Potential Constraints to Neutrino–Nucleus Interactions Based on Electron Scattering Data †

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Abstract: A thorough understanding of neutrino–nucleus interaction physics is crucial to achieving precision goals in broader neutrino physics programs. The complexity of the nuclei comprising the detectors and the limited understanding of their weak response constitute two of the biggest systematic uncertainties in neutrino experiments—both at intermediate energies affecting short- and long-baseline neutrino programs and at lower energies affecting coherent scattering neutrino programs. While electron and neutrino interactions are different at the primary vertex, many underlying relevant physical processes in the nucleus are the same in both cases, and electron scattering data collected with precisely controlled kinematics, large statistics, and high precision allow one to constrain nuclear properties and specific interaction processes. To this end, electron–nucleus scattering experiments provide vital complementary information to test, assess, and validate different nuclear models and event generators intended to be used in neutrino experiments. In fact, for many decades, the study of electron scattering off a nucleus has been used as a tool to probe the properties of that nucleus and its electromagnetic response. While previously existing electron scattering data provide important information, new and proposed measurements are tied closely to what is required for the neutrino program in terms of expanding kinematic reach, the addition of relevant nuclei, and information on the final-state hadronic system.

Keywords: electron–nucleus scattering; neutrino–nucleus scattering; electroweak interactions; neutrino oscillations

1. Introduction

The success of current and future neutrino experiments in achieving discovery-level precision will greatly depend on the precision with which the fundamental underlying process—the neutrino interaction with the target nucleus in the detector—is known [1]. To this end, electron scattering experiments have been playing a crucial role by providing high-precision data as the testbed to assess and validate different nuclear models intended to be used in neutrino experiments [2].

For accelerator-based neutrino programs, such as DUNE, the primary physics goals are determining the mass hierarchy and measuring precision oscillation physics, including the subtle effects of $\delta_{\text{CP}}$ [3]. The main challenges in constraining neutrino–nucleus scattering physics stem from the fact that the neutrino energies in these experiments typically range from 100 s of MeV to a few GeV, where different interaction mechanisms yield comparable contributions to the cross-section. One has to constrain an accurate picture of the initial-state target nucleus, its response to the electroweak probe that includes several reaction mechanisms resulting in various final-state particles, and the final-state interactions that further modify the properties of the hadronic system created at the primary interaction vertex.

For the coherent elastic neutrino–nucleus scattering (CEvNS) program at stopped-pion sources, such as at ORNL, the main source of uncertainty in evaluating the CEvNS
cross-section is driven by the underlying nuclear structure, embedded in the weak form factor, of the target nucleus. The recent detection of the CEvNS process by the COHERENT collaboration [4] has opened up a slew of opportunities to probe several Beyond the Standard Model (BSM) scenarios in CEvNS experiments. In order to disentangle new physics signals from the SM-expected CEvNS rate, the weak form factor, which primarily depends on the neutron density, has to be known with percent-level precision [5,6].

Most of our current knowledge about the complexity of the nuclear environment—nuclear structure, dynamics, and reaction mechanisms—has been accumulated by studying electron scattering off target nuclei. Electron scattering off a nucleus, governed by quantum electrodynamics, has an advantage over proton or pion scattering off nuclei, which are dominated by strong forces. The electromagnetic interaction is well known within quantum electrodynamics and is weak compared to hadronic interactions, and, hence, the interaction between the incident electron and the nucleus can be treated within the Born approximation, i.e., within a single-photon exchange mechanism.

In the last few decades, a wealth of high-precision electron scattering data have been collected, over a variety of nuclei ranging from $^3$He to $^{208}$Pb, at several facilities, including Bates, Saclay, Frascati, DESY, SLAC, NIKHEF, and Jefferson Lab. The ability to vary the electron energy and scattering angle and, hence, the energy and momentum transferred to the nucleus ($\omega, q$)—combined with the advancements in high-intensity electron beams and high-performance spectrometers and detectors—resulted in investigating processes ranging from quasielastic (QE) to the $\Delta$ resonance to complete inelastic (resonant, non-resonant, and deep inelastic scatterings (DISs)) with significant details. A number of those datasets were further utilized to separate the longitudinal and transverse response functions through the Rosenbluth separation. Several decades of experimental work has provided a sufficient testbed to assess and validate several theoretical approximations and predictions and, hence, propelled the theoretical progress staged around nuclear ground-state properties, nuclear many-body theories, nuclear correlations, form factors, nucleon–nucleon interactions, etc. A web archive of accumulated data is maintained at Refs. [7,8].

