Helical Electron Beam Status Online Evaluation for Magnetron Injection Gun

Wei Jiang 1,*, Chaoxuan Lu 1, Binyang Han 1, Boxin Dai 1, Qiang Zheng 1, Guo Liu 1, Jianxun Wang 1 and Yong Luo 1,2

1 School of Electronic Science and Engineering, University of Electronic Science and Technology of China, Chengdu 610054, China; chaoxuanlu@126.com (C.L.); 202311021709@std.uestc.edu.cn (B.H.); 202311021710@std.uestc.edu.cn (B.D.); qiangzheng@uestc.edu.cn (Q.Z.); liuguo@uestc.edu.cn (G.L.); jxunwang@uestc.edu.cn (J.W.); yluo@uestc.edu.cn (Y.L.)
2 Laboratory of Electromagnetic Space Cognition and Intelligent Control, Beijing 100089, China
* Correspondence: jiangwei@uestc.edu.cn

Abstract: The magnetron injection gun (MIG) is an essential component of the gyrotron traveling wave tube (gyro-TWT). Although the electron beam status influences the performance of the device, it cannot be measured directly in the experiment. An online evaluation module (OEM) for the experiment is developed to calculate the instant beam parameters of MIG. The OEM, by reconstructing the geometry of the MIG and related magnetic field distribution, can obtain the electron beam status under the operating parameters through the online simulation. The beam velocity spread of thermal emission with instant temperature and surface roughness are also considered. The validation is done in a W-band gyro-TWT, and the beam performance is evaluated in the experiment. With a pitch factor of 1.06 electron beam, the velocity spread affected by the electric-magnetic mismatch, thermal emission, and roughness is 1.00%, 0.56%, and 0.43%, respectively. The other beam parameters are also presented in the developed module. The OEM could guide and accelerate the testing process and ensure the safe and stable operation of the device.

Keywords: gyro-TWT; MIG; online evaluation module; electron beam status

1. Introduction

The gyro-devices are the primary high-power source in the millimeter-wave band. It is widely used in plasma heating, high-resolution imaging radar, 5G/6G communication, and advanced spectroscopic techniques [1–4].

The MIG is the crucial component of the gyro-devices, which provides the helical electron beam for the beam-wave interaction. The various types of MIG are investigated by many research institutes. At Karlsruhe Institution of Technology (KIT), series triode MIGs are utilized in the 170 GHz, 2 MW coaxial cavity gyrotron [5–8]. At the Institute of Applied Physics, Russian Academy of Sciences (IAP-RAS), the cusp gun is applied in the Ka-band [9] and W-band [10] helically corrugated waveguide gyro-TWT. A W-band gyro-TWT with a continuous-wave power of 3 kW, a gain of 54 dB, and a bandwidth of 2.5 GHz were reported. The University of California Davis (UC Davis) has developed the gyro-TWTs with the single or double anode MIG cover X-band [11], Ku-band [12], and W-band [13]. The preliminary test of the W-band gyro-TWT obtained an output power of 140 kW, a gain of 60 dB, an efficiency of 22%, and a bandwidth of 2.2 GHz. The Communication Power Industries (CPI) has developed a W-band gyro-TWT with a double anode MIG that demonstrates a peak power of 2 kW at 40% duty cycle and bandwidth of 6.5 GHz [14,15]. At Beijing Vacuum Electronics Research Institute (BVERI), a W-band T_E02 mode gyro-TWT with a triode MIG achieved a peak power of 60 kW, a bandwidth of 8 GHz, and a saturated gain of 32 dB under the 1% duty cycle [16]. At the University of Electronic Science and Technology of China (UESTC), triode and diode MIGs are developed and applied to the
gyro-TWTs covering X [17], Ku [18], Ka [19], Q [20], W [21,22], and G bands [23]. A W-band gyro-TWT with a high duty cycle of 40% and a long pulse width of 2 ms, measured a maximum average power of 20.1 kW. The bandwidth over 10 kW is from 94 GHz to 98 GHz except at the point of 96.5 GHz.

