A Review of Point Absorber Wave Energy Converters

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Abstract: There are more than thousands of concepts for harvesting wave energy, and wave energy converters (WECs) are diverse in operating principles, design geometries and deployment manners, leading to misconvergence in WEC technologies. Among numerous WEC devices, the point absorber wave energy converter (PAWEC) concept is one of the simplest, most broad-based and most promising concepts that has been investigated intensively all over the world. However, there are only a few reviews focusing on PAWECs, and the dynamical advancement of PAWECs merits an up-to-date review. This review aims to provide a critical overview of the state of the art in PAWEC development, comparing and contrasting various PAWEC devices and discussing recent research and development efforts and perspectives of PAWECs in terms of prototyping, hydrodynamic modelling, power take-off mechanism and control.

Keywords: point absorbers; wave energy converters; point absorber wave energy converters; wave energy conversion; point absorber prototypes

1. Introduction

“Net zero by 2050” is one of the most urgent missions for the world. By 2020, over 110 countries committed to achieving zero carbon emissions by 2050 [1]. On the other hand, humans’ demand for energy increases dramatically with the continuous growth in the population and economy. The US Energy Information Administration (EIA) predicted that the world’s energy consumption would increase by nearly 50% between 2018 and 2050 [2]. The Emissions Gap Report 2020 [3] highlighted that “despite a dip in greenhouse gas emissions from the COVID-19 economic slowdown, the world is still heading for a catastrophic temperature rise above 3 °C this century—far beyond the goals of the Paris Agreement.” Thus, there exists a widening gap between global energy demand and carbon reduction promises [4], and extra technical and nontechnical efforts are needed.

Renewable energy was predicted, according to the EIA report in 2019 [2], to be the leading source of primary energy consumption by 2050, especially for electricity generation [5]. Among various renewable energy resources, wave energy shows great potential in generating electricity for carbon emission reduction. Although wave energy is considered a relatively untapped resource, its global reserve is estimated to be in the range of 1–10 TW. In terms of the exploitable wave power resource, the estimate was around 29,500 TWh/year [6–10], which exceeded the global electricity consumption in 2018 of around 22,300 TWh [11]. Compared with other renewable resources, especially the more tapped solar and wind power, the advantages of wave power are multiple, as detailed below:

- Wave power is of a higher power intensity than solar and wind power. For instance, the intensities of solar, wind and wave power are 0.17 kW/m², 0.58 kW/m² and 8.42 kW/m², respectively, at a latitude of 15° N within the Northeast Trades [12].
• Wave power has high availability, being available up to 90% of the time, while the availability of solar and wind power ranges from 20% to 30% [13].
• Wave power is of a higher predictability than solar and wind power [14,15], resulting in higher flexibility for regional or national power dispatching.
• Wave energy conversion devices can be integrated with existing offshore wind or solar power plants for smoothing power output and reducing power variability [16–21].
• Harvesting wave energy is currently considered environmentally friendly, as several sea trials only showed little impact on the oceanic environment [22,23]. Currently, most WECs are designed and optimised for energetic sites, and the device size should be downscaled accordingly to perform well in low-energy seas [24].

The idea to utilise ocean waves dates back to 1799 [25], and more than 1000 patents had been registered by 1980 [12]. Since 1998, remarkable advances have been achieved to promote the technology readiness level (TRL) and technology performance level (TPL) [26] of wave energy converters (WECs). Recent research and development (R&D) efforts are devoted to developing novel modelling methods [27–30], applying creative power take-off (PTO) mechanisms [13,31–36], investigating modern control strategies [37–41] and conducting sea trials [42–48].

Compared with the huge reserve of exploitable wave power potential (around 3 TW [8]), the installed capacity of wave energy is as small as 2.31 MW [10,49]. Large-scale application of WEC devices is hindered by its high levelised cost of energy (LCoE), and there is no fully commercial-scale WEC farm in operation [50]. The LCoE of wave energy ranges from EUR 90/MWh to EUR 490/MWh, which is much higher than that of fossil fuels and other renewable resources [51]. Although hundreds of WECs have been developed and tested [52], there still exist a few challenges: (1) Wave force is of a low frequency (about 0.1 Hz) and large amplitude (up to 1 MN) [53]. Hence, the velocity of WEC oscillation may vary significantly. In general, a generator is optimised to operate at a certain high speed and can only perform efficiently around its rated condition. Thus, it is difficult to generate electricity efficiently and effectively from oscillating WEC motion. In addition, a large wave force induced by extreme waves may cause damage to WECs, and the reliability of WEC structures and power take-off (PTO) mechanisms should be high. (2) WECs operate in an offshore environment, and the harsh environment results in a high cost in WEC installation, operation and maintenance (O&M) [50]. Lastly, (3) extreme sea conditions, such as storms, hurricanes and typhoons, occur from time to time. WEC structures are prone to being damaged or even destroyed in extreme sea states, which may cause enormous economic losses. The WEC survivability in extreme events is still challenging.

In general, WEC devices can be classified according to their deployment locations, working principles, operation modes and design geometries [30,53–56]. It is worth noting that there is no such mutually exclusive and collectively exhaustive categorisation method to cover all WEC concepts. In this paper, the classification based on device geometry is used, and WECs are classified as point absorbers (PAs), attenuators and terminators, as shown in Figure 1. The PA concept was first defined in 1975 [57], referring to a WEC with relatively small dimensions with respect to the wavelength. This definition is not associated with PAs’ deployment manners, operating degrees of freedom (DoFs) or hull geometries. Thus, PAs can be installed in a floating or submerged manner, may oscillate in single or multiple DoFs and may capture wave power with single or multiple PA bodies.
Figure 1. According to the geometries and orientations of wave energy converters, WECs can be classified as point absorbers, terminators and attenuators, with the Seabased device [58], the Oyster I device [59] and the Pelamis device [60] as typical prototypes.

A WEC device converts the kinetic or potential energy contained in sea waves to useful energy (mainly in the form of electricity), consisting of floating or submerged bodies, PTO units, control systems, power electronics and other accessories. Several review papers have been published on WEC modelling [29,61–63], PTO [36,64], control [37,39,41] and optimisation [56,65]. These review papers are for generic WECs and hence are inspiring for understanding the modelling, PTO, control and optimisation of PAs. Different from attenuators and terminators, PAs show some distinctively technical and nontechnical characteristics, which are detailed below:

- The PA concept is one of the simplest concepts in system structures [66,67]. Thus, PAs may be easy to manufacture, reliable to operate and economical to maintain.
- The PA concept is one of the most broad-based concepts with intensive R&D activities. More than half of the R&D activities of wave energy are based on the PA concept [13,56,68].
- PAs are appropriate for developing and testing novel ideas, including new modelling methods, novel PTO mechanisms and creative control strategies. For instance, the resonance concept [57], reactive control [69], park effect [70] and power limit [71] were first proposed and tested for PA devices.
- PAs are applicable to a wide range of sea states in various deployment sites, and PAs’ sizes can be easily optimised to fit the wave climates of certain sites. In general, PAs are small and thus expected to be more economical [24,72].

Due to the advantages motioned above, the PA concept was generally used to develop innovative ideas. Based on PA devices, the concepts of “resonance”, “absorption length” and “power optimisation” were first defined [57], the theoretical maxima of absorption were first derived [73], and the latching control and reactive control were first proposed and tested [69,74]. The constructive park effect of WEC arrays was first studied in [70], and the feedforward control was first studied to overcome the non-causality problem of WEC control [75]. Even to date, the PAWEC is one of the “hottest” WEC types. Although the PA concept has been intensively investigated theoretically and practically, there are only a few review papers on PA devices published in the literature. Readers are referred to [76,77]. Thus, this review aims to discuss recent developments in PAWEC devices by (1) demonstrating some typical PAWEC prototypes, (2) reviewing ongoing hydrodynamic...
modelling methods, PTO mechanisms and control strategies for PAWECs and (3) discussing the R&D trends related to PAs.

The reminder of the paper is organised as follows. Section 2 discusses some notable PAWEC prototypes of high TRLs, while Section 3 briefly introduces the hydrodynamic modelling methods. Section 4 summarises the development of PTO systems devoted to PAWECs, with Section 5 examining the control strategies. Section 6 summarises the perspectives on PAWEC concepts, hydrodynamics, PTOs, control and applications. Finally, some concluding remarks are drawn in Section 7.

