Article

Design and Analysis of Trench-Assisted Low-Bending-Loss Large-Mode-Field-Area Multi-Core Fiber with an Air Hole

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Abstract: In this paper, a trench-assisted low-bending-loss large-mode-field-area multi-core fiber with air hole is proposed, which can achieve dual-mode transmission. The influence of structural parameters on fiber performance is analyzed systematically, and the structure of the trench, with a lower refractive index than the cladding, is also analyzed and optimized. By adjusting the structural parameters, the effective mode field area of the fundamental mode can reach 2003.24 μm2 at 1550 nm, and when the bending radius is 1 cm, the bending loss is 2.57 × 10⁻³ dB/m. The practical implementation of the proposed fiber is feasible using existing fabrication technology and is applicable to the transmission of large-capacity optical communication systems and high-power lasers.

Keywords: dual-mode; low-bending-loss; trench-assisted; large-mode-field-area; multi-core fiber

1. Introduction

The advent of the “Internet +” era and the 5G era have put forward higher requirements for the high speed and high bandwidth of optical communication networks. Ultra-high-speed, large-capacity, and ultra-long-distance transmission has become the future trend. The conventional single-mode single-core fiber (SM-SCF) is gradually approaching its 100 Tb/s transmission limit due to the limitation of the nonlinear effect [1]. The rapid development of communication technologies such as wavelength division multiplexing (WDM) and polarization multiplexing (PDM) enables mode division multiplexing (MDM) based on few-mode fibers to be used to increase channel transmission capacity [2]. Increasing the mode field area can reduce the nonlinear effect of the fiber, but it will also increase the number of transmittable modes in the fiber and bring about bending loss. Therefore, low-bending loss and large-mode area few-mode fibers have important research significance in high-power optical communication devices [3].

In recent years, fiber lasers have developed rapidly. In order to overcome the limitation of fiber laser power improvements such as the fiber nonlinear effect and fiber damage, the method of increasing the mode field area can be used to overcome the nonlinear effect. The strong coupling multi-core fiber (MCF) increases the mode field area (MFA) of the fiber by introducing the lateral coupling of the core, thereby reducing the nonlinear effect. Therefore, it is often used in fiber lasers and amplifiers [4]. But multi-core fibers have a higher bending loss [5]. However, the reduction of the bending loss (BL) is conducive to improving the stability and output efficiency of the fiber laser source [6,7]. Adding air holes and a trench in cladding can effectively reduce the bending loss.

Commonly used fiber structures for achieving a large mode field and low bending loss include: photonic crystal fiber, trench-assisted fiber, and multi-core fiber. The photonic crystal fiber has a large mode field area and good bending resistance. However, the structure is complex and asymmetric, and the technological level is high and welding difficulties. Usually, the effective mode field area can reach 794 μm², and the bending
loss is 0.064 dB/m, when the bending radius is 15 cm [8]. The trench-assisted fiber has good bending resistance. However, due to process limitations, the width and depth of the submerged layer will be limited. The fiber can not only support ultra-low bending loss (0.052 dB/turn when bending radius R = 5 mm), but also support an effective mode field area of up to 260 um² at a working wavelength of 1.55 um [9,10].

Multi-core optical fiber has the characteristics of a symmetrical structure distribution, simple design, flexible parameter adjustment, and large mode field area. However, large mode field multi-core optical fiber often has a higher bending loss. The fiber can generally transmit with a low bending loss (less than 1.0 dB/m when the bending radius R = 0.34 m), and the effective area is as high as 1331 um² [11–15].

There is a mutually restrictive relationship between the bending loss of the optical fiber and the mode field diameter (mode field area). The smaller the mode field diameter, the better the light can be confined, thus reducing the bending loss of the fiber. But if the mode field diameter of the fiber is too small, there will be serious nonlinear effects under high power conditions [16]. Therefore, the two must be considered comprehensively.

A trench-assisted low-bending-loss large-mode-field-area multi-core fiber (TA-LBL-LMFA MCF) with an air hole structure is proposed in this paper that can realize dual-mode transmission. The MFA of the fundamental mode of the fiber can reach 2003.24 um. When the bending radius is 1 cm, BL can be as low as \(2.57 \times 10^{-3}\) dB/m. Using the existing fabrication techniques, the practical implementation of the proposed fiber is feasible.

