1. Introduction

Numerous physiological activities in leaves, including photosynthesis, respiration, and transpiration, are primarily regulated by nitrogen [1–3]. Nitrogen is also closely related to chlorophyll concentration, light utilization efficiency, and net crop production [4–6]. In addition to frequently being a limiting factor for plant growth [7–9], nitrogen is a crucial input in the cycle of ecological processes [10,11]. Leaf nitrogen content has also been suggested as one of the crucial biodiversity variables for the monitoring of the progress towards the Aichi Biodiversity Targets by the remote sensing and ecology communities, who acknowledge the significant role of leaf nitrogen in biodiversity and ecosystem functioning [12,13].

Despite being a relatively minor element of leaves (up to 6.5–7%), nitrogen has been reliably recovered using leaf- and canopy-level hyperspectral data [14,15]. By offering contiguous, narrow spectral band data, hyperspectral data can be used to identify the nitrogen’s small absorption properties. Compared to the conventional destructive sample procedures, this provides an effective and economical way to assess leaf nitrogen. The spectra from leaf powder, dry leaves, and fresh leaves were employed in previous research on the determination of nitrogen concentration in vegetation, as well as estimates at the canopy level [16–18]. The mask of the significant water absorption [17,19], the confounding effects coming from the canopy structure, illumination/viewing geometry, and background [20,21], and other obstacles make it difficult to retrieve nitrogen at the canopy level.

Based on the previous studies conducted in the literature to estimate the nitrogen content of the plant, the contributions of this study are as follows:
- Using the radiance values provided by Hyperion data directly without applying any atmospheric correction.
- Developing a proper deep model which transforms VNIR-only vegetation indexes to NDNI with a high correlation.
- Removing the necessity to have high-cost special cameras like SWIR to measure the nitrogen content of the crop.
- Enabling the farmers to follow the nitrogen content of the crop progressively and decide when to/not to fertilize.

2. Related Work

To improve the nitrogen content estimation performance, numerous methods have been employed. One method is spectral transformation, which includes employing first/second derivatives and reflectance log transformation [22,23]. There are also other studies, which include continuum removal [17,24], water removal [25,26], and wavelet analysis [27]. Numerous studies have been proposed to estimate the nitrogen content over forests [18,23,28–30], grasslands [31–33], and crop ecosystems [34–36]. A variety of artificial intelligence techniques, including support vector regression, neural networks, and Bayesian model averaging [32,36,37], as well as traditional regression techniques like stepwise multiple linear regression and partial least square regression, are used to retrieve nitrogen concentration.

Vegetation indices are one of the simplest and most popular empirical methodologies for estimating the biochemical content of leaves, including the nitrogen level. The main sources of nitrogen in leaf cells are proteins and chlorophylls [38]. Since there is a strong correlation between nitrogen and chlorophyll in a variety of species [1,2,39], nitrogen has been estimated using vegetation indices which are proposed and used for chlorophyll estimation [40]. For measuring chlorophyll, spectral wavelengths around 550 nm and 700 nm, as well as the red-edge area (680–780 nm), have been used [35,41], leading to a significant variety of indices [42–44]. In contrast to chlorophyll, there are fewer studies that offer particular indices for nitrogen estimate; the majority of these indices were established for crops [45–48], while just a small number were developed for forests [49].

Given that canopy structure is the primary cause of changes in canopy reflectance, the calculation of foliar nitrogen using canopy spectral data is complicated. According to the study in [7], the NIR reflectance (800–850 nm) and canopy foliar mass-based nitrogen concentration (%N) have a significant association that can be utilized to predict nitrogen, and in [50] the researchers pointed out the association between NIR reflectance and canopy structure. The study in [51] suggested that the biological associations between nitrogen and structural characteristics that affect NIR scattering and reflectance served as the foundation for their ideas. Additionally, in [14,52], scientists indicated that the canopy structure and leaf characteristics may co-vary among plant functional types, contradicting the study in [53], which claimed that the %N-NIR correlation is inherently false.