Numerous articles have also reported experimental measurements pertaining to beam characteristics such as the beam pitch factor \( \alpha \), transverse velocity spread \( \Delta \beta \perp \), stability, and concentricity. UC Davis has introduced an axial energy beam analyzer to test \( \alpha \) and axial velocity spread in the gyro-TWT [24]. At IAP-RAS, investigations into the velocity spread and the oscillatory energy of trapped electrons have been conducted, with results indicating a significant impact on beam parameters [25]. Trapped electron mechanisms and emission inhomogeneity are studied at KIT, where experimental results suggest a correlation between gyrotron performance and the presence of trapped electrons [26–28]. Massachusetts Institute of Technology (MIT) explored low-frequency oscillation in a 1.5 MW, 110 GHz gyrotron, measuring oscillations in the range of 165–180 MHz with a capacitive probe [29]. At Huazhong University of Science and Technology (HUST), an 800 GHz gyrotron prototype with a sapphire window was developed to examine the correlation between misalignment and beam trajectory. The blue-violet spot resulting from the beam bombardment on the sapphire serves allows measurement of the beam’s tilt angle and displacement distance [30]. To the authors’ knowledge, there are presently no reports on real-time online evaluation systems for beam status due to the complex operating environment of the gyro-devices, characterized by high vacuum, high voltage, and high magnetic fields. The currently reported methods for measuring beam performance are all based on experimental data obtained in prototype tubes, and the associated devices are relatively expensive and time-consuming.

Due to gyro-TWT processing and assembly errors, the MIG operates under inappropriate parameters, causing the beam state in the experiments to deviate from the simulation. The discrepancy can significantly impact device performance. (1) In high-frequency gyro-TWTs, especially those in the W-band and above, undesirable magnetic field distributions can induce substantial changes in beam pitch factor, velocity spread, and beam guide radius \( R_0 \). (2) Given the thermal cathode structure adopted by the gyro-TWT, an irrational temperature distribution leads to the generation of ionized or sideband-emitted electrons. (3) Excessive cathode surface roughness contributes to an increased velocity spread. Moreover, operating parameters are scanned to identify optimal conditions in previous experiments.

In our group of UESTC, a previously developed automatic test system (ATS) for gyro-TWT [31,32], has proven effective in accomplishing automatic data acquisition during high average/continuous-wave power operation experiments. To enhance the performance and testing efficiency of the gyro-TWT, a beam status online evaluation module (OEM) technology is built upon the ATS. (1) A comprehensive discussion on the impact of electric-magnetic field mismatch, thermal emission spread, and surface roughness emission spread on beam status is conducted, aligning the simulation data more consistently with experimental results. (2) The MIG is remodeled with actual conditions, enabling real-time acquisition of beam status information through the OEM. Utilizing feedback on beam state, external factors affecting beam quality, such as compensation magnetic field, SCM concentricity, and gyro-TWT position, are further adjusted to quickly reach the best performance. (3) A visualization interface is proposed based on the analysis. The OEM technology is validated in a W-band gyro-TWT, and experimental results indicate that the device operates stably for a long time under high power conditions. In comparison with existing testing methods, the proposed OEM technique can calculate the beam quality of the gyro-TWT under various operating conditions in real-time. Furthermore, the OEM technique is universally applicable to all dielectric-loaded gyro-TWTs developed by our group and has undergone experimental verification across the X-band to G-band [17–23].

2. Building of Online Evaluated Module

The schematic of the dielectric-loaded gyro-TWT with a single anode MIG is shown in Figure 1. The gyro-TWT mainly consists of the MIG, RF circuit, collector, input and
output system. The magnetic field consisting of a superconducting magnet (SCM) and compensation coil (CC) guides the helical electron movement. The helical beam is emitted from the cathode and passes through the acceleration and adiabatic compression ranges in the MIG. Then, the beam is transmitted to the RF circuit to interact with the microwave and finally recovered by the collector. The compensation coil is applied to adjust the magnetic field at the cathode to control the final $a$.

