A Substrate Integrated Waveguide Resonator Sensor for Dual-Band Complex Permittivity Measurement

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Abstract: This paper presents a novel dual-band substrate integrated waveguide (SIW) sensor that is designed to measure the complex permittivities of liquids or solid powders at two industrial, scientific, and medical (ISM) frequencies simultaneously. Resonant frequencies and quality factors are obtained from S-parameter measurements with the proposed SIW sensor, and applied to reconstructing the permittivities of materials under test through an artificial neural network. The water–ethanol mixed liquids were measured with the proposed sensor. The maximum deviations of the measured permittivities at 2.45 and 5.8 GHz are within 3% of literature results. The measurement by the proposed SIW sensor with artificial neural network reconstruction is accurate and efficient.

Keywords: resonator sensor; permittivity; measurement; substrate integrated waveguide (SIW)

1. Introduction

Permittivity \((\varepsilon = \varepsilon' - j\varepsilon'')\) plays a very important role in materials for industrial, scientific, and medical applications [1]. Hence, the measurement of permittivity in industrial applications of microwave energy is of substantial importance. The measurement methods can be divided into resonant type and non-resonant type [2]. Resonator-based approaches are an attractive choice due to their high sensitivity [3,4]. Non-resonant approaches have broadband frequency capabilities [5–7]. Multi-band measurements may combine the advantages of high sensitivities and broadband frequency capabilities together in some particular applications.

In chemistry, we sometimes find that looking at an overall reaction alone fails to tell us accurate information about the dynamics—in particular, the kinetics—of a reaction. Reaction mechanisms act as tools to do this by allowing us to split an overall reaction into a series of intermediate reactions [8,9]. These intermediate properties can then be examined individually and can collectively tell us much about the properties of the overall reaction that we see. In some chemical reactions, the permittivity of reactant mixtures can be measured to examine these intermediate properties and properties of the overall reactions. Dual-band measurements can simultaneously reveal the products in the reaction process at two different frequencies, which can provide more information for the study of the intermediate reactions of the overall chemical reaction, and provide the necessary foundation for the study of the reaction mechanism.

Microwave sensors are key components in permittivity measurement systems, since the measurement results depend on the sensor performance greatly. An increasing number of studies have investigated microwave sensor designs, such as coaxial probes, waveguides, and dielectric resonators, in order to properly characterize their material properties in terms of their complex permittivity [10]. Most of them are costly, since their structure design entails a complicated measurement setup and a complex design construction [11–13].
Permittivity measurement technology has become much more advanced through the development of planar microwave resonator sensors. They provide an ideal platform to realize compact and low-cost sensors with high accuracy and high quality (Q) factor, which present enhanced sensitivity for permittivity measurements [14–17]. SIW structures have been proposed to design a number of planar microwave resonator sensors [18–20]. They are considered to be reliable candidates due to the low-cost mass production of microwave circuits [21,22]. A slotted SIW resonator sensor can measure liquid permittivity accurately at C-band [23]. It is worthwhile mentioning that a multi-band permittivity sensor is quite useful due to the properties of dielectric materials dependent upon frequency [24]. Based on the multi-band measurements, the use of SIW sensors has advantages in permittivity measurement.

Real-time measurement is often required in permittivity measurements. In real-time measurements, material permittivity can be reconstructed by using modern optimization algorithms [25]. The artificial neural network (ANN), a modern optimization algorithm, is one of the fastest growing areas of computer science with far-reaching applications [26]. ANN computational modules have been applied to microwave techniques and have become a useful form of tool recently [27,28]. The ANN is introduced to deal with the complex relationship between the applied electromagnetic field and test materials. To establish the non-linear relationship in a microwave measurement, the ANN is applied to provide a mathematical solution that can be trained to map a set of inputs to another set of outputs [29]. The ANN can be trained to learn the behavior of an effective permittivity of a material under microwave irradiation in a test system, and it can provide a fast and accurate result in material permittivity measurements. Thus, an on-line measurement may be realized based on the ANN.

