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Understanding the Effects of Market Volatility on Profitability Perceptions of Housing Market Developers

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Abstract: Drastic shifts in prices and housing market trends in recent years, representing shocks to the housing system, have led many residential developers to pause or cancel their projects. In the already heated housing markets of the Greater Toronto Area (GTA), these supply frictions can have ramifications for affordability. Our study formulates a standardized “proforma” model of the profitability of a hypothetical condominium project in the city of Toronto, Canada, scheduled between 2019 to 2023, to explore the combined effect of developers’ price expectations and market volatility on developers’ decisions. Using the proposed proforma, we first identify the key drivers of development decisions. We then evaluate the impact of the expectation formation of key factors influencing perceived development profitability, including construction costs, sales prices, and interest rates, on the financial feasibility of potential developments. The results highlight that boundedly rational expectations can cause variations in profitability perceptions and potentially reverse development decisions in volatile market conditions. Our results highlight the sources of risk and uncertainty in development decisions, facilitating the recognition of possible solutions to mitigate these risks and increase affordable housing supplies. The proposed model can also enhance the realism of decision models in agent-based representations of land and housing markets.

Keywords: housing prices; land use and real estate market; real estate modeling; institutional economics analysis of the real estate market; price expectations; development proforma; construction costs; interest rates; housing supply; bounded rationality

1. Introduction

As housing markets continually evolve, influenced by factors such as economic volatility, demographic shifts, and policy changes, traditional models of land and housing prices often prove inadequate in their ability to fully grasp the multifaceted complexities and nuances of these developments, failing to accurately predict housing prices and development trends (Hunt et al. 2005; Wegener 2021). Further, as argued by Lee and Reed (2014) in a comprehensive review of the literature on housing market volatility, housing policy analysis should consider impacts on housing price volatility and associated market uncertainty. Volatile housing prices can disrupt market equilibrium, affecting affordability, home ownership, investment decisions, and overall housing supply. Understanding and quantifying this volatility provides policymakers with crucial insights into the dynamics of housing markets, enabling them to design interventions that can mitigate the adverse effects of market swings, such as policies that provide subsidies for first-time buyers (Lee and Reed 2014). However, the models historically used to measure housing price volatility at a macro-economic scale show predictive limits. A comparison between the forecast performance of widely used univariate time series methods when applied to housing prices...
suggested that while GARCH models exhibit strong predictive performance in forecasting stationary volatility, their efficacy may diminish when confronted with significant regime changes (Crawford and Fratantoni 2003).

One of the primary challenges models of housing market volatility face is a reliance on aggregate historical data and simplistic assumptions that inadequately account for the dynamic nature of the housing market (Bishop et al. 2020; Ho et al. 2021; Liu et al. 2020; Pai and Wang 2020). Economic events, such as recessions or unexpected shocks to the market, can swiftly alter the landscape, rendering past data less relevant (Balemi et al. 2021). Moreover, expectations in the market arise from, and consequently influence, the historical trajectory of land transactions and realized prices (Filatova 2015; Leung et al. 2009; Taltavull and McGreal 2009), impacting the actors’ financial perceptions, especially in volatile market conditions (Kuchler et al. 2023).

Spatial and temporal variability, combined with rapid demographic changes, present other significant challenges to modelling housing prices and market supply (Jeanty et al. 2010; Yang et al. 2020b). The ever-evolving nature of housing market and policy regulations, with price trends and supply dynamics differing markedly from one location to another, are subject to rapid changes over time and can further complicate predictions, as they can have substantial impacts on supply-and-demand dynamics (Salvati et al. 2019; Yang et al. 2020a). Furthermore, demographic changes, including shifts in population growth, urbanization trends, and generational preferences, introduce new dimensions of uncertainty that can drastically impact housing prices and cause market volatility by influencing the housing preferences and demand for different housing products (Engelhardt and Poterba 1991; Gong and Yao 2022). Factors driving prices and supply can transform abruptly, necessitating models that are both flexible and adaptive.

Microsimulation models offer promise to address these heterogeneous dynamics, but their success in modelling housing supply and prices is mixed. For instance, the ILUMASS model, aimed at creating a fully microscopic model of urban land use, transport, and environment for the metropolitan area of Dortmund, could not prove an adequate level of accuracy in predicting housing prices and market supply (Wagner and Wegener 2007), due in part to simplistic assumptions on individual decision-making that could not capture spatial and temporal variability. Through experimenting with a generalized Agent-Based Model of land use and housing applied in the USA, Laos, and China, Magliocca et al. (2014a) showed missing mechanisms and simplistic assumptions in the representation of real-world land-use dynamics, such as the underlying labour- and risk-minimizing decision-making frameworks, that can lead to failures in simulating land-use patterns and prices, causing the models to fall short in forecast performance.

This study is motivated by a growing need for more advanced and adaptable models that can better account for the real-world intricacies and uncertainties inherent in land-use and housing price forecasting to improve the current projections of prices and housing supply. While price expectations are an essential factor in shaping the asking prices and transaction values of properties in land and housing markets (Filatova 2015; Taltavull and McGreal 2009), the majority of the current models of land and housing markets do not consider the effect of actors’ expectations in their behaviours and decisions (Martin et al. 2021; Taltavull and McGreal 2009), diminishing their ability to predict market trends and capture the effect of market shifts, especially in volatile market conditions. For instance, the integrated land use–transport microsimulation model for the Paris Region (SIMAURIF) showed significant challenges in modelling land and housing markets. While the model could forecast housing prices at an aggregate level, it failed to predict housing supply and market prices at the cell level due to a lack of detail in modelling socioeconomic components and actors’ behaviours (Nguyen-Luong 2008).

Our study explores the impact of alternative theoretical financial perceptions of housing market developers on the financial analyses that support real-world housing supply decisions. The inclusion of such models can be transformative for models of land and housing markets by providing a more realistic representation of developers’ financial per-
ceptions and how changes in these perceptions in response to price shocks can abruptly shift housing supply. In essence, more enhanced models of land and housing markets can shed light on the relationships between housing supply and volatile cost and revenue price dynamics, empowering policymakers and planners to navigate the complexities of the contemporary housing landscape and develop strategies that foster sustainable and equitable housing markets.

Since the late 1990s, there has been an extraordinary proliferation of condominium developments across the Greater Toronto Area (GTA), Canada, as shown in Figure 1, fueled by an influx of private investments in condominium stock and government-sponsored redevelopment of social housing (Lehrer et al. 2010). Private developers have significantly increased the vertical residential space in the housing landscape by pursuing significant re-zonings related to building height and land uses (Buckley and Brauen 2022). In recent years, however, in spite of housing supply shortages in Canada’s largest metropolitan areas, including the GTA, Toronto has experienced a cascade of cancellations of new condominium projects as a result of major shifts in housing market dynamics (Feinstein 2023; Fox 2022; Sherman 2022; Younglai 2022) (see Figure 2).

![Figure 1.](image1.png)

**Figure 1.** Historical development project starts by the intended market in Toronto (CMHC 2023c).

![Figure 2.](image2.png)

**Figure 2.** Historical condo project cancellations in the GTA land and housing market by Urbanation (2023): (a) total number of projects and (b) total number of units.

Alterations in development projects and supply decisions can be traced back to the behaviour of housing market developers, who base development decisions on their expectations of market trends, such as construction costs and potential demand for different housing products. Developers and other key market actors such as lenders seek to maximize their profit from potential developments according to their perception of market conditions, such as rising interest rates (Bank of Canada 2023). This behaviour of residential
developers to undertake potential developments aligns with the notion of economic rationality (Magliocca et al. 2014b; Mohamed 2006). However, if developers are fully rational, why do sudden cost and revenue changes take them by surprise and lead to major changes in project plans?

While more than 260,000 housing projects were started in Canada in 2022, this supply rate is insufficient. Although Canada is projected to build 2.3 million new homes by 2030, CMHC (2022, 2023b) estimates that it actually needs to build an additional 3.5 million homes to restore housing affordability by 2030, with around 1.5 million additional homes needed in Ontario alone. Currently, around half the construction activity in major centres where demand is greatest, such as Toronto and Vancouver, is in the condominium and rental segments. This number will only continue to grow over time given that apartment living is generally less expensive per unit than ground-facing options, even considering the relatively high-rise construction costs. Municipalities also continue to seek high-density housing to minimize urban expansion and create critical mass for transit projects. Financing models for high-rise development are also well-developed. Thus, high-rise condominiums and rental construction in high-demand areas can be a pragmatic approach to providing more housing options. As this trend gains momentum, understanding the factors that impact high-rise developer supply decisions is critical to help inform governments at all levels on what policies may be needed to incentivize the construction of more high-density housing.

Developers’ expectations with regard to factors such as construction costs, interest rates, and market prices are critical drivers of the decision to supply housing. Developers use a financial analysis tool, called “proforma,” to estimate the financial return from the potential developments and reach development decisions (Barer 2011; Hollander and Stephens 2023; Jennings 2012; Murray 2022). Developers and their investors require these proformas to assess the profitability of a new development when deciding if, when, and where they should begin new high-rise projects. Volatile macroeconomic conditions can represent a shock to the housing system, leading to uncertainty and volatility in the new housing supply. This uncertainty heightens the investment risk for developers and investors, which can increase the required return on investment to offset the perceived risks.

To mitigate the uncertainties in financial projections, developers often rely on cost consultants, who possess a wealth of historical data derived from comparable projects (Betts 1991; Okwilagwe and Apostolakis 2017; Smyth 2005). These seasoned actors play a pivotal role in establishing parameters for prospective developments, offering a perceived higher degree of reliability in the estimation of forthcoming prices and costs (Wood and Ellis 2003). Nevertheless, we argue that it is impossible for even seasoned actors to perfectly predict market trends, especially in volatile market conditions.

Additionally, given that the development of high-rise residential buildings are long-term endeavours, builders need to price their projects at the early phase of their sales and marketing campaigns. However, projects will not usually break ground until 24 months after a condo sale is registered, leading to significant risk if expectations around costs prove incorrect. This can lead to project delays and cancellations as projects become less economically viable. The recent run-up in labour and building material costs coming out of the pandemic is a case in point. According to Urbanation data, shown in Figure 2b, approximately 10,000 condominium units in Toronto have been cancelled in recent years.

This paper aims to address the following research questions:

- What are the main factors impacting the profitability perceptions of potential high-rise developments?
- How do profitability perceptions shift when boundedly rational price expectations are used to project market trends for construction costs, unit sales prices, and interest rates?
- Can boundedly rational expectations of market trends explain project cancellations, when the housing system experiences unanticipated price shocks?

