A Hybrid Triple Collocation-Deep Learning Approach for Improving Soil Moisture Estimation from Satellite and Model-Based Data

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Abstract: Satellite retrieval and land surface models have become the mainstream methods for monitoring soil moisture (SM) over large regions; however, the uncertainty and coarse spatial resolution of these products limit their applications at the regional and local scales. We proposed a hybrid approach combining the triple collocation (TC) and the long short-term memory (LSTM) network, which was designed to generate a high-quality SM dataset from satellite and modeled data. We applied the proposed approach to merge SM data from Soil Moisture Active Passive (SMAP), Global Land Data Assimilation System-Noah (GLDAS-Noah), and the land component of the fifth generation of European Reanalysis (ERA5-Land), and we then downscaled the merged SM data from 0.36° to 0.01° resolution based on the relationship between the SM data and auxiliary environmental variables (elevation, land surface temperature, vegetation index, surface albedo, and soil texture). The merged and downscaled SM results were validated against in situ observations. The results showed that: (1) the TC-based validation results were consistent with the in situ-based validation, indicating that the TC method was reasonable for the comparison and evaluation of satellite and modeled SM data. (2) TC-based merging was superior to simple arithmetic average merging when the parent products had large differences. (3) Downscaled SM of the TC-based merged product had better performance than that of the parent products in terms of ubRMSE and bias values, implying that the fusion of satellite and model-based SM data would result in better downscaling accuracy. (4) Downscaled SM of TC-based merged data not only improved the representation of the SM spatial variability but also had satisfactory accuracy with a median of R (0.7244), ubRMSE (0.0459 m\(^3\)/m\(^3\)), and bias (−0.0126 m\(^3\)/m\(^3\)). The proposed approach was effective for generating a SM dataset with fine resolution and reliable accuracy for wide hydrometeorological applications.

Keywords: soil moisture; merging; spatial downscaling; triple collocation; long short-term memory

1. Introduction

Soil moisture (SM) is a critical hydrological variable that links the water, energy, and carbon cycles between the land and atmosphere and plays a fundamental role in many hydrological, ecological, and biogeochemical processes [1,2]. Accurate and detailed information on SM have been increasingly important to a wide range of applications, such as drought monitoring [3], flood forecasting [4], agricultural production [5], carbon cycle [6], and water resource management [7]. SM spatial variability is associated with meteorological, topographic, pedologic, and vegetative factors, the complex interactions between these factors lead to high spatial heterogeneity in SM [8,9]. Therefore, deriving accurate SM information at fine spatial scales is challenging.
SM data are traditionally acquired from in situ measurements, which can provide reliable SM information at specific locations, times, and soil layers. However, in situ measurements at a single point make it difficult to represent SM over a large area [10]. In addition, the observation process is laborious [1]. Microwave (active and passive) remote sensing has shown promise in SM observations, such as the Advanced Scatterometer ( ASCAT) [11], Soil Moisture and Ocean Salinity (SMOS) [12], the Soil Moisture Active Passive (SMAP) mission [13], and Global Navigation Satellite System-Reflectometry (GNSS-R) SM retrievals [14]. Satellite-based SM products can acquire spatially continuous SM estimates of the surface soil layers (0–5 cm) on a large scale. However, their performances depend on the underlying conditions, sensor specifications, and retrieval algorithms [15,16]. Land surface models (LSMs) may serve as alternative ways to monitor SM with spatial completeness and temporal continuity globally. For example, the Global Land Data Assimilation System (GLDAS) [17] and the global dataset for the land component of the fifth generation of European Reanalysis (ERA5-Land) [18] provide SM estimates at various depths and time scales. Nevertheless, these LSM-based SM products are associated with uncertainties due to model parameterization and forcing data [19,20].

Given the strengths and weaknesses of each source of SM data, merging ground measurements, satellite, and modeled SM products would reduce uncertainty and improve SM estimates [21–24]. Data assimilation is one of the most widely used approaches for combining products from different sources. However, inadequate or incorrect prior knowledge of the uncertainties associated with SM products has limited the use of data assimilation. Additionally, data assimilation is complex and computationally expensive [25,26]. Statistical methods are alternative ways to directly merge multi-source SM products. Triple collocation (TC) is a method used for evaluating the unknown errors of three mutually independent datasets without the need for an additional reference dataset [27]. TC analysis has been widely used to evaluate SM data from satellites and LSMs [28–30]. Accordingly, the TC-based merging method offers a potential solution for multi-source SM data merging due to its simplicity and transparency [19,21,22,25,31].

Regional hydrometeorological studies usually require SM data with high spatial resolution. However, satellite or model-based SM products usually have low spatial resolution. Therefore, various methods have been introduced to downscale SM at fine spatial scales. These downscaling methods can be broadly classified into three groups: (1) satellite-based methods including active and passive microwave data fusion and optical/thermal and microwave data fusion [32–35]; (2) methods using geoinformation data, such as topography, soil attribute, and vegetation characteristics [36–39]; and (3) statistical and physical model-based methods [40–43]. Although the above-mentioned methods differ in the type of input data and the characteristics of the scaling model, the essence was to establish statistical correlations or physics-based models between coarse spatial SM and auxiliary variables [44]. Therefore, constructing a relationship model to well describe the complex nonlinear relationship between SM and auxiliary variables was still a major task in most downscaling methods [10].