In this paper, a novel dual-band SIW resonator was designed and fabricated. It is composed of two square SIW resonators with cascading connection along diagonal direction. Compared with traditional SIW resonators, the proposed SIW sensor can measure liquid complex permittivity at both C- and S-band simultaneously. It realized highly sensitive measurements at dual-frequency in broadband. Due to the specific structure, the sensor has high-quality factors at both operating frequencies, which makes it suitable to measure a wide range of permittivity with high accuracy. We used an ANN to reconstruct the complex permittivity of measured materials. The proposed SIW sensor can realize real-time measurements. It has a bright future in microwave chemistry applications.

2. Measurement Method and Setup
2.1. Structure of the Proposed Sensor

Figure 1 shows the proposed sensor. It consists of three parts: a small and a large resonant cavity working at 5.85 GHz and 2.45 GHz, respectively, and an interconnection between them. The length of each square SIW resonator is determined by the measurement frequency. In the coupling structures, the gaps ($G_{c1}$, $G_{c2}$, and $G_{c3}$ in Figure 1) between the center conductor and the SIW ground plane are minimized to suppress the undesired power leakage. The coupling between two cavities is along the diagonal direction to realize two independent resonances. To minimize reflection, the length of the center feeding to each resonator was tuned to achieve a better resonance at 2.45 GHz and 5.85 GHz, respectively. The resonant mode of each cavity is $TE_{101}$. We choose an F4B-2 substrate with $\varepsilon_r = 2.51$, $\tan \delta = 0.0025$, and thickness 1 mm to build the sensor. Its dimensions are as follows (referring to Figure 1): $W_{50} = 2.8$ mm, $L_{c1} = 12.0$ mm, $L_{c2} = 12.0$ mm, $L_{c3} = 4.0$ mm, $slot1_W = 2.8$ mm, $W_{sl1} = 55.2$ mm, $slot1_L = 20.0$ mm, $W_{sl2} = 23.6$ mm, $slot2_W = 1.4$ mm, $slot2_L = 10.0$ mm, $G_{c1} = 1.0$ mm, $G_{c2} = 2.8$ mm, $G_{c3} = 0.5$ mm, the diameter of the vias $D = 0.8$ mm, and the center-to-center spacing $S_{vp} = 1.2$ mm. The thickness of the copper foil is 17 µm. The total dimension of the sensor is $128 \times 88 \times 1$ mm³. There are two narrow slots along its diagonal line at the center of each top layer, and the materials to be measured are placed on the slots when measuring. The length of each slot is approximated to $\lambda_g/4$, where $\lambda_g$ is the guided wavelength of the $TE_{10}$ mode at the resonant frequency.
2.2. Electric Field Distribution of the Proposed Sensor

The electric field distribution is achieved from the ANSYS high-frequency structure simulator (HFSS), as shown in Figure 2. The behavior of SIW resonators at two resonance frequencies was analyzed. It is obvious from Figure 2a,b that the electric fields at 2.45 GHz and 5.8 GHz are focused to the large and small cavities, respectively. Each resonator has its own independent corresponding resonance frequencies, which benefit from coupling along the diagonal direction. Furthermore, these two resonators are sufficiently distanced to minimize the interference between them. The specific structures that connect the two resonators contribute to reduced mutual coupling between the resonators and hence an improved performance. The material on the slot affects the electromagnetic field leakage, which in turn affects the resonant frequency and quality factor. However, the slot is very narrow and has no great impacts on the resonators. In addition, the impedance matching was factored into the design and optimized with the inclusion of the two slots. At resonant frequencies, the electric field is weakly affected by the slot, which is similar to the measurement based on the disturbance method.
2.3. Measured and Simulated Results of the Proposed Sensor

The simulated and measured results at either frequency are shown in Figure 3. There is good agreement between the simulated and measured results. Detailed results regarding the resonant frequencies and quality factors are shown in Table 1. The simulation results are basically the same as the measurement results. When the frequency increases, the dielectric and conductor losses will increase, resulting in not much difference between the two resonator $Q$ values.

<table>
<thead>
<tr>
<th>Measurement</th>
<th>Simulation</th>
</tr>
</thead>
<tbody>
<tr>
<td>2.4414 GHz</td>
<td>2.4417 GHz</td>
</tr>
<tr>
<td>319.2</td>
<td>301.5</td>
</tr>
<tr>
<td>5.8412 GHz</td>
<td>5.8415 GHz</td>
</tr>
<tr>
<td>317.9</td>
<td>324.3</td>
</tr>
</tbody>
</table>

Figure 2. Distribution of electric field of the proposed SIW at (a) 2.45 GHz and (b) 5.85 GHz.