Besides being immensely interesting in itself, electron scattering turned out to be of great importance for neutrino programs. The data collected with electron–nucleus scattering have provided the benchmark to test the nuclear models that can be further extended to neutrino–nucleus scattering. The extension of the formalism from electron–nucleus scattering, where only the vector current contributes, to neutrinos requires the addition of the axial current contribution. Despite the fact that (unpolarized) electron scattering provides access to only the vector response, the vector current is conserved between the electromagnetic and weak responses through the conserved vector current (CVC).

While previous and existing electron scattering experiments provide important information, new dedicated measurements whose goals align more closely with the needs of constraining neutrino–nucleus interaction physics in neutrino programs are needed. Dedicated electron scattering experiments with targets and kinematics of interest to neutrino experiments (CEvNS, supernova, and accelerator-based experiments) will be vital in the development of the neutrino–nucleus scattering physics models that underpin neutrino programs [2].

The rest of this article is structured as follows: In Section 2, we briefly describe the neutrino interaction challenges faced by neutrino programs in their key physics goals. We then identify connections between electron– and neutrino–nucleus scattering physics in Section 3. In Section 4, we present a brief summary of the current and planned electron scattering experiments that are input to various neutrino programs. We summarize in Section 5.

2. The Importance of Constraining Neutrino–Nucleus Interaction Physics

In accelerated-based neutrino oscillation programs, neutrino–nucleus interactions constitute one of the dominant systematic uncertainties. In the event of a neutrino oscillating from $\nu_i$ to $\nu_j$ and for a given observable topology, the observed event rate at the far detector
is a convolution of neutrino flux at the near detector \( (\phi_{\nu_i}) \), the probability of oscillation from flavor \( i \) to \( j \), and the neutrino–nucleus cross-section for neutrino flavor \( j \) \( (\sigma_{\nu_j}) \), and detection efficiency at the far detector \( (\epsilon_{\nu_j}) \) is

\[
R(\nu_i \rightarrow \nu_j) \propto \phi_{\nu_i} \otimes P(\nu_i \rightarrow \nu_j) \otimes \sigma_{\nu_j} \otimes \epsilon_{\nu_j}
\]  

(1)

with oscillation probability, considering a simple example of two neutrino flavors, given as

\[
P(\nu_i \rightarrow \nu_j) \simeq \sin^2 \frac{1}{2} \theta \sin^2 \left( \frac{\Delta m^2 L}{4E_{\nu}} \right),
\]

(2)

where \( \theta \) and \( \Delta m^2 \) are the mixing angle and the squared-mass difference, respectively; \( E_{\nu} \) is the neutrino energy; and \( L \) is the oscillation baseline. Typically, the ratio of the oscillated event rate at the far detector to the unoscillated event rate at the near detector does not cancel out flux and cross-section dependence.

The systematic challenges in neutrino experiments are manifold. The energy of the interacting neutrino is not known, the kinematics of the interaction in the target nucleus is not known, and the only known (to some degree) quantity—the topology of the final-state particles and their energy—is subjected to detector type, detection thresholds, and the accuracy of particle identification and background reduction processes. The necessity of an accurate neutrino interaction model is essential at almost every step of the analysis. The accuracy of the measurement of the (energy-dependent) neutrino oscillation probability relies strongly on the accuracy with which a Monte Carlo event generator can describe all neutrino–nucleus interaction types that can produce the observed event topology (this depends on both the initial- and final-state nuclear effects). As it stands currently, a lack of reliable nuclear models contributes to the main source of systematic uncertainty and is considered one of the main hurdles in further increasing the obtained precision. For current long-baseline neutrino experiments, T2K and NOvA, neutrino–nucleus interactions constitute one of the largest uncertainties. In future long-baseline neutrino experiments, DUNE and HyperK, the statistics will significantly increase, and neutrino interaction systematic uncertainties will be dominant.