Recently, machine learning (ML) techniques, such as support vector machines, classification, regression trees, Bayesian, random forest, and artificial neural networks have been widely applied in the field of SM downscaling because of their superior intelligence capabilities [10,36–39,45]. Compared with some traditional ML algorithms, state-of-the-art deep learning algorithms have better data fitting and generalization capabilities [46,47]. Powerful deep learning algorithms, such as convolutional neural networks (CNNs) and long short-term memory networks (LSTM), have attracted broad attention to SM prediction [48,49].

To summarize, this study aims to present a hybrid merging and downscaling approach based on the TC analysis and LSTM model, which was designed to generate a high-quality SM dataset at 0.01° resolution and a monthly temporal interval from satellite and modeled data. The main objectives of this study were: (1) to merge the SMAP, GLDAS-Noah, and ERA5-Land SM data based on the TC analysis; (2) to downscale the merged SM data using the LSTM network based on the environmental variables data; and (3) to evaluate
the performance of merging and downscaling methods using in situ observations. Our work will be beneficial for future research involving estimations of high-resolution SM datasets with reliable accuracy in much wider hydrometeorological applications at regional or local scales.

2. Study Area and Data

2.1. Study Area

Yunnan province is located in the southwestern region of China, which has an area of approximately 394,000 km² (21°08′–29°15′N, 97°31′–106°11′E) (shown in Figure 1). The climate belongs to the subtropical plateau monsoon and is characterized by distinct dry and wet seasons [50]. Accordingly, precipitation falls during the monsoon season (May–October), accounting for 85% of the total annual precipitation (approximately 1100 mm) [51]. The elevation varies from 6740 to 76 m and decreases from the northwest to the southeast. The mean annual temperature ranges from 5.52 to 23.88 °C, and the mean annual precipitation varies from 560 to 2300 mm [52]. There are many large rivers, such as the Salween, Mekong, Red, Yangtze, and Pearl River, flowing through or originating from this area, which is also an important ecological defense construction area in China. However, increasingly frequent droughts have caused huge socioeconomic losses over the past two decades [52,53]. For example, a record-breaking and persistent drought hit Yunnan from autumn 2009 to spring 2010, resulting in 7.57 million residents suffered from a lack of drinking water. Approximately 21,741 km² of crops planted in autumn and winter were affected by drought, and the direct agricultural loss exceeded RMB 20 billion [52]. Therefore, SM data derived from multi-sources with fine resolution are necessary for regional drought monitoring.

2.2. Data

2.2.1. SM Data

The SMAP satellite was launched in 2015, carrying an L-band radiometer and radar (non-imaging SAR), which is devoted to providing a global surface (0–5 cm) volumetric SM with a spatial resolution of 36, 9, and 3 km at local overpass times of 06:00 AM (descending orbit) and 06:00 PM (ascending orbits), respectively. Unfortunately, owing to the failure of the radar, only SM from the radiometer is available [54]. The SM data used here was, “SMAP L3 Radiometer Global Daily 36 km EASE-Grid Soil Moisture, Version 7 (L3SMP)”. The L3SMP SM at ascending and descending modes were averaged to obtain daily SM. The L3SMP data were collected from January 2016 to December 2020.

ERA5-Land, a reanalysis dataset released by the European Center for Medium-Range Weather Forecasts (ECMWF), was produced by replaying the land component of the ERA5 data and combining model data with global observations using laws of physics [18]. ERA5-Land includes four layers of SM estimates including 0–7, 7–28, 28–100, and 100–289 cm, which have been available from 1950 to present with a spatial resolution of 0.1° × 0.1° and
an hourly temporal resolution. The SM estimate of the top layer (0–7 cm) was used in the current study.

GLDAS generates optimal fields of land surface states by combining satellite data and ground data and utilizing sophisticated land surface modeling and data assimilation methods [17]. GLDAS runs multiple surface models, such as Noah, Mosaic, Community land, and variable infiltration capacity. We obtained the SM estimates from the GLDAS-2.1 Noah model (hereafter GLDAS) with a 0.25° × 0.25° and 3-hourly/monthly resolutions. The GLDAS provides four-layer SM estimates, including 0–10, 10–40, 40–100 and 100–200 cm; the SM estimate at a depth of 0–10 cm was used in the current study.

In situ SM data were collected from 36 automatic measurement stations in Yunnan province (Figure 1), which were obtained from the Yunnan Meteorological Service. These stations provide hourly SM values at different soil depths. In order to match the satellite and modeled SM products, in situ SM data at soil depths of 0–10 cm were used and the time intervals were resampled into monthly average values.

2.2.2. Auxiliary Data

Four Terra Moderate Resolution Imaging Spectroradiometer (MODIS) products were used here, including the monthly normalized difference vegetation index (NDVI) (MOD13A2) product, 8-day land surface temperature (LST) product (MOD11A1), 8-day surface reflectance product (MOD09A1), and yearly land cover type product (MCD12Q1). For LST, the daytime and nighttime LSTs were averaged to obtain daily SM. The surface reflectance product was used to calculate the surface albedo [55]. The outliers of surface reflectance, LST, and NDVI were first eliminated based on the quality flag. Furthermore, null values were interpolated using the Savitzky–Golay (S–G) filter [56]. The land cover type product was utilized here to identify the pixels classified as water bodies and ice/snow. The pixels classified as water and ice/snow were excluded in the analysis. In addition, elevation data with a spatial resolution of 90 m was obtained from the Shuttle Radar Topography Mission (SRTM) [57]. Soil texture is defined as the content of clay, silt, and sand per unit volume of soil mass, which were acquired from the Harmonized World Soil Database (HWSD) [58]. In addition to the above data, precipitation data were adopted to assist the intercomparison of downscaled SM data. The Climate Hazards Group Infrared Precipitation with Stations (CHIRPS) is a 40-year (from 1981 to present) rainfall dataset, which covers most regions of the world (50°S–50°N) [59]. Here, the 0.05° × 0.05° CHIRPS monthly precipitation datasets were used from 2016 to 2020.