Figure 3. Measured and simulated $|S_{11}|$ of the SIW resonator, (a) 2.45 GHz, (b) 5.85 GHz.
Table 1. Measurement and simulated resonant characteristics.

<table>
<thead>
<tr>
<th></th>
<th>Low Working Frequency</th>
<th>High Working Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>( f_0/\text{GHz} )</td>
<td>( Q )</td>
</tr>
<tr>
<td>Simulation</td>
<td>2.4417</td>
<td>301.5</td>
</tr>
<tr>
<td>Measurement</td>
<td>2.4414</td>
<td>319.2</td>
</tr>
</tbody>
</table>

Two plastic frames are applied in order to keep the material under test above the slots. The dimensions of the two frames are \( 40 \times 16 \times 5 \text{ mm}^3 \) and \( 22 \times 9 \times 5 \text{ mm}^3 \), respectively. According to the simulated and measured results, the two frames have no influence on the sensor. The liquids under test influence the resonant frequencies and quality factors of the sensor through two slots. During measurements, the slots are completely covered with the liquid mixtures of ethanol and water. By varying the ethanol concentrations, the resonant frequencies and quality factors vary with the complex permittivities of liquid under test. The fabricated sensor for complex permittivity measurement and the measurement system are shown in Figures 4 and 5, respectively. In order to reduce the errors, each sample is measured 10 times in order to generate average values for consideration.

Figure 4. The fabricated SIW resonator sensor.

Figure 5. The measurement system.
3. Extraction of Permittivities

3.1. Measurements of the Sensor Resonant Frequency and Quality Factor

The resonant frequencies of the TE\textsubscript{mnp} mode for an SIW resonator are as follows:

\[ f_{\text{SIW}}^{mnp} = \frac{1}{2\pi \sqrt{\varepsilon \mu}} \sqrt{\left( \frac{m\pi}{L_{\text{eff}}} \right)^2 + \left( \frac{n\pi}{h} \right)^2 + \left( \frac{p\pi}{W_{\text{eff}}} \right)^2} \]  

(1)

where \( m = 1, 2, \ldots, n = 1, 2, \ldots, p = 1, 2, \ldots, \mu = \mu_0 \mu_r, \) and \( \varepsilon = \varepsilon_0 \varepsilon_r \) are the permeability and permittivity of the substrate, respectively. \( L_{\text{eff}}, h, \) and \( W_{\text{eff}} \) are length, thickness, and width, respectively. They are related to the resonator dimensions. The dimensions of the two resonators are different, and the resonant frequencies are also different. The thickness of the SIW resonator is \( h \). Its equivalent length and width are as follows:

\[ W_{\text{eff}} = W_{\text{SIW}} - 1.08 \frac{D^2}{S_{vp}} + 0.1 \frac{D^2}{W_{\text{SIW}}} \]  

(2)

\[ L_{\text{eff}} = L_{\text{SIW}} - 1.08 \frac{D^2}{S_{vp}} + 0.1 \frac{D^2}{L_{\text{SIW}}} \]  

(3)

where \( L_{\text{SIW}} \) and \( W_{\text{SIW}} \) are the length and width of the SIW resonator [30], respectively, for the designed sensor \( L_{\text{SIW}} = W_{\text{SIW}} \).

Characterization of the SIW resonator can be achieved according to the letter [31]. The unloaded quality factor of the SIW resonator is influenced by \( Q_c \) and \( Q_d \), respectively.

\[ \frac{1}{Q_u} = \frac{1}{Q_c} + \frac{1}{Q_d} \]  

(4)

where \( Q_c \) and \( Q_d \) represent the quality factor of the resonator, when the dielectric is lossless and the metal is a perfect metal, respectively. The relationship between \( Q_d \) and \( \tan \delta \) is as follows.

\[ Q_d = \frac{\varepsilon'}{\varepsilon''} = \frac{1}{\tan \delta} \]  

(5)

where \( \varepsilon' \) and \( \varepsilon'' \) are the real and imaginary part of the permittivity, respectively.