In the energy regime of accelerator-based neutrino experiments, 100 s of MeV to a few GeV, several mechanisms contribute to the nuclear response: from the excitation of nuclear collective states in the lowest energy part of the spectrum up to the deep inelastic scattering at the highest energy transfers, encompassing the quasielastic region, corresponding to one-nucleon knockout, and the resonance region, corresponding to the excitation of nucleon resonances, followed by their decay and the subsequent production of pions and other mesons. There is no unified underlying theory to describe neutrino–nucleus interactions for this broad energy range. It truly is a multi-scale, multi-process, many-body non-perturbative problem subject to complex nuclear structure and dynamics that include transitions between different degrees of freedom. One needs a description of the initial-state target nucleus, its response to the electroweak probe that includes several reaction mechanisms resulting in various final-state particles, and the final-state interactions that further modify the properties of the hadronic system created at the primary interaction vertex.

Similarly for low-energy (10 s of MeV) neutrinos, with the uncertainties of inelastic neutrino–nucleus interactions, the detection channel for supernova neutrinos in DUNE and HyperK is large and is often not even quantified \([9,10]\). Although theoretical uncertainties, primarily driven by the poorly known neutron density distributions, are relatively small in the CEvNS case, percent-level precision might be needed to disentangle new physics signals \([5]\).

### 3. Connecting Electron– and Neutrino–Nucleus Scattering Physics

The electron–nucleus scattering process, represented in Figure 1a, is primarily governed by electromagnetic interactions, where (to the first order) the interaction is mediated...
by a (virtual) photon. The neutrino–nucleus scattering process, represented in Figure 1b, is primarily governed by weak interactions via the exchange of a $W^\pm$ or $Z^0$ boson for a charged or a neutral weak process, respectively.

Figure 1. Diagrammatic representation of (a) electron–nucleus and (b) neutrino–nucleus scattering processes ($l = e, \mu, \tau$), where $X$ represents outgoing hadronic final state.

In the Born approximation [11], the lepton–nucleus differential cross-section $d\sigma$ is proportional to the contraction of the leptonic ($L_{\mu\nu}$) and hadronic ($W_{\mu\nu}$) tensors:

$$d\sigma \propto L_{\mu\nu} W_{\mu\nu}$$

with the hadronic tensor written in terms of nuclear current operators, $J$:

$$W_{\mu\nu} \propto \sum_f \langle \psi_f | j_{\mu}^A(q) | \psi_f \rangle \langle \psi_f | j_{\nu}^A(q) | \psi_i \rangle \delta(E_0 + \omega - E_f)$$

where $\psi_i$ and $\psi_f$ are the initial- and final-state wave functions, and $\omega$ and $q$ are the energy and momentum transferred to the nucleus.

By contracting the leptonic and hadronic tensors, we obtain a sum involving projections of the current matrix elements. It is convenient to choose these to be transverse and longitudinal with respect to the virtual boson direction. The electron–nucleus scattering cross-section becomes

$$d\sigma_e \propto V_L R_L + V_T R_T$$

and the neutrino–nucleus scattering cross-section becomes

$$d\sigma_\nu \propto V_C R_C + V_L R_L + 2V_C L_R + V_T R_T + V_T' R_T'$$

where $R$ represents nuclear responses that are functions of $\omega$ and $q$. The subscripts $C$, $L$, and $T$ correspond to Coulomb, longitudinal, and transverse components. The last term in Equation (6), the transverse interference term, is positive for neutrino scattering and negative for antineutrino scattering.