2.2.3. Data Preprocessing

Table 1 lists the SM and auxiliary data used in this study. As the SM and auxiliary data adopted have different resolutions, we established a unified standard for data preprocessing. The georeference of all grid data were set as GCS-WGS-1984. SMAP, ERA-land and GLDAS SM data were resampled to a spatial resolution of 0.36° using the nearest neighbor method. All SM data were averaged to the temporal resolution of a month. The units of all SM data were volume water content (m³/m³). MODIS products were reprojected to the GCS-WGS-1984 coordinate system using the MODIS Reprojection Tool. NDVI, LST, surface albedo, elevation and soil texture were resampled to 0.36° and 0.01°, respectively. In addition, the monthly LST and surface albedo were generated by using the weighted temporal average based on the 8-day LST and 8-day surface albedo in a one month window, respectively. To facilitate comparison, a common period of record from January 2016 to December 2020 was used for all datasets.
Table 1. List of data used in this study.

<table>
<thead>
<tr>
<th>Type</th>
<th>Datasets</th>
<th>Index</th>
<th>Resolution</th>
</tr>
</thead>
<tbody>
<tr>
<td>SM data</td>
<td>SMAP</td>
<td>Surface SM</td>
<td>36 km (~0.36°), daily</td>
</tr>
<tr>
<td></td>
<td>ERA5-Land</td>
<td>Surface SM</td>
<td>0.1°, hourly</td>
</tr>
<tr>
<td></td>
<td>GLDAS v2.1/Noah</td>
<td>Surface SM</td>
<td>0.25°, monthly</td>
</tr>
<tr>
<td></td>
<td>In situ</td>
<td>Surface SM</td>
<td>Point, hourly</td>
</tr>
<tr>
<td></td>
<td>MOD09A1</td>
<td>Surface albedo</td>
<td>500 m (~0.005°), 8-day</td>
</tr>
<tr>
<td></td>
<td>MOD11A2</td>
<td>LST</td>
<td>1 km (~0.01°), 8-day</td>
</tr>
<tr>
<td></td>
<td>MOD13A3</td>
<td>NDVI</td>
<td>1 km (~0.01°), monthly</td>
</tr>
<tr>
<td></td>
<td>MCD12Q1</td>
<td>Land Cover Type</td>
<td>500 m (~0.005°), yearly</td>
</tr>
<tr>
<td></td>
<td>CHIRPS</td>
<td>Precipitation</td>
<td>0.05°, monthly</td>
</tr>
<tr>
<td></td>
<td>SRTM</td>
<td>Elevation</td>
<td>90 m (~0.0009°), –</td>
</tr>
<tr>
<td></td>
<td>HWSD</td>
<td>Content of clay, sand, and silt</td>
<td>0.0083°, –</td>
</tr>
</tbody>
</table>

3. Methodology

We proposed a hybrid approach combining the TC and LSTM, which was designed to generate a high-quality SM dataset from satellite and modeled data. Figure 2 shows the flowchart of the hybrid approach. This approach includes two steps: (1) SM merging, SMAP, GLDAS, and ERA5-Land SM products are merged by combining the product errors obtained from the TC analysis and the least-squares framework in every pixel [22]; (2) spatial downscaling. The idea was to establish a statistical relationship between the low spatial resolution SM data and environmental variables using LSTM, and then input high spatial resolution environmental variables into verified LSTM to obtain the downscaled SM [44]. The specific process of downscaling can be described as follows:

I. The relationship between the environmental variables and the SM data at a low spatial resolution (0.36°) was established using the LSTM network.

\[ SM_o = f_{LSTM}(LST, NDVI, surface\ albedo, elevation, soil\ texture) + \epsilon \] (1)

where \( SM_o \) denotes original SM data, \( f_{LSTM} \) is a nonlinear function by establishing a relationship between the variables and \( SM_o \), and \( \epsilon \) is residual, which represents the amount of SM that could not be predicted by LSTM.

II. The LSTM network established in step (I) and the variables at 0.36° scale were applied to predict SM (\( SM_{LSTM} \)). By subtracting the predictive values from \( SM_o \), the residuals at the 0.36° scale were obtained.

\[ \epsilon = SM_o - SM_{LSTM} \] (2)

III. The residuals (\( \epsilon \)) were spatially interpolated to form residual maps at a 0.01° resolution (\( \epsilon_k \)) using the simple Kriging technique.

\[ \epsilon_k = \sum_{i=1}^{n} \lambda_i \epsilon_i \] (3)

where \( \lambda_i \) are Kriging weights, and \( \epsilon_i \) is the residual at location \( i \).

IV. High spatial resolution variables were entered into the LSTM network established in step (I), and a predicted SM of 0.01° resolution (\( SM_{LSTMH} \)) was achieved.