2. Point Absorber Prototypes

2.1. Classification of Point Absorbers

As shown in Figure 2, PAs can be further classified as (1) one-body and multi-body PAs according to design geometry, (2) floating and submerged devices, according to the deployment manner, and (3) single-DoF and multi-DoF prototypes, according to the operating DoFs. This paper uses the geometry-based classification method, and this section briefly introduces some typical prototypes of the one-body and multi-body PAs in Sections 2.2 and 2.3, respectively. These typical prototypes, which are detailed in this section, are of a high TRL (>6) and have been experimentally tested in a representative environment (sea trail).

![Figure 2](image)

**Figure 2.** Point absorber wave energy converters can be further classified into subcategories according to the design geometry, manner of installation and operating mode.

2.2. One-Body Point Absorbers

A one-body PA device is referenced to a fixed or absolute point (e.g., the sea bed). There are two main subtypes of one-body PAs: the floating one-body PAs and the submerged one-body PAs, as shown in Figure 3. The most notable floating one-body PAs include the Seabased device, the LifeSaver model and the CorPower prototype, detailed in Section 2.2.1. The AWS device and the CETO device are exemplified as the typical submerged one-body PAs in Section 2.2.2.

![Figure 3](image)

**Figure 3.** The working principles of floating and submerged one-body point absorbers are illustrated in (a,b), respectively.

2.2.1. Floating One-Body Point Absorbers

A floating PA comprises a floating body interacting with surface waves and a PTO unit referenced or anchored to the sea bed. The floating body oscillates under the excitation of waves, and its motion drives the PTO mechanism to generate electricity. Among various floating one-body PAs, the Seabased device, the LifeSaver model and the CorPower prototype are typified in Figure 4.
The Seabased device is one of the most notable floating one-body PAs. As shown in Figure 4a, a floating truncated cylinder is used to capture wave power, and its motion drives a seabed-mounted linear generator via a rope to produce electricity [80]. Although the Seabased device oscillates in 6 DoFs, its dynamics are dominated by the heave motion, and a simplified mathematical model with heave only can give a good representation of the device’s performance [81]. At full scale, the buoy is 3 m in diameter and 0.8 m in height, with a permanent magnate linear generator rated at 10 kW [82,83]. The Seabased devices can be easily deployed to form an array. The sea trial of a small array with four devices addressed the importance of passive control in power maximisation [84], and another sea trial at Lysekil also demonstrated that PAs have a limited negative impact on the ocean environment [85].

As shown in Figure 4b, the LifeSaver device utilises a circular buoy consisting of three segments. For each segment, a PTO unit is installed and moored to the seabed via a winch line. The full-scale device has an outer diameter of 16 m, an inner diameter of 10 m and a height of 1 m, with a total rated power of 30 kW [86,87]. The mooring lines are uniquely integrated as part of the winch and rope PTO units, which can only generate electricity when the circular buoy moves upwards. Thus, the peak-to-average power ratio is as high as 60, and energy storage is required to smooth the generated power [86]. In extreme conditions, the PTO units experienced several structure failures. The redundant design in the PTO ensured the device would operate continuously in a long duration [88].

The CorPower device utilises a heaving buoy to capture the kinetic wave energy, as shown in Figure 4c. The buoy is connected to the seabed using a tensioned mooring line. Inside the buoy, a gearbox is used to transfer the reciprocating motion of the buoy into the spinning motion for a conventional generator. The full-scale CorPower C4 device in development has a diameter of 9 m, a height of 18 m and a weight of 70 tonnes, with a nominal power rating of 300 kW [89]. The CorPower device utilises a “negative” spring technology named “WaveSpring”, and tank testing demonstrated that the WaveSpring technology is able to increase power absorption by a factor of three [90].

In general, the dynamics of floating one-body PAs are of low-pass characteristics in the frequency domain, and the natural frequency and response amplitude operator (RAO) significantly rely on the geometric shape of the floating body [56]. Hence, the hydrodynamic efficiency of floating one-body PAs can be significantly improved by optimising the bottom shape [91,92]. As sea states vary from time to time, and the wave frequency is generally off the natural frequency of a PA device, it is hence important to apply control strategies to tune the device’s natural frequency towards the wave frequency for maximising the power captured [37,39–41,67].

2.2.2. Submerged One-Body Point Absorbers

The working principle of a submerged one-body PA is similar to its floating counterpart, and the only difference lies in the status of the body, which can stand on or anchor to the sea bed with positive buoyancy. Among various submerged one-body PAs, the famous representatives are the Archimedes wave swing (AWS) device [93,94] and the CETO (named after a Greek sea goddess) device [95], shown in Figure 5.
Figure 5. The AWS device [96] and the CETO device [97] are shown as typical examples of submerged one-body PAs in (a, b), respectively.

The AWS device consists of a bottom-fixed cylindrical chamber fully filled with air and a movable captor, which heaves due to the pressure difference induced by wave crests and troughs. The captor’s motion drives a linear generator for electricity production. The captor has a diameter of 9.5 m and a stroke of 7 m (±3.5 m), and the linear generator is rated at 1 MW [33, 98]. The natural frequency of the AWS device can be controlled to match the prevailing wave frequency [33, 98]. Hence, various control strategies have been compared numerically, and the findings have addressed the importance of control of increasing annual energy production [99].

The CETO device uses a fully submerged buoy for wave power capture. The CETO 5 device is anchored to the seabed by a single tether, and its heave motion drives a cylinder to pump fluid to an onshore hydroelectric PTO unit [95]. Meanwhile, the CETO 6 device utilises three-tethered mooring lines to drive the mechanical PTO inside the buoy. The CETO 5 device has a diameter of 20 m, a height of 6 m and a hydraulic PTO rated at 240 kW [95], while the CETO 6 device has a diameter of 25 m, a height of 5 m and 3 mechanical PTOs rated at 1 MW [100, 101]. Compared with the CETO 5 device, the CETO 6 device makes use of multiple DoFs (i.e., heave, pitch and surge) to harness more energy [102].

Compared with floating one-body PAs, submerged ones are expected to be more robust to extreme waves but less efficient. In addition, the submergence depth becomes an important factor that should be taken into account in geometric optimisation, as it significantly affects hydrodynamic performance and power capture [103].

2.3. Multi-Body Point Absorbers

Multi-body PAs can be further divided into two-body PAs and multi-point WECs, as shown in Figure 6. In general, a two-body PA is self-referenced, and its relative motion between the two bodies is utilised to drive the PTO system for electricity production. The multi-point absorber device is referred to a WEC consisting of several floaters referenced to a large offshore platform, and the floaters’ motion drives the PTO units to generate electricity. Two-body PAs can be further divided into self-reacting PAs and self-contained PAs, which are discussed in Sections 2.3.1 and 2.3.2, respectively, while a couple of notable multi-point absorbers are detailed in Section 2.3.3.

2.3.1. Self-Reacting Two-Body Point Absorbers

A self-reacting two-body device has a floater, mainly to interact with surface waves for wave power capture, and a reacting body, mainly to provide a reference point. The relative motion between these two bodies drives a PTO system to generate electricity. The OPT PowerBuoy device [104] and the Wavebob device [105] are typified in Figure 7.
Figure 6. The self-reacting, self-contained and multi-point PAs are illustrated in (a–c), respectively.

Figure 7. The OPT PowerBuoy device [106] and the Wavebob device [107] are shown as typical examples of self-reacting two-body PAs in (a,b), respectively.

The OPT PowerBuoy device consists of a torus floater and a spar. The floater is optimised to resonantly heave up and down with surface waves, while the spar is designed to remain stationary by adding a heavy plate at its bottom. A ball-screw mechanical PTO is installed inside the spar to transfer the bidirectional relative motion of the two bodies into unidirectional rotation for a rotary generator [104,108]. For the first commercial PB3 device, the torus had a diameter of 3 m, while the spar had a diameter of 1 m. The rated power was 3 kW [104]. It is worth noting that the survivability problem was prioritised at the early stage of development, and the device response and load in 100-year storms and extreme wave conditions were studied to improve device survivability.

The Wavebob device consists of a torus and a float-neck-tank (FNT). The torus is essentially a wave follower over the range of the wave frequencies of interest for power conversion, while the FNT has a much lower natural frequency and acts as a reference for the torus [109]. The torus and the FNT are coupled via a hydraulic PTO unit or a direct-drive linear generator [107,110]. At full scale, the torus has a diameter of 17.6 m, a draft of 4.86 m and a freeboard of 3.0 m, while the FNT has a draft of 57 m [110]. A 1/4 downscaled prototype, rated at 500 kW [111], was deployed at the Galway Bay Ocean Energy Test Site in 2006, becoming the first sea-tested WEC in Ireland. It is worth noting that the Wavebob device is prone to parametric resonance in roll and pitch [105,107].