![Figure 1. (a) Magnetic field distribution consists of SCM and CC. (b) Schematic configuration of the dielectric-loaded gyro-TWT.](image)

The transverse velocity of the electron at the interaction region $\beta_{\perp}$ can be roughly estimated by Equation (1) [33].

$$\beta_{\perp} \approx \frac{1}{\gamma} \sqrt{F_m} \frac{E_c \cos \theta_c}{B_c}$$

Here $\gamma$ is the relativistic factor, $\theta_c$ is the emission angle, which is determined by the distribution of the electric and magnetic fields. $F_m$ is the magnetic compression ratio. $E_c$ and $B_c$ are the electric and magnetic fields at the emitter, respectively. The detailed status and trajectory of the beam can be calculated by electron optics software EGUN V3.799.

The factors influencing the velocity spread in the experiment can be classified into three types which are static electric and magnetic fields and trajectory of the beam can be calculated by electron optics software EGUN V3.799.

The total transverse spread $\Delta \beta_{\perp}$ can be evaluated by Equation (2) [33].

$$\Delta \beta_{\perp} = \sqrt{(\Delta \beta_{\perp})_{\text{mis}}^2 + (\Delta \beta_{\perp})_{\text{rough}}^2 + (\Delta \beta_{\perp})_{\text{thermal}}^2}$$

The $(\Delta \beta_{\perp})_{\text{mis}}$ is caused by the $E_c$ and $B_c$ distribution on the cathode and could be calculated by Equation (3). Here $n$ is the number of electrons. The lower $(\Delta \beta_{\perp})_{\text{mis}}$ can be guaranteed by adjusting the $E_c$ and $B_c$ at the emitter, which could be optimized in the electron optics design.

$$(\Delta \beta_{\perp})_{\text{mis}} = \sqrt{\frac{\sum (\beta_{\perp} - \bar{\beta}_{\perp})^2}{n}} / \bar{\beta}_{\perp}$$

However, the other two mechanisms are not considered during the electron trajectory analysis. They can be evaluated by Equations (4) and (5) [34].

$$(\Delta \beta_{\perp})_{\text{thermal}} = \frac{1}{\bar{\beta}_{\perp}} \sqrt{\frac{kT_c F_m}{\gamma m_0}}$$
(\Delta \beta_\perp)_{\text{rough}} = \frac{0.4}{\beta_\perp} \sqrt{\frac{2eE_cR_aF_m}{\gamma m_0}}

Here \( \epsilon \) and \( m_0 \) are the electron charge and mass. \( T_e \) is the emitter temperature, and \( k \) is the Boltzmann constant. \( R_a \) is the radius hemispherical bump on the cathode surface.

The experimental test system setup of gyro-TWT is shown in Figure 2. The testing process and parameters related to MIG are discussed here. The ATS controls the test instruments through the programmable logic controller (PLC). (1) The power supply provides the filament voltage \( (V_f) \) and filament current \( (I_0) \), which could heat the cathode. (2) The voltage on the cathode is \( V_0 \), then the beam current \( I_0 \) is emitted. (3) The magnetic field amplitude is determined by the SCM current \( (I_e) \) and CC current \( (I_i) \). The relative axial position between gyro-TWT and SCM \( (H) \) is adjusted to change the relative magnetic ratio for the RF circuit and MIG. (4) The beam obtains a special \( \alpha \) at the entrance of the RF circuit, then interacts with the microwave. The water load is a crucial component of the power detection device. By monitoring the liquid temperature, the output power of the gyro-TWT can be calculated. The frequency was measured by the spectrometer. The optimal output status of the gyro-TWT will be achieved by sweeping parameters like \( H, V_0, I_0, \) and \( B_z \).