2. Optical Fiber Structure and Theoretical Analysis

The fiber structure is shown in Figure 1. The yellow part is the central core and the gray part is the silica cladding. The blue part is a trench with a lower refractive index (RI) than the cladding. This structure adds 10 cores (green part) to the traditional hexagonal 19-core optical fiber structure (pink part), removes the cores on both sides of the 19-core optical fiber, and adds air holes and a trench in the cladding. The green part, yellow part, and pink part constitute the core area.

![Figure 1. Schematic diagram of optical fiber cross section.](image-url)
structural parameters are composed of seven parameters: \( \Lambda, d, \Delta n, d_{\text{center}}, \Delta n_{\text{center}}, W_{\text{trench}}, \) and \( L_{\text{trench}} \).

This paper is mainly based on the finite element method (FEM) software to analyze the fiber structure [17].

The refractive index of the beam propagating in a specific mode changes with the wavelength and the geometric structure of the waveguide. This is called the effective refractive index \( n_{\text{eff}} \) of the mode. The conduction of specific mode in optical fiber needs to satisfy the conduction mode condition of the optical waveguide theory: \( n_{\text{eff}} < n_{\text{clad}} < n_{\text{core}} \). Otherwise, the mode will be cut off and does not exist in the fiber. The effective refractive index \( n_{\text{eff}} \) calculation formula can be expressed as [18]:

\[
n_{\text{eff}} = \text{Re}\left(\frac{\beta}{k_0}\right). \tag{1}
\]

Among these figures, \( \beta \) is the propagation constant, the \( \text{Re} \) is the real part of the whole, the wave number in vacuum is \( k_0 = \frac{2\pi}{\lambda} \), and \( \lambda \) is the working wavelength.

The electromagnetic field of each mode along the cross section of the fiber is called the mode field. An optical fiber with a large mode field area can suppress the nonlinear effect in the optical fiber. The effective mode field area \( A_{\text{eff}} \) can be expressed as [19]:

\[
A_{\text{eff}} = \frac{\int (EE^*dA)^2}{\int (EE^{*2})dA} \tag{2}
\]

where \( E \) represents the electric field of the mode, and \( E^* \) represents the conjugate complex number of the electric field of the mode.

When the fiber is bent in the positive direction of the x-axis, and the equivalent refractive index distribution of the fiber cross-section is [20]:

\[
n(x, y) = n_0(x, y) \sqrt{1 + \frac{2x}{R_{\text{eff}}}}. \tag{3}
\]

Among them, \( n(x, y) \) is the equivalent refractive index of the fiber after bending, and \( n_0(x, y) \) is the initial refractive index of the fiber. \( R \) is the bending radius of the optical fiber along the positive x-axis. When the elastic optical correction factor is introduced, the equivalent bending radius \( R_{\text{eff}} = 1.28R \).

The calculation formula of fiber bending loss \( \alpha \) can be expressed as [20]:

\[
\alpha = -\frac{20\pi}{ln10} \text{IM}(\beta) \approx -8.6862 \frac{2\pi}{\lambda} \text{IM}\left(n_{\text{eff}}\right) \tag{4}
\]

where \( \text{IM} \) represents the imaginary part, and \( n_{\text{eff}} \) represents the effective refractive index of the fiber.

3. Analysis and Optimization of Optical Fiber Structure Parameters

The fiber structure can effectively destroy the circular symmetrical structure of the traditional 19-core optical fiber. It cuts off the higher-order modes (\( \text{TE}_{01}, \text{TM}_{01} \)), leaving two degenerate fundamental modes (\( \text{HE}_{11} \)) and second-order modes (\( \text{HE}_{21} \)), as shown in Figure 2. In addition, the 10 fiber cores increase the lateral coupling of the fiber, which significantly increases the mode field area of the fiber. The effective refractive index of the cladding is reduced by adding air holes and grooves in the cladding. As a result, the refractive index difference between the core and the cladding is increased, and the BL is significantly reduced.
3.1. Analysis of Three Structural Parameters $\Lambda$, $d$, and $\Delta n$

For this paper, we conducted research on the basis of strict dual-mode transmission. $\Lambda$, $d$, and $\Delta n$ three structural parameters were analyzed. The working wavelength $\lambda$ was set at 1550 nm, and the initial structure parameter was set as $\Lambda = 15 \text{ um}$, $d = 3 \text{ um}$, $\Delta n = 0.003$, $d_{\text{center}} = d$, $\Delta n_{\text{center}} = 0.003$, $W_{\text{trench}} = 5.5 \text{ um}$, $L_{\text{trench}} = 52 \text{ um}$, $\Delta n_1 = 0.004$.