Compared with one-body PAs, two-body ones are not referenced to a fixed point. Thus, two-body PAs are suited well to deep-water applications with a proper mooring design. In the frequency domain, two-body PAs perform like bandpass filters, and their passbands can be optimised to match a certain wave climate. However, the number of design parameters is much larger than that of one-body PAs.
2.3.2. Self-Contained Two-Body Point Absorbers

A self-contained PA only utilises its hull to interact with surface waves and uses a pendulum structure to generate electricity. The notable self-contained two-body PAs are the SEAREV device with a vertical pendulum [112] and the Penguin device with a horizontal pendulum [113], as shown in Figure 8.

![Figure 8](image_url)

Figure 8. The SEAREV device [114] and the Wello Penguin device [115] are shown as typical examples of self-contained two-body PAs in (a,b), respectively.

The SEAREV device consists of a closed floating hull in which a circular pendulum oscillates. The relative motion is used to produce electricity via a hydraulic or direct-drive PTO system. At full scale, the SEAREV device was supposed to have a length of 26.64 m, a width of 13.25 m, a height of 20.7 m, a draft of 14.6 m and a rated power up to 400 kW [112,116]. The development trajectory of the SEAREV device is detailed in [112,117], which addresses the importance of geometric optimisation and power maximisation control. In addition, parametric resonance was observed in tank testing [118], which reduced the energy production by a factor of four.

The Penguin device uses its hull to capture wave power in the pitch and roll modes, and an eccentric pendulum inside the hull directly drives a rotary generator for electric power. At full scale, the Penguin hull ranges from 30 m to 56 m, with its rated power varying from 0.5 MW to 1 MW. The LCoE was predicted to range from EUR 60 to 320/MWh [113], which is inviable in the electricity market. In addition, an acoustic noise study of the Penguin device was conducted [119] which concluded that the source sound pressure level of the Penguin device was measured to be 140.5 dB re µPa at 1 m, while the mean value of the ambient noise was 112 dB re 1 µPa. The underwater sound pressure level is expected to decrease to the ambient background noise level within approximately 10 m from the device [119]. Thus, the ecological impact on mammals (e.g., dolphins and whales) is expected to be minimal.

Different from self-reacting PAs, a self-contained PA only uses the hull to capture wave power. In terms of DoF, self-reacting PAs mainly operate in heave mode, while the self-contained ones can operate in heave, pitch or roll mode. In addition, pendulum-based WEC systems have attracted wide attention. For more information, readers are referred to the inertial sea wave energy converter (ISWEC) [120], the AMOG device [121], the pendulum wave energy converter (PeWEC) [122], the whatever input to torque transfer (WITT) device [123], the inverted pendulum wave energy converter (IPWEC) [124], etc.

2.3.3. Multi-Point Absorbers

For multi-point absorbers, a jacked-up structure or a semi-submersible platform is used to host several floating bodies to harvest wave power. The floating bodies can operate in heave, pitch and other modes. The WaveStar device [125] and the FO3 device [126] are shown in Figure 9.
The WaveStar device has a couple of spherical bottomed cylinders attached to a jacked-up frame via steel arms, and each arm utilises a hydraulic PTO or linear generator to generate electricity. At full scale, the platform is supposed to have 40 bodies. Each floater has a diameter of 5 m, the steel arm has a length of 10 m, and the power rating of each PTO unit is 55 kW [129]. Experimental tests showed that the WaveStar device was able to achieve a high hydrodynamic efficiency of up to 40–60% [127]. In extreme waves, the WaveStar device can enter into survival mode by lifting up the floating bodies. Several sea trials have demonstrated that the WaveStar device has good survivability, high reliability and limited maintenance requirements [129].

The FO3 device uses a semi-submersible platform to host several egg-shaped cylinders. Excited by surface waves, the cylinders heave up and down with respect to the semi-submersible platform, and their motion drives hydraulic PTO systems to generate electricity. At full scale, the semi-submersible platform has a length of 36 m, a width of 36 m and a height of 24 m [130]. The nominal power was estimated to be 2.52 MW when subjected to a sea state with a wave height of 6 m and a period of 9 s [130]. In addition, the LCoE is predicted to around EUR 2.8/kWh [130], which is not competitive in the utility market.

It is worth noting that the multi-point absorber device is different from the WEC array of several PAs. The multi-point absorber device has a main structure to host multiple bodies. Thus, the number and spacing of floaters are constrained by the size of the main structure. On the contrary, the number, spacing and layout of a PA array are only constrained by the area of its deployment site.

3. Hydrodynamic Modelling

In terms of PA hydrodynamic modelling, its methodology is the same as the other types of WEC devices. As there is a mass of publications dealing with WEC hydrodynamic modelling, this paper only gives a brief introduction of the PA hydrodynamic modelling. For more detailed information on hydrodynamic modelling, the readers are referred to [27–30,63,131–133].

In this paper, a floating cylinder in Figure 10 is given to demonstrate the hydrodynamics modelling problem of a generic PA device. The PA’s dynamics are governed by Newton’s second law as follows:

\[
M \ddot{\xi}(t) = f_h(t) + f_g(t) + f_{pto}(t) + f_m(t) + f_{add}(t),
\]

where \(M\) is the inertial matrix of the cylinder, \(\xi\) is the floater’s displacement of the WEC, \(f_h\) is the hydrodynamical force or torque, \(f_g\) is the force or torque induced by gravity, \(f_{pto}\) is the PTO force or torque, \(f_m\) is the force or torque induced by the mooring system and \(f_{add}\) represents some other additional forces or torques. The dimensions of the aforementioned parameters or variables rely on the number of PA bodies and DoFs. As shown in Figure 10, the cylinder can oscillate in six DoFs (i.e., the surge, sway, heave, roll, pitch and yaw modes).
As shown in Figure 10, the hydrodynamical force or torque is represented by the integral of the pressure $p$ on the wetted surface $S$, written as

$$f_{h,i} = \begin{cases} - \int_S p \, n \, dS, & i = 1, 2, 3, \\ - \int_S p \, (r \times n) \, dS, & i = 4, 5, 6, \end{cases}$$

where $n$ is the normal vector on the wetted surface and $r$ is the vector from the reference point to the wetted surface. $i = 1, 2, 3 \cdots 6$ indicates the DoFs of surge, sway, heave, roll, pitch and yaw, respectively. For simplicity, $n_h = [n, r \times n]'$ is defined, and Equation (2) can be simplified as

$$f_h = - \int_S p \, n_h \, dS.$$ 

The key for PA modelling is to compute the hydrodynamic force $f_{h,i}$ and the hydrodynamic modelling methods are summarised in Figure 11, which can be divided into numerical and experimental methods. Numerical methods are generally used to solve the Navier-Stokes equations to obtain the pressure field in the fluid. Hence, the hydrodynamic force or torque can be computed according to Equation (3). Furthermore, the numerical methods can be further classified into three subtypes: the computational fluid dynamics (CFD) methods, the potential flow theory (PFT) methods and the hybrid methods. In addition, experimental testing is generally applied to collect data for deriving or identifying PA models. The aforementioned modelling methods are discussed below.

3.1. Computational Fluid Dynamics Methods

CFD methods are broadly used in modelling WEC hydrodynamics due to their capability to provide high-fidelity results and to capture highly nonlinear phenomena [29]. Currently, the Navier-Stokes equations cannot be solved analytically, and CFD methods
can provide relatively accurate numerical approximations by computing the pressure and velocity field in the fluid. Thus, the hydrodynamic force can be calculated according to Equation (3).

CFD methods include the Eulerian and Lagrangian methods. The Eulerian methods discretise the fluid into small cells, while the Lagrangian approaches discretise the fluid as a set of particles. Most CFD software packages follow the Eulerian methods, and the notable ones include ANSYS Fluent, CFX, FLOW-3D, Star-CD/CCM+ and OpenFOAM. Those packages are broadly used for PA modelling since they are capable of handling various nonlinear PA hydrodynamics (e.g., viscosity [92,134,135], vortex shedding [136,137], overtopping [138,139] and slamming [138]). Among several Lagrangian methods, the smoothed particle hydrodynamics (SPH) method is investigated intensively, and the DualSPHysics, an open-source SPH package, is available online [140]. The SPH method shows advantages in the automatic conversion of mass and simplification of surface tracking, and hence, it can easily compute the wave load of PA devices in extreme waves [141,142].