To address these research questions, our paper explores the key drivers of the profitability of development projects, using a hypothetical prototype proforma to identify the
relative influence of cost and revenue factors on development returns and which factors most influence a development’s profitability. We assume that such factors will be primary drivers of the development decisions of housing market developers. To this end, we formulated a standardized proforma representing the essential financial elements of sales development projects, including project financing, potential revenues, and costs. We examined the sensitivity of the Net Present Value (NPV) and Internal Rate of Return (IRR) of the project to various model parameters to evaluate the role of different proforma assumptions on the financial profitability of the project. This analysis highlights the importance of three factors that have shown unexpected volatility in recent years, construction costs, unit sales prices, and interest rates.

We then evaluated the impact of the boundedly rational expectation formations of developers on their development decisions. Developers, like all human actors, lack perfect foresight of future economic conditions. To account for this limited foresight, we identified several expectation formation models based on the review of the literature and incorporated these models into the proposed proforma. Inclusion of these mechanisms allows us to further explore how different decision strategies and expectation formations of primary factors influencing the financial analysis of a potential development project, including construction costs, unit sales prices, and interest rates, influence profitability thresholds for new developments.

The rest of this paper is organized as follows: Section 2 discusses the literature on developer decisions and their price expectations, also highlighting the key factors influencing the financial profitability of projects and the development decisions of housing market developers. Section 3.1 presents the formulation of a standardized sales proforma as a financial analysis tool that uses the Net Present Value (NPV) and the Internal Rate of Return (IRR) as the primary measures to evaluate the profitability of potential development projects. Section 3.2 discusses the application of the proposed proforma to a case study of a hypothetical potential condo project in the city of Toronto, scheduled between July 2019 and June 2023, to showcase the impact of various factors on development decisions. Section 4.1 presents the results of numerical sensitivity analyses with several model parameters to identify key drivers of the project’s profitability calculations. Section 4.2 explores how boundedly rational price expectations and correlation between decision parameters can explain project postponement and cancellation based on profitability perceptions in volatile market conditions. Finally, Section 5 discusses the policy implications and introduces future model applications.

2. Literature Review

Perspectives on developers’ economic rationality. Various perspectives have been used to describe the behaviours and expectation formation of developers in land and housing markets. The “rational expectations” economic model assumes that developers will best use all available information to precisely estimate future price trends. However, the “complexity economics” (Arthur 2018) point of view argues that economic actors can behave at best as boundedly rational, as the real world is too complex to predict all outcomes. Some studies qualitatively characterize developers as profit-seeking, risk-taking, and innovative (Maruani and Amit-Cohen 2011; Winarso 2000), while other studies find evidence of “boundedly rational” decision behaviour, including satisficing (the tendency to find and select the closest satisfactory solution), loss aversion (weighing losses more than gains), and weighing relative rather than absolute wealth shifts (prospect theory) (Magliocca et al. 2014b).

Primary factors in development decisions of developers. Developers rely on their expectations of future market trends and profitability perceptions to decide on their actions. For instance, high risk perceptions of project failure combined with low expectations of resident demand can lead to under-supply of particular housing typologies, such as “Missing Middle” housing, referring to low-rise high-density homes such as duplexes, triplexes, and townhouses (Parker et al. 2023). On the other hand, expectations of land...
up-zoning coupled with expectations of high demand by investors can trigger oversupply of products such as small high-rise condos. Both trends have recently been observed in Ontario land and housing markets (Parker et al. 2023; Paull 2022; Sarnoff 2022).

Pro formas allow developers to test the revenue and cost assumptions for potential development projects to evaluate whether they support a decision to purchase land and/or develop housing. Pro formas help private developers evaluate the financial viability of the development projects and achieve the “highest and best use” for a potential project (Johnson et al. 2018). Development pro formas consider financing options (e.g., equity and debt funds), market analytics (e.g., sales prices and construction costs), and planning requirements (e.g., density requirement and development typologies), to assess the revenue generation and opportunity costs (the potential return on alternative investments). The use of development pro forma to represent developers’ decision-making is consistent with a hypothesis that developers are boundedly rational profit maximizers (Magliocca et al. 2014b, 2011).

To arrange the financial aspects of projects using pro forma, housing market developers face a range of significant market and planning risks, influencing their development decisions regarding new housing projects. Developer–investor relationships fraught with planning dynamics and tensions interact to create or inhibit financing opportunities for the new developments (Brill 2022). Financing costs and the financial feasibility of development projects can also be significantly impacted by the fluctuations in interest rates, since they directly influence the cost of borrowing money for development projects. Developers need to carefully consider interest rate trends and potential risks when structuring their financing strategies to effectively manage financial risks.

Previous observations of market trends have shown that interest rates can impact the housing market in several ways, as shown in Figure 3. An increase in interest rates can influence housing demand by reducing affordability, which in turn can have a suppressing effect on unit sales prices (Chong 2023; Justiniano et al. 2019; Sutton et al. 2017). In such a situation, the profitability of the project is significantly impacted by the shifts in the two variables. On the cost side, the increasing interest rates would increase the project financing costs, imposing extra financial burden on the project. On the revenue side, depressing housing prices would decrease the expected revenue for the projects, implying that the project might not achieve its expected financial goal Arslan (2014); Chong (2023). Therefore, understanding the association between interest rates and housing prices is crucial for housing market developers when considering market volatility and financial return from potential developments.

In addition to interest rates, various market factors, such as construction costs, sales price appreciation and volatility, and pricing of land options, guide developers’ expectations of financial viability and subsequent land development decisions (Cunningham 2007; Felsenstein and Ashbel 2010; Filatova et al. 2009; Imrie and Street 2009; Silva 2002; Taltavull and McGreal 2009). Construction costs can impose a significant financial barrier to development projects. In the early stage of the project, developers must rely on their initial construction cost expectations for their development decisions. However, those expectations may be based on limited information and have a high degree of uncertainty (Jennings 2012; Koo et al. 2011). As the project proceeds, the construction costs are updated based on the available information about the development, and incoming information may alter the viability of the project.

Other market trends, such as sale and rent price trends, the vacancy and absorption rates (i.e., how quickly new builds are rented or sold when completed), and land pricing options, can also influence developers’ estimation of the generated revenue in their potential development projects (Antczak-Śtepiak 2021; Huang 2020; Murray 2022). For instance, a local increase in housing and land supply can lead to a decline in absorption rates, which impacts the expected revenues from the project and could be a signal for developers to alter their decisions about land developments (Barer 2011).
Modelling the price expectation of housing market developers. Our review of the literature indicates that the majority of studies on price expectations have employed statistical Huang et al. (2021); Taltavull and McGreal (2009) or agent-based models (Ettema 2011; Gilbert et al. 2009; Magliocca et al. 2011; Parker and Filatova 2008) of land and housing markets, as modelling boundedly rational price expectations and their interactions is challenging or impossible using analytical approaches. Leung et al. (2009) assumed that housing market developers could develop heterogeneous boundedly rational expectations, including naive expectations, biased beliefs, trend-following expectations, and adaptive expectations. Another perspective characterizes the adaptation of price expectation models from the financial agent-based literature (Arthur 1994, 2006; Axtell 2005). Magliocca et al. (2011) evaluated the conversion of farmland to housing developments over time by developing an ABM housing and land market model in which developers use adaptive price expectations to predict the next period’s price based on current and past price information. Agents use a set of different prediction methods, such as the mean model, the cycle model, and the projection model, and select the prediction model with the least error to make pricing decisions in the current period.

Another group of studies, mainly from the literature on finance and general economics, have conducted experiments with human subjects (e.g., learning-to-forecast experiments) to understand price expectations in a controlled setting (Hommes 2021). For instance, Hommes et al. (2005) conducted four rounds of experiments in a laboratory setting to evaluate the individual expectations of asset prices. The findings highlighted that as the experiment progresses, the subjects use more complicated strategies to form expectations, helping them improve their learning and convergence over the rounds. Bao and Hommes (2015) designed an experimental housing market and evaluated the effect of the price elasticity of supply on market stability. They used learning-to-forecast experimental analysis to study individual decisions and housing price expectations and their impact on market stability. The experiments indicated that speculators rely on trend-following expectations in the absence of endogenous housing supply, where the housing demand does not add negative feedback to the market prices, leading to significant market bubbles and crashes. Although this group of studies explored the expectation formation of human subjects.
regarding asset prices, the results of the experiments and proposed models cannot comprehensively reflect the behaviour of housing market developers as the experiments are not originally designed to evaluate the developers’ behaviours in the land and housing markets.

Conclusions from literature review. Review of the literature indicated that there is a gap in the study of decision strategies of housing market developers through understanding their profitability perceptions and price expectations. Moreover, to our knowledge, diverse approaches to representing developer expectations have not been explored and compared within the same model. To fill this gap, our study identifies the important drivers of development decisions by formulating and exploring a standardized proforma as a financial model used to assess the financial viability of potential development projects. To account for the impact of the price expectations of developers on their development decisions, we incorporated various models of expectation formation into the proposed proforma to explain the boundedly rational behaviour of housing market developers regarding the projection of market trends that primarily influence a project’s profitability, including construction costs, unit sales prices, and loan interest rates. Our study establishes an understanding of the development proforma and primary factors contributing to the financial viability of potential developments and how these are impacted by price expectations, providing insights into the function of housing markets.

3. Materials and Methods

The proforma models in this study are built through a collaborative work between UrbanSim, CMHC, and the Urban Growth and Change Research Group (UGC) at the University of Waterloo. UrbanSim provided the preliminary models, CMHC developed the test case scenarios, and the UGC research group implemented the models in spreadsheets and Python programming language and cross-verified the information between models. Please refer to the Supplementary Materials for the model code.

3.1. Model Development: Formulation of a Standardized Proforma for a High-Rise Condo Project

Several financial metrics are often used to assess the profitability of investment projects, such as the Net Present Value (NPV) and the Internal Rate of Return (IRR), mostly evaluating potential revenues against project costs to calculate the financial return (Dudley 1972; Hollander and Stephens 2023). Development proforma tools used by land developers often employ the IRR as the primary criterion for determining the financial viability of the potential developments (Finnegan Marshall 2023). The NPV is the discounted cash flow of the project concerning the annual revenues, costs, and initial investment (Fraser and Jewkes 2012), formulated as

\[
NPV(C, R_1, \ldots, R_T, \rho, T) = -C + \sum_{t=1}^{T} \frac{R_t}{(1 + \rho)^t}
\]

where \( C \) is the investment costs at time zero, \( R_t \) is the net cash flow at time \( t \), and \( \rho \) is the discount rate.

The IRR is the rate of return at which the sum of all discounted inflows and outflows are balanced at the end of the project, and can be defined as the value \( \rho \) such that

\[
NPV(C, R_1, \ldots, R_T, \rho, T) = 0
\]

Intuitively, the IRR represents the rate of return at which the investor would be indifferent between undertaking the development investment and receiving that cash rate of return on the investment over the time period of the project.

