Development and Evaluation of a Threshold-Based Motion Cueing Algorithm

Edward Kraft *, Ping He and Stephan Rinderknecht

Abstract: In this paper, a motion cueing algorithm (MCA) without a frequency divider is proposed, which aims to reproduce the longitudinal reference acceleration as far as possible via tilt coordination. Using a second-order rate limit, the human perception thresholds can directly be taken into account when parameterizing the MCA. The washout is compensated by tilt coordination and means of feedback from the translational acceleration. The proposed MCA is compared with the classical washout algorithm and the compensation MCA based on selected qualitative metrics and their workspace demand. In addition, a subjective study on the evaluation of the MCA was conducted. The results show that even high washout rates are not noticeable by the test subjects. Overall, the MCA was rated as very good.

Keywords: driving simulation; ideal motion cueing algorithm; compensation algorithm; longitudinal driving simulator; subjective evaluation; human perception thresholds
and the compensation MCA (see Section 2.1). Furthermore, the subjective evaluation of the proposed MCA was examined. It is of particular interest if the test subjects recognize the high washout rate or if the washout can be completely compensated by tilt coordination.

This study was carried out in the longitudinal dynamic driving simulator “Driveception” at IMS. The Driveception was developed at IMS in order to investigate longitudinal driving maneuvers such as gear shifting and driving-off processes. The translational workspace has a total length of 10 m, and the driver’s cabin can be tilted by a maximum of 25 degrees [6] (pp. 56–78). For practical use, only tilts up to 20 degrees are used. Further technical specifications can be found in Table 1.

Table 1. Specifications of the longitudinal driving simulator “Driveception” at IMS [6] (pp. 56–78).

<table>
<thead>
<tr>
<th>Actuator</th>
<th>Linear Motion</th>
<th>Rotation Rear</th>
<th>Rotation Front</th>
</tr>
</thead>
<tbody>
<tr>
<td>Nom. force</td>
<td>3000 N</td>
<td>6880 N</td>
<td>1660 N</td>
</tr>
<tr>
<td>Nom. speed</td>
<td>5 m/s</td>
<td>0.25 m/s</td>
<td>1.25 m/s</td>
</tr>
<tr>
<td>Max. force</td>
<td>4000 N</td>
<td>16 000 N</td>
<td>2848 N</td>
</tr>
<tr>
<td>Max. travel</td>
<td>10 m</td>
<td>0.15 m</td>
<td>1 m</td>
</tr>
<tr>
<td>Sensor type</td>
<td>SinCos (relative)</td>
<td>Resolver (relative)</td>
<td>SSI/SinCos (absolute)</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Degree of Freedom</th>
<th>Travel</th>
<th>Velocity</th>
<th>Acceleration</th>
</tr>
</thead>
<tbody>
<tr>
<td>Translational</td>
<td>±5 m</td>
<td>±5 m/s²</td>
<td>±8 m/s²</td>
</tr>
<tr>
<td>Rotational</td>
<td>±25°</td>
<td>&gt;±6°/s</td>
<td>&gt;±6°/s²</td>
</tr>
</tbody>
</table>

Since the Driveception was designed to investigate only longitudinal driving maneuvers, maneuvers with lateral dynamics cannot be represented by the motion system. Hence, this study focused on longitudinal motion cueing. Lateral dynamics motion cueing was not considered.

2. Methods

In this section, three state-of-the-art motion cueing algorithms are described. Then, a new motion cueing algorithm is developed. All MCAs are characterized in terms of their functions and limitations.