Compared with the other modelling methods, the CFD methods have the following advantages: (1) CFD methods are more cost-effective than experimental methods. (2) CFD methods can give more accurate results than those of PFT methods, especially when nonlinear phenomena are considered, and (3) CFD can ease the modification of WEC for parametric study. Meanwhile, CFD methods may be unsuitable in some scenarios due to their drawbacks, which are as follows: (1) CFD software packages are unfriendly to new learners and may take some time to get started, (2) it is complex to set CFD modelling parameters and boundary conditions properly, and an improper configuration may result in modelling results away from reality. Thus, experimental validation is required. Finally, (3) CFD modelling requires a huge amount of computing power, which has been satisfied by the rapid development of computer science.

3.2. Potential Flow Theory Methods

By assuming that the fluid is ideal, the Navier–Stokes equations can be simplified to the Laplace and nonlinear Bernoulli equations, and the fully nonlinear potential flow theory (FNPFT) is developed to solve the Laplace and nonlinear Bernoulli equations. By further assuming that the wave steepness is small, the nonlinear Bernoulli equation can be simplified, leading to the linear potential flow theory (LPFT). As the FNPFT and LPFT use a potential function \( \phi \) to obtain the pressure field \( p \) in the fluid, they both belong to the potential flow theory.

The FNPFT only assumes the fluid is incompressible, inviscid and irrotational. Hence, it can handle nonlinear and steep waves as well as large body oscillations. Currently, there is no such universal software package for solving the Laplace and nonlinear Bernoulli equations, but there are some trials for WEC modelling. By further assuming that the motion of a floater is small, the wetted surface can be treated as invariant, the normal vector \( n_h \) can be computed at the equilibrium point of the floating body, and the wave–buoy interaction can be linearised at the equilibrium point. Based on the LPFT, the potential function can be divided into incident, diffracted and radiated components [143] as follows:

\[
\phi = \phi_i + \phi_d + \phi_r, \tag{4}
\]

where \( \phi_i \) is the incident potential function determined by the incident wave when the floating body is absent, \( \phi_d \) is the diffraction potential function, assuming the body is stabilised at the equilibrium point, and \( \phi_r \) is the radiation potential function, assuming the floater oscillates in still water. Thus, the pressure field is given by

\[
p = -\rho g z - \rho \frac{\partial \phi}{\partial t}, \tag{5}
\]
where $\rho$ is the water density, $g$ is the gravitational constant, $z$ is the vertical position (to see Figure 10) and $t$ is the time. Hence, the hydrodynamic force $f_h$ can be rewritten as

$$f_h = f_{\text{FK}} + f_d + f_r + f_{\text{hs}}, \quad (6)$$

$$f_{\text{FK}} = \rho \int_S \frac{\partial \phi_i}{\partial t} n_h dS, \quad (7)$$

$$f_d = \rho \int_S \frac{\partial \phi_d}{\partial t} n_h dS, \quad (8)$$

$$f_r = \rho \int_S \frac{\partial \phi_r}{\partial t} n_h dS, \quad (9)$$

$$f_{\text{hs}} = \rho \int_S gz n_h dS, \quad (10)$$

where $f_{\text{FK}}$ is the Froude–Krylov (FK) force, $f_d$ is the diffraction force, $f_r$ is the radiation force and $f_{\text{hs}}$ is hydrostatic force.

In general, the buoyancy of a floating buoy in still water is neutral, and hence, $f_{\text{hs}} + f_g = 0$ holds. When the floating body deviates from the equilibrium point, there will be a mismatch between the buoyancy and gravity, which provides a restoring force or torque in the heave, roll and pitch modes. For the case where $f_{\text{hs}} + f_g > 0$, the positive buoyancy should be balanced by a pretensioned mooring design.

In addition, the summation of the incident problem ($\phi_i$) and the diffraction problem ($\phi_d$) is called the excitation problem, and the excitation force is given as $f_e = f_{\text{FK}} + f_d$. For linear wave theory, an analytical solution for $\phi_i$ exists. The analytical solutions for $\phi_d$ and $\phi_r$ only exist for some simple and basic geometries (e.g., a truncated floating cylinder) [144,145].

For a floating body with an arbitrary geometry, the $\phi_d$ and $\phi_r$ are difficult to solve analytically, and the boundary element methods (BEMs) are broadly applied to provide numerical approximations. Based on two one-body PAs, one with a spherical floater and the other with a cylinder-cone floater, a comparison study for evaluating the aforementioned modelling methods was conducted under the framework of the OES Wave Energy Conversion Modelling Task, which concluded that the linear, weakly nonlinear and fully nonlinear methods give similar results for experimental data for small and medium wave conditions [131]. This is the rationality for using LPFT methods to model PA hydrodynamics in operation mode. Thus, BEM solvers (WAMIT, NEMOH, AQWA, etc.) are generally used for PA hydrodynamic modelling.

Compared with the other modelling methods, the PFT-based methods are of high computational efficiency. Thus, both the FNPFPT-based and LPFT-based methods work well for PA design at low TRLs and performance evaluation over a long duration. However, the assumptions of an ideal fluid, small wave amplitude and small body motion can seldom be met. Hence, the modelling fidelity is doubtful, especially when PAs are tuned to resonance by control.

### 3.3. Hybrid Modelling Methods

As mentioned above, the LPFT-based BEM solvers assume the fluid is ideal, the wave height is small, and the body motion is small. However, the motion of a PA device can be significantly amplified by power-maximising control, resulting in some important nonlinear factors (e.g., nonlinear viscous force [134] and nonlinear FK force [146,147]).

To treat some key nonlinearities, hybrid modelling methods are developed to augment the LPFT-based Cummins’ equation. Thus, the concepts of excitation and radiation hold, and the Cummings’ equation [148] can be written as

$$(M + M_\infty) \ddot{\xi}(t) = f_e(t) - K\dot{\xi}(t) - k_r(t) * \ddot{\xi}(t) + f_{\text{pto}}(t) + f_m(t) + f_{\text{nl}}(t), \quad (11)$$
where \( M_\infty \) is the added mass, \( K \) is the hydrostatic stiffness, \( k_r \) is the radiation kernel function, and \( f_{nl} \) is the treated nonlinear force. In general, nonlinear treatments can be classified as the following four types:

- **For the body-exact treatment method**, the instantaneous body position is considered in computing the FK, diffraction, radiation and restoring forces in Equations (7)–(10), while the wave is still assumed to be small. When the body size is small, the nonlinearity in diffraction and radiation are neglectable. For a body with a varying horizontal cross-section, the nonlinearity in the hydrostatic force appears obvious. Considering the large body motion, the nonlinearity in the FK force is more critical than the other force and has a significant impact on PA hydrodynamics [146,149,150].

- **For the weak scatterer treatment method**, the instantaneous free surface is considered in computing the forces in Equations (7)–(10), while the wetted surface is linearised at the equilibrium point. This method linearises the free-surface boundary condition at \( z = \eta(t) \). Thus, the second-order terms of \( \phi_d \) and \( \phi_r \) can be added to compute the diffraction and radiation forces in Equations (8) and (9). However, the importance of the nonlinear diffraction and radiation terms mainly depends on the body size. For a small body, these nonlinear forces can be neglected [151].

- **For the viscosity treatment method**, the viscosity is considered by adding a quadratic term to the Cummins’ equation, according to the Morison equation [152]. This method can significantly improve the modelling accuracy with little computing cost when the relative velocity between the body and fluid is large. The viscous coefficient can be determined analytically, numerically or experimentally [134,153,154]. However, a wide range of wave conditions should be tested to obtain a consistent value [155].

- **The mixed treatment method** has two subclasses: the body-exact viscosity treatment considering both large body motion and fluid viscosity and the weak-scatter viscosity treatment considering both a large wave height and fluid viscosity. In AQWA, the weak-scatter viscosity treatment is realised by computing the nonlinear FK and hydrostatic forces according to instantaneous wave elevation and adding the viscous force according to the Morison equation [156,157]. In general, PAs’ motion is significantly amplified by power maximisation control, and hence, the nonlinearity induced by large body motion is more critical than that induced by a large wave height. Therefore, the body-exact viscosity treatment is broadly used in PA modelling.