The rest of this section discusses the development costs and project financing, and relies on Equation (1) to draw the cash flow of a standardized condo development project and calculate the IRR based on the NPV formulation.
3.1.1. Total Development Costs

Before estimating the cash flow of the project, developers must make assumptions regarding the total development costs and project finance. The total project costs (excluding the land costs), $TPC$, is estimated as the sum of the planning costs, development charges, other governmental costs, other initial costs, and construction costs:

$$TPC = P + (1 + \zeta)NDc + Z + N\tau Aa$$  \hspace{1cm} (3)

where $P$ shows planning costs, $N$ is the total number of proposed units for the development project, $Dc$ is the average development charges per unit, $\zeta$ is a safe margin to cover other governmental fees (e.g., Section 37 and park cash in lieu for the city of Toronto), $Z$ shows other initial costs imposed to the project (e.g., amenities and off-site construction), $\tau$ shows the average construction costs per square foot, and $Aa$ shows the average unit area for the proposed typology. In the case that the development charges is determined on a per square foot basis, Equation (3) can be formulated as

$$TPC = P + (1 + \zeta)NDcAa + Z + N\tau Aa$$  \hspace{1cm} (4)

where $Dc$ is development charges per square foot.

The developer’s fee (i.e., the developer’s compensation for managing the development process) is added to the total project costs to determine the total development costs, $TDC$. The developer’s fee is formulated using a coefficient of $Df$ corresponding to the developer’s fee as a percentage of total project costs. Total development costs, $TDC$, is formulated as

$$TDC = (1 - Df)(P + (1 + \zeta)NDc + Z + N\tau Aa)$$  \hspace{1cm} (5)

It is assumed that the developer’s fee is collected in one installment in the last year of the project construction.

3.1.2. Project Financing

Developers typically use a hybrid financing model that involves a combination of equity, pre-sales, and debt funds to cover the total development costs. For simplicity of analysis and comparison of expectations mechanisms, our current proforma does not represent pre-sales. In the context of real estate development, equity funds refer to investments made by individuals or entities in exchange for ownership or equity stake in a project. Debt funds, on the other hand, involve borrowing money from various sources such as banks, financial institutions, or private lenders to cover the financing needs of a development project. In this proforma, we assumed that the developer invests the amount of equity in the project at project initiation and recoups this amount at the end of the construction phase. (Again, for simplicity, we do not consider borrowing of equity funds.) Considering $\eta$ as the equity funds as a percentage of total development costs, the total equity funds provided by the developer, $E$, are

$$E = \eta TDC$$  \hspace{1cm} (6)

On the other hand, the total amount of loan required to help cover total development costs, $\sigma$, is formulated as

$$\sigma = (1 - \eta)TDC$$  \hspace{1cm} (7)

Replacing $TDC$ from Equation (5), the total amount of loan required to finance the project can be formulated as

$$\sigma = (1 - \eta)(1 - Df)(P + (1 + \zeta)NDc + Z + N\tau Aa)$$  \hspace{1cm} (8)
Developers must return the loan funds over a period of $Y$ years. The proforma assumes that the loan funds are returned annually starting in the second year of project construction. Considering a loan interest rate of $i$, the annual loan payments, $L_p$, is formulated as

$$L_p = \sigma \frac{(1+i)^Y}{(1+i)^Y - 1}$$

Replacing the total loan amount, $\sigma$, from Equation (8), the annual loan payments can be shown as

$$L_p = (1 - \eta)(1 - D_f)(P + (1 + \zeta)ND_c + Z + N\tau A_a) \frac{i(1+i)^Y}{(1+i)^Y - 1}$$

3.1.3. Cash Flow of the Project

Considering $I_t$ as the annual net cash inflow at year $t$ and $O_T$ as the annual net cash outflow at year $t$, Equation (2) can be rewritten as

$$NPV = -C + \sum_{t=1}^{T} \frac{I_t - O_t}{(1 + \rho)^t}$$

Net cash outflow of the project is composed of project expenses such as initial investments and annual construction costs. The initial investment costs at time zero, $C$, can be formulated as the land acquisition cost $L$, planning costs $P$, development charges, other governmental costs, and other initial costs:

$$C = L + P + (1 + \zeta)ND_c + Z$$

where $N$ is the total number of proposed units for the development project, $D_c$ is the average development charges per unit, $\zeta$ is a safe margin to cover other governmental fees (e.g., Section 37 City of Toronto (2023)), and $Z$ shows other initial costs imposed on the project (e.g., amenities and off-site construction).

The recurring fees that constitute annual net cash outflow during the construction period, $O_t$, include annual costs for building construction, property taxes, and loan payments:

$$O_t = \kappa \tau A_a + \theta L + L_p$$

where $\kappa$ is the construction rate defined as the total number of units constructed per year, $\tau$ is the construction costs per square foot, $A_a$ is the average unit area as square foot, $\theta$ is the annual tax rate as a percentage of land value, $L$ is the land value, and $L_p$ is loan payments formulated using Equation (10).

Net cash inflow of the project comprises the project revenues primarily created by the sales of the developed units:

$$I_t = n_t \pi (1 + \beta)$$

where $n_t$ shows the total number of units closed at time $t$, $\pi$ shows the average unit sales price, and $\beta$ encodes the broker fees as a percentage of gross sales, defined as the fee charged by brokers facilitating the project sales. Considering $\omega$ as the market absorption rate and $\kappa$ as the total number of units constructed per year, the total number of units closed at time $t$ is estimated as $n_t = \omega \kappa$.

As another cost to the project, the developer receives the amount equal to the developer’s fee, $D_f$. As a source of revenue, the developer recoups the initial equity funds, $E$, at the end of project construction.

According to Equation (11) and considering the project’s costs and revenues, the $NPV$ for the project can be formulated as the sum of the investment costs at time zero, discounted annual net cashflows, discounted developer’s fee, and discounted developer’s equity funds:
\[ NPV = -(L + P + (1 + \zeta)ND_c + Z) + \left( \sum_{t=1}^{T_c} (\kappa \omega \pi (1 + \beta)) - (\kappa T A_a + \theta L + L_p) \right) - \]

\[
\left( \frac{D_f TPC}{(1 + \rho)^{T_c}} \right) + \left( \frac{E}{(1 + \rho)^{T_c}} \right)
\] (15)

Replacing total project costs, TPC, and equity funds, E, from Equations (3) and (6), Equation (15) can be rewritten as

\[ NPV = -(L + P + (1 + \zeta)ND_c + Z) + \left( \sum_{t=1}^{T_c} (\kappa \omega \pi (1 + \beta)) - (\kappa T A_a + \theta L + L_p) \right) - \]

\[
\left( \frac{D_f (P + (1 + \zeta)ND_c + Z + N\tau A_a)}{(1 + \rho)^{T_c}} \right) + \left( \frac{\eta (1 + D_f)(P + (1 + \zeta)ND_c + Z + N\tau A_a)}{(1 + \rho)^{T_c}} \right)
\] (16)

3.1.4. Profitability Criteria

Developers’ decision to proceed with a development project is dependent on if the estimated financial return from the project (i.e., the IRR) exceeds a reasonable minimum threshold of return on investment. The Minimum Attractive Rate of Return (MARR), which may also encompass a risk premium, is defined as a reasonable rate of return established for the evaluation and selection of alternatives (Fraser and Jewkes 2012). A development project is not financially justified unless it is expected to return at least the MARR (White et al. 2020). The value of the MARR should be selected to be greater than the standard discount rate, \( \mu \), to ensure that the project makes more return on investment than typically available investments (e.g., banking investment alternatives). Therefore, an increase in the interest rates would lead to an increase in the MARR so that the project would return a profit margin higher than generic investments. The condition under which the developer might decide to undertake a potential development project can be represented as

\[ \mu < MARR \leq \rho \] (17)

According to Equation (17), the decision of developers to proceed with a potential development project is directly influenced by the choice of MARR for the project. Overestimating the IRR for a potential project can raise the likelihood of validating Equation (18), thus increasing the chance of undertaking the project, while the project might not return the anticipated profit. On the other hand, underestimating the IRR can refute Equation (17), convincing the developers to not undertake, postpone, or cancel the development project, while the project might still meet their profitability criteria.

3.2. Case Study

To evaluate the drivers of the project’s financial return, we applied this proforma model to the analysis of the NPV and the IRR in a hypothetical case study. The proforma is built on a sample development typology (e.g., building size and unit mix) corresponding to a high-rise residential building located in the city of Toronto, Canada. The development project in the test case proposes a total of 357 units with an average unit area of 704.75 square feet. The project starts in July 2019 and runs over a 4-year period until June 2023. Key characteristics of the development typology and inputs to the proforma (parameters) are summarized in Table 1.
Table 1. Key model parameters and their values at project initiation in July 2019 for the baseline scenario (Altus Group 2022; Bank of Canada 2023; CMHC 2023a; Statistics Canada 2023).

<table>
<thead>
<tr>
<th>Notation</th>
<th>Description</th>
<th>Variable Unit</th>
<th>Variable Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>Land size</td>
<td>Acres</td>
<td>2.50</td>
</tr>
<tr>
<td>N</td>
<td>Total units to sell</td>
<td>Units</td>
<td>357.00</td>
</tr>
<tr>
<td>A(a)</td>
<td>Average unit area</td>
<td>Square feet</td>
<td>704.75</td>
</tr>
<tr>
<td>(\tau)</td>
<td>Construction costs</td>
<td>Dollar per square foot</td>
<td>298.93</td>
</tr>
<tr>
<td>L</td>
<td>Land acquisition costs</td>
<td>Dollar</td>
<td>60,000,000.00</td>
</tr>
<tr>
<td>P</td>
<td>Planning and design</td>
<td>Dollar</td>
<td>1,150,000.00</td>
</tr>
<tr>
<td>D</td>
<td>Development charges per unit</td>
<td>Dollar</td>
<td>17,274.00</td>
</tr>
<tr>
<td>E</td>
<td>Other initial costs (amenities, off-site construction, etc.)</td>
<td>Dollar</td>
<td>8,650,000.00</td>
</tr>
<tr>
<td>(\zeta)</td>
<td>Other government fees (Section 37 and Park Cash in Lieu)</td>
<td>Percent of total development charges</td>
<td>15%</td>
</tr>
<tr>
<td>(\theta)</td>
<td>Annual property tax rate</td>
<td>Percent of land value</td>
<td>3%</td>
</tr>
<tr>
<td>(D_f)</td>
<td>Developer’s fee</td>
<td>Percent of total project costs</td>
<td>5%</td>
</tr>
<tr>
<td>(\beta)</td>
<td>Broker fees</td>
<td>Percent of gross sales</td>
<td>6%</td>
</tr>
<tr>
<td>M</td>
<td>Management &amp; overhead</td>
<td>Percent of gross sales</td>
<td>15%</td>
</tr>
<tr>
<td>(t_{\text{init}})</td>
<td>Project initiation time (i.e., land purchase)</td>
<td>YYYY-MM</td>
<td>2019-07</td>
</tr>
<tr>
<td>(\kappa)</td>
<td>Construction rate</td>
<td>Unit per quarter</td>
<td>30.00</td>
</tr>
<tr>
<td>(\eta)</td>
<td>Equity amount</td>
<td>Percent of total development costs</td>
<td>20%</td>
</tr>
<tr>
<td>(Y)</td>
<td>Loan length in years</td>
<td>Years</td>
<td>3.00</td>
</tr>
<tr>
<td>(i)</td>
<td>Loan interest rate</td>
<td>Dimensionless percentage</td>
<td>3.75%</td>
</tr>
<tr>
<td>(\pi)</td>
<td>Sales unit price</td>
<td>Dollar</td>
<td>1,005,833.00</td>
</tr>
<tr>
<td>(\omega)</td>
<td>Absorption rate</td>
<td>Percent of units per quarter</td>
<td>99%</td>
</tr>
</tbody>
</table>

3.3. Models of Expectation Formation

To investigate the impact of the expectation formation of housing market developers on their development decisions, we modified the proposed sales proforma to represent several expectation models that can approximate developers’ expectation formation strategies. These strategies characterize the expectation of primary factors influencing development decisions, including construction costs, market absorption rates, and unit sales prices.