The purpose of the study in [54] was to assess how well 32 vegetation indicators collected from airborne hyperspectral imaging performed when used to calculate canopy foliar nitrogen in a mixed temperate forest. For comparison, the widely used partial least squares regression was carried out. These vegetation indicators can be divided into three groups, most of which are connected to the biochemical and structural characteristics of vegetation (e.g., nitrogen, chlorophyll, and leaf area index (LAI)). The nitrogen indicators are selected based on how nitrogen absorption characteristics’ physical underpinnings affect canopy reflectance. The biological connections between nitrogen, chlorophyll, and canopy structure were used to justify the inclusion of the structural and chlorophyll indices in this study. Nitrogen (N) losses and the ensuing environmental issues are what define the production of vegetable crops [55–57]. The most frequent environmental issues include nitrous oxide (N\(_2\)O) emissions, ground and surface water contamination, and the eutrophication of surface waters [58,59]. These issues are frequently a result of the extensive use of N fertilizer [60], which typically exceeds the requirement of the crops [57,61,62], which is
performed to ensure optimal growth and production. In order to decrease N contamination of water bodies by intensive vegetable production, it is necessary to understand crop nitrogen requirements and match crop demand with nitrogen supply [57,63,64].

There are numerous techniques available for tracking crop nitrogen status [57,65]. Leaf nutritional analysis is a common method, but it is time-consuming and labor-intensive in the lab, and it typically cannot quantify the temporal and geographical variability of nitrogen status [66,67]. These are significant drawbacks, since it is much easier to match the supply of nitrogen to crop requirements when one is aware of the temporal and spatial variability of crop nitrogen status [68].

Optical sensors are tools that quickly, accurately, and nondestructively monitor the crop’s nitrogen status in the field [57,69]. They make it possible to regularly evaluate a crop and evaluate spatial variability. Canopy reflectance sensors, which are among the proximal optical sensors, have two highly advantageous characteristics in that they can monitor huge portions of a crop while they are in motion [70]. Field crops’ nitrogen status can be evaluated via measures of crop reflectance [65]. These measures are based on the differential reflection of light wavelengths [57], which, depending on crop nitrogen status [69], are absorbed and reflected by the crop in varying amounts. Typically, red, green, and near-infrared light wavelengths are employed for nitrogen estimation [65]. Recently, the red edge has been suggested as a solution for nitrogen estimation of the red band’s apparent saturation [71,72].

The nitrogen nutrition index (NNI) [67,73] is another commonly utilized strategy. The critical crop nitrogen content [74,75] is the lowest crop nitrogen content required for non-limiting growth, and it is used to calculate the NNI by dividing the actual crop nitrogen content by it. Any variation from 1 indicates either excess nitrogen (i.e., NNI > 1) or insufficient nitrogen (i.e., NNI < 1) crop status, with values of NNI equal to 1 indicating adequate nitrogen feeding [76].

Due to the high cost of SWIR band sensors, a regression-based method should be developed which maps the VNIR band indexes to SWIR band indexes. The majority of studies have been performed on cereal crops [77,78] like wheat [12,79] and rice [80–82]; very few have been carried out on vegetable crops like sweet pepper.

In [83], the crop nitrogen status of sweet pepper was estimated using eight vegetation indices that were computed from canopy reflectance data taken with two separate proximate sensors. First, crop NNI calibration regression models were fitted for each vegetation index. Second, a different dataset was used to validate these regression equations. Thirdly, sufficient values for each vegetative index for optimal nitrogen nutrition, for the main phenological stages of sweet pepper crops, were obtained utilizing the validated equations between vegetation indices and crop NNI.

The findings of the study [84] supported the use of the normalized difference vegetation index (NDVI) as a useful tool for determining the nitrogen status of cotton leaves at various growth stages. Using vegetation indices, the study in [85] calculated the nitrogen nutrition index (NNI), canopy nitrogen density (CND), and leaf nitrogen content of winter wheat over the course of the entire growth period. This study demonstrated that the correlations between each nitrogen index and the Vogelmann red-edge index (VOG), simple ratio pigment index (SRPI), modified red-edge simple ratio index, and red-edge position based on the linear interpolation method (REPliner) were not significantly influenced by growth period, and the estimation model $R^2$ for CND was higher than 81%. The estimation model’s accuracy was higher than NNI; however, it would become saturated if CND was calculated using just one vegetation index. The red-edge chlorophyll index, $C_{red-edge}$, was demonstrated by [86] to be responsive to the canopy structure. The correlation between the nitrogen content of cotton leaves and several spectral ratio measures was examined in [87], who also conducted a cluster analysis based on prediction accuracy and overall accuracy.

The ratio of the red-edge position to the near-infrared band was shown to have a pretty high prediction accuracy and overall accuracy. The estimation of the winter wheat spectral index was investigated by [88] in a variety of environments, seasons, varieties, and
growth stages. According to their findings, the growth stage had a significant impact on the performance of various vegetation indices and the choice of a sensitive wavelength for plant nitrogen concentration (PNC) estimation. The simple ratio of reflectivity at 370 nm and 400 nm (R\text{370}/R\text{400}) displayed the most consistent estimation accuracy in an indoor experiment (R^2 = 0.58) and field experiment (R^2 = 0.51). According to the studies, there are obvious changes in the relevant spectral index for different crops, or for various kinds and ecological zones of the same crop, when employing the spectral index to estimate crop nitrogen [89,90].