The four types of hybrid modelling methods can achieve a trade-off between modelling fidelity and computational efficiency. However, they can only handle some “weak” nonlinearities induced by a large motion, large wave or viscosity. In addition, the determination of critical nonlinearities is not unique and should be conducted in a case-by-case manner. To capture all kinds of nonlinear phenomena, CFD and experimental methods are recommended.

### 3.4. Experimental Modelling Methods

Downscaled PA prototypes are generally used for tank testing to investigate PA dynamics in a more real scenario. The collected data are used to verify or validate the aforementioned modelling methods. On the other hand, the collected data can be used to identify PA models in a data-driven manner. For scaling down a PA prototype, the Froude number is used to ensure the kinematic and dynamic similarities of the prototype with respect to those of its original model [132]. Thus, the PA hydrodynamics and power capture can be easily scaled up.

For identifying empirical or data-driven models of PA devices, numerous tank tests are required to cover a wide range of wave conditions in order to depict all possible hydrodynamics that a PA device may come across in reality. Data-based modelling from physical experiments has been applied to derive mathematical models for various WEC systems [158–162]. In addition, experimental data can be used to identify the viscous coefficient [134,155,163–165].
Strictly speaking, open sea testing in a wide range of sea states is the “gold standard” for verifying and validating modelling methods. However, it is extremely costly and time-consuming, even if downscaled prototypes are used. In addition, numerical modelling methods can provide a fully controlled environment, which offers an easy, economical and flexible way to adjust the PA design and wave conditions.

4. Power Take-Off Mechanisms

For a PA device, the PTO mechanism is one of the most important components which generates electric power and, simultaneously, works as an actuator for control implementation. In the literature, several review papers on PTO have been published, and readers are referred to [35,36,166–169]. This paper only focuses on the PTO systems related to PA devices, classified as (1) hydraulic PTOs [34,170–173], (2) mechanical PTOs [174,175], (3) direct-drive PTOs [176–178] and (4) some novel PTOs [179,180], as shown in Figure 12. These PA-related PTO mechanisms are discussed below.

![Figure 12. Four types of power take-off mechanisms used for point absorber wave energy converters.](image)

4.1. Hydraulic PTO Mechanisms

The hydraulic PTO mechanism is the most mature one for wave energy conversion, comprising hydraulic cylinders, pipes, regulating valves, accumulators, hydraulic motors, rotary generators, etc. The working principle and a case study of hydraulic PTO systems are shown in Figure 13.

![Figure 13. Hydraulic power take-off mechanisms with a schematic plot (a) and a hydraulic PTO system under tank testing (b), adapted from [13,181].](image)

Compared with the other PTO mechanisms, the hydraulic PTO has shown some unique advantages: (1) The hydraulic technology is mature and broadly used in the in-
dustrial sector [31]. Thus, all the hydraulic components are market-accessible, and the accumulated O&M experience is portable for PA applications. (2) Hydraulic systems are capable of providing a large force at a low speed, and this feature suits the wave energy application scenarios well since wave force has a large amplitude and a low frequency [55,182]. That is why the hydraulic PTO mechanism is preferred by WEC developers. (3) Hydraulic PTO systems can be feasibly and flexibly used for a variety of PA devices regardless of the operating DoFs, installation manners or geometries [34]. Finally, (4) with the assistance of the regulating valves and accumulators, a hydraulic PTO system is able to overcome the variation in wave power and provide stable electrical power.

However, the application of the hydraulic PTO mechanism for PA devices is constrained by some drawbacks: (1) Compared with the other PTO systems, the overall efficiency of a hydraulic PTO system is low, mainly due to the friction and viscous loss in the hydraulic system [183]. A case study based on a hydraulic PTO for a WaveStar-like device showed that the friction loss was almost as large as the generated electrical power [173]. In addition, the energy conversion steps are complex [184]. (2) In general, a hydraulic PTO system requires regular maintenance, and hence, the O&M cost may be high, considering the harsh offshore environment. As reported in [31], the hydraulic oil should be replaced after some thousand hours of operation; that is, the hydraulic oil should be refilled once or twice a year. Finally, (3) there exists a pollution risk as hydraulic oil is used. Thus, it is challenging to seal a hydraulic PTO system in an effective and efficient manner [53].

From the viewpoint of control, the properties of hydraulic PTO systems are manifold. Some control strategies (e.g., latching, declutching and bang-bang control approaches) can be easily realised by hydraulic PTO systems [55,185]. On the other hand, the features of hydraulic PTO units also limit the control strategies in the discrete time domain [31]. More hydraulic rams and accumulators are required to smooth out the control performance, which will increase the system complexity significantly.

4.2. Mechanical PTO Mechanisms

Mechanical PTO systems are broadly used in PA devices. For instance, a rack and pinion mechanism is used by the CorPower device, belt drive mechanisms are used by the LifeSaver device and the CETO 6 device, and a ball screw mechanism is used by the OPT PowerBuoy device in order to convert reciprocating motion to rotation for driving rotary generators. To demonstrate the working principle of the mechanical PTO mechanism, a ball screw unit is shown in Figure 14.

![Figure 14. A ball screw mechanism is shown as an example to illustrate the working principle of the mechanical power take-off mechanism, with a schematic plot (a) and a mechanical motion rectifier (b), adapted from [174,186].](image)
Compared with the other PTO mechanisms, the mechanical PTO mechanism shows some technical advantages: (1) The mechanical transmission is mature and broadly applied in industrial applications. (2) In general, the energy loss of a mechanical PTO system is low, and the efficiency of a mechanical transmission system is high. For instance, a rack and pinion mechanism can achieve an efficiency up to 97% [61]. Lastly, (3) a variety of mechanical transmission mechanisms provides flexible means to regulate the reciprocating motion of WEC bodies into unidirectional rotation, which is more friendly for driving conventional rotary generators.

However, there are still some drawbacks that hinder the commercial application of WECs with mechanical PTO systems: (i) The mechanical transmission systems suffer from a fatigue problem, and they are prone to structure failures. Their reliability and lifespan should be improved. (2) In general, a mechanical PTO system itself is complex. Considering the dynamics of a mechanical PTO system, the complexity of a PA device will be critically high. (3) The mechanical PTO systems suffer from various nonlinear dynamics (friction, backsloshing, etc.). Finally, (4) regular O&M work is required (e.g., lubrication) to keep the mechanical PTO systems operating under an ideal condition.

As the mechanical PTO systems are capable of changing linear motion to rotational motion, they show promising potential for easing the connection of generators. However, a mechanical PTO unit may toughen the implementation of some control strategies. For instance, the mechanical motion rectifier in Figure 14 does not easily permit reactive power flow, which hinders the application of reactive control [174,186].

4.3. Direct-Drive PTO Mechanisms

Direct-drive PTO systems have been successfully used for wind turbines, and some experience is portable for WEC devices. The permanent magnet linear generator (PMLG) concept was proposed in [187] to produce electrical power from sea waves. A PMLG, as shown in Figure 15, was designed and tested in [33,98,188–190] as PTO mechanisms for the AWS device [93,94] and the Seabased device [82,83]. A variety of PMLGs was compared in [178,182,191,192]. In addition, a rotary generator is used as the direct-drive PTO system for the Columbia Power PA device [193].

![Direct-drive power take-off mechanisms with a schematic plot (a) and a heaving point absorber with a linear generator (b), adapted from [194].](image)

Compared with the other PTO systems, the main advantages of the direct-drive PTO units are as follows: (1) The direct-drive mechanism can provide high efficiency, since it can convert the buoy motion into electricity directly with only two energy conversion stages [55,191]. (2) The reliability is expected to be high since a direct-drive PTO unit compromises fewer components. (3) The maintenance requirement is low, mainly due to its simple topological structure [31]. (4) The direct-drive PTO system is feasible for control via electrical approaches, which have been generally used in the electricity
industry [195]. Lastly, (5) direct-drive PTO systems can operate reliably, even when the peak-to-average power ratio is up to 20 [196,197].

On the other hand, the drawbacks of direct-drive PTO systems are as follows: (1) The power or force density is low, and hence, the PTO volume and weight should be large enough to achieve a certain power rating [13,55], and (2) the manufacturing cost of a direct-drive PTO system is relatively high compared with the hydraulic PTO systems due to the high cost of the permanent magnets [182]. The permanent magnet materials have advanced significantly, resulting in a larger force density and a lower cost [33]. However, the force density and manufacturing cost of direct-drive PTO systems are still relatively higher those that of hydraulic PTO systems.