Past studies have used many different mathematical algorithms to represent price expectations, almost entirely relying on historical data to create expectations. These algorithms consider a variety of factors to characterize belief formation. In this paper, we evaluated algorithms such as boundedly rational expectations (Leung et al. 2009), financial prediction models (Arthur 1994, 2006; Axtell 2005, Magliocca et al. 2011), heuristic rules derived from empirical experiments (Hommes 2021; Hommes et al. 2005), and a GARCH model to represent developers’ expectations, summarized as follows:

- A naive model of expectations assumes that the expected price at time \(t + 1\) would be equal to the current price at time \(t\), or that \(p_{t+1}^e = p_t\).
- A mean model assumes that the expected price is the mean value of the previous \(x\) periods, or \(p_{t+1}^e = \frac{1}{x} \sum_{i=t-x}^{t} p_i\).
- A cycle model assumes that the expected price in the next step is same as the price at \(x\) periods ago, where \(p_{t+1}^e = p_{t-x}\).
- A projection model estimates the price as the least-square, non-linear trend over the past \(x\) periods. The projection model is formulated as \(p_{t+1}^e = ap_t^2 + bpt_s + c\), where \(t_s\) is the ratio of \(t - x\) to \(t\), and \(a\), \(b\), and \(c\) are model coefficients.
- A re-scale model estimates that the future price will be a given factor \(g\) of the current price, \(p_{t+1}^e = gp_t^e\).
- Adaptive expectations pose that the expected price is shaped based on the last observed price, \(p_{t-1}\), and the last expected price, \(p_t^e\): \(p_{t+1}^e = xp_{t-1} + (1-x)p_t^e\), where \(0 \leq x \leq 1\).
- Trend-following models extrapolate the last price change, either with a weak-trend rule (WTR) or with a strong-trend rule (STR) parameter, \(g\), formulated as \(p_{t+1}^e = p_{t-1} + g(p_{t-1} - p_{t-2})\).
A Learning Anchor and Adjustment (LAA) rule extrapolates a price change from a more flexible anchor, 
\[ p_{t+1}^e = \frac{p_{t-1}^e + p_{t-1}}{2} + (p_{t-1} - p_{t-2}), \]
where \( p_{t-1}^e = \sum_{j=0}^{t-1} p_j \).

A GARCH model that estimates the parameters that best describe the conditional variance of the time series: 
\[ p_t = \mu + \phi_1 p_{t-1} + \theta_1 \epsilon_{t-1} + \epsilon_t. \]

### 3.4. Datasets and Model Parameterization

To parameterize the models of expectation formation, we used historical data on construction costs (Altus Group 2022; Statistics Canada 2023), unit sale prices (CMHC 2023a), and loan interest rate (Bank of Canada 2023) as demonstrated in Figure 4. Data on building construction price indexes are collected and published by Statistics Canada (Statistics Canada 2023). These data are available on a quarterly basis from 1988. The base period for the index in this data set is 2017. The data on unit sales prices are obtained from the Canada Mortgage and Housing Corporation (CMHC) data portal (CMHC 2023a) and are available on a monthly basis since 1990. The development loan interest rate is estimated as Canada’s prime interest rate (Bank of Canada 2023) plus 2%.

Major shifts in the market trends during the selected period (i.e., 2019 to 2023) can significantly influence the development projects, potentially countering policymakers’ attempts to address housing supply and affordability challenges (Lorga et al. 2022). According to Figure 4a, the historical trend for construction costs has rapidly increased since 2017. This increasing trend has accelerated since 2021 following the pandemic, which can be a potential reason for alterations in the projects initiated before 2021 due to their failure to foresee the drastic rises in construction costs. Similar to construction costs, the actual trend for unit sales prices has significantly increased since 2017. According to Figure 4b, the market experienced a significant increase in unit sales prices in 2019 (before project initiation). The unit sales prices have experienced significant oscillations after the project start due to market instability; however, the overall prices continued to rise, which can increase the potential revenues for the development projects. Interest rates have also seen significant changes since 2017, as shown in Figure 4c. Prime interest rates dropped from 1.75% to 0.25% in 2020. More recently, interest rates have significantly increased since March 2022 up to 6.75% in June 2023, which can cause remarkable changes in project financing costs. Understanding the potential impact of rising costs and interest rates at this time is essential for longer term housing market planning.

Based on the initial experiments with different observation window for expectation models (see Appendix B), we parameterized models of expectation formation to capture the overall trends in the most recent data (i.e., a period of one year), as summarized in Table 2. We are thereby making the assumption that developers are using the most accurate observation window. By focusing on the more recent data, developers can obtain a better understanding of the current market conditions and make more accurate predictions regarding the escalating trends, as implied by the results of the initial experiments. However, it should be noted that our choices of expectation mechanisms and observation window do not necessarily reflect the reality of developers’ behaviours. Future studies can conduct interviews or experiments with housing market developers to understand their decision strategies more closely.
Figure 4. Historical market trends for (a) construction costs (Altus Group 2022; Statistics Canada 2023), (b) sales prices of properties (CMHC 2023a), and (c) loan interest rates estimated as the prime interest rate plus 2% (Bank of Canada 2023) in the Toronto land and housing markets.

Table 2. Parameters of various models of expectation formation parameterized based on the available data sets.

<table>
<thead>
<tr>
<th>Expectation Model</th>
<th>Characteristic</th>
<th>Unit</th>
<th>Estimated Value</th>
<th>Notes</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>Construction Cost</td>
<td>Unit Sales Price</td>
</tr>
<tr>
<td>Mean model</td>
<td>Observation window (x)</td>
<td>quarter</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>Cycle model</td>
<td>Cycle frequency (x)</td>
<td>quarter</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>Projection model</td>
<td>Observation window (x)</td>
<td>-</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>Re-scale model</td>
<td>Re-scale factor (g)</td>
<td>-</td>
<td>1.058</td>
<td>1.0871</td>
</tr>
<tr>
<td>Adaptive expectations</td>
<td>Weight of the observed data (a)</td>
<td>-</td>
<td>0.65</td>
<td>0.65</td>
</tr>
<tr>
<td>Weak-trend rule</td>
<td>Weight of the changed rate (g)</td>
<td>-</td>
<td>0.4</td>
<td>0.4</td>
</tr>
<tr>
<td>Strong-trend rule</td>
<td>Weight of the changed rate (g)</td>
<td>-</td>
<td>1.3</td>
<td>1.3</td>
</tr>
<tr>
<td>Anchor and adjustment</td>
<td>Observation window (x)</td>
<td>quarter</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>GARCH</td>
<td>Observation window (x)</td>
<td>quarter</td>
<td>4</td>
<td>4</td>
</tr>
</tbody>
</table>

4. Results
4.1. Key Drivers of Project’S Profitability

To identify the key drivers of the project’s financial return, we evaluated the role of various model parameters in the financial profitability of the project. To this end, we performed numerical sensitivity analyses to evaluate the impact of a change in each of the model parameters on the overall NPV and IRR of the project. To conduct the numerical sensitivity analyses, we measured the change in the NPV and IRR of the project as a result
of incrementally increasing the value of each model parameter, while keeping all other model parameters constant. The results of this analysis along with the magnitude of the increments in the model parameters are summarized in Tables 3–5. A positive change in the NPV and IRR indicates an increase in the profitability of the project as a result of the imposed change in the value of the parameters, while a negative value for change in NPV and IRR suggests a decrease in the profitability of the project. Note that as different parameters have different unit values, the relative magnitudes of change are not exactly comparable; i.e., a one dollar change may be quite different than a percent change in an interest rate. Therefore, these results should be interpreted carefully, including reference to the measurement units. To aid interpretability, we also provided elasticities (percent change in the IRR for a percentage change in the input parameter) in Tables 3–5. To support the results of sensitivity analyses, an analytical analysis of the partial derivatives of the NPV function with respect to several model parameters is provided in Appendix A.

Table 3. Results of the numerical sensitivity analysis of the NPV, the IRR, and elasticity of the IRR with respect to a change in model parameters related to project financing. Note that the units of change vary.

<table>
<thead>
<tr>
<th>Notation</th>
<th>Description</th>
<th>Variable Value</th>
<th>Variable Unit</th>
<th>Marginal Change</th>
<th>NPV Change in Dollar</th>
<th>IRR Change</th>
<th>Elasticity</th>
</tr>
</thead>
<tbody>
<tr>
<td>η</td>
<td>Equity amount</td>
<td>20% Percent of total development costs</td>
<td>1%</td>
<td>2,432,863.90</td>
<td>0.015577</td>
<td>3.04247</td>
<td></td>
</tr>
<tr>
<td>i</td>
<td>Loan interest rate</td>
<td>3.75% Dimensionless percentage</td>
<td>0.25%</td>
<td>-670,723.97</td>
<td>-1.004338</td>
<td>-1.635822</td>
<td></td>
</tr>
<tr>
<td>Y</td>
<td>Loan length in years</td>
<td>3.00 Years</td>
<td>1.00</td>
<td>2,911,235.73</td>
<td>0.025341</td>
<td>0.742858</td>
<td></td>
</tr>
</tbody>
</table>

Table 4. Results of the numerical sensitivity analysis of the NPV, the IRR, and elasticity of the IRR with respect to a change in parameters related to cost and revenue assumptions. Note that the units of change vary.