Additionally, compared to employing sensitive spectral features alone or vegetation indexes, modeling techniques like deep machine learning can produce greater prediction effects [91]. These techniques can also be used to monitor agricultural nutrients and growth indicators [92–94]. Support vector machine regression (SVR) was shown to be the most effective method for assessing crop nutrient contents in [95], which evaluated artificial neural network and SVR methods. The authors proposed that the creation of models with large sample sizes is appropriate for an artificial neural network. The hyperspectral reflectance of leaves was used in [90] to study the generalized partial least-squares regression (PLSR) model, and this approach was successful in retrieving leaf nitrogen concentration (r = 0.85).

The study in [96] is based on data for two types of drip-irrigated cotton at various growth stages from April 2019 to September 2020. The data include canopy nitrogen density (CND) and leaf nitrogen concentration (LNC) values. Pearson’s correlation analysis was used to determine which of the thirty hyperspectral vegetation indexes and the two nitrogen indexes (LNC and CND) that were used in the three modeling techniques of simple multiple linear regression (MLR), PLSR, and support vector regression (SVR) were relatively stable. The models were employed to investigate the possibility of measuring the nitrogen nutrient status of cotton in each growth period based on a multi-vegetation index in order to give a theoretical background for the application of remote sensing technology in cotton nutrition monitoring and diagnostics.

The nitrogen attitude of paddy rice was studied in [97], including plant nitrogen content (PNC), leaf nitrogen content (LNC), plant nitrogen accumulation (PNA), and leaf nitrogen accumulation (LNA). The data used in this study were collected by using a hyperspectral camera integrated to an unmanned aerial vehicle (UAV). The results handled in this study report that the correlation between the nitrogen traits and biochemical traits, canopy chlorophyll content, leaf chlorophyll content and aboveground biomass, depend on the growth stage of the crop.

The study in [98] fused the information from different sensors and developed new spectral indices based on a coverage-adjustment and estimated the content of leaf nitrogen of maize in different stages of the growth. According to the results, CASIs perform better than the traditional vegetation indices.

According to the results of the study in [99], which developed an estimation method of potato nitrogen, combining the visible light vegetation indexes and plant morphological properties provides a better estimation of nitrogen, since by using multiple linear regression methods it achieves a 0.79 R^2 score.

Researchers developed a new method in [100] which extracts the leaf region from the color images and computes the color similarity between the extracted leaf with some predefined color information. In particular, a green color intensity was used for the reference of nitrogen content. The proposed method was tested on a Spinacia oleracea dataset and results showed that there exists a high correlation between the laboratory analysis and the analysis of the color images.

3. Materials and Methods

Image data of the Hyperion sensor were used in this study. As a push-broom hyperspectral instrument, Hyperion is housed on the EO-1 satellite, which is depicted in Figure 1.
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![EO-1 Satellite View](image)

Figure 1. EO-1 Satellite View [101].

With a 10 nm bandwidth spanning from 357 nm to 2576 nm, it collects 220 different spectral channels. All bands have a spatial resolution of \((30 \times 30)\, \text{m}^2\). The VNIR band, SWIR band, and VNIR-SWIR band indices can all be estimated from the same image data because Hyperion includes both the VNIR and SWIR bands. There is no need for a geometric correction because the Hyperion images have already been rectified geometrically. In addition, no atmospheric correction is applied to the data. This is due to the fact that atmospheric correction tools are not free to use, so, bring high financial costs. In addition, they cannot achieve a perfect correction, which produces incorrect reflectance values among the pixels and affects the results negatively. The properties of the Hyperion sensor are given in Table 1.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Hyperion Sensor Details</th>
</tr>
</thead>
<tbody>
<tr>
<td>Spectral range</td>
<td>400–2500 nm</td>
</tr>
<tr>
<td>Spatial resolution</td>
<td>30 m</td>
</tr>
<tr>
<td>Radiometric resolution</td>
<td>12 bits</td>
</tr>
<tr>
<td>Swath width</td>
<td>7.5 km</td>
</tr>
<tr>
<td>Spectral resolution</td>
<td>10 nm</td>
</tr>
<tr>
<td>Spectral coverage</td>
<td>Continuous</td>
</tr>
<tr>
<td>Number of rows, columns, bands</td>
<td>3271, 871, 220</td>
</tr>
</tbody>
</table>

Different test images were collected from Hyperion data on the Harran region based in the south-west of Turkey. Google Earth and Earth explorer views of Harran and the Hyperion image are shown in Figure 2.