V. The final downscaled SM (\( SM_{Final} \)) were obtained by adding the residual term to the predicted SM.

\[ SM_{Final} = SM_{LSTMH} + \epsilon_k \] (4)
3.1. TC Analysis

TC [27] is a statistical method used for estimating the random error variance of three datasets required with independent errors [60]. A commonly used error model in the TC approach has the following form:

$$SM_i = SM'_i + \epsilon_i = \alpha_i + \beta_i T + \epsilon_i, \quad (5)$$

where $SM_i$ (i.e. {1, 2, 3}) is the value from the three collocated SM datasets linearly related to $T$, which represents the actual SM value, with random errors $\epsilon_i, \beta_i$, and $\alpha_i$ as the bias and scale factors.

We assumed that the errors from independent datasets had zero mean ($E(\epsilon_i) = 0$), and they were uncorrelated with each other ($\text{Cov}(\epsilon_i, \epsilon_j) = 0, i \neq j$) and $t(\text{Cov}(\epsilon_i, T) = 0)$. Therefore, the covariances between the different SM datasets are expressed as follows:

$$C_{ij} = \text{Cov}(SM_i, SM_j) = \begin{cases} \beta_i \beta_j \sigma_T^2, & i \neq j \\ \beta_i^2 \sigma_T^2 + \sigma_{\epsilon'_i}^2, & i = j \end{cases} \quad (6)$$
where $\sigma_i^2 = \text{Var}(\varepsilon_i)$. Because the number of unknowns (seven) is greater than that of $C$ (six), there is no unique solution to the equations mentioned above. To solve this problem, a new variable is defined as $\theta_i = \beta_i \sigma_T$. Therefore, Equation (6) can be represented by

$$C_{ij} = \begin{cases} \theta_i \theta_j, & i \neq j \\ \theta_i^2 + \sigma_i^2, & i = j \end{cases}$$

(7)

The problem can be solved by using six equations and six variables. The RMSE ($\sigma_e$) was obtained as follows:

$$\sigma_e = \begin{cases} \sqrt{C_{11} - \frac{C_{13} C_{12}}{C_{12} C_{13}}}, \\ \sqrt{C_{22} - \frac{C_{23} C_{12}}{C_{12} C_{13}}}, \\ \sqrt{C_{33} - \frac{C_{13} C_{23}}{C_{12} C_{13}}} \end{cases}$$

(8)

Another extended TC approach was introduced to investigate the correlation with an unknown true SM [61]. $\beta_i$ can be written as:

$$\beta_i = R_{T,SM} \frac{C_{ij}}{\sigma_T},$$

(9)

where $R_{T,SM}$ is the correlation coefficient between and $T$ and $SM_i$. From Equations (6) and (8), the correlations of the SM data are obtained:

$$R_{T,SM} = \pm \begin{cases} \sqrt{\frac{C_{13} C_{23}}{C_{12} C_{13}}}, \\ \text{sign}(C_{13} C_{23}) \sqrt{\frac{C_{13} C_{23}}{C_{12} C_{13}}}, \\ \text{sign}(C_{12} C_{23}) \sqrt{\frac{C_{13} C_{23}}{C_{12} C_{13}}} \end{cases}$$

(10)

which provides important information about the collocation datasets.

### 3.2. Merging Scheme

It is advantageous to merge different SM products to combine the merits of multi-source SM data and minimize random errors. The least squares method is an evaluation theory and has been used in many studies since it was originally published in 1809 by Gauss [62]. The desired SM value of the merged data can be expressed as [22]:

$$\text{SM}_{\text{Aver}} = w_1 \text{SM}_1 + w_2 \text{SM}_2 + w_3 \text{SM}_3,$$

(11)

where $w_1$, $w_2$, and $w_3$ represent the weights of three SM products: $\text{SM}_1$, $\text{SM}_2$, and $\text{SM}_3$, respectively. To obtain unbiased fusion data, the following is required:

$$w_1 + w_2 + w_3 = 1.$$  

(12)

Based on the above constraints, our goal was to express the weights as a function of the mean square error of the three datasets. Therefore, the mean square errors of the merged data can be expressed as:

$$\sigma_m^2 = w_1^2 \sigma_1^2 + w_2^2 \sigma_2^2 + w_3^2 \sigma_3^2,$$

(13)

which is:

$$\sigma_m^2 = w_1^2 \sigma_1^2 + (1 - w_1 - w_3)^2 \sigma_2^2 + w_3^2 \sigma_3^2.$$  

(14)

Setting $\frac{\partial \sigma_m^2}{\partial w_1} = 0$ and $\frac{\partial \sigma_m^2}{\partial w_3} = 0$ in Equation (15) and solving for $w_1$, $w_2$, and $w_3$, we obtain the following:

$$W_1 = \frac{\sigma_3^2 \sigma_2^2}{\sigma_1^2 \sigma_2^2 + \sigma_1^2 \sigma_3^2 + \sigma_2^2 \sigma_3^2}.$$  

(15)
\[ W_2 = \frac{\sigma_1^2 \sigma_2^2}{\sigma_1^2 \sigma_2^2 + \sigma_1^2 \sigma_3^2 + \sigma_2^2 \sigma_3^2}, \]  
(16) \[ W_3 = \frac{\sigma_1^2 \sigma_2^2}{\sigma_1^2 \sigma_2^2 + \sigma_1^2 \sigma_3^2 + \sigma_2^2 \sigma_3^2}. \]  
(17)

The solution is intuitive because the weights are proportional to the errors of the other two estimates.