<table>
<thead>
<tr>
<th>Notation</th>
<th>Description</th>
<th>Variable Value</th>
<th>Variable Unit</th>
<th>Marginal Change</th>
<th>NPV Change in Dollar</th>
<th>IRR Change</th>
<th>Elasticity</th>
</tr>
</thead>
<tbody>
<tr>
<td>N</td>
<td>Total units to sell</td>
<td>357.00 Units</td>
<td>1.00</td>
<td>257,057.30</td>
<td>0.001656</td>
<td>5.775678</td>
<td></td>
</tr>
<tr>
<td>Aᵣ</td>
<td>Average unit area</td>
<td>700.00 Square feet</td>
<td>1.00</td>
<td>-1,772.90</td>
<td>-1.001013</td>
<td>-1.930912</td>
<td></td>
</tr>
<tr>
<td>τ</td>
<td>Construction costs</td>
<td>298.93 Dollar per square foot</td>
<td>1%</td>
<td>-1,097,410.30</td>
<td>-1.007097</td>
<td>-1.934501</td>
<td></td>
</tr>
<tr>
<td>θ</td>
<td>Annual property tax rate</td>
<td>3% Percent of land value</td>
<td>1%</td>
<td>-1,085,990.38</td>
<td>-1.013421</td>
<td>-1.346193</td>
<td></td>
</tr>
<tr>
<td>Dᵣ</td>
<td>Developer’s fee</td>
<td>5% Percent of total project costs</td>
<td>1%</td>
<td>-1,097,478.19</td>
<td>-1.007237</td>
<td>-1.348035</td>
<td></td>
</tr>
<tr>
<td>β</td>
<td>Broker fees</td>
<td>6% Percentage of gross sales</td>
<td>1%</td>
<td>-1,937,121.47</td>
<td>-1.019041</td>
<td>-1.790847</td>
<td></td>
</tr>
<tr>
<td>η</td>
<td>Construction rate</td>
<td>30.00 Unit per quarter</td>
<td>1.00</td>
<td>547,431.80</td>
<td>0.013511</td>
<td>14.618123</td>
<td></td>
</tr>
<tr>
<td>π</td>
<td>Unit sales price</td>
<td>1,005,833.00 Dollar</td>
<td>1%</td>
<td>2,320,325.96</td>
<td>0.014960</td>
<td>14.618470</td>
<td></td>
</tr>
<tr>
<td>ω</td>
<td>Absorption rate</td>
<td>99% Percent of units per month</td>
<td>1%</td>
<td>2,343,763.60</td>
<td>0.015111</td>
<td>14.618123</td>
<td></td>
</tr>
</tbody>
</table>

Table 5. Results of the numerical sensitivity analysis of the NPV, the IRR and elasticity of the IRR with respect to a change in model parameters related to initial investments. Note that the units of change vary.

<table>
<thead>
<tr>
<th>Notation</th>
<th>Description</th>
<th>Variable Value</th>
<th>Variable Unit</th>
<th>Marginal Change</th>
<th>NPV Change in Dollar</th>
<th>IRR Change</th>
<th>Elasticity</th>
</tr>
</thead>
<tbody>
<tr>
<td>L</td>
<td>Land acquisition costs</td>
<td>60,000,000.00 Dollar</td>
<td>1%</td>
<td>-1,001,079.84</td>
<td>-1.006428</td>
<td>-1.281418</td>
<td></td>
</tr>
<tr>
<td>P</td>
<td>Planning and design</td>
<td>1,150,000.00 Dollar</td>
<td>1%</td>
<td>-1,892.77</td>
<td>-1.000122</td>
<td>-1.119297</td>
<td></td>
</tr>
<tr>
<td>D</td>
<td>Development charges</td>
<td>20,904.00 Dollar</td>
<td>1%</td>
<td>-1,443.05</td>
<td>-1.000752</td>
<td>-1.734819</td>
<td></td>
</tr>
<tr>
<td>ζ</td>
<td>Other government fees</td>
<td>15%</td>
<td>1%</td>
<td>-1,254.83</td>
<td>-1.000654</td>
<td>-1.095855</td>
<td></td>
</tr>
</tbody>
</table>

The results of the sensitivity analysis show that the parameters related to project financing, including the loan repayment period, Y, equity funds, η, and the loan interest rate, i, play a key role in profitability calculations. According to Table 3, a unit increase in equity funds, η, and loan repayment period, Y, would increase the NPV of the project by CAD 2,555,422 and CAD 2,038,852, respectively. On the other hand, a quarter percent increase in the value of loan interest rate, i, causes a decrease of CAD 697,679 in the NPV of the project.

The loan interest rate, i, and the loan repayment period, Y, are the main drivers of the loan payments occurring over the entire project timeframe and serve as a major cost...
to the developer. A percent increase in the loan interest rate will significantly increase the finance costs, leading to a reduction in the NPV of the project. Moreover, the loan repayment period, $Y$, determines the timeframe that developers are required to pay back the borrowed loan. An increase in the loan repayment period will reduce the amount of each loan installment. As assumed here, developers must return the entire loan amount, even if the loan repayment period is longer than the project construction. Keeping the interest rate constant, an increase in the loan repayment period would decrease the amount of loan payments. In this case, this means that developers would repay a significant amount of the principal loan amount in a longer run and delay the loan payoff, thus increasing the NPV of the project.

The amount of equity funds can also impact the amount of loan payments. An increase in equity funds, $\eta$, will decrease the amount of loan required to cover the project costs, decreasing the project financing costs. This increase in equity funds causes a reduction in the loan payments over the entire repayment period and mitigates the cash outflow of the project, leading to an increase in the overall financial return from the project.

In addition to financing factors, the interplay between the construction rate and total number of units plays a key role in profitability calculations as it influences the distribution of costs and revenues over the duration of the project, thus impacting the overall NPV of the project. The construction rate and the total number of units determine the duration of the project:

$$T = \frac{N}{\kappa}$$  \hspace{1cm} (18)

where $T$ is the duration of the project, $N$ is the total number of units to sell, and $\kappa$ is the construction rate.

According to Equation (18), the construction rate can be defined as the total number of units built in a year. The construction rate can directly influence two main sources of project costs and revenues, namely the total construction costs and the sales schedule. On the one hand, an increase in the construction rate will increase the construction costs over the early stages of the construction phase since it increases the construction activity. An increase in the construction activity means that the construction costs are imposed on the project sooner than expected. In other words, an increase in the construction rate shifts the construction costs to the earlier stages of the project. In this case, the total units built are increased in the earlier stages of the project with a higher construction rate, and the total units built in the later stages of the construction (e.g., the last year of construction) is decreased since the project is committed to build a particular number of units and most of the units are already built in the earlier stages of the construction phase. Assuming that construction costs stays the same during the construction phase of the project, accumulation of the construction costs in the earlier stages of the project will decrease the NPV of the project since the developers have to pay the same amount of construction costs sooner than expected.

On the other hand, an increase in the construction rate will increase the sources of revenue in the early stages of the project. Since the project sales are formulated as a percentage of units constructed each year, increasing the construction rate precedes the project sales sooner than expected, increasing the sources of project revenue, and thus increasing the NPV of the project. Therefore, the impact of increasing construction costs on the NPV of the project is dependent on the trade-off between the extra costs imposed to the project by shifting the construction costs and the extra revenue added to the project by preceding the sales schedule. According to Table 4, results of the sensitivity analyses showed that in the test case presented here, a unit increase in construction rate, $\kappa$, will increase the NPV of the project by CAD 426,774, suggesting that the revenue added to the project is higher than the extra financial burden imposed by increasing the construction rate.

Moreover, according to results from Table 4, a unit increase in total number of units to sell, $N$, will increase the NPV of the project by CAD 271,021. An increase in the total number
of proposed units will increase the overall scale of the project by increasing the project costs and revenues. On the one hand, it will increase the total development costs by increasing the total construction costs, formulated per square foot, and development charges, formulated per unit, impacting the overall cash flow of the project over the construction phase. An increase in the total development costs also increases the amount of loan required to cover the project costs, increasing the loan payments over the entire project. On the other hand, an increase in the total number of proposed units will increase the project revenues by increasing the unit sales and also by increasing the developer’s fee, since the developer’s fee is formulated as a percentage of the total project costs and is collected in the last year of the project. However, since an increase in the number of proposed units does not impact the fixed costs (e.g., land acquisition costs), the revenue generated as a result of additional units would increase the NPV of the project, a reason that developers push for more height and density in most cases.

Other model parameters that play a considerable role in the profitability of the project include the broker fees, $\beta$, the project overhead costs, $M$, the annual tax rate, $\theta$, and the absorption rate, $\omega$. Both broker fees and project overhead costs are formulated as a percentage of gross sales, and thus, significantly influence the cash outflow of the project. Since the gross sales stay the same in the experiments where the broker fees, $\beta$, and project overhead, $M$, are changed, a unit increase in both broker fees and project overhead costs will equally decrease the NPV of the project by CAD 3,082,494.

Parameters such as taxes and absorption rate also directly impact the project costs and revenues. Since the taxes are formulated as a percentage of land value and considering that land value is one of the enormous costs for land acquisition, a percentage change in the tax rate, $\theta$, substantially influences the cash flow of the project in the construction period. More specifically, an increase in tax rate will increase the project costs by increasing the tax payments over the construction period, thus decreasing the NPV of the project. Moreover, absorption rates can vary based on the interaction between housing market supply and demand. An increase in the absorption rate can lead to a substantial increase in project revenues, as developers gain extra profit from the unit sales.

As another important cost that can impact the developers’ decisions, construction costs, $\tau$, here formulated as per square foot, are the main costs to the project over the construction phase. An increase in the total construction costs will add to the overall project costs, thus decreasing the overall return. However, the impact of construction costs on the NPV profitability calculations also depends on the distribution of the costs over the construction phase, adjusted by the construction rate. More specifically, spending the same amount of money on construction costs in the earlier stages of the construction phase rather than the later stages would decrease the NPV of the project.

Furthermore, the developer’s fee, $D_f$, is a one-time cost to the project that impacts the cash flow of the project on the last year. The developer’s fee is defined as a percentage of total project costs. A percentage increase in the developer’s fee will slightly increase the total development costs by increasing the developer’s salary from the project, increasing the loan amount and loan payments.

According to Table 5, the results also suggest that some of the parameters have a minor impact on the NPV of the project compared to other model parameters. These parameters include development charges, $D_c$, and planning and design costs, $P$. However, land costs, $L$, have a significant influence on profitability. All of these parameters represent a large cost/revenue influencing the cash flow of the project only once during the project’s lifetime. Development charges, land costs, and planning costs serve as initial investments for the development project, and an increase in each of these parameters will increase the costs in the first year at the beginning of the project.

4.2. Impact of Rational Expectations on Perceptions Shifts

Figures 5–7 represent various expectation mechanisms used at project initiation in 2019 to project construction costs, unit sales prices, and interest rates, respectively. In comparing
and interpreting different expectation formation models to predict market trends, it is important to consider the characteristics and limitations of each model. While some models are simple and easy to implement, they often lack accuracy due to their simplistic assumptions. For instance, models that make less use of historical data, such as the naive model, may not capture market fluctuations, cyclical patterns, or underlying factors affecting price trends. The naive model can be basically considered the “no expectation” scenario since it assumes that future prices will remain unchanged.