The Harran Plain is a region that starts from the southeast of the city of Şanlıurfa and extends to the Syrian border. It is a plain with very fertile soil. It is located between the 36°43′–37°08′N parallels and 38°57′–39°55′E meridians in the Upper Mesopotamian area of Şanlıurfa province.

In the main, corn and cotton farming is carried out. In the Harran Plain, under the influence of the Mediterranean climate, the continental climate is dominant. Winters are cold and rainy, and summers are very hot and dry. Annual precipitation is 365 mm, annual evaporation is 1848 mm, and annual average temperature is 17.2 °C.
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Figure 2. Google Earth view of Harran (top) and Earth Explorer view of Hyperion (color image) (bottom).

The Hyperion image downloaded from Earth Explorer covers roughly 900 km², which is both required and sufficient to investigate the reliability of the proposed method. The QGIS Geographic Information Software Tool was used to determine the area of the Hyperion images [102]. Figure 3 shows the image data taken from the Harran region, in which a large amount of corn, cotton and wheat planting is undertaken by farmers. The image acquisition time was 8 August 2016, when the crop was dense and mature. The image’s latitude and longitude values and the scale of the map are given on the figure as well.
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Figure 3. Hyperion data. RGB Image of Harran Region.

Figure 4 shows a drone camera view and a ground image of a region from Harran taken in July 2019.
In the Harran region, to show the vegetation density and the spreading over the area, an NDVI estimation was first applied. The Hyperion image and the resulting NDVI index map are shown in Figure 5. The Hyperion image has a spatial resolution of 3241 × 1241, totaling 4,022,081 pixels, where 2,859,262 pixels are the black regions surrounding the target region. Therefore, the vegetation index analysis is implemented on 1,162,819 pixels. Each pixel corresponds to 30 × 30 m² ground area. By recalling that NDVI values can be changed from −1 to 1, in Table 2 it can be seen that the number of pixels with a high NDVI value, like >0.75, was lower, relatively speaking. An important reason for this is the ground spatial resolution of the Hyperion sensor, in which one pixel covers 30 × 30 m². This is, relatively, a large area in which spectral mixing occurs, and therefore the spectra of soil, water and vegetation is mixed, which may reduce the NDVI indices [104]. Nonetheless, the data are powerful and exhibit a good distribution, which enables an accurate analysis of vegetation indices.

Table 2. Number of pixels falling in specific intervals of NDVI values.

<table>
<thead>
<tr>
<th>NDVI &lt; 0</th>
<th>0 ≤ NDVI &lt; 0.25</th>
<th>0.25 ≤ NDVI &lt; 0.5</th>
<th>0.5 ≤ NDVI &lt; 0.75</th>
<th>0.75 ≤ NDVI &lt; 1</th>
</tr>
</thead>
<tbody>
<tr>
<td>447,396</td>
<td>193,177</td>
<td>214,010</td>
<td>269,860</td>
<td>49</td>
</tr>
</tbody>
</table>
To increase the accuracy, the pixels with NDVI values higher than 0.2 were taken into account. This is due to the typical vegetation pixel having an NDVI greater than 0.2.

The study in [105] states that NDNI can be used effectively for the estimation of the nitrogen content of the vegetation. Since, in this study, we develop a deep model which established a correlation between VNIR band vegetation indices and NDNI, the most important vegetation indices which hold information about the nitrogen content of the plants were estimated. These indices are NDVI [106], GNDVI [107], EVI [108], GOSAVI [109], GSAVI [109], MCARI2 [110], and VREI2 [111]. To establish the correlation, NDNI [112] was estimated as well. Table 3 shows the corresponding indices, the bands or wavelengths, and the equations which were used to estimate them.

Table 3. Vegetation indices, bands or wavelengths and equations.

