at $t = 0$, 50, and 100 years after its construction in order to address the impact of corrosion on seismic fragility throughout the building’s service life. In all, 21 cases were examined, i.e., 3 uncorroded and 18 corroded building realizations. The limit states are considered and are identified based on the roof displacement of the static pushover curve. For this purpose, the pushover curve is trilinearized in order to identify the yield and the ultimate displacements, denoted as $d_y$ and $d_u$, respectively. Figure 9a presents both pristine and ideal pushover curves. Therefore, the three limit states correspond to moderate damage ($d_y$), severe damage ($d_y + 0.25(d_u - d_y)$),
and complete damage ($d_n$). Figure 9b shows the IDA curve that corresponds to the pushover curve of Figure 9a, as obtained from the SPO2IDA tool [15].

Figure 9. (a) Pushover curve of the pristine building and (b) the corresponding IDA curves.

Fragility analysis is more representative of the building’s capacity compared to static pushover analysis Figure 10, as it correlates demand with the corresponding limit state exceedance and, eventually, the limit state exceedance probability. Figure 10 compares the pushover curves, assuming either $t = 50$ years or $t = 100$ years and $i_{corr} = 0.1, 2$ µA/cm$^2$. The seismic fragility curves of the case study building were obtained using the methodology presented in Section 3. We should note that possible brittle collapse mechanisms (shear failure) of the columns are not considered in the fragility assessment. In all cases, they are estimated, assuming the first-mode spectral acceleration $S_a(T_1, 5\%)$ as IM and the maximum roof drift $RDR$ as EDP. The fragility curves shown below focus on the moderate damage (LS1) and complete damage (LS3) limit states.

Figure 10. Effect of $i_{corr}$ on pushover curves, assuming $c_d = 25$ mm and (a) $t = 50$ years, and (b) $t = 100$ years.

Figures 11 and 12, investigate the influence of corrosion, considering different assumptions for the age of the case study structure, i.e., $t = 0, 50, 100$ years. Figure 11 examines the LS1 while Figure 12 considers the LS3. In both plots, very small and medium corrosion rate values, i.e., $i_{corr} = 0.1$ µA/cm$^2$ and $i_{corr} = 2$ µA/cm$^2$, are assumed. Due to the two-dimensional structure, all columns are assumed with the same corrosion rate, even if different values should be adopted for external and internal columns of a three-dimensional structure.

From Figures 11a and 12a, it can be observed that small values of the corrosion rate, i.e., $i_{corr} = 0.1$ µA/cm$^2$, cannot affect the fragility curve, even if the cover depth is $c_d = 25$ mm.
However, $i_{corr} = 2 \, \mu\text{A/cm}^2$ always reduces the structural capacity, a point that becomes obvious considering Figures 11b and 12b.

Furthermore, in Figure 13, the influence of cover depth is examined. LS1 and LS3 are assumed in Figure 13a and Figure 13b, respectively. It is highlighted that a cover depth equal to 45 mm improves seismic fragility, especially in the case of larger building service life, i.e., $t = 100$ years for both limit states considered. For the first limit state, the difference between the fragility curves that correspond to cover depths equal to 35 and 45 mm is not as substantial as in the case of the complete damage limit state.

In all cases examined, the results demonstrate the discrepancy between the fragility curves of the corroded and uncorroded buildings, as well as the range of the mean values of the fragility curves, assuming that the standard deviation of the curves remains, practically, constant. It can be observed that the dispersion of the mean values of the fragility curves decreases as the cover depth increases. This observation verifies the impact of the cover depth on the seismic performance of RC buildings.

![Figure 11](image1)

**Figure 11.** Moderate damage (LS1) fragility curves when comparing the different $t$-values examined when the corrosion rate is equal to (a) $i_{corr} = 0.1 \, \mu\text{A/cm}^2$ and (b) $i_{corr} = 2 \, \mu\text{A/cm}^2$.

![Figure 12](image2)

**Figure 12.** Complete damage (LS3) fragility curves when comparing the different $t$-values examined when the corrosion rate is equal to (a) $i_{corr} = 0.1 \, \mu\text{A/cm}^2$ and (b) $i_{corr} = 2 \, \mu\text{A/cm}^2$. 
Figure 13. Fragility curves for constant $i_{\text{corr}} = 2 \, \mu A/cm^2$ and $c_d = 25, 35, 45 \, \text{mm}$ for (a) LS1 and (b) LS3.