Figure 5. Parameterized expectation models at project initiation in 2019 to predict the market trends for construction costs during the project until 2023.

Figure 6. Parameterized expectation models at project initiation in 2019 to predict the market trends for unit sales prices during the project until 2023.
Figure 7. Parameterized expectation models at project initiation in 2019 to predict the market trends for interest rates during the project until 2023.

The IRR estimated for our hypothetical project is demonstrated in Figure 8, considering the same boundedly rational expectation mechanisms are used at project initiation in 2019 to project construction costs, unit sales prices, and interest rates. In the examples provided in Figure 8, the IRR calculated based on the actual data, shown in black bar, represents the IRR over the lifetime of the development project given that developers could perfectly predict market trends. Therefore, this value can be used as a gauge to evaluate how each of the incorporated expectation models replicates or deviates from the actual IRR values for the project.

Figure 8. Estimated IRR for the development project when considering the same expectation mechanisms to project construction costs, unit sales prices, and loan interest rate.

Results highlight that alternative expectation mechanisms for each of the primary factors influencing the profitability of the development project can alter the estimated IRR
value. According to Figure 8, the IRR for the development project is estimated to be 12.6% using perfect expectation of construction costs, unit sales prices, and interest rates, while use of various models of expectation formations to project these trends leads to various IRR estimations at project initiation. The results suggest that boundedly rational developers who consider a MARR of 10% (the lower limit of IRR for project initiation according to key developer informants) would probably undertake the project in most cases, since the project meets their financial profitability criteria based on their perception of market trends.

As the project progresses, developers update their perception of costs and revenues based on new observation of market trends. By actively monitoring market trends, incorporating new data, and adapting their expectations, developers ensure that their financial projections remain relevant and reflective of the current market realities. This continuous updating process allows them to make more informed decisions throughout the development process and respond effectively to changing market dynamics.

To explore how developers’ expectations of market trends during the project timeline can cause alterations in the projects, we estimated the project IRR when boundedly rational expectations are used to project construction costs, unit sales prices, and interest rates, at different times during the project. The results of this analysis are shown in Figure 9. In performing this analysis, we used the historical data prior to the decision time to reparameterize the expectation models using the same methods described in Section 3.4. This means that developers update their perceptions of market trends according to their new observations. For instance, when estimating the IRR a year after project initiation, developers use the historical data observed during the first year of the project to update their perceptions of trends for construction costs, unit sales prices, and interest rates for the rest of the project timeline.

As shown in Figure 9, use of boundedly rational expectation mechanisms to project construction costs, unit sales prices, and interest rates can lead to significant variation in the estimated IRR for the project over the project timeline. Although the initial estimation of IRR in 2019 may suggest undertaking the project, the adaptively estimated IRR for the project can significantly drop in early 2020, according to the observed decreasing trends in unit sales prices and continuously increasing construction costs. According to Figure 9, after one year of project initiation in April 2020, expectation models such as the naive, the mean, the cycle, and the weak-trend estimate the project IRR at −1.63%, 1.62%, 3.42%, and

![Figure 9. Estimated IRR for the project at different times during the project when the same boundedly rational expectation mechanisms are used to project construction costs, unit sales prices, and interest rates.](image-url)
−1.21%, respectively. This significant drop in the estimated IRR can put the project on pause, considering that the project is no longer expected to achieve the initially estimated financial return. These results also align with historical project cancellation trends, as shown in Figure 2, where there is an increase in the total number of project cancellations in 2020.

As time proceeds, two spikes in the project’s IRR are estimated in late 2020 and late 2021, due to decreasing interest rates and increasing unit sales prices in this period. Although the increase in construction costs has accelerated in late 2021, the results indicated that the significant increase in unit sales price during the same period could cover the extra costs imposed on the project and justify the financial feasibility of the project at this time. Observing these market trends can encourage boundedly rational developers to continue on the initiated development, hoping to achieve even higher financial returns than their initial estimations at the project start. For instance, the IRR is estimated at 33.94%, 26.55%, 33.08%, 52.01%, and 46.02% using the naive, the mean, the projection, the re-scale, and the weak-trend models, respectively. However, moving forward in the project, the estimated IRR for the project can significantly drop in 2022 and early 2023 to values below 8%, according to the rising interest rates, decreasing unit sales prices, and increasing construction costs at this period. Therefore, re-examining the financial feasibility of the project at this period can inform what adjustments in the builder’s behaviour are necessary to avoid further financial losses.

The results also indicate that adaptive expectation models that capture shifts in the market with higher accuracy can more precisely estimate the IRR values for the project. According to Figure 9, while using the naive, the mean, the cycle, and the re-scale models of expectation leads to higher variations in the IRR estimation during the project, other models that adapt to changing trends in data, such as the projection and the adaptive model, can lead to more realistic estimations of IRR during the project timeline, meaning that these models can potentially help developers make more accurate decisions. For instance, the re-scale, the weak-trend, and the anchor and adjustment models estimate the IRR to be 47.23%, 5.9%, and −1.0% at project initiation, while the projection and the adaptive models estimate the IRR to be 16.47% and 20.34%, which are closer to the actual IRR of 12.6%. Furthermore, the GARCH model failed to capture the major shift in construction cost trends and mostly overestimated the housing prices, although it captures more accurately the volatility in prices compared to other boundedly rational expectation models. The use of the GARCH model to project construction costs, unit prices, and interest rates led to an overestimation of the expected IRR by 40.3%, as the model significantly overestimated future housing prices. According to Figure 5, the GARCH model failed to capture the major shift in construction costs trends in 2020. Moreover, according to Figure 6, it mostly overestimated the housing prices since 2021, although it can more accurately capture the volatility in prices compared to other boundedly rational expectation models. However, according to Figure 9, the GARCH model can still represent the shifts in financial perceptions of housing market developers. As the project proceeds in time, recalculating the financial projections using the GARCH model for construction costs, housing prices, and interest rates, as well as also reassessing the financial viability of the projects, led to variation in the estimated IRR for the project.

5. Discussion and Conclusions

Rapid shifts in housing development costs, combined with interest rate increases resulting from recent inflationary trends in consumption goods, have significantly impacted the viability of development projects in the past few years by introducing more risks to developers’ supply decisions. Cancellation trends in condo and rental development projects can exacerbate Canada’s already severe housing shortage and further intensify its affordability crunch. Our study helps to unpack the underlying factors behind development decisions through the lens of housing market developers and understand the impact of
housing market shifts on profitability perceptions and supply decisions, thus shedding light on potential solutions to our housing supply challenges.

Through formulating a sample high-rise condo proforma, we explored the primary factors influencing the profitability perceptions of housing market developers. Results highlighted that factors related to project financing and loan terms (e.g., equity funds and interest rates), property taxes, and also factors that involve a degree of uncertainty, such as construction costs and unit sales prices, can substantially influence the project revenues and costs, making them important factors in development decisions. Real-world trends in these factors have shown unexpected volatility, constituting an unexpected shock to the housing supply system.

We also explored how boundedly rational expectations of market trends can alter profitability perceptions of private developers when primary market trends (e.g., construction costs, housing prices, and interest rates) experience significant shifts, which can cause alterations in development project during the project timeline. The results suggest that boundedly rational behaviours can fail to accurately capture market trends in volatile market conditions and sometimes lead to overly optimistic projections (e.g., re-scale, trend-following, and projection models) in forecasting market trends. When relying on boundedly rational expectations, updating the profitability perceptions after project initiation can cause striking changes in the expected profit margin in unstable market conditions. This change in profitability perceptions can explain the cascade of project cancellations in the Toronto housing market, as a result of major shifts in construction costs and interest rates in the past few years.

Given the critical impact of developers on the housing market supply, paying close attention to developers’ profitability perceptions is crucial for effective policy-making in the housing market. Our findings imply that planners require a thorough understanding of development decisions and developers’ expectations, especially in volatile market conditions, to help them understand how they might best influence developer activity. This understanding can help planners encourage development decisions that align with both profit incentives and affordable housing goals through policies that can strike a balance between market dynamics and the needs of the community, such as inclusionary zoning (August and Tolfo 2018; Schuetz and Meltzer 2012) and density bonuses (Ellery 2019; Mah 2022). Our identification of high-impact factors for development profitability underscores the critical role that planners can play in shaping the financial viability of projects, when they have the agency to do so statutorily. By having a comprehensive understanding of these primary factors in development decisions, planners can transparently understand and communicate the impact of their proposed policies on potential development profitability.

Our model’s implications can vary considerably across different regions, contingent upon the prevailing policy context and market conditions. In regions marked by heightened volatility, such as those experiencing rapid price fluctuations or regulatory shifts, policy responses that directly mitigate changes in project profitability, such as the Canadian government’s recent decision to not charge sales tax for housing construction, can re-stabilize volatile markets, smoothing the housing supply (Balintec 2023). Yet, care needs to be taken to ensure that policies supports are cost-feasible for governments at all levels. In less volatile financial environments, delays in development approvals caused by planning processes, such as negotiations with city planners regarding density bonuses and inclusionary requirements, can increase uncertainty and risk for developers and their investors, potentially affecting project timelines and financial projections. Opaque zoning constraints and requirements for applications of zoning amendments can further increase uncertainty. This view supports a mandate for policymakers to formulate policies that create a more predictable environment for developers, which can contribute to a more stable and attractive investment landscape that facilitates housing supply.

While not explored in detail in this paper, the MARR reflects the perceived risk premia of developers and their investors. Feedback from local developers highlights that developers often estimate the MARR using common sense achieved through their
experience from different developments, analyzing comparable projects and risk-free rates of return. It also suggests that lenders calculate risk premiums in their investment decisions to account for the risks and uncertainties associated with their decisions. Volatile market conditions often bring heightened uncertainty and unpredictability into the financial calculation and profitability estimations. Investors factor in risk premiums to mitigate potential losses stemming from unforeseen market fluctuations. These premiums could act as a financial cushion, helping to absorb losses and maintain a healthy financial position even when significant shifts impact the market (Dorofeenko et al. 2010; Trouw et al. 2020). However, a persistent increase in uncertainty and the corresponding risk premia can make a project appear less financially appealing and increase market volatility.

In modelling the financial decisions of developers, the MARR is exogenous to our model of financial profitability of potential developments, and its value is selected based input from local developers. Although understanding and modelling the effect of risk premiums on the financial decisions of lenders and developers is an important measure in investment decisions, it is beyond the focus of this paper. Nevertheless, the question of how developers and lenders formulate risk premia is an important area for future research, and would facilitate sensitivity analysis of factors that impact risk premia, such as macroeconomic volatility, construction cost fluctuations, and financial market uncertainty.