<table>
<thead>
<tr>
<th>Index</th>
<th>Bands and/or Wavelengths</th>
<th>Equation for Estimation</th>
</tr>
</thead>
<tbody>
<tr>
<td>NDVI [106]</td>
<td>NIR, RED</td>
<td>$\frac{NIR - Red}{NIR + Red}$</td>
</tr>
<tr>
<td>GNDVI [107]</td>
<td>NIR, Green</td>
<td>$2.5 \times \frac{NIR - Red}{NIR + Green + 0.16}$</td>
</tr>
<tr>
<td>EVI [108]</td>
<td>NIR, Green, Blue</td>
<td>$1.5 \times \sqrt{\frac{(2.5(\rho_{800} - \rho_{747})-1.3(\rho_{800} - \rho_{734}))^2}{(2.5(\rho_{800} + 1)^2 - (6(\rho_{800} - 5(\sqrt{\rho_{734}}) - 0.5))}}$</td>
</tr>
<tr>
<td>GOSAVI [109]</td>
<td>NIR, Green</td>
<td>$\log\left(\frac{\rho_{734}}{\rho_{747}}\right) - \log\left(\frac{\rho_{726}}{\rho_{715}}\right)$</td>
</tr>
<tr>
<td>GSAVI [109]</td>
<td>NIR, Green</td>
<td>$\log\left(\frac{\rho_{1510}}{\rho_{1680}}\right)$</td>
</tr>
<tr>
<td>MCARI2 [110]</td>
<td>$\rho_{800}, \rho_{670}, \rho_{550}$</td>
<td></td>
</tr>
<tr>
<td>VREI2 [111]</td>
<td>$\rho_{734}, \rho_{747}, \rho_{726}, \rho_{715}$</td>
<td></td>
</tr>
<tr>
<td>NDNI [112]</td>
<td>$\rho_{1510}, \rho_{1680}$</td>
<td></td>
</tr>
</tbody>
</table>

The black regions on the Hyperion data were excluded first. Then, each vegetation index was estimated for the pixels left. $N$ was the number of pixels in each index map, and a vector of index values was created, as shown in Equation (1), where $Map_{vi}$ was the index.
map of the corresponding vegetation index and \( \text{index}_i \) was the estimated index value at pixel \( i \).

\[
\text{Map}_{vi} = [\text{index}_1, \text{index}_2 \ldots \text{index}_N]
\]  

(1)

Then, new index data were created, as shown in Equation (2), where \( I_{b,i,ab} \) was the estimated index for the (b). pixel of vegetation index (a). (i.e., 3rd pixel of NDVI map).

\[
data = \begin{bmatrix} I_{b,11} & \cdots & I_{b,1N} \\ \vdots & \ddots & \vdots \\ I_{b,i,1} & \cdots & I_{b,i,MN} \end{bmatrix}
\]  

(2)

Since this study uses 7 vegetation indices from the VNIR region, a total of 7 \( \text{Map}_{vi} \) were created at the beginning. Therefore, the size of the data matrix was \((7 \times 1,162,819)\). After handling the data matrix, a further analysis was carried out.

- Due to the division by 0, some index values were calculated as infinite and/or NaN. Therefore, those kinds of pixels were found and the corresponding column was deleted.
- Another analysis was also carried out for the pixels with an abnormally large vegetation index. Therefore, the index values which had an absolute value above 5 were also deleted from the data.
- Finally, 1,113,529 pixel values were used, and to normalize the effect of the environment at the time of the capturing, each index row in the data was normalized between \(-1 \) and \( 1 \). To normalize the data, the \textit{normalize} function of Matlab was used with a ‘range’ parameter.

Similarly, the above operations were also applied on the NDNI Map. Finally, the input data had the shape of \((7 \times 1113529)\) and the output data had \((1 \times 1113529)\).

To train a model which matches the input data to the output data, Matlab deep learning toolbox [113] was used. By using this tool, a deep neural network was designed with 4 dense (hidden) layers, each with 25 neurons. Figure 6 shows the designed neural network. The number of input neurons was 7 due to the shape of the input data and 1 for output, hence that was the NDNI index value.

![Figure 6. Feed forward deep neural network (proposed).](image)

Data were split into train, validation, and test datasets with the default ratio of 0.7:0.15:0.15. The number of epochs was set as 1000. Training function and adaption learning functions were set as TRAINLM (Levenberg–Marquardt) and LEARNGDM. LEARNGDM is a gradient descent algorithm with momentum. The cost can be pushed farther to go around a saddle point by adding a momentum element to the gradient descent, even if the current gradient is insignificant. The performance function is MSE. Training was carried out on CPU on a Windows PC with 8 GB Ram and an 11th Gen Intel(R) Core(TM) i7-1165G7 @ 2.80 GHz processor. The reason not to use GPU was that in Matlab, the TRAINLM function is not supported.