In order to compare the current work with the literature, Table 4 is introduced. Table 4 presents the percentage decrease (Equation (8)) of the mean value of the fragility curves between the corroded and pristine buildings. It includes both 50 and 100 years for comparison purposes. It can be observed that this increase is larger for LS3, while in all cover depths, this increase is almost similar for LS2 and LS3. The fragility modification is always more critical for lower values of the cover depth, considering all limit states and both $t = 50$ and 100 years. For example, the mean value of the fragility curve, considering LS1, is modified approximately 40% for $c_d = 25 \, \text{mm}$ in $t = 100 \, \text{years}$, while the same modification is equal to 18% when $c_d = 45 \, \text{mm}$. Comparing Table 4 with Table 1, it can be observed that the fragility curve of a new building that follows contemporary design codes and has a minimum cover depth equal to 35 mm has not changed by more than 10% during its service life. This percentage can be equal to 37% in the case of $t = 100 \, \text{years}$. In fact, the current work demonstrates the modifications, showing that when the cover depth increases, the fragility curve modification is not as significant as in the case of lower values of the cover depth. The worst case is always the larger value for the corrosion rate, i.e., $i_{\text{corr}} = 2 \, \mu A/cm^2$, and the minimum value for the cover depth, i.e., $c_d = 25 \, \text{mm}$.

Table 4. The influence of aging on the fragility curves in terms of percentage modification, considering the evaluation for 50 and 100 years after the construction of the case study building.

<table>
<thead>
<tr>
<th>$t$ Years</th>
<th>$c_d$ mm</th>
<th>LS1 Min</th>
<th>LS1 Max</th>
<th>LS2 Min</th>
<th>LS2 Max</th>
<th>LS3 Min</th>
<th>LS3 Max</th>
</tr>
</thead>
<tbody>
<tr>
<td>50</td>
<td>25</td>
<td>0.00</td>
<td>0.21</td>
<td>0.00</td>
<td>0.22</td>
<td>0.00</td>
<td>0.22</td>
</tr>
<tr>
<td></td>
<td>35</td>
<td>0.00</td>
<td>0.09</td>
<td>0.00</td>
<td>0.03</td>
<td>0.00</td>
<td>0.04</td>
</tr>
<tr>
<td></td>
<td>45</td>
<td>0.00</td>
<td>0.04</td>
<td>0.00</td>
<td>0.05</td>
<td>0.00</td>
<td>0.06</td>
</tr>
<tr>
<td>100</td>
<td>25</td>
<td>0.00</td>
<td>0.40</td>
<td>0.00</td>
<td>0.49</td>
<td>0.00</td>
<td>0.51</td>
</tr>
<tr>
<td></td>
<td>35</td>
<td>0.00</td>
<td>0.31</td>
<td>0.00</td>
<td>0.35</td>
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</tr>
<tr>
<td></td>
<td>45</td>
<td>0.00</td>
<td>0.18</td>
<td>0.00</td>
<td>0.19</td>
<td>0.00</td>
<td>0.19</td>
</tr>
</tbody>
</table>

7. Conclusions

Quantifying the impact of aging on RC structures is a complex task characterized by considerable variability. Quantifying the impact of corrosion on the dynamic characteristics of numerical models is not proposed in the current work. However, it should be noted that for corroded cases, the fundamental period is always larger than the pristine structure. In this study, the impact of aging on fragility assessment is investigated through a seismic fragility analysis of a case study structure. It was found that the most significant parameter that affects corrosion initiation is the cover depth. Moreover, the corrosion rate, $i_{\text{corr}}$, affects the area of the rebar during the propagation phase of chloride-induced corrosion; thus,
both parameters are investigated in detail. In order to systematically assess the influence of both structural and environmental factors on fragility assessment, the outcomes of this study are compared with findings from the literature. It should be noted that, despite the inherent complexity of the problem at hand, this paper can be considered an attempt to quantify the impact of aging at a probabilistic level.

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**References**


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