The proposed model of proforma can facilitate the incorporation of relevant uncertainties into the analysis of the profitability of potential development projects. These uncertainties stem from a lack of knowledge, especially about several input parameters of the proforma (e.g., loan interest rate and construction costs). Accounting for these uncertainties facilitates the analysis of all potential credible outcomes regarding the development project. As shown in Appendix C, incorporating relevant uncertainties can increase confidence in the model’s outputs and provide insights into the impact of uncertainties on the development decisions for developers.

Our study is motivated by a critical need for enhanced models that can better capture the real-world nuances and underlying dynamics of housing supply, which can improve the current projections of housing prices and land supply. As housing markets continually evolve, more studies are needed to improve the current projection and traditional models of land and housing prices to provide adequate capabilities that can support more reliable and evidence-based policymaking. The models presented in this study can improve the realism of actor decision models in micro-simulations/Agent-Based Models (ABMs) of land and housing markets. The review of the literature showed that few studies have incorporated price expectations into the behaviour of actors involved in land and housing markets. By more closely linking the modelled behaviours of the market actors to their real-world behaviours, the simulation dynamics will link more closely to real-world dynamics, ideally improving the simulation platforms (Sterman 2000; Valaei Sharif et al. 2023). To facilitate the replication of the proposed models, we produced Python code blocks that model the proforma and alternative expectation formation strategies, which could be utilized by any modelling team striving to represent expectation formation in agent-based market models (please refer to the Supplementary Materials for the model code). The flexible and modular design of the model facilitates the modification of the assumptions and allows for extending the model to include further details about the development projects and strategies to represent other expectation formation models.

While various expectation mechanisms representing the behaviour of housing market developers regarding estimating the market trends can lead to different outputs, the results imply that adaptive decision rules can more precisely capture the volatility and thus, predict the future trends with higher accuracy. On the other hand, models such as the naïve, re-scale, trend-following, and anchor and adjustment expectations lack predictive accuracy, since they make less use of past data, leading to higher variations in predictions. The difference in the accuracy of expectation mechanisms raises a need for understanding the actual expectation formation of developers to unravel their development decisions. Understanding the actual behaviour of developers through interviews or experiments with
private developers can more closely explore their decisions in unstable market conditions and help explain market volatility. Future studies can incorporate various developers’ decision strategies, drawing comparisons between different strategies and examining how actual developers’ decision strategies align with different boundedly rational models of developer decisions introduced in the literature.


Funding: This research was funded by Mitacs Accelerate Award FR85015, Canada Mortgage and Housing Corporation, and SSHRC grant 890-2021-0021.


Acknowledgments: We thank all participating colleagues: Steven Lamothe and Bert Pereboom from the Canada Mortgage and Housing Corporation, Arezoo Besharati from UrbanSim, Region of Waterloo area developers, and 2022 Social Simulation Conference participants for their helpful comments and feedback, without which this research would not have been possible. The views expressed are solely the authors.

Conflicts of Interest: The authors declare no conflict of interest.

Abbreviations
The following abbreviations are used in this manuscript:

<table>
<thead>
<tr>
<th>Abbreviation</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>IRR</td>
<td>Internal Rate of Return</td>
</tr>
<tr>
<td>NPV</td>
<td>Net Present Value</td>
</tr>
<tr>
<td>TDC</td>
<td>Total Development Costs</td>
</tr>
<tr>
<td>TPC</td>
<td>Total Project Costs</td>
</tr>
</tbody>
</table>

Appendix A. Formulation of Partial Derivatives of NPV Function

Using the equations formulated in Section 2, in this Appendix, we report an analytical analysis of the partial derivatives of the NPV in the proposed sales proforma with respect to several model parameters to account for the influence of different factors on the profitability analysis.

The results of this analysis showed that the partial derivative equation of the NPV with respect to several parameters does not represent the parameter itself, implying that the NPV of the project is linearly linked to these model parameters. For instance, the partial derivative of the NPV with respect to planning costs, $L$, is formulated as

$$\frac{dNPV}{dL} = -D_f(\rho + 1)^{-T} + \eta \left(1 - D_f\right)(\rho + 1)^{-T} + \sum_{i=1}^{T} \left( -i \left(1 - D_f\right)(1 - \eta)(i + 1)^Y \right) \left( \frac{i + Y}{i + 1} - \theta \right) - 1$$  \hspace{1cm} (A1)
According to Equation (A1), the sensitivity of the NPV with respect to \( L \) is linearly associated with parameters such as developer’s fees, \( D_f \), and equity funds, \( \eta \). This means that an increase in these parameters directly increases the sensitivity of the NPV with regard to \( P \). On the other hand, the loan repayment period, \( Y \), is represented in a exponentially decreasing relationship in Equation (A1), implying an increase in \( Y \) causes an exponential increase in \( \frac{\partial NPV}{\partial L} \). Moreover, the interest rate, \( i \), is in a power relationship with the derivative of NPV with respect to land costs, suggesting that an increase in \( i \) causes an accelerated decrease in \( \frac{\partial NPV}{\partial L} \).

As other examples of parameters that are linearly associated with the NPV calculation, the partial derivatives of the NPV with respect to sales price, \( \pi \), and absorption rate, \( \omega \), are presented in Equations (A2) and (A3), respectively.

\[
\frac{\partial NPV}{\partial \pi} = \sum_{t=1}^{T} \kappa \omega (\beta + 1) \tag{A2}
\]

\[
\frac{\partial NPV}{\partial \omega} = \sum_{t=1}^{T} \kappa \pi (\beta + 1) \tag{A3}
\]

Considering construction rate, \( \kappa \), unit sales price, \( \pi \), absorption rate, \( \omega \), and broker fees, \( \beta \), to be positive, partial derivatives of NPV with respect to sales price, \( \pi \), and absorption rate, \( \omega \), always have a positive value and have a linear relationship with construction rate, \( \kappa \), and broker fees, \( \beta \), as the main drivers of gross sales revenue, suggesting that an increase in any of these variables can cause a linear increase in the derivatives of the NPV. Moreover, the derivative of the NPV with respect to construction rate, \( \kappa \), is formulated as

\[
\frac{\partial NPV}{\partial \kappa} = \sum_{t=1}^{T} (-A_a \tau + \omega \pi (\beta + 1)) \tag{A4}
\]

where it is linearly impacted by parameters such as the average unit area, \( A_a \), construction costs, \( \tau \), absorption rate, \( \omega \), unit sales price, \( \pi \), and broker fees, \( \beta \). According to Equation (A4), \( \frac{\partial NPV}{\partial \kappa} \) is positively impacted by the unit sales prices and negatively impacted by the construction costs.

The partial derivative of the NPV with respect to construction costs, \( \tau \), is represented as

\[
\frac{\partial NPV}{\partial \tau} = -A_a D_f N (\rho + 1)^{-T} + A_a N \eta \left(1 - D_f\right) (\rho + 1)^{-T} + \sum_{t=1}^{T} \left(-\frac{A_a N i \left(1 - D_f\right) (\rho + 1)^{Y}}{(i + 1)^{Y} - 1} - A_a \kappa\right) \tag{A5}
\]

According to Equation (A5), the derivative of the NPV with respect to construction costs is linearly impacted by parameters such as average unit area, \( A_a \), developer’s fee, \( D_f \), total units to sell, \( N \), equity funds, \( \eta \), and construction rate, \( \kappa \). Similar to land costs, the derivative of the NPV with respect to construction costs is exponentially associated with the repayment period, \( Y \), implying an increase in \( Y \) causes an exponential increase in \( \frac{\partial NPV}{\partial \tau} \). It is also linked to the loan interest rate, \( i \), in a power relationship, where an increase in \( i \) would cause an accelerated decrease in \( \frac{\partial NPV}{\partial \tau} \).

Another model parameters that play a key role in sensitivity analyses of the NPV is the loan interest rate. Partial derivative of the NPV with respect to \( i \) can be formulated as
\[
\frac{\partial \text{NPV}}{\partial i} = \sum_{t=1}^{T} \frac{Y_t(1 - D_f)(1 - \eta)(i + 1)^Y N \left( \frac{1 + \tau \kappa + \zeta + E + L + P}{1 + \kappa (i + 1)^Y} \right)}{(i + 1) (i + 1)^Y - 1} \]

\[
\text{NPV} = \sum_{t=1}^{T} \frac{Y_t(1 - D_f)(1 - \eta)(i + 1)^Y (A_n \tau + D_c N \left( \frac{1 + \tau \kappa + \zeta + E + L + P}{1 + \kappa (i + 1)^Y} \right))}{(i + 1) (i + 1)^Y - 1} \]

Parameters such as equity funds, \(\eta\), developer’s fee, \(D_f\), average unit area, \(A_n\), total units to sell, \(N\), construction costs, \(\tau\), construction rate, \(\kappa\), development charges, \(D_c\), and initial investments (e.g., planning costs and land costs) enter linearly in Equation (A6), suggesting that partial derivative of the NPV with respect to interest rate is linearly associated with these parameters. However, interest rate, \(i\), enters Equation (A6) in a power relationship, where a change in \(i\) causes an escalated change in \(\frac{\partial \text{NPV}}{\partial i}\).

More generally, the formulation of partial derivatives showed that all partial derivative equations are non-linearly linked to the loan interest rate, \(i\), and loan repayment period, \(Y\). This non-linearity highlights the importance of these parameters in the profitability calculations as a minor change in the value of these parameters can significantly impact the sensitivity of the NPV to all other model parameters due to the escalated non-linear effect.

Although parameters such as equity funds, \(\eta\), construction rate, \(\kappa\), and absorption rate, \(\omega\), are linearly entered in the partial derivative equations, they influence the primary source of project costs and revenues, including building expenses and all the sales, influencing the cash flow over the entire project. Therefore, a change in the value of these parameters can impact the project’s revenues over the construction stage, influencing the expected profitability of the development project. Therefore, it is expected that these variables play a key role in the project’s profitability analysis.

**Appendix B. Initial Experiments with Models of Expectation Formation**

When looking into the past data to estimate future trends, the length and composition of the observation period can significantly impact the accuracy and reliability of the forecast results. To evaluate the impact of having different observation periods on the prediction accuracy and to estimate the suitable observation period to capture the overall trends in data, we conducted initial experiments with different observation periods for the expectation formation models that rely on historical data for a variable time period (the observation window), including the mean model, the cycle model, the projection model, and the re-scale model, as summarized in Table A1. For each of the models, we experimented with two, four, and twelve quarters of data as the observation window to compare the effect of considering a short observations period and relatively longer periods for forecasting future trends. For the re-scale model, we estimated the re-scale factor, \(g\), as the average value of the re-scale factors corresponding to each quarter in the observation period.

The results of initial experiments with different observation periods for various models of expectation for construction costs, unit sales prices, and loan interest rates are demonstrated in Figures A1, A2 and A3, respectively. Based on the comparison between the Mean Squared Errors (MSE) for various expectation models, reported in Table A2, findings suggested that a longer observation period of three years can capture a more comprehensive range of market conditions and offer a better understanding of the market trends and potential variations, potentially capturing significant cyclical patterns. However, due to the rapid changes in the data during the prediction period (i.e., 2019 to 2023), a shorter observation period actually yielded higher accuracy in predictions in most cases.
Table A1. Initial scenarios conducted with different expectation models at project initiation in 2019 to explore the impact of observation window on the model accuracy.