The underlying nuclear physics processes, probed by electrons and neutrinos, are intimately connected to each other. The initial nucleus description is the same. The weak current carried by neutrinos has a vector and an axial component, while the electromagnetic current carried by electrons is purely a vector. Though, the vector current is conserved (CVC) between the electromagnetic and weak interactions leaving the axial nuclear response unique to neutrinos (or polarized electrons). The final-state interaction effects are the same. Therefore, various aspects of nuclear structure and dynamics influencing the neutrino–nucleus cross-section can be studied in electron scattering. Any model or event generator that does not work for electron scattering would likely not work for neutrino scattering. In typical electron scattering experiments, the incident beam energy is known with good accuracy; hence, the transferred energy, $\omega$, and momentum, $q$, can be precisely determined by measuring the outgoing lepton kinematics. The high-precision, high statis-
The tens-of-MeV neutrinos, from stopped-pion sources or from core-collapse supernova, primarily interact via two processes: coherent elastic neutrino–nucleus scattering (CEvNS) and inelastic charged and neutral current scattering. A precise determination of the Standard Model CEvNS cross-section will enable new physics searches in CEvNS experiments, while a precise inelastic cross-section determination will enable the detection of supernova signals in DUNE experiments.

The CEvNS cross-section (at tree level) is given as

$$
\frac{d\sigma}{dT}(E_\nu, T) \approx \frac{G_F^2}{4\pi} M \left[ 1 - \frac{M T}{2E_\nu^2} \right] Q^2 W F^2_{\nu N}(q^2),
$$

where $G_F$ is the Fermi constant; $M$ is the mass of the nucleus; and $E_\nu$ and $T$ are the energy of the neutrino and the nuclear recoil energy, respectively. The weak form factor $F_{\nu N}(q^2)$ is given as

$$
F_{\nu N}(q^2) = \frac{1}{Q^2 W} [NF_n(q^2) - (1 - 4\sin^2\theta_W)ZF_p(q^2)]
$$

where $\theta_W$ is the Weinberg mixing angle. In Equation (8), the quantities $F_p(q^2)$ and $F_n(q^2)$ are the proton ($p$) and neutron ($n$) form factors, respectively. While the proton distributions are relatively well known through elastic electron scattering experiments [12], neutron distributions are much more difficult to constrain. Since $1 - 4\sin^2\theta_W(0) \approx 0$, the weak form factor becomes $F_{\nu N}(q^2) \approx F_n(q^2)$. In order to disentangle new physics signals from the SM-expected CEvNS rate, the weak form factor, which primarily depends on the neutron density, has to be known with percent-level precision.

Recent advancements in parity-violating electron scattering (PVES) experiments, utilizing polarized electron beams, provide relatively model-independent ways of determining weak form factors that can be used as direct inputs in determining the CEvNS cross-section. Both processes are described in the first-order perturbation theory via the exchange of an electroweak gauge boson between a lepton and a nucleus. While in CEvNS the lepton is a neutrino and a $Z^0$ boson is exchanged, in PVES, the lepton is an electron, but measuring the asymmetry allows one to select the interference between the $\gamma$ and $Z^0$ exchange. As a result, both the CEvNS cross-section and the PVES asymmetry depend on the weak form factor $F_W(Q^2)$, which is mostly determined by the neutron distribution within the nucleus. The parity-violating asymmetry $A_{pv}$ for elastic electron scattering is the fractional difference in the cross-section for positive helicity and negative helicity electrons. In the Born approximation, $A_{pv}$ is proportional to the weak form factor $F_W(q^2)$ [13,14],

$$
A_{pv} = \frac{d\sigma/d\Omega_+ - d\sigma/d\Omega_-}{d\sigma/d\Omega_+ + d\sigma/d\Omega_-} = \frac{G_F q^2 |Q_W| F_W(q^2)}{4\pi \alpha \sqrt{2} Z F_{eb}(q^2)}.
$$

Here, $F_{eb}(q^2)$ is the (E+M) charge form factor that is typically known from unpolarized electron scattering. Therefore, one can extract $F_W$ from measurements of $A_{pv}$. Note that Equation (9) must be corrected for Coulomb distortions [14], though these effects are absent for neutrino scattering.