The result of analyzing the influence of the structural parameter $\Lambda$ on $n_{\text{eff}}$ and $A_{\text{eff}}$ is shown in Figure 3. To realize dual-mode transmission and cut high-order modes of optical fiber, its effective refractive index should be less than $n_{\text{clad}}$. Figure 3a shows that the transmission mode can be adjusted by modifying $\Lambda$. If dual-mode transmission is to be realized, $\Lambda$ should be greater than or equal to 11.5 um. Figure 3b shows that as $\Lambda$ goes from 10 um to 15 um, the $A_{\text{eff}}$ of HE_{11} grows from 1451 um$^2$ to 2201 um$^2$ and then drops to 1996 um$^2$, and finally reaches the maximum value at 14.5 um; in addition, the $A_{\text{eff}}$ of HE_{21} grows from 1219 um$^2$ to 1717 um$^2$. From the above discussion, it can be concluded that 14.5 um is the best choice for $\Lambda$. 
When $\Lambda$ is 14.5 um, the results of analyzing the influence of structure parameter $d$ on $n_g$ and $A_{eff}$ are shown in Figure 4. Figure 4a shows that as $d$ increases, the effective refractive index of each mode also increases. If $d$ is less than or equal to 3.3 um, then the fiber realizes dual-mode transmission. It can be seen from Figure 4b that as $d$ increases to 3.4 um, the $A_{eff}$ of HE$_{11}$ rises to the maximum value of 2032 um$^2$, and the $A_{eff}$ of HE$_{21}$ decreases from 1706 um$^2$ to 1616 um$^2$. However, due to the limitation of dual-mode transmission conditions, $d$ is the most suitable to be 3.3 um. At this time, the $A_{eff}$ of HE$_{11}$ is 2029 um$^2$, and the $A_{eff}$ of HE$_{21}$ is 1632 um$^2$. Optical fiber can achieve dual-mode transmission, but also has a large $A_{eff}$.

When $d$ is 3.3 um, the effect of $\Delta n$ on $n_{eff}$ and $A_{eff}$ is shown in Figure 5. Figure 5a shows that with the increase of $\Delta n$, the neff of TE$_{01}$ and TM$_{01}$ also increase. In order to ensure dual-mode transmission, $\Delta n$ should be less than or equal to 0.00315. It can be seen from Figure 5b that the maximum $A_{eff}$ of HE$_{11}$ at 3.1 um is 2031 um$^2$ for $\Delta n$, and the $A_{eff}$ of HE$_{21}$ at this time is 1622 um$^2$. In order to ensure that the fundamental mode obtains a larger mode field area, $\Delta n$ is selected as 0.003.
Figure 5. (a) The $n_{eff}$ of each mode varies with $\Delta n$; (b) the change of $A_{eff}$ of HE$_{11}$ and HE$_{21}$ with $\Delta n$.

3.2. Analysis of Structural Parameters of Central Core

In order to enhance the core’s ability to confine light, the central core diameter $d_{center}$ is increased to reduce the central core refractive index $\Delta n_{center}$, thereby reducing the bending loss. This part analyzes the $d_{center}$ and $\Delta n_{center}$ structure parameters of the center core and initializes the center core structure parameters to $\Delta n_{center} = 0.001$ and $d_{center} = 3$ um.

Based on the optimization of the above structural parameters, the influence of $d_{center}$ on $n_{eff}$ and $A_{eff}$ is studied, as shown in Figure 6. Figure 6a shows that the effective refractive index of the higher-order modes TE$_{01}$, TM$_{01}$ is around 1.444, intersecting with ncl at 7.2 um. To ensure dual-mode transmission, $d_{center}$ should be less than 7.2 um. As shown in Figure 6b, HE$_{11}$ has the largest $A_{eff}$ at 4.8 um in $d_{center}$, which is about 2039 um$^2$ and the $A_{eff}$ of HE$_{21}$ has been stable around 1622 um$^2$, so 4.8 um is the best choice for $d_{center}$.