![Figure 2. The experimental testing system. 1—Gyro-TWT; 2—Super-conducting magnet; 3—Compensation coil; 4—Fuel tank of power supply and 5—MIG.](image)

The deviated parameter from the MIG design can lead to an unknown beam status. So, the beam status is necessary to be evaluated to guide the test. In the experiment, the gyro-TWT is tested under the control of ATS, the experimental data such as beam voltage, beam current, and magnetic field are automatically acquired by the ATS and stored in the database. Then, combined with the data, such as temperature, and fabrication size of MIG, measured before assembly, the beam status of MIG is calculated by OEM. The specific implementation details of OEM technology are discussed below.

As shown in Figure 3, when the testing status changes, the OEM reads the operating parameters and then simulates and calculates the new beam status. (1) The electric and magnetic fields for the operating MIG are rebuilt according to instant operating parameters. Then, the trajectory is quickly simulated by the electron optics software. The beam status, such as \( \alpha, (\Delta \beta_\perp)_{\text{mis}}, R_0 \), is evaluated. (2) The instant \( T_e \) is evaluated, and \( (\Delta \beta_\perp)_{\text{thermal}} \) is calculated. (3) Read the roughness data and calculate \( (\Delta \beta_\perp)_{\text{rough}} \). Finally, the beam status is online feedback and presented to the tester. The results calculated by OEM can represent the actual beam status in the experiment. With reference to the assessed beam quality, adjustments to input parameters, such as \( H, V_0, I_0, \) and \( B_z \), are made to further enhance the device’s performance while ensuring safe operation.
Due to the requirement for quick feedback, some complex experimental statuses are simplified in OEM. (1) The 2D electric optics software is utilized. The axisymmetric misalignment induced by installation between gyro-TWT and SCM is ignored. (2) The trapped electron from magnetic adiabatic compression is considered, but those from ionization and secondary electrons are neglected. Although the above effects on electron performance are not considered, it has little effect on the status of the main electron beam. The evaluation could also support the optimal status searching of gyro-TWT in the experiment. The detailed process is discussed below.

2.1. Online Trajectory Simulation and Evaluation

The online electron trajectory simulation is realized based on the electron optics software EGUN. The trajectory simulation needs the MIG geometry, operating electric parameters, and magnetic field distribution. The OEM communicates with the testing system and instantly achieves related data, such as the fabrication data, \( V_0 \), \( I_0 \), \( I_s \), \( I_t \), and \( H \).

The detailed online simulation and evaluation process of the beam status is shown in Figure 4. First, the MIG geometry is updated based on the fabrication error of each part and axial deviation in the assembly. Then, it is transferred to the simulation input files.

Second, the actual operating \( V_0 \) and \( I_0 \) fluctuate over time. The instantaneous values of those parameters are applied in the online simulation.

Third, the magnetic field distribution is determined by the SCM and CC, as shown in Figure 1a. \( I_s \) and \( I_t \) is the current of SCM and CC. The operating distribution is the linear combination of these two coils and could be calculated by Equation (6). Here \( B_s(z) \) and \( B_t(z) \) are the normalized magnetic distribution of SCM and CC.

\[
B(z) = I_s \times B_s(z) + I_t \times B_t(z)
\]  

Then, we need to confirm the \( B_c \) of MIG. The magnet plant is set as the base point. The gyro-TWT will axially displace to adjust the magnetic field of the RF circuit or MIG. The cathode position in the magnetic field also varies. The cathode coordinate \( z_c \) could be calculated by Equation (7).

\[
z_c = H - \Delta z
\]
$\Delta z$ is the distance from the beam emitting strip of the cathode to the gyro-TWT reference point. And the magnetic compression ratio $F_m$ could be calculated by Equation (8). Then, the cathode coordinate is confirmed in the magnetic field.

$$F_m = \frac{\max(B(z))}{B(z_c)} \quad (8)$$

After all of the above data is written to the input files, the trajectory simulation automatically runs. After several seconds, the electron trajectory is given, as shown in Figure 5. The instant beam parameters such as $\alpha$, $(\Delta \beta_\perp)_{mis}$, $R_0$, and Larmor radius ($R_L$) can be calculated.