<table>
<thead>
<tr>
<th>Factor</th>
<th>Mean Model</th>
<th>Cycle Model</th>
<th>Projection Model</th>
<th>Re-Scale Model</th>
</tr>
</thead>
<tbody>
<tr>
<td>Construction costs</td>
<td>12 quarters $(x = 12)$</td>
<td>12 quarters $(x = 32)$</td>
<td>12 quarters $(x = 12)$</td>
<td>12 quarters $(g = 1.0104)$</td>
</tr>
<tr>
<td></td>
<td>4 quarters $(x = 4)$</td>
<td>4 quarters $(x = 16)$</td>
<td>4 quarters $(x = 4)$</td>
<td>4 quarters $(g = 1.0058)$</td>
</tr>
<tr>
<td></td>
<td>2 quarters $(x = 4)$</td>
<td>2 quarters $(x = 16)$</td>
<td>2 quarters $(x = 4)$</td>
<td>2 quarters $(g = 1.0042)$</td>
</tr>
<tr>
<td>Unit sales price</td>
<td>12 quarters $(x = 12)$</td>
<td>12 quarters $(x = 12)$</td>
<td>12 quarters $(x = 12)$</td>
<td>12 quarters $(g = 1.0324)$</td>
</tr>
<tr>
<td></td>
<td>4 quarters $(x = 4)$</td>
<td>4 quarters $(x = 4)$</td>
<td>4 quarters $(x = 4)$</td>
<td>4 quarters $(g = 1.0871)$</td>
</tr>
<tr>
<td></td>
<td>2 quarters $(x = 4)$</td>
<td>2 quarters $(x = 4)$</td>
<td>2 quarters $(x = 4)$</td>
<td>2 quarters $(g = 1.0943)$</td>
</tr>
<tr>
<td>Interest rate</td>
<td>36 months $(x = 12)$</td>
<td>36 months $(x = 12)$</td>
<td>36 months $(x = 12)$</td>
<td>36 months $(g = 1.0117)$</td>
</tr>
<tr>
<td></td>
<td>12 months $(x = 4)$</td>
<td>12 months $(x = 4)$</td>
<td>12 months $(x = 4)$</td>
<td>12 months $(g = 1.0124)$</td>
</tr>
<tr>
<td></td>
<td>6 months $(x = 4)$</td>
<td>6 months $(x = 4)$</td>
<td>6 months $(x = 4)$</td>
<td>6 months $(g = 1.0000)$</td>
</tr>
</tbody>
</table>

Table A2. The estimated Mean Squared Errors (MSE) for various observation periods when different expectation models are used to project market trends.

<table>
<thead>
<tr>
<th>Factor</th>
<th>Mean</th>
<th>Cycle</th>
<th>Projection</th>
<th>Re-Scale</th>
<th>Adaptive</th>
<th>Weak-Trend</th>
<th>Strong-Trend</th>
<th>Anchor and Adjustments</th>
</tr>
</thead>
<tbody>
<tr>
<td>Construction costs</td>
<td>2 quarters</td>
<td>7720.7</td>
<td>7763.0</td>
<td>4185.3</td>
<td>4966.8</td>
<td>7927.5</td>
<td>7405.6</td>
<td>35693.3</td>
</tr>
<tr>
<td></td>
<td>4 quarters</td>
<td>7821.4</td>
<td>7617.1</td>
<td>5850.6</td>
<td>4991.4</td>
<td>7955.5</td>
<td>7405.6</td>
<td>35693.3</td>
</tr>
<tr>
<td></td>
<td>12 quarters</td>
<td>8973.2</td>
<td>10689.3</td>
<td>10349.4</td>
<td>3261.0</td>
<td>7993.1</td>
<td>7405.6</td>
<td>35693.3</td>
</tr>
<tr>
<td>Unit sales price $(\times 10^3)$</td>
<td>2 quarters</td>
<td>1.22</td>
<td>1.21</td>
<td>39.1</td>
<td>245.0</td>
<td>0.874</td>
<td>2.23</td>
<td>91.4</td>
</tr>
<tr>
<td></td>
<td>4 quarters</td>
<td>2.18</td>
<td>4.38</td>
<td>32.9</td>
<td>186.0</td>
<td>1.88</td>
<td>2.23</td>
<td>91.4</td>
</tr>
<tr>
<td></td>
<td>12 quarters</td>
<td>6.18</td>
<td>10.0</td>
<td>2.96</td>
<td>8.70</td>
<td>1.95</td>
<td>2.23</td>
<td>91.4</td>
</tr>
<tr>
<td>Interest rate $(\times 10^{-1})$</td>
<td>6 months</td>
<td>2.524</td>
<td>2.524</td>
<td>2.524</td>
<td>2.524</td>
<td>2.524</td>
<td>2.524</td>
<td>2.524</td>
</tr>
<tr>
<td></td>
<td>12 months</td>
<td>2.514</td>
<td>2.477</td>
<td>2.552</td>
<td>4.189</td>
<td>2.524</td>
<td>2.524</td>
<td>2.524</td>
</tr>
<tr>
<td></td>
<td>36 months</td>
<td>2.526</td>
<td>3.937</td>
<td>4.359</td>
<td>3.944</td>
<td>2.524</td>
<td>2.524</td>
<td>2.524</td>
</tr>
</tbody>
</table>

Figure A1. Comparison between the expectation of construction costs with different observation window for (a) mean model, (b) cycle model, (c) projection model, and (d) re-scale model. The models predict the trends at project initiation in July 2019, with no data assimilation or updating.
Figure A2. Comparison between the expectation of market sales price with different observation window for (a) mean model, (b) cycle model, (c) projection model, and (d) re-scale model. The models predict the trends at project initiation in July 2019, with no data assimilation or updating.

Figure A3. Comparison between the expectation of interest rates with different observation window for (a) mean model, (b) cycle model, (c) projection model, and (d) re-scale model. The models predict the trends at project initiation in July 2019, with no data assimilation or updating.
Appendix C. Joint Impact of Shifts in Sales Price and Interest Rate

As discussed in the paper, changes in interest rates impact both the cost side (in terms of finance costs) and the revenue side (in terms of drops in unit sales). Our proforma analysis does not explicitly consider that developers might anticipate that an increase in interest rates will lower sales prices. However, it is helpful to understand if this scenario (increase in finance interest rates combined with lower sales prices) is seen in our data. To examine the model behaviour under the uncertainty associated with unit sales prices and interest rates, we performed joint numerical sensitivity analysis with these model parameters. The sensitivity analysis evaluates whether the model outcomes (e.g., the IRR estimated for the project) vary significantly when the model assumptions (e.g., unit sales prices and loan interest rates) are varied over their plausible range of uncertainty (Kashani et al. 2022; Sterman 2000; Valaei Sharif et al. 2022). The results of the joint numerical sensitivity analysis of the IRR with respect to unit sales price, $\pi$, and interest rate, $i$, are presented in Figure A4, given that other model parameters remain constant during the project timeline.

![Figure A4. Results of joint numerical sensitivity analysis of IRR with respect to unit sales price ($\pi$) and loan interest rate ($i$), given construction costs remain constant during the project. The circle marks the IRR corresponding to the baseline pair values for interest rates and unit sales price at project initiation in July 2019.](image)

The results of this analysis highlight that while changing one of the two parameters can alter the estimated IRR for the project, considering the joint effect of change in both parameters can lead to more significant variations in the profitability perceptions. For instance, as demonstrated in Figure A4, the project is estimated to have an IRR of 12% using a naive expectation of construction costs at a unit sales price of CAD 1,010,000 and an interest rate of 3.75%. Assuming that unit sales prices remain unchanged while interest rates increase to 4.75%, the estimated IRR for the project will drop to 10%; however, considering a 5% depression in housing prices.

As a result of a 1% increase in interest rates, the estimated IRR for the project would decrease to 2.4%. Meanwhile, an IRR of 10% might still be justifiable to undertake the project as it generates more revenues than costs, considering that the joint effect of increasing interest rates and depressing housing prices leads to a significant drop in the expected IRR for the project, making it unattractive for developers.
We also performed a Monte-Carlo simulation to evaluate the impact of uncertainty in interest rates and unit sales prices on the profitability calculations by sampling from randomly distributed variables assigned to these model inputs. Because we did not have access to prior data for these parameters, they are assumed to be uniformly distributed in their plausible range of values between a minimum and a maximum threshold, as shown in Table A3. The simulations are performed in three different scenarios where a naive model, a projection model, or a perfect model is used to represent developers’ expectations of construction costs. A number of 21,742 sampling iterations were carried out for each scenario to achieve an absolute error lower than 1% of the average initial results at a 95% confidence level. The number of simulations required to characterize the possible scenarios and estimate the outcomes at the desired level of accuracy can be determined based on the approach proposed by Banks (Banks 2005).

Table A3. Distribution of model parameters for Monte-Carlo simulations.

<table>
<thead>
<tr>
<th>Notation</th>
<th>Description</th>
<th>Distribution</th>
<th>Min Value</th>
<th>Max Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>(i)</td>
<td>Loan interest rate</td>
<td>Uniform</td>
<td>0.75%</td>
<td>6.75%</td>
</tr>
<tr>
<td>(\pi)</td>
<td>Unit sales price</td>
<td>Uniform</td>
<td>CAD 860,000</td>
<td>CAD 1,160,000</td>
</tr>
</tbody>
</table>

The results of the Monte-Carlo simulations are presented in Figure A5. These findings underscore the critical role that uncertainty plays in calculating the financial profitability and shaping the volatility of output variables. Particularly, when the uncertainty in interest rates and unit sales prices are considered in profitability calculations, we observed a range of wide range of values for the IRR. For the scenario with a naive model of expectation, the IRR ranges between −1% to 39%, with an average of 14.5%. This outcome emphasizes how external factors, such as fluctuating interest rates and market prices, can significantly influence the behaviour of the system under investigation.

![Figure A5](image)

Figure A5. Results of Monte-Carlo simulations for the distribution of IRR when loan interest rates \((i)\) and unit sales prices \((\pi)\) are considered as randomly distributed inputs to the model.

The results also showed that the utilization of naive and projection models to capture these expectation dynamics tends to result in an overestimation of the Internal Rate of Return (IRR) compared to a scenario with perfect expectations. This overestimation can have
profound implications for making development decisions, when developers or investors rely on simplistic or overly optimistic expectation models, they may misjudge the actual financial feasibility of projects, potentially leading to suboptimal investment decisions. This, in turn, emphasizes the importance of employing more realistic and adaptive expectation formation strategies in situations where market volatility and uncertainty are prevalent.

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