### 3.3. LSTM

LSTM was proposed to solve the problem of exploding and vanishing gradients [63]. A common LSTM unit consists of several memory cells, each of which contains three gates (input, output, and forget). These gates control the information that is discarded and retained from the previous moment; therefore, LSTM has an inherent advantage in extracting contextual information, such as temporal characteristics [64]. A memory cell of the LSTM framework can be expressed as

\[ i_t = \sigma(W_i \cdot [h_{t-1}, x_t] + b_i), \]  
(18) \[ f_t = \sigma(W_f \cdot [h_{t-1}, x_t] + b_f), \]  
(19) \[ o_t = \sigma(W_o \cdot [h_{t-1}, x_t] + b_o), \]  
(20) \[ \tilde{C}_t = \tanh(W_c \cdot [h_{t-1}, x_t] + b_c), \]  
(21) \[ C_t = f_t \cdot C_{t-1} + i_t \cdot \tilde{C}_t, \]  
(22) \[ h_t = o_t \cdot \tanh(C_t), \]  
(23)

where \(i_t, f_t, o_t, \) and \(\tilde{C}_t\) represent the three gates and an intermediate state that are input, forget, output gates, and candidate state, respectively, which are the output vectors of the sigmoid layer with a range of 0 to 1. \(C_t\) and \(C_{t-1}\) indicate the cell states delivering information in the current and last moments, respectively, while \(x_t\) indicates the input information at the current moment. \(h_t\) and \(h_{t-1}\) carry the output information of the cells at the current and last moments, respectively. \(W_i, W_f, W_o,\) and \(W_c\) are the parameter matrices to be trained, and \(b_i, b_f, b_o,\) and \(b_c\) are bias items to be trained. In addition, \(\tanh\) is defined as a hyperbolic tangent function in mathematics. First, Equations (19)–(21) are used to determine whether the information from the last moment (\(h_{t-1}\)) and that from this moment (\(x_t\)) is to be retained or not. Then, Equation (23) is used to calculate the result of this moment and pass it to the next moment. More details about LSTM can be found in previous studies [65–67].

Connecting such multiple cells to form more complex structures can solve practical sequence problems. In this study, a two-layer LSTM structure with 80 and 100 cells was used to fit the relationship between the SM data and explanatory variables (LST, NDVI, surface albedo, elevation, and soil texture), which was accomplished using the TensorFlow package of Python. In addition, modeling processes often have the problem of overfitting, which depends on the model structure when the samples are the same. Generally, it can be solved by utilizing the dropout function and the early stopping method [65]. Therefore, in this study, a dropout layer with a parameter of 0.2 was added after each layer of LSTM to discard 20% of the data, in order to avoid overfitting. Additionally, some other parameters also needed to be set. For example, the maximum number of iterations was 200, and the optimizer used was Adam, whose initial learning rate and loss function were set as 0.001 and mean squared error, respectively.

### 3.4. Evaluation Metrics

The accuracy of satellite, modeled, merged, and downscaled SM data were evaluated using in situ data as the reference. In this study, four metrics consisting of the correlation
coefficient (R), root mean square error (RMSE), unbiased root mean square error (ubRMSE), and bias were used [68]. Detailed information on the four metrics is presented in Table 2.

Table 2. The evaluation metrics in this study.

<table>
<thead>
<tr>
<th>Metric</th>
<th>Equation</th>
<th>Range</th>
<th>Best Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>R</td>
<td>$R = \frac{\sum_{i=1}^{n} (SM_{obsi} - \bar{SM}<em>{obs}) \cdot (SM</em>{prei} - \bar{SM}<em>{pre})}{\sqrt{\sum</em>{i=1}^{n} (SM_{obsi} - \bar{SM}<em>{obs})^2 \cdot \sum</em>{i=1}^{n} (SM_{prei} - \bar{SM}_{pre})^2}}$</td>
<td>[0,1]</td>
<td>1</td>
</tr>
<tr>
<td>RMSE</td>
<td>$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (SM_{obsi} - SM_{prei})^2}$</td>
<td>[0, +∞]</td>
<td>0</td>
</tr>
<tr>
<td>ubRMSE</td>
<td>$ubRMSE = \sqrt{\frac{\sum_{i=1}^{n} (SM_{obsi} - \bar{SM}<em>{obs}) - (SM</em>{prei} - \bar{SM}_{pre})^2}{n}}$</td>
<td>[0, +∞]</td>
<td>0</td>
</tr>
<tr>
<td>Bias</td>
<td>$Bias = \frac{\sum_{i=1}^{n} (SM_{obsi} - SM_{prei})}{n}$</td>
<td>[−∞, +∞]</td>
<td>0</td>
</tr>
</tbody>
</table>

$SM_{obs}$ and $SM_{pre}$ represent the $i$th observed values of the site and predicted values, respectively. $\bar{SM}_{obs}$ represents the average of the observed values of the site, whereas $\bar{SM}_{pre}$ represents the average of the predicted value.

4. Results
4.1. TC-Based Assessment

In this study, a satellite product (SMAP) and two modeled products (ERA5-Land and GLDAS) were used in one TC triplet. The TC-based error estimates required three collocated SM datasets that were significantly correlated [21,22]. We evaluated the cross correlation of ERA5-Land, GLDAS, and SMAP using Pearson correlation coefficients (Figure S1). The results showed significant correlations among ERA5-Land, GLDAS, and SMAP over most areas ($p < 0.05$), suggesting a strong mutual linear relationship among the three SM products. Figure 3 displays the spatial distribution of the random error variance and correlation for ERA5-Land, GLDAS, and SMAP products based on TC analysis. The unresolved pixels, due to violation of assumptions in the TC analysis were excluded, which accounted for approximately 14% of the total pixels in the study area. The spatial pattern of the random error variance varied among the different SM products. For example, ERA5-Land had relatively high errors in the northwest region, where the topography is complex. In the central region, the error of the GLDAS was generally relatively low and spatially homogeneous. In addition, SMAP performed better in the northwest and southeast regions. In terms of the correlation, all products showed a high correlation (above 0.8) with the unknown truth in most areas, except in the northwest and southeast regions.