4.4. Novel PTO Mechanisms

For the past decade, some novel materials have been used for WEC applications (e.g., dielectric elastomers and triboelectric materials). The dielectric elastomer, also called the electroactive polymer artificial muscle, can be used as a PTO mechanism for WEC devices, named a dielectric elastomer generator (DEG). The working principle of the DEG is shown in Figure 16. The DEG can convert mechanical transformation into electrical energy from the stretched and released four-phase cycle. For more information, readers are referred to [198,199].

![Figure 16](image)

Figure 16. The working principle of a dielectric elastomer generator (a) and its application for a heaving point absorber (b), adapted from [198].

The main advantages of the DEG technology are the following: (1) A DEG can be easily controlled in an electrical manner. Thus, it can operate partially as a generator and partially as an actuator. (2) The conversion efficiency of a DEG is relatively high, with a theoretical value of up to 80–90% [200]. In practical applications, its achieved conversion efficiency was 70–75% [201]. In addition, (3) the conversion efficiency is not sensitive to the frequency, and hence, a DEG is well suited to irregular waves. Finally, (4) the material is flexible and environmentally friendly [202].

On the other hand, the DEG technology suffers from some drawbacks: (1) The DEG technology is untapped, at least for wave energy, and more testing is required. (2) It is difficult to design the coating and sealing for a DEG PTO unit [203]. (3) For a certain rated power, the DEG volume is much larger than that of the other PTO systems [202]. In turn, the complexity of a WEC geometric design and optimisation increases dramatically. Lastly, (4) the rubber-like material shows high nonlinearity in its dynamics and suffers from fatigue and durability problems [180].

More recently, a new energy conversion technology, called the triboelectric nanogenerator (TENG), has been used for wave energy harvesting. As shown in Figure 17, a torus-shaped point absorber with a movable ball inside is used for triboelectric power generation. In addition, this kind of point absorber can be easily extended to form an array [179]. As there are only a few tests on TENGs for wave energy conversion, the advantages and drawbacks are not discussed in this paper.
5. Control Strategies

Ocean waves show a high irregularity in direction, amplitude and frequency, while WEC devices are designed to operate efficiently under certain conditions. Thus, it is essential to adjust the WEC dynamics according to the time-varying wave conditions by a variety of power maximisation control strategies, including reactive control [57], phase and amplitude control [143], optimisation-based control [39] and adaptive control [204,205]. As there are several review papers dedicated to WEC control (see [37,39–41]), this paper only gives a brief overview of PA-related control approaches.

5.1. Classical Control Strategy

By assuming the wave is harmonic, the wave–buoy interaction is linear, and the PTO is as ideal as a mass-spring-damper system, the resonant concept for power maximising control of WEC systems was first proposed in 1975 [57,143]. Thus, Cummins’ equation in Equation (11) can be rewritten as

\[
\frac{V(\omega)}{F_e(\omega) + F_{pto}(\omega)} = \frac{1}{Z_i(\omega)},
\]

(12)

where \(V(\omega), F_e(\omega)\) and \(F_{pto}(\omega)\) are the body velocity, excitation force and PTO force in the frequency domain, respectively. \(\omega\) is the circular frequency. \(Z_i(\omega)\) is defined as the intrinsic impedance [143], written as

\[
Z_i(\omega) = B_r(\omega) + j\omega\left[M + M_a(\omega) - \frac{K}{\omega^2}\right],
\]

(13)

where \(B_r(\omega)\) and \(M_a(\omega)\) are the radiation damping coefficient and added mass to represent the radiation effect in the frequency domain.

According to the maximum power transfer theorem, the optimal PTO impedance should meet

\[
Z_{pto}(\omega) = B_{pto}(\omega) + j\omega\left[M_{pto}(\omega) - K_{pto}(\omega)/\omega^2\right] = Z_i^*(\omega),
\]

(14)

where \(Z_{pto}(\omega), B_{pto}(\omega), M_{pto}(\omega)\) and \(K_{pto}(\omega)\) are the PTO impedance, damping coefficient, mass and stiffness, respectively. Thus, the power absorbed by the PTO is maximised when the PTO impedance \(Z_{pto}\) is the complex conjugate of the intrinsic impedance \(Z_i\). Thus, a control strategy that follows the philosophy of Equation (14) belongs to the so-called complex conjugate control category [143]. As complex conjugate control allows bidirectional power flow in the wave energy transformation chain, it is also called reactive control (RC), meaning that the PTO unit feeds power into the WEC body during a part of the wave period. However, some PTO mechanisms can only provide unidirectional power flow. For
instance, a pure damper cannot feed any power back to WEC systems, and the reactive control degenerates to the so-called passive control (PC), given as

\[ B_{\text{PTO}}(\omega) = |Z_i(\omega)|. \] (15)

For reactive control, Equation (14) holds. Thus, the optimal body velocity can be written as

\[ V_{\text{opt}}(\omega) = \frac{F_e(\omega)}{2B_r(\omega)}. \] (16)

That is to say, the absorbed power by the PTO is maximised under the conditions that (1) the amplitude of the body velocity is proportional to the amplitude of the excitation force and (2) the body velocity is in phase with the excitation force, given as

\[ V_{\text{opt}}(\omega) = \frac{|F_e(\omega)|}{2|B_r(\omega)|}, \] (17)

\[ \sqrt{V_{\text{opt}}(\omega)} = \sqrt{\frac{F_e(\omega)}{2B_r(\omega)}}. \] (18)

Thus, Equations (17) and (18) are called the amplitude and phase conditions, respectively.

A control strategy to achieve Equations (17) and (18) belongs to the amplitude and phase control categories [143]. In practice, the amplitude condition in Equation (17) can be realised by selecting a suitable damper, while the phase condition can be realised by latching control (LC) [143] or declutching control (DC) [206].

5.2. Modern Control Strategies

The power-maximising control laws in Equations (13)–(18) are derived under harmonic wave conditions. In practice, ocean waves are irregular and panchromatic, and the RC, PC, LC and DC approaches cannot be used directly. Thus, a variety of R&D activities has been conducted to extend the application scenarios of the classic control strategies to irregular waves. In general, the extended control strategies follow two philosophies, shown in Figure 18: the approximate complex conjugate (ACC) and approximate velocity tracking (AVT) frameworks [41]. The ACC framework can optimise the PTO set-ups according to the prevailing frequency of irregular waves, but extra efforts are required to implement physical constraints. On the contrary, the AVT framework shows more flexibility in handling physical constraints by formulating the power maximisation problem as a constrained optimisation problem. However, such a framework needs the current or future information of the excitation force. As the excitation force cannot be measured directly for an oscillating body, extra estimators or predictors are required [207–211].

![Figure 18](image-url)

Figure 18. (a) Approximate complex conjugate (ACC) and (b) approximate velocity tracking (AVT) control frameworks.
The AVT-based control is broadly used for WEC devices, and the power maximisation control is formulated as a constrained optimisation problem, written as

$$\min_{f_{pto}} - \int_0^T f_{pto}(t) v(t) \, dt$$

s.t.  
$$\xi(t) \leq \xi_{\text{max}},$$

$$f_{pto}(t) \leq f_{\text{max}},$$

where $\xi_{\text{max}}$ is the displacement constraint, mainly determined by the WEC geometric design, and $f_{\text{max}}$ is the PTO force limit, mainly depending on the PTO absolute parameters. Based on this optimisation formulation, several optimal control algorithms are summarised in [39]. As power-maximising control is a general problem for all kinds of WEC devices, it has been intensively investigated, and several reviews have been published. For more specific information, readers are referred to [37–41].

6. Discussion

This section discusses some perspectives of PA concepts, hydrodynamics, PTO, control and applications, which are detailed below.

6.1. Perspectives on PA Concepts

For a specific site, the selection of PA types is determined by the site’s environmental conditions (depth, distance from the coast, wave climate, etc.) and application scenarios. One-body PAs fit well with nearshore applications, as they are referenced to absolute points. For seas of low power densities, the floating one-body PAs are preferred, while the submerged ones are preferred in harsh seas since the floating one-body PAs are more efficient, and the submerged ones are less prone to extreme wave loads. For deep sea applications, two-body PAs are preferred, as they are self-referenced. To achieve a large installation capacity and smooth power production, multi-point absorbers are preferred. Multi-point absorbers with a jacked-up structure can only stand in shallow waters, while ones with a semi-submerged platform can operate in deep seas. It is worth noting that the system complexity increases dramatically from one-body PAs to multi-point absorbers.