![Figure 4. Process of electron beam status online simulation and evaluation.](image)

![Figure 5. Online simulation for beam trajectory.](image)

The developed online evaluation process was utilized and validated in a W-band gyro-TWT experiment. Figure 6a gives the beam status variation in testing by online simulation. The changing of $V_0$, $I_0$, $I_t$, $F_m$, $\alpha$, $(\Delta \beta_\perp)_{mis}$, and peak output power ($P_{out}$) are presented. $V_0$, $I_0$, and $I_t$ were read from the testing system instantly. $P_{out}$ and spectrum were measured by a high-power water load and spectrometer, respectively. $F_m$, $\alpha$, $(\Delta \beta_\perp)_{mis}$ are calculated by the OEM.
At Stage 1, $V_0$ was applied gradually to the MIG, leading to a concurrent increase in both $I_0$ and $\alpha$. Upon reaching Stage 2, $V_0$ and $I_0$ attained the designated working values, with an evaluated $\alpha$ of about 1.11 and a measured $P_{\text{out}}$ of 122 kW. The gyro-TWT operated stably, and the spectrum of the output signal was pure, as depicted in Figure 6b. Moving to Stage 3 involves adjusting $I_0$ to modify $F_m$, causing a reduction in $\alpha$ to 1.05. Correspondingly, $P_{\text{out}}$ decreased to 108 kW. At stage 4, $\alpha$ was further diminished to 1.0, leading to a rapid reduction in $P_{\text{out}}$ to 47 kW. However, at stage 5, due to the increase in compensation current, the beam pitch factor increases, resulting in oscillations and power degradation. The corresponding oscillation frequency was noted to be at 85.1 GHz, as shown in Figure 6c. The realization of online beam status evaluation in the experiment enhances the transparency and safety of the testing process. It should be noted that the beam–wave interaction status of the gyro-TWT is not at the optimal frequency point for testing the evaluation module.
2.2. Thermal Emission Spread Evaluation

A thermal cathode structure is employed in the gyro-TWT, and the beam quality was influenced by the temperature distribution of the cathode, as mentioned in Equation (4). An inhomogeneous temperature distribution on the cathode surface can give rise to phenomena such as sideband electron emission, making the device unable to operate stably. The emitter operating temperature \( T_e \) is about 1050 °C. However, the actual \( T_e \) was hard to detect because of the vacuum environment and high voltage in an enclosure MIG. The temperature evaluation method by heating power \( (P_{\text{heat}}) \) is utilized. The detailed process flow is shown in Figure 7. The relationship between \( T_e \) and \( P_{\text{heat}} \) was simulated and stored in the database. Then, according to the instant \( V_f \) and \( I_f, T_e \) was evaluated. Finally, the \( (\Delta\beta_{\perp})_{\text{thermal}} \) was calculated.

![Figure 7. Process of \( (\Delta\beta_{\perp})_{\text{thermal}} \) evaluation.](image)

Before the assembly of the MIG into the gyro-TWT, thermal analysis and temperature distribution tests are conducted on the cathode, as shown in Figure 8. Utilizing a reasonable filament winding method, an obvious temperature gradient was established between the emitter and the rear and front electrodes. \( T_e \) reaches 1043 °C when \( P_{\text{heat}} \) is 22.5 W in the simulation. The temperature difference between the front and rear electrodes is 130 °C and 337 °C, respectively. The fabricated cathode was enveloped in the glass shield and heated, as shown in Figure 8b. The temperature was measured using an infrared thermometer, and the simulated and measured temperature deviations are shown in Figure 8c. The results indicate that the temperature deviation at each point is less than 0.6%.