Figure 6. (a) The $N_{eff}$ of HE$_{11}$ and HE$_{21}$ varies with $d_{center}$; (b) The change of $A_{eff}$ of HE$_{11}$ and HE$_{21}$ with $d_{center}$.

When the $d_{center}$ is 4.8 um, the influence of $\Delta n_{center}$ on $n_{eff}$ and $A_{eff}$ is shown in Figure 7. Figure 7a shows that TE$_{01}$, TM$_{01}$, and ncl intersect at 0.002. To ensure dual-mode transmission, $\Delta n_{center}$ must be restricted within 0.002.
The greater the refractive index of the central core of the optical fiber, the stronger its ability to confine light, but the mode field area will decrease. It can be seen from Figure 7b that when $\Delta n_{\text{center}}$ exceeds 0.002, the $A_{\text{eff}}$ of HE$_{11}$ decreases rapidly. The $A_{\text{eff}}$ of HE$_{21}$ is stable at 1622 $\mu$m$^2$, and the $A_{\text{eff}}$ of HE$_{11}$ is 2002 $\mu$m$^2$ at 0.002. $\Delta n_{\text{center}}$ is selected as 0.002 as the best, which not only has a large mode field area, but also has a better ability to bind light.

4. Bending Characteristic Analysis

This part studies the effect of $R$ on the $A_{\text{eff}}$ and $BL$ of HE$_{11}$ and HE$_{21}$ when the working wavelength is 1550 nm.

When the bending radius is 1.5 cm, the mode field and electric field will deviate from the core area to the direction of the trench as shown in Figure 8, resulting in a reduction in the mode field area and an increase in the bending loss. In order to prevent the electric field from deviating to the trench, a circle of air holes is added in the middle of the cladding. The air holes have a lower refractive index, which can effectively prevent the electric field from deviating to the trench. At the same time, it reduces the refractive index of the cladding and the bending loss is reduced.

![Figure 7](image1.png)

**Figure 7.** (a) The $N_{\text{eff}}$ of HE$_{11}$ and HE$_{21}$ varies with $\Delta n_{\text{center}}$; (b) the change of $A_{\text{eff}}$ of HE$_{11}$ and HE$_{21}$ with $\Delta n_{\text{center}}$.

![Figure 8](image2.png)

**Figure 8.** Cont.
This article Mode field area of the fundamental mode can reach 2003.24 μm² when the bending radius is 20 cm, the effective mode area of the fiber can reach 914 μm².[17] Mode area of 2622 μm², when the bending radius is greater than 11 cm, the A_eff of HE_{11} and HE_{21} changes with R.

Table 1 is a comparison table between this article and other recent work and literature.

<table>
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<tr>
<th>Article</th>
<th>Description</th>
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<tr>
<td>[21]</td>
<td>Mode area of 2622 μm² at a bend radius of 20 cm can be achieved. Bending loss can be reduced to about 0.092 dB/m at 1550 nm. When the bending radius is 20 cm, the effective mode area of the fiber can reach 914 μm² at 1.06 μm, and loss ratio between lowest-HOMs and fundamental mode is larger than 100.</td>
</tr>
<tr>
<td>[17]</td>
<td>Mode field area of the fundamental mode can reach 1916.042 μm² at 1550 nm, and when the bending radius is 1.4 cm, the bending loss is 2.96 × 10^{-3} dB/m.</td>
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<tr>
<td>[22]</td>
<td>Mode field area of the fundamental mode can reach 2003.24 μm², and when the bending radius is 1 cm, the bending loss is 2.57 × 10^{-3} dB/m at 1550 nm.</td>
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5. Structural Optimization of the Trench

Adding trench in the cladding can effectively reduce the bending loss of the optical fiber and improve the bending resistance of the optical fiber. However, the bending loss of the optical fiber and the mode field area are mutually restrictive, so the two parts must be taken into consideration at the same time in the design. In order to balance the relationship between the bending loss and the mode field area, this paper defines the performance factor $PI$ [23] of the fiber, and the expression is:

$$PI = \frac{BL}{A_{eff}}$$  \hfill (5)

$PI$ is used to measure the trade-off between $BL$ and $A_{eff}$. When $A_{eff}$ increases and $BL$ decreases, $PI$ will decrease, and the comprehensive performance of the fiber will be better.