In terms of the operating mode, there is a trend of harnessing wave power in multiple DoFs. To date, most PA devices operate in a single-mode manner, mainly in heave or pitch, as their modelling, control, design, manufacturing and deployment are simple, but the efficiency may be low. In order to harvest as much power as possible, several studies have shown that a multi-DoF PA device can extract more energy than its counterpart of a single DoF [102,103,135,212]. However, the hydrodynamics become much more complex, and attention must be paid to the coupling between different DoFs. If the behaviour of each mode is not designed properly, the captured power may reduce severely [135,163]. In addition, the coupling between different DoFs may induce rich and complex nonlinear phenomena, such as parametric resonance in roll or pitch [105,107,213,214].

Recently, several novel PA concepts have been proposed, and some representatives are shown in Figure 19. A guided inclined point absorber was developed to increase the power capture by optimising the inclination angle [215], as shown in Figure 19a. Both numerical and experimental studies show that the guided PA with an optimised angle (ranging from 30° to 60°) are capable of harvesting more power than its vertically heaving counterpart (90°) by a factor of up to 4.52. Similar results have been obtained for the CECO device [216,217], as both the heave and surge DoFs are used for energy harvesting. In addition, both numerical and experimental studies have shown that the performance of the CECO device, as a representative of the sloped type, is significantly influenced by, for example, the wave climate [218], water depth [219], geometric design [220,221] and control design [222].
Figure 19. Some novel point absorber concepts, with a guided inclined PA [215], multiple PAs in a moonpool [223] and a novel heaving PA with underwater impeller PTO [224] in (a–c), respectively.

As shown in Figure 19b, five heaving PAs situated inside a moonpool structure form a multi-point absorber [223,225]. By properly optimising the moonpool dimension, PA number and spacing, the moonpool’s resonance and the interaction between PAs can significantly improve the overall energy generation. In Figure 19c, a novel heaving PA is shown. A floating sphere heaves subjected to incident waves, and the heaving motion drives two underwater impellers. Each impeller has blades, which can swing as the sphere heaves. Thus, the reciprocating motion is transferred to unidirectional rotation for generating electricity. To some extent, the working principle of this novel device is close to that of a wave glider.

6.2. Perspectives on PA Hydrodynamics

Four categories of hydrodynamics modelling methods are discussed in Section 3, and the selection of modelling methods is determined by the purposes of modelling rather than the PA types. To capture all kinds of nonlinear wave–buoy interaction, CFD methods are preferred. To evaluate or optimise PA performance in a wide range of sea states (e.g., annual energy production), LPFT-based methods can give preliminary results. If only some weak nonlinearities are non-negligible, FNPFT-based methods and hybrid methods can both give accurate approximations. For the purpose of control, none of the modelling methods can be used directly. System identification and simplification are required to derive accurate and effective transfer functions or state-space models for control design. In addition, all the aforementioned modelling methods should be verified or validated by experimental testing in the representative environment.

Currently, the LPFT-based BEM methods are the most widely used. However, there is a trend to consider nonlinearity in hydrodynamic modelling by considering the nonlinear viscous, hydrostatic and mooring properties, end-stop forces and even extreme wave loads. In addition, the operation of PA arrays has been attracting broad attention. Thus, the nonlinear hydrodynamics, extreme wave load and array operation are discussed below.

6.2.1. Nonlinear Hydrodynamics

In general, PAs with sharp edges suffer from the viscosity, especially when the relative velocity between the body and water particles is large [134,135,153], and the viscous loss can be attenuated by optimising the hull shape [56,92]. PA devices with varying cross-section areas (e.g., floating spheres) are prone to nonlinear hydrostatic force [151,226], and PAs with significantly varying wetted surfaces (e.g., floating spars) are prone to nonlinear FK force [146,147,149,150]. In extreme waves, PAs also suffer from overtopping and slamming [138,227], nonlinear mooring force [228], end-stop force [229–232], etc.

Since PAs operating in multiple modes have been attracted an increasing R&D focus, the nonlinear interaction between different DoFs has been studied in several papers. For the CETO-like device, subharmonic excitations were found in numerical simulations to illustrate the nonlinear couple between the heave and surge DoFs [135]. Another notable piece of evidence to show nonlinear coupling between different DoFs is the paramet-
ric resonance, which was observed in both numerical and experimental studies of PA devices [105,213,214,233–235]. A large heave motion may make the PA’s metacentric height change periodically, leading to a periodic variation in pitch or roll restoring stiffness, which excites the pitch or roll modes, inducing Mathieu instability [236]. The onset conditions of parametric resonance are complex and significantly rely on the mass distribution [237], mooring configuration [238,239], hull geometry [235,240] and hydrodynamic modelling methods [107,233,235,241,242]. For the viewpoint of hydrodynamics, the nonlinear interaction between different DoFs or modes can be modelled well using CFD methods [235] and the hybrid modelling methods considering nonlinear FK force [107,150,242].

6.2.2. Extreme Wave Loads

Several WEC structure failures were reported [50], which suggests that the survivability problem seems more important than the efficiency problem. For the past decade, several studies have been dedicated to PAs’ survivability in extreme waves, and some typical cases are shown in Figure 20. Extreme waves (e.g., the 100-year wave) are generally used for PA design to predict the extreme motions and loads exerted on the structure, PTO and mooring systems.

Figure 20. Extreme wave loads of the Seabased-like device [139], the CETO-like device [243] and the WaveStar-like devices [244], shown in (a–c), respectively.

As shown in Figure 20a, 100-year extreme waves at the Humboldt Bay site in California were used to investigate the extreme response of a Seabased-like device via OpenFOAM [139], and it was concluded that the wave steepness and the wave length play important roles in extreme response. As shown in Figure 20b, a focused wave group was used to obtain the maximum PTO extension, heave and surge motions of CETO-like devices both in experiments and simulations [95,243]. In addition, the survivability of a WaveStar-like device was numerically and experimentally tested by being subjected to focused wave events [244,245], as shown in Figure 20c. The WaveStar-like PA may experience various extreme motions (e.g., fully submerging, slamming or overtopping).

The survivability of PAs in extreme waves is one of the most important and challenging problems. Currently, numerical experiments (e.g., CFD simulation) are used to investigate extreme wave loads of PAs for load mitigation [141,142,246]. A good example is given by the OPT PowerBuoy PB150 device, which uses 100-year storms to optimise its design at the early stage of development [104,247]. As a consequence, the PB150 device survived Hurricane Irene in 2011 [104,247].

6.2.3. Array Operation

For commercial applications, a large number of WEC devices are installed to form a WEC array, which is expected to reduce the LCoE by sharing the infrastructure and O&M service. In addition, a WEC array can smooth the power output to ease the grid connection. Based on PA concepts, the constructive park effect was first proposed in 1981 [70], and several studies were devoted to optimising the PA array’s layout [248–258]. These studies are mainly based on linear hydrodynamics modelling methods, and the nonlinear interaction between PAs are neglected.
Recently, CFD methods with experimental validations are capable to provide high-fidelity modelling for WEC arrays with a large number of devices, since commutating power advances rapidly. An example is shown in Figure 21, in which physical and numerical models of a PA array with up to 25 heaving devices are tested to understand array interactions. Numerical results show a high accordance to experimental data, demonstrating the capability of CFD methods for accurately modelling large PA array.

![Figure 21. Point absorber arrays with physical and numerical models in (a,b), respectively, adapted from [259,260].](image)

6.3. Perspectives on PA PTOs

Four types of PA-related PTO mechanisms were detailed in Section 4, of which the hydraulic and mechanical PTOs can be used for all types of PAs, while the direct-drive PTO fits well with PAs mainly operating in heave. In theory, PTO systems can be assumed to be ideal and simplified as mass-spring-damper systems. In practice, PTO systems have their own dynamics and suffer a variety of nonlinearities. Hydraulic PTOs are prone to delays, dead zones, hysteresis effects [184], etc., mechanical PTOs suffer from friction, saturation [173], etc., and direct-drive PTOs are subjected to cogging force [261], load effects [262], etc. Neglecting the dynamics and nonlinearities in PTOs may lead to improper PA design. In addition, PTOs are designed to operate efficiently under certain conditions. As waves vary all the time, PTOs seldom operate under their rated conditions, and their efficiency decreases dramatically. Thus, the captured power may be dissipated significantly by PTO systems themselves in terms of hydraulic losses [183], mechanical losses [173,174,183], copper losses [263–265], etc.