2.1. State of the Art

2.1.1. Classical Washout Algorithm

A frequently used MCA is the classical washout algorithm [7], from here on referred to as the CWA. Its structure can be seen in Figure 1. First, the reference acceleration is scaled, i.e., the input acceleration is reduced. This is necessary, since common driving simulators have only a limited workspace. On the basis of literature research and his own investigations, Fischer showed that a scaling factor of 0.5 is a widely used and acceptable value [3] (pp. 57–58). After scaling, the reference acceleration is divided into a high-frequency component and a low-frequency component by two filters, HPf and LPf, respectively [3] (p. 29). The low-frequency component is represented by tilting the cabin (tilt coordination). Due to the human perception threshold, the rotation rate has to be limited to values between 3°/s [8] and 6°/s [9]. The high-frequency component is represented by the translational motion system. Therefore, a second-order high-pass filter, HPwo, applied to the high frequency path, pulls the simulator back to its neutral position (so-called washout). This allows new acceleration cues without violating workspace limits.
The CWA has some disadvantages. The parametrization of the filters can be difficult, since the filters’ cut-off frequency has no meaning with regard to the human perception threshold [6] (p. 27). In addition, the washout sometimes produces false motion cues [3] (p. 65). This results in a mismatch between the visually perceived movement and the vestibular perceived movement and can lead to simulator sickness with symptoms such as nausea, indisposition and headaches [10] (p. 332).

2.1.2. Compensation Motion Cueing Algorithm

The aim of the compensation algorithm is to compensate false cues resulting from the washout. For this purpose, the acceleration component that is lost due to the washout is added to the rotary path and, together with the low-frequency component, transferred to the tilt coordination (see Figure 2). A disadvantage is the high rotational acceleration, meaning that the acceleration has to be scaled more [11] (p. 55). According to [3] (p. 33), an error in the translational acceleration occurs at high tilt angles due to the lack of a coordinate transformation.

The ideal motion cueing algorithm (from here on referred to as the IMCA) was introduced by Betz in 2012 [4]. Its structure can be seen in Figure 3. (Instead of the specific forces $f_V$, the vehicle accelerations $a_V$ are used. These can easily be transformed into each other using the gravitational acceleration $g$ [3] (p. 10).) This MCA tries to map as much of the acceleration as possible to be represented via the tilt coordination. For this purpose, the washout is not realized via the translational path, but with feedback of the translational displacement and speed. The feedback is multiplied by factors $\frac{1}{\tau_0}$ and $\frac{1}{\tau_1}$, converted back into the inertial system and added to the reference acceleration signal. Further information on this MCA can be found in [4,5].
Betts stated that the higher accuracy of this MCA comes with a higher workspace demand [5] (p. 51). Thus, in certain circumstances, a lower scaling factor has to be chosen. As stated above, another difficulty comes with the parametrization of the low-pass filters’ cut-off frequency and the feedback gains.

2.2. Ideal Motion Cueing Algorithm

To overcome these difficulties, the IMCA was modified in the following way and will be referred to as the “threshold-based motion cueing algorithm” (TBMCA): Instead of a low-pass filter and a rotation rate limit, a rotation rate limit and a rotation acceleration limit (rate limit 1. + 2. order) are used (see Figure 4). The rotation rate limit can now be parameterized based solely on the human perception threshold. Since the 2nd-order rotation rate limit does not return to the input signal, a feedback is realized by means of a PID gain. This PID element can be designed iteratively or parameterized using optimization methods.

Washout is realized via a 2nd-order high-pass filter, $HP_{wo}$, as in the CWA:

$$HP_{wo} = k_0 \cdot \frac{s^2}{s^2 + 2Dw_{0,HP} + w_{0,HP}^2}$$  \(1\)

As stated by [11], the transfer function of Equation (1) can be interpreted as a single-mass oscillator. The natural frequency of the washout filter $w_{0,HP}$ can be calculated according to [3] (p. 64) by

$$w_{0,HP} = \sqrt{\frac{x_{\text{max}}}{x_{\text{max}}}}$$  \(2\)

with the acceleration perception threshold $x_{\text{max}}$ and the workspace limit $|x_{\text{max}}|$. For the TBMCA, a higher value can be chosen for the natural frequency, as the washout is compensated by tilt coordination. A too high value, however, leads to higher tilt rotation and therefore increases the risk of exceeding the maximum tilt rotation rate limit. For our studies, a value of twelve times the natural frequency according to Equation (2) seemed a good compromise between washout speed and compliance with the workspace limits. The PID gain is parametrized iteratively.