The inelastic neutrino–nucleus cross-sections in this tens-of-MeV regime are quite poorly understood. There are very few existing measurements, none at better than the 10% uncertainty level. As a result, the uncertainties in the theoretical calculations of, e.g., neutrino–argon cross-sections are not well quantified at all at these energies. Because inelastic neutrino interactions have large uncertainties, in the future, it will be crucial to measure inelastic electron scattering cross-sections at energies below the 50 MeV mark and to use those data to calibrate theoretical models for the neutrino scattering process. Overall, we expect the nuclear structure effects to be definitely larger than in CEvNS and
presumably at least at the 10% level. To this end, 10 s of MeV electron scattering data will be vital in constraining neutrino–nucleus interactions at this energy scale.

4. Current and Future Electron Scattering Experiments for Neutrino Programs

For over five decades, electron scattering experiments at different facilities around the world have provided a wealth of information on the complexity of nuclear structure, dynamics, and reaction mechanisms. Decades of experimental work has provided a vital testbed to assess and validate the theoretical approximations and predictions that propelled theoretical progress. A large dataset of high-precision electron–nucleus scattering exists, meant to study various nuclear physics aspects, covering many nuclei and wide energy ranges corresponding to different reaction mechanisms. While previous and existing electron scattering experiments provide important information, new dedicated measurements whose goals are tied to the needs of neutrino programs are needed. New data can expand relevant kinematic reach, the addition of relevant nuclei, and the information on the final-state hadronic system.

In Table 1, we present a summary of the current and planned electron scattering experiments. These electron scattering experiments are primarily motivated by the needs of the accelerator neutrino experiments. They include complementary efforts that cover a broad range of kinematics and carry a varied level of particle identification and other detection capabilities. The work is mainly carried out with a cross-community effort of nuclear and high-energy physicists. For more information on the details of individual experiments, we refer readers to a recent Snowmass white paper, Ref. [2].

<table>
<thead>
<tr>
<th>Collaborations</th>
<th>Kinematics</th>
<th>Targets</th>
<th>Scattering</th>
</tr>
</thead>
<tbody>
<tr>
<td>E12-14-012 (JLab)</td>
<td>$E_e = 2.222$ GeV</td>
<td>Ar, Ti</td>
<td>$(e,e')$</td>
</tr>
<tr>
<td>(Data collected: 2017)</td>
<td>$15.5^\circ \leq \theta_e \leq 21.5^\circ$</td>
<td>Al, C</td>
<td>$e, p$</td>
</tr>
<tr>
<td></td>
<td>$-50.0^\circ \leq \theta_p \leq -39.0^\circ$</td>
<td>in the final state</td>
<td></td>
</tr>
<tr>
<td>e4nu/CLAS (JLab)</td>
<td>$E_e = 1, 2, 4, 6$ GeV</td>
<td>H, D, He, C, Ar, $^{40}$Ca, $^{48}$Ca, Fe, Sn</td>
<td>$(e,e')$ in the final state</td>
</tr>
<tr>
<td>(Data collected: 1999, 2022)</td>
<td>$\theta_e &gt; 5^\circ$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>LDMX (SLAC)</td>
<td>$E_e = 4.0, 8.0$ GeV</td>
<td>W, Ti, Al</td>
<td>$(e,e')$</td>
</tr>
<tr>
<td>(Planned)</td>
<td>$\theta_e &lt; 40^\circ$</td>
<td></td>
<td>$e, p, n, \pi, \gamma$ in the final state</td>
</tr>
<tr>
<td>A1 (MAMI)</td>
<td>$50$ MeV $\leq E_e \leq 1.5$ GeV</td>
<td>H, D, He, C, O, Ar, Xe</td>
<td>$(e,e')$</td>
</tr>
<tr>
<td>(Data collected: 2020)</td>
<td>$7^\circ \leq \theta_e \leq 160^\circ$</td>
<td></td>
<td>2 additional charged particles</td>
</tr>
<tr>
<td>(More data planned)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>A1 (eALBA)</td>
<td>$E_e = 500$ MeV</td>
<td>C, CH</td>
<td>$(e,e')$</td>
</tr>
<tr>
<td>(Planned)</td>
<td>-few GeV</td>
<td>Be, Ca</td>
<td></td>
</tr>
</tbody>
</table>