Recently, there has been a trend of utilising nonlinear mechanisms for enhancing the power capture of floating PAs. In general, a floating one-body PA has a relatively large hydrostatic stiffness with respect to its mass, resulting in a resonant frequency higher than the wave frequency. Thus, a “negative” spring is required to passively tune the PA for resonating with incident waves. A good case is the CorPower device, which uses the “wavespring” technology to implement the phase control in a passive manner [90]. In addition, several studies utilise bistable mechanisms to improve PTO performance [230,266–273], as shown in Figure 22.

The nonlinear dynamics of the properly designed bistable mechanisms in Figure 22 can extend the bandwidth of a PTO system in the frequency domain. Therefore, the power capture in real waves can be improved passively. In addition, the reactive power flow and peak-to-average power ratio of the PTO system can be reduced. On the other hand, the bistable mechanisms induce rich and complex nonlinear phenomena, which complicate the modelling and optimising of a PA’s design. In practice, these bistable mechanisms may significantly suffer from fatigue problems, especially when springs are used.
6.4. Perspectives on PA Control

Sea states vary from time to time, and waves are irregular in frequency and height. Therefore, control systems are indispensable for PAs to harvest wave power under moderate waves and to survive in extreme wave events. The importance of control is proven by the study based on the SEAREV G21 device [114], in which a properly designed control system increased the annual energy production from 730 MWh to 1300 MWh, while the capture expenditure of the device only increased from EUR 5 M to EUR 5.3 M. In addition, a couple of preliminary studies tried to apply fault-tolerant control for PA devices while considering the actuator and sensor faults [274–276].

As discussed in Section 5, PA devices’ motion is significantly exaggerated by power-maximising control, and consequently, some nonlinearities (e.g., viscous and FK forces) are amplified. Thus, high-fidelity PA models considering nonlinear hydrodynamics and PTO losses are required for control development. Such models are naturally complex, and model simplification should be performed for real-time control implementation [28,40,41,61,277]. In general, modelling errors and uncertainties are inevitable, and control should be robust to modelling errors [278–283], external disturbances [284–286] and estimation or prediction errors of the excitation force [287].

Recently, model-free control methods have advanced rapidly and are applied to maximise PA power capture. Among a variety of model-free control methods, the notable ones include the extremum-seeking algorithms [288], artificial neural networks [96] and machine learning methods [289–291]. However, some model-free control methods may require numerous data or iterations for training or optimising, hindering their implementation for real PA devices.

6.5. Perspectives on PA Application

Wave energy harvesting mainly targets the utility-scale electricity market. Currently, its LCoE is estimated to range from USD 120 to USD 470/MWh [292], which is much higher than that of some other mature renewable energy resources such as solar and wind power.
or fossil fuels [293]. With an accumulated install capacity up to GWs, the LCoE can be reduced to EUR 100–150/MWh by 2030–2035 [294].

To reduce the LCoE of wave energy further, PAs can be easily integrated into existing offshore wind farms [16,19,295,296], as shown in Figure 23a. Such a combination has several legislative and technical synergies for both technologies [17] (e.g., smoothing the power output and reducing the hours of zero production). To further smooth out the power variation and reduce the LCoE, a wind-solar-wave hybrid power system has been proposed [297], which is shown in Figure 23b. However, the design and optimisation of those hybrid power systems significantly depend on the climate of their installation waters [16,19,20]. In addition, PAs can be integrated to floating or onshore breakwaters to form multi-function platforms [298], as shown in Figure 23c.

Figure 23. Point absorber wave energy converters are integrated with offshore structures to form a wind-wave platform [295] (a), a wind-solar-wave hybrid power system [297] (b) and a breakwater-WEC multi-function structure [298] (c).

Recently, many countries have introduced various incentive policies to accelerate the “blue economy”. Thus, ocean-based applications ask for an economical and clean in situ power supply [299]. Wave energy technologies are well-poised for ocean-related applications, and a number of PA devices have been used for ocean navigation and observation [300], coastal protection [298,301], desalination [302], etc. Compared with the utility market, the rated capacity of PA devices for ocean-related applications is much smaller, ranging from milliwatts to kilowatts.

7. Conclusions

This review summarises the state of the art of PAWEC R&D activities and foci, including PAWEC prototyping, hydrodynamic modelling, PTO development, control design and application scenarios. Although wave energy technology is still immature, characterised by a high LCoE, tremendous advancements have been made in PAWEC technology in the past two decades. With a greater accumulated installation capacity and operation experience, the LCoE is projected to be reduced to an accessible and affordable level by 2030–2035, being around EUR 100–150/MWh [294]. To achieve this, innovations in modelling, PTO, control and prototyping are required.

Among various WEC concepts, the PA concept is the best platform with which to test and develop innovative ideas of novel operating principles, modelling methods, PTO mechanisms and control strategies, mainly due to its simple structure. Several fundamental theories and critical findings were first proposed for or revealed from PAWECs (e.g., the resonance concept, theoretical maximum efficiency, LC, RC, constructive park effect and DC). It is also expected that novel ideas will be tested on the basis of PAWECs before their extension to other WECs.

PAWECs can be further classified as one-body and multi-body ones according to their geometric design. One-body PA devices are simple and operate as low-pass filters with narrow bandwidths. Floating one-body PAWECs are capable of harvesting more energy than fully submerged ones, while the submerged ones suffer less from extreme wave loads. Multi-body PAWECs include two-body devices and multi-point absorber prototypes. The former are characterised by a bandpass feature, showing high design flexibility to fit
certain sea states, while the latter have multiple floaters hosted by a large offshore platform, showing a favorable property for reducing the peak-to-average power ratio. In addition, multi-point absorber devices are designed to survive in storms, as the floaters can be lifted up to enter survival mode. However, the cost of a large offshore platform may be high.

In terms of modelling, PTO and control, the PAWEC technology advances in a similar way to other WEC technologies, with current hydrodynamic modelling forces on nonlinear dynamics and phenomena, extreme wave loads and array interaction. For PTO innovation, nonlinear mechanical structures (e.g., snap-through and multi-stable mechanisms), novel materials (e.g., dielectric elastomers) and triboelectric material are used to harvest wave power, though their TRLs are low. From the control perspective, the new trends are to develop or apply robust, model-free and intelligent strategies.

Wave energy technologies originally target the utility market to provide low-carbon electric power. However, the LCoE from wave energy is higher than those from other resources, which makes wave energy uncompetitive or inviable for the utility industry. One possible solution is to integrate WECs with existing offshore wind turbines for reducing the LCoE and smoothing out the power output. In addition, wave energy technologies have shown high potential for niche markets (e.g., powering ocean applications).

For the past few years, the net-zero mission and the blue economy strategy have attracted global attention, consolidating the industry-academia-government cooperation to advance the TRL and TPL of wave energy technologies. Many countries have developed and implemented numerous national strategies and market incentives, giving wave energy technologies a new opportunity for commercialisation in both the utility and niche markets. It is believed that the PA concept will be the bellwether, as it was.

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**Abbreviations**

The following abbreviations are used in this manuscript:

- **WEC** Wave energy converter
- **PAWEC** Point absorver wave energy converter
- **TRL** Technology readiness level
- **TPL** Technology performance level
- **LCoE** Levelised cost of energy
- **PTO** Power take-off
- **O&M** Operation and maintenance
- **PA** Point absorber
- **DoF** Degree of freedom
- **R&D** Research and development
RAO  Response amplitude operator
EMEC  European Marine Energy Centre
AWS  Archimedes wave swing
UPS  Uninterruptible power supply
FNT  Float-neck-tank
CFD  Computational fluid dynamics
PFT  Potential flow theory
FNPT  Fully nonlinear potential flow theory
LPFT  Linear potential flow theory
FK  Froude–Krylov
PMLG  Permanent magnet linear generator
DEG  Dielectric elastomer generator
TENG  Triboelectric nanogenerator
RC  Reactive control
PC  Passive control
LC  Latching control
DC  Declutching control
ACC  Approximate complex conjugate
AVT  Approximate velocity tracking

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