![Figure 3. Spatial distribution of random error variance and correlation obtained from TC analysis.](image-url)
Figure 4 shows a summary of the correlation and random error variance for ERA5-Land, GLDAS, and SMAP products based on TC analysis. At the regional scale, GLDAS showed the highest average correlation with the unknown truth (0.92), followed by ERA-land (0.91) and SMAP (0.88). The error variance was slightly different from the correlation, with the lowest averaged RMSE for GLDAS (0.018 m$^3$/m$^3$), and slightly larger RMSE for SMAP (0.019 m$^3$/m$^3$) and ERA-land (0.021 m$^3$/m$^3$). It can be seen that the GLDAS has the best performance with high correlation and relatively low errors among the three products. This is consistent with previous work reporting that GLDAS outperformed SMAP and ERA5 in root zone SM estimates on a global scale [30].

Figure 4. The box plots of RMSE and R for the three SM products based on TC analysis.

4.2. SM Merging Based on TC

Figure 5 shows the merging weights of ERA5-Land, GLDAS, and SMAP. The spatial distribution of the merging weights was consistent with the random error variance (Figure 3), specifically, the pixels with high RMSE had low weights, while the pixels with low RMSE were assigned high weights. Model-based SM is strongly dependent on externally supplied meteorological forcing data, which can significantly influence SM simulation [69]. In the northwest region with the complex terrain, input precipitation is less reliable, which may explain the less accuracy and low weight of ERA5-Land and GLDAS. In addition, SMAP SM is sensitive to vegetation, higher vegetation intensity will reduce the quality of SM [70]. For instance, the SMAP was assigned low weights in the western and southern regions, which attributed to dense vegetation. Overall, GLDAS had the highest space-averaged weight (0.36), followed by SMAP (0.33) and ERA5-Land (0.31). It can be seen that the merging weights varied among the parent products and showed spatial variability. It is worth noting that the blank areas in the maps, due to violation assumptions in TC analysis, were merged using a simple arithmetic average to increase the coverage of the merged product.

Figure 5. The spatial distributions of merging weights for the parent products.

Figure 6 shows the spatial distributions of the SM for the three parent products and the merged product using TC analysis; the SM levels in January and June 2019 were used
as examples. Generally, the three parent datasets showed distinct spatial differences. For example, ERA5-Land showed much wetter conditions in the southern and eastern regions than GLDAS and SMAP. In theory, the merged data should integrate the characteristics of the three parent products and minimize the errors of the parent products. Although distinct spatial variation was observed in parent products, the merged SM dataset had similar patterns of wet and dry distributions to these parent products, which presented lower SM in the northwestern region, and a general increase in the eastern and southern parts of Yunnan province.

Figure 6. The spatial distributions of three original and merged SM products in January (a) and June 2019 (b).

To evaluate the accuracy of these parent products and the merged products, we compared the SM estimates with the in situ observations. Figure 7 shows box plots of the validation results of different SM datasets at the in situ stations. The median R-values for ERA5-Land, GLDAS, SMAP, and the merged datasets were 0.77, 0.80, 0.79, and 0.84, respectively. The medians of ubRMSE were 0.055, 0.039, 0.040, and 0.039 m$^3$/m$^3$, and the medians of bias were $-0.086$, $-0.014$, 0.038, and $-0.017$ m$^3$/m$^3$ for ERA5-Land, GLDAS, SMAP, and merged datasets, respectively. Among the three parent products, GLDAS had the best performance with the lowest median of ubRMSE and bias and the highest median of correlation, followed by SMAP and ERA5-Land. These results were consistent with those of the TC-based assessment (Figure 4). The highest median R-value and lowest median of ubRMSE from the merged datasets compared with the in situ observations were very encouraging. We found that the median bias of the merged datasets was lower than that of ERA5-Land and SMAP, but the median bias for GLDAS was slightly better than that for the merged datasets. This may be attributed to the parent products having large biases (a median bias of $-0.086$ for ERA5-Land) compared to in situ observations; thus, there may be limited improvements in the merged product. Overall, the merged dataset showed its advantages integrated from satellite and modeled products, indicating that the TC-based merging method can be used to generate high-quality, spatiotemporal continuous SM data from satellite and modeled SM data.
4.3. SM Downscaling Based on LSTM

The downscaling method assumed that the regression relationship between the SM data and auxiliary environmental variables (elevation, LST, NDVI, surface albedo, and soil texture) at a coarse spatial scale (0.36°) was equally effective at a fine scale (0.01°). The first step was to train and verify the LSTM network using the environmental variables sampled from locations where merged SM data (0.36°) were available. In the training process, 70% of the total data were selected randomly as the training set and the other 30% as the verification set [71]. Figure 8 illustrates the scatter plot showing the merged SM and predicted test dataset by fitting the merged SM and environmental variables based on the LSTM network. The LSTM revealed a significant relationship between the merged SM data and environmental variables. There is very good agreement between the original and predicted SM values (R = 0.8877, RMSE = 0.0325 m³/m³, and bias = 0.0015 m³/m³). Additionally, the slope and intercept of the regression linear equation were 0.82 and 0.05, respectively, indicating that the predicted SM values were close to the merged SM, and the overestimation and underestimation values were not significant. In the next step, the verified LSTM network was applied to the auxiliary environmental variables at 0.01° resolution to obtain high-resolution SM data over the period from January 2016 to December 2020. The spatial patterns of the downscaled SM in January and June 2019, are shown in Figure 9. The downscaled SM not only had a similar distribution as the original merged SM data but also captured detailed information on the spatial heterogeneity of SM compared to the original merged SM data (Figure 6).