The kinematics is presented in Figure 2, where it is overlaid on the regions expected to contain 68% (light shaded) and 95% (dark shaded) of the charged current interactions of muon neutrinos with argon in the DUNE near detector [15], as estimated using GENIE 3.0.6. The e4nu experiment at JLab [16] employs a broad range of energies and has the potential to study a significant phase space of DUNE kinematics. The beam energy of the LDMX experiment at SLAC [17], 4 GeV, closely corresponds to the average neutrino energy in DUNE, and it can perform extensive studies of pion production. The A1 collaboration at MAMI covers a broad range of scattering angles—from $7^\circ$ to $160^\circ$—and beam energies—from $\sim 50$ MeV to 1.5 GeV—and it will be able to perform extensive studies of the quasielastic and $\Delta$ peaks. In these experiments, in general, a lot of attention will be given to measuring exclusive cross-sections.

In Table 2, we present a summary of the current and planned PVES experiments. These experiments probe complementary information for the CEvNS experiment in constraining...
the weak form factor of the nucleus. For tens-of-MeV inelastic neutrino scattering, there is currently no ongoing program, though the potential exists for a lower-energy electron beam at MESA in Mainz. Dedicated electron scattering experiments with targets and kinematics of interest to low-energy neutrino experiments will be crucial in achieving the precision goals of low-energy neutrino programs. For more information, we refer readers to a recent Snowmass white paper, Ref. [2]

![Figure 2](https://example.com/figure2.png)

**Figure 2.** Kinematic coverage of the ongoing and planned electron scattering experiments for electron scattering on targets, including argon and titanium, presented in the (a) (|q|, ω) and (b) (|q|, W) planes. The thin solid dashed and dotted lines correspond to the kinematics of quasielastic scattering, Δ excitation, and the onset of deep-inelastic scattering at W = 1.7 GeV on free nucleons. Figure taken from Ref. [2].

**Table 2.** Parity-violating elastic electron scattering experiments. For more details, please see Ref. [2].

<table>
<thead>
<tr>
<th>Collaborations</th>
<th>Target</th>
<th>q² (GeV²)</th>
<th>A_{pv} (ppm)</th>
<th>±δR_n (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>PREX</td>
<td>$^{208}$Pb</td>
<td>0.00616</td>
<td>0.550 ± 0.018</td>
<td>1.3</td>
</tr>
<tr>
<td>CREX</td>
<td>$^{48}$Ca</td>
<td>0.0297</td>
<td></td>
<td>0.7</td>
</tr>
<tr>
<td>Qweak</td>
<td>$^{27}$Al</td>
<td>0.0236</td>
<td>2.16 ± 0.19</td>
<td>4</td>
</tr>
<tr>
<td>MREX</td>
<td>$^{208}$Pb</td>
<td>0.0073</td>
<td></td>
<td>0.52</td>
</tr>
</tbody>
</table>

5. Summary

Neutrino physics has entered a precision era, and exciting neutrino experimental programs at low and high energies can lead to discoveries. The importance of constraining systematics resulting from neutrino–nucleus interaction physics in key neutrino measurements, in particular in accelerator-based experiments, cannot be overstated. To this end, the electron scattering experiments play a key role in constraining the underlying nuclear physics in nuclear models and event generators intended to be used in neutrino experiments.

Electron and neutrino interactions carry many similarities in underlying relevant physical processes, and electron scattering data collected with precisely controlled kinematics, large statistics, and high precision allow one to constrain nuclear properties and specific interaction processes. Electron scattering data provide the necessary testbed to assess and validate different nuclear models intended to be used in neutrino experiments. While previously existing electron scattering data provide important information, new and proposed measurements whose goals are closely tied to the needs of neutrino programs in terms of expanding kinematic reach, the addition of relevant nuclei, and information on the final-state hadronic system are vital. The NP-HEP cross-community collective efforts are playing a key role in this endeavor.

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