The Levenberg–Marquardt [114] technique, which was developed for minimizing functions that are sums of squares of nonlinear functions, is derived from Newton’s method [115]. The Levenberg–Marquardt algorithm is designed to minimize sum-of-square error functions of the form (3). In (3), \( err_k \) is the error in the kth instance and \( err \) is
a vector with element at $k$. A Taylor series can be used to expand the error vector to first order if the difference between the old and new weight vectors is modest.

$$E = \frac{1}{2} \sum k (err_k)^2 = \frac{1}{2} ||err||^2$$  (3)

$$err(j + i) = err_j + \frac{\partial err_k}{\partial w_i} (w(j + 1) - w(j))$$  (4)

As a result, the error function can be expressed as

$$E = \frac{1}{2} \left\| err(j) + \frac{\partial err_k}{\partial w_i} (w(j + 1) - w(j)) \right\|^2$$  (5)

After minimizing the error function with respect to the updated weight vector, (6) can be written.

$$w(j + 1) = w(j) - (Z^T Z)^{-1} Z^T err(j)$$  (6)

where

$$Z_{ki} = \frac{\partial err_k}{\partial w_i}$$  (7)

Since the Hessian for the sum-of-square error function is as shown in (8),

$$H_{ij} = \frac{\partial^2 E}{\partial w_i \partial w_j} + \sum \left\{ \left( \frac{\partial err_k}{\partial w_i} \right) \left( \frac{\partial err_k}{\partial w_j} \right) + err_k \left( \frac{\partial^2 err_k}{\partial w_i \partial w_j} \right) \right\}$$  (8)

By ignoring the second term, Hessian can be written as:

$$H = Z^T Z$$  (9)

For nonlinear networks, updating the weights therefore entails the inverse Hessian. Since the Hessian is based on first order derivatives with respect to the network weights, which can be easily handled by back propagation, it can be calculated rather quickly. Although iterative application of the updating formula to reduce the error function is an option, this may provide a step size that is too big, invalidating the linear approximation that the method is based on.

The Levenberg–Marquardt approach minimizes the error function while maintaining a small step size to guarantee the accuracy of the linear approximation. Utilizing a form’s customized error function allows for this.

$$E = \frac{1}{2} \left\| err(j) + \frac{\partial err_k}{\partial w_i} (w(j + 1) - w(j)) \right\|^2 + \alpha \| (w(j + 1) - w(j)) \|^2$$  (10)

where $\alpha$ is a parameter adjusting the step size. When the modified error is minimized with respect to $w(j + 1)$, (11) is handled.

$$w(j + 1) = w(j) - (Z^T Z + \alpha I)^{-1} Z^T err(j)$$  (11)

With very large values of $\alpha$, Levenberg–Marquardt approaches standard gradient descent, whereas for very small values of $\alpha$ it approaches the Newton method.

This study aims to investigate the relation between VNIR-only vegetation indexes and NDNI. For that purpose, linear regression was employed by using a deep neural network. Linear regression can be explained as follows:

$$Y = a + bX + \epsilon$$  (12)
where

\[ a = \frac{(\sum y)(\sum x^2) - (\sum x)(\sum xy)}{n(\sum x^2) - (\sum x)^2} \quad (13) \]

\[ b = \frac{n(\sum xy) - (\sum x)(\sum y)}{n(\sum x^2) - (\sum x)^2} \quad (14) \]

In Equation (12), \( Y \) is the dependent (outcome) variable, \( a \) is y-intercept, \( b \) is the slope of the regression line, \( X \) is the independent variable, and \( \varepsilon \) is the error term. The calculation of linear regression includes 3 steps:

1. First, the values of formula components \( a \) and \( b \) are found by using \( \sum x \), \( \sum y \), \( \sum xy \), and \( \sum x^2 \);
2. Then, the values derived in the first step are substituted into \( a \) and \( b \);
3. Finally, \( a \) and \( b \) values are used with the formula \( Y = a + bX + \varepsilon \) to establish the linear relationship between \( X \) and \( Y \) variables.

Since a deep neural network is used in this study, the calculation is performed by the neural network tool defined in Matlab and linear regression is employed.

4. Results

Regression and loss plots are given in Figures 7 and 8, respectively, for training, validation, test, and overall data. The \( R^2 \) values for test and validation data are above 0.91 and 0.93, respectively, which is very promising. Similarly, the MSE loss values are all below \( 10^{-4} \). The best validation loss score is \( 7.01 \times 10^{-5} \), which means 70 over 1 million. As can be observed from Figure 7, although the number is low, there are some outlier values which do not fit the regression line. They are the points which are far from the regression line and whose correlation error is generally high. Therefore, the outliers affect the regression score negatively. Those points are generally the anomaly points/regions in the flat areas. The best validation score was achieved at epoch 124, and therefore the training was stopped at epoch 130.