![Figure 8. (a) Thermal analysis in the simulation. (b) Heated cathode. (c) Temperature deviation.](image)
The relationship between $T_c$ and $P_{\text{heat}}$ is shown in Figure 9. $T_c$ higher than 850 °C is recorded in the experiment because of the measuring range of the infrared thermometer. The measurement result matches well with the simulation, and the maximum deviation is about 5% at 1200 °C. The $T_c$–$P_{\text{heat}}$ curve is stored in the database and employed to evaluate the operating $T_c$ in testing.

![Figure 9. $T_c$ varies with heat power.](image)

The fundamental principle of filament heating is shown in Figure 10. Here, $R_f$ represents the filament resistance, which is influenced by $T_c$. $R_1$ denotes the contact resistance induced by the assembly and is measured before testing. During MIG operation, $V_f$ and $I_f$ are loaded, and the effective $P_{\text{heat}}$ can be estimated by Equation (9). Subsequently, the operating $T_c$ can be evaluated through the $T_c$–$P_{\text{heat}}$ curve. Through a synergistic approach involving both experimentation and simulation, the emitter temperature was estimated quickly based on the filament heating power.

$$P_{\text{heat}} = I_f \cdot V_f - I_f^2 \cdot R_1$$  \hspace{1cm} (9)

![Figure 10. Equivalent thermal circuit of cathode heating.](image)

$T_c$ evaluation is validated in the W-band MIG. The measured $R_1$ is about 0.03 Ω. In Figure 11, the instant $T_c$ is calculated as the heating power increases. When $P_{\text{heat}}$ is 22.6 W, $T_c$ reaches 1047 °C. Then, the instant $(\Delta \beta_\perp)_{\text{thermal}}$ could be calculated using 4. Here, $F_{\text{me}}, \gamma$ and $\beta_\perp$ are read from the synchronized trajectory simulation.

![Figure 11. Temperature evaluation in the experiment.](image)
2.3. Roughness Spread Evaluation

\((\Delta \beta_\perp)_{\text{rough}}\) depends on the surface roughness \(R_a\) in the fabrication process, and the evaluation process is shown in Figure 12a. The surface roughness of various cathodes has been measured prior to assembly and stored in the database. An emitter sample was measured by an Atomic Force Microscope (AFM), as shown in Figure 12b. \(R_a\) was about 23 nm for this cathode type under the current fabrication process. \(R_a\) is stored in the OEM, and the instant \((\Delta \beta_\perp)_{\text{rough}}\) is calculated using 5. The rest of the parameters are also read from the synchronized trajectory simulation.

\[
\Delta \beta_\perp = \beta_\perp - \beta_\perp^\text{ref}
\]

Figure 12. (a) Process of \((\Delta \beta_\perp)_{\text{rough}}\) evaluation. (b) Emitter sample. (c) Roughness measurement by AFM.

Finally, the total beam velocity spread \(\Delta \beta_\perp\) was calculated using 2. After the entire electron beam parameters are evaluated, the results are fed back and presented to the user interface. It could guide the optimal testing process and make it more scientific.

3. Evaluation of Experiment

To validate the feasibility of the OEM technology in the context of the W-band gyro-TWT, a test platform is established, and the OEM is integrated into the system, as shown in Figure 13. The system consists of the testing controlling platform, PLC, testing instruments, and gyro-TWT. The controlling platform sends the test order to the instruments through PLC. Then, the electric parameters and input signal are applied to the gyro-TWT. The OEM is deployed on the testing controlling platform.

Figure 13. OEM validation experiment setup.

After considering the impact of electric-magnetic field mismatch, thermal emission spread, and surface roughness emission spread on the beam status, a visualization interface
The accuracy of OEM technology can be further improved by taking into account the influence of other factors. First, (1) the axial misalignment from fabrication and assembly is ignored due to the 2D trajectory simulation. Then, (2) the emission inhomogeneity and side-band emission are also neglected. The actual velocity spread and the maximum beam radius are larger than the evaluated result. Next, (3) if the low-frequency oscillation occurs, the backstream bombardment electron heats the cathode. The evaluated temperature is inaccurate. A novel method of measuring filament resistance by varying temperatures will be considered in the future to improve accuracy. Finally, (4) the surface roughness of the emitter will deteriorate after a long operation due to the ionization and backstream electron bombarding the cathode. The estimated roughness spread is smaller than the actual value.