The complex permittivity of the substrate and liquid under test mainly affect the effective complex permittivity of the SIW resonator at working frequency. The above Equations (1), (4), and (5) explain the relationship.

3.2. Diagram of the BP-ANN Algorithm

The complex permittivity of liquid under test mainly affects the quality factors and resonant frequencies of the SIW resonator in the working frequency band. We used a back-propagation artificial neural network (BP-ANN) (Figure 6) to reconstruct the complex permittivity of the material measured by the unloaded quality factor \( Q \) and resonant frequency \( f_0 \). The measured \( Q \) and \( f_0 \) along with permittivities of the methanol–water mixtures constitute the input and output of the BP-ANN, respectively. We obtained the relationship between the complex permittivities of liquids under test and measured parameters including the unloaded quality factors and resonant frequencies, which are determined by the simulation results with the HFSS. These data are applied to the training of the BP-ANN, which is influenced by the connection strength of the neural units and the transfer rules.
3.3. Reconstruction of Material Permittivity by the BP-ANN Algorithm

The training process is terminated when the training errors are less than a given value or the processes are converged. At this moment, the complex permittivity of the liquid under test can be determined from the BP-ANN whose weight matrixes are on a suitable state. We measured the S-parameters of the sensor at working frequencies to get the resonant frequencies and the unloaded quality factors of the sensor. The complex permittivity of the liquid under test is calculated in real-time when the measured resonant frequencies and unloaded quality factors are input into the trained BP-ANN, and the calculation speed from measured S-parameters for obtaining the permittivity of the material under test is less than 3 s on a normal personal computer with 3 GHz CPU and 4 GB RAM.

4. Experimental Results

4.1. Measurement Process with the Proposed Sensor

The permittivity of ethanol–water mixtures for the entire concentration range in the frequency range from 500 MHz to 25 GHz is known [32]. Ethanol–water mixtures are used because the permittivities for the mixtures of solvents have calculated values, which are easy to compare with the measured values and to verify the accuracy of the measurements. Moreover, binary liquid mixtures of ethanol and water have a wide permittivity range, which means that they are suitable to be measurement standard templates. We measured ethanol–water mixtures with different molar fractions of ethanol, and the scattering parameters were recorded when the mixtures were put into the experimental system. We obtained the unloaded quality factors and resonant frequencies from the measured scattering parameters. We used a 5-mL measuring cylinder and a 20-mL glass beaker to prepare different concentrations of ethanol by mixing purified water at 20 °C. When measuring the $|S_{11}|$ of the sensor at working frequency, we dropped the prepared liquids into the frames. The measurement bandwidth and the number of sweeping points was 200 MHz and 1601, respectively. Before the next measurement with a different volume fraction of ethanol, we cleaned the sensor to reduce measurement errors. The measured results were obtained from an average of 10 measurements. The sensor was connected to an Agilent N5230A Vector Network Analyzer with a coaxial cable. We put the measured resonant frequencies and unloaded quality factors into the BP-ANN, which had been trained already. The complex permittivity can be quickly and accurately obtained from the BP-ANN.

4.2. Measurement Results with the Proposed Sensor

The room temperature and relative humidity were 20 °C and 70%, respectively, when the measurements were made. Figure 7 shows the reconstruction of the real and imaginary parts of the complex permittivity at working frequencies. They have good agreement with the dielectric relaxation parameters of ethanol–water mixtures with different mole fractions in [32]. The relative errors of $\varepsilon'$ and $\varepsilon''$ were 1.98%
and 1.28% at 2.45 GHz, and are 2.51% and 2.68% at 5.85 GHz, respectively. The results show that the SIW sensors can be used in permittivity measurements at 2.45 GHz and 5.8 GHz frequency bands. The average and standard deviation for each volume fraction of ethanol shown in Table 2.

Figure 7. Reconstructed complex permittivity (real and imaginary parts) with respect to the volume fraction of ethanol from 0% to 100%, (a) 2.45 GHz, (b) 5.85 GHz.

Table 2. Measured permittivities with average and standard deviation.