![Regression plots for training, validation, test and all data.](image-url)
The regression equations between input and output handled for training, validation, test and all data are given in Table 4.

**Table 4. Regression equations between output and target.**

<table>
<thead>
<tr>
<th>Data</th>
<th>Equation for Estimation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Training</td>
<td>$\text{Output} = 0.87 \times \text{Target} + 0.0066$</td>
</tr>
<tr>
<td>Validation</td>
<td>$\text{Output} = 0.89 \times \text{Target} + 0.0059$</td>
</tr>
<tr>
<td>Test</td>
<td>$\text{Output} = 0.83 \times \text{Target} + 0.0089$</td>
</tr>
<tr>
<td>All</td>
<td>$\text{Output} = 0.87 \times \text{Target} + 0.0069$</td>
</tr>
</tbody>
</table>

Various machine learning methods based on regression were also trained and tested. In Table 5, the best regression scores handled are given for comparison with the proposed method. It can be obviously seen from the table that the proposed method achieves the best and superior results compared to all other methods.

**Table 5. Benchmark of the proposed method with various regression models.**

<table>
<thead>
<tr>
<th>Method</th>
<th>Regression Score ($R^2$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Linear Regression</td>
<td>-0.29</td>
</tr>
<tr>
<td>SVM Regression</td>
<td>0.15</td>
</tr>
<tr>
<td>Gradient-boosted decision trees (GBDT)</td>
<td>0.37</td>
</tr>
<tr>
<td>Random Forest Regressor</td>
<td>0.46</td>
</tr>
<tr>
<td>Stochastic Gradient Descent (SGD)</td>
<td>0.35</td>
</tr>
<tr>
<td>PLSRegression</td>
<td>0.36</td>
</tr>
<tr>
<td>Proposed</td>
<td>0.91</td>
</tr>
</tbody>
</table>

**Ablation Study**

In this study, a deep neural network was employed to investigate the correlation between VNIR-Only vegetation indexes and the NDNI index. For this purpose, various combinations of different networks on normalized and/or unnormalized data were tried. Figure 9 shows the regression results when the depth of the network was reduced to two deep layers and data were normalized. Even if test score was improved a bit, validation and all data scores were not good as the proposed network.
Figure 9. Two-deep layer with 25 neurons on Normalized Data.

Figure 10 shows the regression result for two deep layers on unnormalized data, which were worse and unbalanced among training, validation and test data. Therefore, when the network is not deep enough, normalization of the data is crucial.

Figure 10. Two-deep layer with 25 neurons on unnormalized data.
When the depth of the network is kept and data are not normalized, similar regression results to the proposed network can be seen (Figure 11). However, the results are still a bit better when the data are normalized. In addition, when the data are normalized, the depth of the network can be reduced to two with very little and tolerable reduction in accuracy. In this way, the response time of the network to new data can be reduced, which is crucial for near real-time and/or real-time applications.

![Figure 11. Four-deep layer with 25 neurons on unnormalized data.](image)

Various neural networks with different numbers of deep layers and neurons were trained with the normalized data, and the obtained regression scores for training, validation, test, and all data are given in Table 6. The best scores are colored in red and the second-best scores are colored in blue. As (#L, #N) shows the number of deep layers and neurons at each deep layer, (4,15) includes the three best scores; however, the validation score is low. Similarly, (5,15) includes the three best scores; however, the test score is low. (3,25) and (4,25) have the three best scores, and the total score of (4,25) was above (3,25). Other different combinations had two best/second-best scores, one best/second-best score or no best/second-best scores. Therefore, in this study, the combination of (4,25) is proposed.

After training the network with (4,25), the trained model was tested on the Hyperion image. Figure 12 shows the difference image between NDNI and the estimated NDNI with the proposed neural network. It can be observed from the figure that the difference between the estimated and actual NDNI is very low, especially for the regions where the vegetation density is high and farming is being carried out actively.
Table 6. Regression scores obtained by training various neural networks.