This section provides analysis and optimization of the $L_{trench}$ and $\Delta n_1$ parameters of the trench. We used $PI$ to evaluate the comprehensive performance of the optical fiber. $W_{trench}$ has little effect on the $A_{eff}$ of each mode, and the larger the thickness, the smaller the bending loss. Therefore, the larger the $W_{trench}$, the better the comprehensive performance of the fiber. However, $W_{trench}$ is limited by the diameter of the cladding layer to a maximum of 5.5 um.

When the $W_{trench}$ is 5.5 um, the influence of the $L_{trench}$ on the $A_{eff}$ and $PI$ of the fiber under the condition of a 1.5 cm bending radius is shown in Figure 10. From Figure 10(a), it can be seen that the $A_{eff}$ of HE$_{11}$ drops rapidly at 53.9 um, and the $A_{eff}$ of HE$_{21}$ slightly rises. When the $L_{trench}$ exceeds 53.8 um, the trench will exceed the cladding and the structure will be disordered, resulting in a sudden change in the curve. It can be seen from Figure 10(b) that with the increase of $L_{trench}$, the $PI$ of HE$_{11}$ first drops and then rises rapidly, with a minimum value at 53.8 um, while the $PI$ of HE$_{21}$ is relatively stable. So, at 53.8 um, the fiber has the best comprehensive performance.

When $L_{trench}$ is 53.8 um, the influence of $\Delta n_1$ on $N_{eff}$ and $PI$ is shown in Figure 11. Figure 11(a) shows that with the increase of $\Delta n_1$, $A_{eff}$ of the two modes firstly decreases, then increases, and finally stabilizes. In Figure 11(b), the $PI$ of the fiber decreases with the increase of $\Delta n_1$. This indicates that the larger the $\Delta n_1$, the better the comprehensive performance of the fiber. Due to the limitation of the manufacturing process, $\Delta n_1$ cannot be too large, and is usually set to 0.004.

![Figure 10](image-url)  \hfill (a)

![Figure 10](image-url)  \hfill (b)
In summary, the final optimized parameters are as follows: \( \Lambda = 14.5 \text{ um}, d = 33 \text{ um}, \Delta n = 0.0031, d_{\text{center}} = 4.8 \text{ um}, \Delta n_{\text{center}} = 0.002, W_{\text{trench}} = 5.5 \text{ um}, L_{\text{trench}} = 53.8 \text{ um}, \Delta n_1 = 0.004 \).

6. Conclusions

A dual-mode TA-LBL-LMFA MCF with air hole structure is investigated in this paper. By removing the core on both sides of the traditional 19-core fiber, the fiber can destroy the circular symmetry structure of traditional 19-core fiber and cut off the high-order modes TE_{01} and TM_{01} with circular symmetry. Adding a circle of air holes at the periphery of the core area can confine the mode field in the core area effectively. Also, adding a trench that is lower than the refractive index of the cladding at the periphery of the air hole can effectively reduce the BL. The introduction of 10 cores into the silica region between the 19 cores increases the lateral coupling in the core area and increases the mode field area. In this way, a large mode field dual-mode transmission with low bending loss is realized. \( \Lambda = 14.5 \text{ um}, d = 33 \text{ um}, \Delta n = 0.0031, d_{\text{center}} = 4.8 \text{ um}, \Delta n_{\text{center}} = 0.002, W_{\text{trench}} = 5.5 \text{ um}, L_{\text{trench}} = 53.8 \text{ um}, \Delta n_1 = 0.004 \) are the optimized parameters. At this time, the \( A_{\text{eff}} \) of the optical fiber HE_{11} can reach 2003.24 um\(^2\). When the bending radius \( R \) is 1 cm, the bending loss \( BL \) is \( 2.57 \times 10^{-3} \text{ dB/m} \). Potential applications are anticipated in the transmission of large-capacity optical communication systems and high-power lasers.

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References