The downscaled SM data were validated using the observation records of 36 in situ sites (Figure 10). The results indicated that the downscaled SM data had a high correlation with in situ data almost everywhere across Yunnan province, except for a few individual sites with slightly low correlation in the central and southern regions. There were similar patterns in ubRMSE and bias, which have relatively small values in most sites of Yunnan province and slightly larger values at some sporadic points. Generally, the downscaled SM data agreed well with the in situ observations. The mean and median values of R, ubRMSE, and bias were 0.6858 and 0.7244; 0.0469 m³/m³ and 0.0459 m³/m³; and −0.0136 m³/m³ and −0.0126 m³/m³, respectively. It is worthy to note that the validation results are inevitably affected by the limited number of in situ stations, the spatial scale differences between the in situ networks and downscaled data, and the differences in the surface soil depths of SM products [72]. Figures 11 and S2 show that the temporal variation of the downscaled SM agreed well with the precipitation data, both at regional and station scales. The variations
between dry and wet seasons and the effect of precipitation can be well reflected by the downscaled SM data. In addition, the downscaled SM data reflected the severe drought conditions of Yunnan province in 2019. The results demonstrated that the downscaled SM could reflect actual SM dynamics.

**Figure 8.** The scatter plot and performance metrics for the LSTM network.

**Figure 9.** The downscaled SM data in January (a) and June (b) 2019.

**Figure 10.** Results of validation for downscaled SM data with in situ observations: (a) R; (b) ubRMSE; (c) Bias.
The downscaled SM of the merged product was also compared with those downscaled SM levels from ERA5-Land, GLDAS, and SMAP (Figure 12). It was shown that the performances of all downscaled products varied over different stations. At most stations, the downscaled SM of the merged product outperformed other downscaled SM products with lower ubRMSE and bias. At the regional scale, the downscaled SM of the merged product showed a higher median R (0.7244) than that of SMAP (0.6814), but a lower median R than that of ERA5-Land (0.7647) and GLDAS (0.7332). The median ubRMSE of the downscaled SM of the merged product was 0.0459 m³/m³, which was slightly better than that of ERA5-Land (0.0556 m³/m³), GLDAS (0.0473 m³/m³), and SMAP (0.0467 m³/m³).

In terms of median bias, the lowest absolute value was found for the merged product (−0.0126 m³/m³), followed by SMAP (−0.0159 m³/m³), ERA5-Land (0.0267 m³/m³), and GLDAS (0.0483 m³/m³). The comparison results indicated the downscaled SM of the merged product had better performance, including the acceptable R, lowest ubRMSE, and bias values among all the evaluated products. It is worth noting that the proposed downscaling method contained several assumptions and possible uncertainties from the auxiliary data; however, the validation results implied that the fusion of satellite- and model-based SM data would result in better downscaling accuracy.

5. Discussion

The uncertainties of ERA5-Land, GLDAS, and SMAP were first evaluated by a TC analysis. The results showed that GLDAS outperformed SMAP and ERA5-Land (Figure 4).
Similar results were obtained from direct comparisons with in situ observations (Figure 7), indicating that the TC analysis was reasonable for the comparison and evaluation of satellite or modeled SM datasets in data-scarce areas. As shown in Figure 7, the TC-based merged dataset showed its advantages integrated from satellite and modeled products. In the TC analysis, the errors of SM datasets are assumed to be mutually independent and orthogonal to the truth [73]. The simultaneous use of both model-based products (ERA5-Land and GLDAS) may imperil the mutual error independence results underlying the application of TC analysis [74]. Therefore, a triple combination of an active-based product (active SM product of the European Space Agency Climate Change Initiative (v06.1), CCI-active) [75], a passive-based product (SMAP), and a model-based product (ERA5-Land) was also applied here to calculate TC-based metrics. Figure S3 shows box plots of the validation results of different SM datasets at the in situ stations. The results also confirmed the merged SM data based on TC was superior to their parent products, which proves that TC-based merging was a reliable way to blend satellite and model-based SM products [19, 21, 22, 25, 31].

In theory, the TC-based merged data should outperform simple averaging data. However, this was not the case in some studies [19, 22, 25]. Figure S4 shows a comparison between the two SM datasets obtained by TC and simple arithmetic mean merging methods. For triplet A (SMAP, ERA5-Land, and GLDAS), it was found that the TC-based merged data were only slightly better than the simple averaging data in terms of R and bias. The reason could be that the differences among the three parent products were small or the weights of the three parent products were approximately equal [19]. However, for triplet B (CCI-active, SMAP, and ERA5-Land), the TC-based merged data were preferred over simple averaging data, because it can provide optimal weights and generate a better merged product in areas where the parent products have large differences (Figure S3) [19]. In addition, it should be noted that only 36 in situ stations were used for comparison and validation. The validated results were affected by the representativeness errors of the limited stations.