Despite the above limitations, the OEM technology also provides useful instant electron beam information in operation, which guides the testing of the gyro-TWTs. First, the gyro-TWT is often designed to operate in an extensive range of voltage (45~60 kV) and current (3~10 A) for different applications. A significant margin adjustment may lead to an unwanted velocity ratio or electron trapping. The OEM presents the instant beam status, which could ensure the MIG operates in a reasonable scope. Second, the instant operating parameters of MIG are obtained from the testing system. Subsequently, online evaluation is conducted, and the results are presented in the left area. The test duration for gyro-TWTs in our group typically exceeds one hour, and the evaluation results experience only a minimal delay of about 8 s due to trajectory simulation. This delay is acceptable for real-time results. The W-band gyro-TWT is driven by a 59.8 kV-10.4 A electron beam with a $B_0$ of 3.61 T and an $F_m$ of 17.1. The operating $T_e$ is ~965 °C. The corresponding $\alpha$ is 1.06, with velocity spread of $(\Delta\beta_{\perp})_{\text{mix}}$, $(\Delta\beta_{\perp})_{\text{thermal}}$, and $(\Delta\beta_{\perp})_{\text{rough}}$ at 1.00%, 0.56%, and 0.43%, respectively. The total $\Delta\beta_{\perp}$ is 1.23%. The guide center radius $R_0$ is about 1.00 mm, while the maximum beam radius is 1.29 mm. The beam status varies with the time presented in the right area. It indicates the beam status could be instantly evaluated when adjusting the MIG parameters such as $F_m$, and $I_0$, $\alpha$.

Figure 14. The W-band gyro-TWT evaluation results in the OEM interface.

The accuracy of OEM technology can be further improved by taking into account the influence of other factors.
4. Conclusions

An online evaluation module for helical electron beam status is developed. The instant operating parameters for MIG are achieved from the testing system. The geometry and magnetic field are rebuilt and connected according to the corresponding parameters to realize the online trajectory simulation. The electron beam status is calculated after the online trajectory simulation. The velocity spread considering thermal emission and surface roughness is also evaluated. The OEM has been validated in a W-band gyro-TWT experiment. The evaluated $a$ is 1.08, $R_0$ is 1.00 mm, three-velocity-spread of $(\Delta \beta_\perp)_{\text{miss}}$, $(\Delta \beta_\perp)_{\text{thermal}}$, and $(\Delta \beta_\perp)_{\text{rough}}$ is 1.00%, 0.56%, and 0.43%, respectively. And the calculated total $\Delta \beta_\perp$ is 1.23%. Instant electron status evaluation could guide and accelerate the testing process. And the OEM is already utilized in a series of gyro-TWTs testing.

Author Contributions: Conceptualization, W.J.; methodology, C.L., B.H., B.D., Q.Z., G.L., J.W. and Y.L.; writing—original draft, W.J. and C.L.; writing—review and editing, W.J. and Y.L. All authors have read and agreed to the published version of the manuscript.

Funding: This research was funded by the Sichuan Science and Technology Program under Grant 2022YFSY0063.

Data Availability Statement: All data included in this study are available upon request by contacting with the corresponding author.

Conflicts of Interest: The authors declare no conflicts of interest.

References


25. Tsimring, S.E.; Zapevalov, V.E. Experimental study of intense helical electron beams with trapped electrons. *Int. J. Electron. 1996*, 81, 199–205. [CrossRef]

26. Ruess, S. *Pushing the KIT 2 MW Coaxial-Cavity Short-Pulse Gyrotron towards a DEMO Relevant Design*; KIT Scientific Publishing: Baden-Württemberg, Germany, 2021. [CrossRef]