<table>
<thead>
<tr>
<th>Number of Deep Layers</th>
<th>Number of Neurons</th>
<th>Regression Scores (Train-Validation-Test-All)</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>10</td>
<td>0.93-0.90-0.85-0.91</td>
</tr>
<tr>
<td>3</td>
<td>10</td>
<td>0.93-0.92-0.91-0.92</td>
</tr>
<tr>
<td>4</td>
<td>10</td>
<td>0.93-0.91-0.92-0.93</td>
</tr>
<tr>
<td>5</td>
<td>10</td>
<td>0.93-0.93-0.90-0.93</td>
</tr>
<tr>
<td>2</td>
<td>15</td>
<td>0.92-0.92-0.88-0.91</td>
</tr>
<tr>
<td>3</td>
<td>15</td>
<td>0.93-0.91-0.90-0.92</td>
</tr>
<tr>
<td>4</td>
<td>15</td>
<td>0.95-0.89-0.93-0.94</td>
</tr>
<tr>
<td>5</td>
<td>15</td>
<td>0.94-0.94-0.87-0.93</td>
</tr>
<tr>
<td>2</td>
<td>20</td>
<td>0.93-0.92-0.91-0.92</td>
</tr>
<tr>
<td>3</td>
<td>20</td>
<td>0.93-0.88-0.91-0.92</td>
</tr>
<tr>
<td>4</td>
<td>20</td>
<td>0.95-0.92-0.89-0.94</td>
</tr>
<tr>
<td>5</td>
<td>20</td>
<td>0.91-0.92-0.90-0.91</td>
</tr>
<tr>
<td>2</td>
<td>25</td>
<td>0.91-0.91-0.92-0.93</td>
</tr>
<tr>
<td>3</td>
<td>25</td>
<td>0.94-0.90-0.92-0.93</td>
</tr>
<tr>
<td>4</td>
<td>25</td>
<td>0.94-0.93-0.91-0.93</td>
</tr>
<tr>
<td>5</td>
<td>25</td>
<td>0.92-0.88-0.89-0.91</td>
</tr>
</tbody>
</table>

Figure 12. Difference image between actual NDNI and estimated NDNI with proposed network.

5. Discussion

In this study, the correlation between VNIR-only indexes and the NDNI index was investigated and a deep neural network was trained to establish that correlation. The results show that there exists a high correlation between them. The most important contribution of this study is proving that the VNIR-Only band vegetation indexes have a high correlation with NDNI, which is calculated by using the SWIR band region of the electromagnetic spectrum. Results show that when VNIR-only indexes are chosen and combined properly and used as the input for a deep neural network, it is possible to
establish a high correlation. In this way, researchers and the farmers do not need to use an SWIR band camera, which generally means a high cost for them. By using a VNIR-Only band multispectral/hyperspectral camera and/or satellite, it is possible to estimate the nitrogen content of the plant progressively with a high accuracy. This will enable farmers to detect the regions with high and/or low amounts of nitrogen, so that they can reduce or increase the fertilization specific to different regions in a field.

To this point, the vegetation index studies in the literature have been based on either a single electromagnetic region (like VNIR) or multiple regions (VNIR-SWIR). The most important improvement of this study is in investigating and establishing the correlation between VNIR-only vegetation indexes and the NDNI index. So, without using any SWIR band cameras and/or satellites, it can be possible to estimate the nitrogen content easily and with high accuracy and very little loss. The bands used in this study from the VNIR region were Red, Green, Blue, NIR, 550 nm, 670 nm, 715 nm, 726 nm, 747 nm, 734 nm, and 800 nm of Hyperion image data. As is given in detail in the results section, the correlation ($r^2$) values were handled above 91% for the training, validation, and test data by using the proposed deep neural network.

6. Conclusions

In this study, an NDNI index which can be calculated by using SWIR bands from the electromagnetic spectrum was estimated by using a proper combination of VNIR band indexes. Seven different vegetation indexes were used as the input and NDNI was used as the output (target) in the training. As a result, very high accuracy was achieved since the correlation for target data was achieved above 91%. Therefore, by using the proposed network, the researchers can estimate the nitrogen content of the plant with respect to NDNI without the calculation of NDNI. SWIR band cameras are generally expensive and not easy to access. Therefore, the most important contribution of this study is in removing the necessity to have an SWIR band camera and atmospheric correction tool to estimate the nitrogen content. In addition, by using the VNIR-only vegetation indexes which are proposed in this study, a specific camera which has the capability of estimating the nitrogen content directly can be produced in the future. It can be used either standalone or by integrating on a satellite. When it is used standalone, the real-time tracking of the nitrogen content of the vegetation can be achieved. This study employs a deep neural network to achieve that purpose. In addition, the Hyperion data used in this study and the trained network are shared at https://github.com/ycimtay/VNIR_to_NDNI (accessed on 3 July 2023).

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Data Availability Statement: Publicly available datasets were analyzed in this study. This data can be found here: [https://earthexplorer.usgs.gov/].

Conflicts of Interest: The authors declare no conflict of interest.

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