The merging method based on TC analysis could be further improved in the following aspects. It only allowed the input of three parent products, which resulted in the merged result of TC varying with a change in choice of the three inputs. Theoretically, the more input of SM products, the better the merged SM data that may be obtained. To overcome this limitation, Pan et al. (2015) proposed an improved TC method that allowed the input of more than three products when evaluating them [76]. In addition, a three-cornered hat is an alternative used for estimating the error variance of more than three products [15, 77]. Moreover, the TC-based merging method assumed that the errors of the data in the time dimension were constant. In fact, the errors in SM data exhibit significant temporal variations with time changes [78]. A constant weight for the entire period may not reflect the error characteristics. Therefore, spatial and temporal non-stationary errors should be considered to improve the TC merging skill [26, 79].

Analysis of the importance of different environmental variables in the SM downscaling process can help understand the mechanism of the impact of surface variables on SM [10, 38]. In order to analyze the importance of input variables (LST, NDVI, surface albedo, elevation, and soil texture) in the downscaling process, we conducted a leave-one-out approach in which one of the input environmental variables was removed and downscaling was accomplished [36]. Figure S5 shows the validation results for the different input schemes. It was found that elevation, NDVI, and surface albedo were the three most important variables in SM downscaling. The local topography is important in determining SM over regions with sharp elevation fluctuations [8, 37]. NDVI and surface albedo also exhibited high importance in SM downscaling due to their ability to reflect vegetation status and surface energy exchange [80]. LST was identified as the most important variable in some previous studies [10, 38]; however, our results indicated LST showed relatively less influence on the downscaling results. This may be attributed to poor quality of MODIS LST due to cloud contamination in the study area.

ML was widely used to downscale SM data in case studies [10, 36–39, 45]. The performance of ML in SM spatial downscaling varies with the algorithms and regions [37].
However, traditional ML algorithms cannot consider the feature abstraction of sequence data and contextual correlation on the time axis. As a class of recurrent neural networks (RNNs), the LSTM network can consider contextual information of the original data and would theoretically be more suitable for modeling time-series data [49,81]. For example, it was used in rainfall–runoff modeling [82], terrestrial water storage reconstructing [83], drought forecasting [84], and rice yield predicting [71]. The SM downsampling based on LSTM had a satisfactory performance in this study (Figures 8 and 10), although the accuracy of downscaled results was associated with the uncertainties from input remotely sensed products, the effect of the scale, and the accuracy and representativeness of in situ observations [44]. Our results showed that LSTM had broad application prospects in SM downsampling and prediction [85]. However, LSTM is designed to process sequence data, it can only obtain a temporal relationship. We also recommended CNNs in subsequent research because they can capture the spatial features from three-dimensional images [86,87]. Furthermore, the convolutional LSTM (ConvLSTM) combines the capabilities of CNN and LSTM, which not only account for the temporal relationship, but also extract spatial features through the convolution layer and are expected to further improve the SM predictive performance [48,88,89].

6. Conclusions

This study presented a hybrid TC-LSTM approach to generate a high-quality SM dataset with a 0.01 resolution and a monthly temporal resolution based on satellite- and model-based data. For the evaluation of the SMAP, GLDAS, and ERA5-Land SM products, similar results were obtained from direct comparisons with in situ observations and TC error estimation, indicating that the TC analysis was reasonable for the comparison and evaluation of satellite and model-based SM products. In addition, TC-based merging was superior to simple arithmetic average merging when the parent products had large differences. The downscaled SM of TC-based merged product had better performance, including the acceptable R, lowest ubRMSE, and bias values among all of the evaluated products, implying that the fusion of satellite and model-based SM data would result in better downsampling accuracy. The downscaled merged SM data obtained using the LSTM not only improved the spatial resolution of the SM data and captured the spatial heterogeneity and dynamics of SM but also yielded satisfactory results with a median value of R (0.7244), ubRMSE (0.0459 m$^3$/m$^3$), and bias (−0.0126 m$^3$/m$^3$) when validated with in situ observations. Overall, the proposed approach in this study had no strict boundary conditions and, thus, had better universality in various climate conditions. It could generate a SM dataset with a fine resolution and reliable accuracy for wide hydrometeorological applications.

Supplementary Materials: The following supporting information can be downloaded at: https://www.mdpi.com/article/10.3390/rs14071744/s1, Figure S1: The spatial distribution of the cross-correlation of three SM products, Figure S2: Temporal variations of downscaled SM and CHIRPS precipitation at representative site, Figure S3: The evaluation of SM datasets using in situ observations for validation, Figure S4: The evaluation of SM datasets merged by TC and simple arithmetic averaging (SAA) for two triplets using in situ observations for validation, Figure S5: Performance evaluation of the downsampling algorithms under different input schemes using in situ observations.

Author Contributions: Conceptualization and methodology, Y.L. and X.J.; software, W.M., Y.W., and J.L.; validation, W.M. and X.J.; formal analysis, W.M., C.L., and Y.L.; investigation, W.M., C.L., and M.Z.; resources, M.Z. and X.L.; data curation, W.M. and M.Z.; writing—original draft preparation, W.M.; writing—review and editing, Y.L., W.M., and X.J.; visualization, Y.W. and J.L.; supervision, Y.L. and X.J.; project administration, Y.L.; funding acquisition, Y.L. All authors have read and agreed to the published version of the manuscript.

Funding: This research was funded by the National Natural Science Foundation of China (grant number 42067033) and the Applied Basic Research Programs of Yunnan province (grant number 202001BB050073).
Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.


Acknowledgments: The authors would like to thank the reviewers and the managing editor for their comments and suggestions, which improved this paper.

Conflicts of Interest: The authors declare no conflict of interest.

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