<table>
<thead>
<tr>
<th>Volume Fraction of Ethanol</th>
<th>2.45 GHz</th>
<th></th>
<th>5.85 GHz</th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\epsilon'$ Average</td>
<td>$\epsilon'$ Standard Deviation</td>
<td>$\epsilon''$ Average</td>
<td>$\epsilon''$ Standard Deviation</td>
<td>$\epsilon'$ Average</td>
<td>$\epsilon'$ Standard Deviation</td>
<td>$\epsilon''$ Average</td>
</tr>
<tr>
<td>0%</td>
<td>77.34</td>
<td>1.91</td>
<td>10.38</td>
<td>1.47</td>
<td>72.52</td>
<td>1.99</td>
<td>23.31</td>
</tr>
<tr>
<td>10%</td>
<td>71.60</td>
<td>1.65</td>
<td>13.23</td>
<td>0.95</td>
<td>65.66</td>
<td>1.73</td>
<td>27.49</td>
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<tr>
<td>20%</td>
<td>64.83</td>
<td>1.84</td>
<td>16.21</td>
<td>1.25</td>
<td>53.11</td>
<td>1.56</td>
<td>27.84</td>
</tr>
<tr>
<td>30%</td>
<td>56.52</td>
<td>1.56</td>
<td>18.35</td>
<td>1.40</td>
<td>41.46</td>
<td>1.65</td>
<td>28.26</td>
</tr>
<tr>
<td>40%</td>
<td>50.90</td>
<td>1.92</td>
<td>19.59</td>
<td>1.36</td>
<td>33.04</td>
<td>1.47</td>
<td>24.81</td>
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<tr>
<td>50%</td>
<td>41.20</td>
<td>1.39</td>
<td>18.64</td>
<td>1.22</td>
<td>24.71</td>
<td>1.39</td>
<td>21.22</td>
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<tr>
<td>60%</td>
<td>36.09</td>
<td>1.25</td>
<td>17.79</td>
<td>1.32</td>
<td>20.68</td>
<td>1.13</td>
<td>18.40</td>
</tr>
<tr>
<td>70%</td>
<td>26.67</td>
<td>1.48</td>
<td>15.92</td>
<td>1.04</td>
<td>14.44</td>
<td>1.30</td>
<td>14.31</td>
</tr>
<tr>
<td>80%</td>
<td>19.25</td>
<td>1.35</td>
<td>14.12</td>
<td>0.87</td>
<td>10.48</td>
<td>1.14</td>
<td>10.27</td>
</tr>
<tr>
<td>90%</td>
<td>12.10</td>
<td>1.04</td>
<td>10.23</td>
<td>0.36</td>
<td>7.55</td>
<td>0.96</td>
<td>6.16</td>
</tr>
<tr>
<td>100%</td>
<td>6.76</td>
<td>0.87</td>
<td>6.47</td>
<td>0.44</td>
<td>4.96</td>
<td>0.87</td>
<td>3.23</td>
</tr>
</tbody>
</table>
5. Conclusions

In summary, the proposed dual-band SIW sensor with the BP-ANN algorithm was found to be able to accurately determine the complex permittivities of liquids in the ISM bands. A BP-ANN was trained from simulated data and applied to reconstructing the complex permittivities of liquids. The relative errors of \( \varepsilon' \) and \( \varepsilon'' \) were 1.98% and 1.28% at 2.45 GHz, and were 2.51% and 2.68% at 5.85 GHz, respectively. The proposed sensor was able to realize real-time measurements of the permittivity, and the reconstruction time of obtaining material permittivities from measured S-parameters was less than 3 s. The proposed sensor, therefore, offers high sensitivity with a simple structural design, a fast-sensing response, and cost-effectiveness. In addition, the sensor can be used not only for liquids, but also for measuring the permittivity of solid powders. The solid powders can be placed in the area to be measured for permittivity measurements. The sensor can be integrated with other kinds of planar circuits or RF front-ends. It is low cost and with high sensitivity for dual-band permittivity measurements, and it could be applied to microwave chemistry industrial applications in the future.

Author Contributions: Q.C., Z.L. and C.L. developed the model, finished the experiment, and analyzed the data. Q.C. wrote the initial draft of the manuscript; Q.C., N.S. and C.L. reviewed and contributed to the final manuscript. All authors have read and agreed to the published version of the manuscript.

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Conflicts of Interest: The authors declare no conflict of interest.

References