![Figure 3. Ideal motion cueing algorithm, based on [5] (p. 51).](image1)

![Figure 4. Structure of the proposed TBMCA.](image2)
3. Performance

The CWA, CMCA and TBMCA were analyzed in a simulation environment in terms of their workspace demand and accuracy by means of two driving maneuvers. These are as follows:

1. Acceleration from standstill over 25 s at different accelerator pedal positions (APPs) and subsequent coasting over 25 s; the reference acceleration signal was calculated using an electric vehicle model of the Speed4E driveline [12].
2. WLTC, which represents a more realistic driving cycle.

3.1. Maximum Scaling Factor

For both cases, we analyzed the needed workspace demand to perform these maneuvers in our driving simulator. Therefore, we investigated which maximum scaling factor can be chosen without violating the workspace limitations. For reasons of comparability, a scaling factor is considered valid if the maximum absolute difference between the reference acceleration and the MCA output is smaller than 0.15 m/s². This was found to be the differential threshold for linear acceleration identified in a field study by [13] (as cited in [14] (p. 330)).

The results in Table 2 show that the valid scaling factors for the CWA drop very fast, since the high inaccuracies violate the requirement related to the maximum absolute difference between the reference acceleration and the MCA output. The CMCA and TBMCA reach nearly the same results. This confirms that the CMCA and the TBMCA are suitable for accurately reproducing the reference acceleration at relatively high scaling factor values.

Table 2. Scaling factors (calculated in steps of 0.05) of all three MCAs at different APPs.

<table>
<thead>
<tr>
<th>APP in %</th>
<th>10</th>
<th>20</th>
<th>30</th>
<th>40</th>
<th>50</th>
<th>60</th>
<th>70</th>
<th>80</th>
<th>90</th>
<th>100</th>
</tr>
</thead>
<tbody>
<tr>
<td>Max. acceleration in m/s²</td>
<td>0.55</td>
<td>1.13</td>
<td>1.70</td>
<td>2.27</td>
<td>2.80</td>
<td>3.36</td>
<td>3.92</td>
<td>4.48</td>
<td>5.04</td>
<td>5.32</td>
</tr>
<tr>
<td>Scaling factor CWA</td>
<td>1.00</td>
<td>0.60</td>
<td>0.40</td>
<td>0.30</td>
<td>0.25</td>
<td>0.20</td>
<td>0.15</td>
<td>0.15</td>
<td>0.10</td>
<td>0.10</td>
</tr>
<tr>
<td>Scaling factor CMCA</td>
<td>1.00</td>
<td>1.00</td>
<td>0.95</td>
<td>0.70</td>
<td>0.60</td>
<td>0.50</td>
<td>0.45</td>
<td>0.40</td>
<td>0.35</td>
<td>0.35</td>
</tr>
<tr>
<td>Scaling factor TBMCA</td>
<td>1.00</td>
<td>1.00</td>
<td>1.00</td>
<td>0.80</td>
<td>0.65</td>
<td>0.55</td>
<td>0.50</td>
<td>0.45</td>
<td>0.40</td>
<td>0.35</td>
</tr>
</tbody>
</table>

Figure 5 shows the MCA outputs of an acceleration with 50% APP and a scaling factor of 0.5. It can be seen that the output of the TBMCA exactly follows the reference acceleration. The CMCA follows the reference acceleration only with a small error in the beginning. For the CWA, the biggest inaccuracies occur after dynamic changes in the acceleration (3–7 s and 20–30 s).

Regarding the workspace demand, the translational displacement for the TBMCA can be reduced by 22% compared to the CWA and by 37% compared to the CMCA due to the high washout rate. This, on the other hand, comes with a higher maximum tilt angle.

The results for the WLTC are summarized in Table 3 and discussed later.

Table 3. Comparison of the MCAs for the WLTC driving cycle.

<table>
<thead>
<tr>
<th>MCA</th>
<th>Scaling</th>
<th>CC</th>
<th>AD</th>
<th>RMSE</th>
<th>Workspace Demand</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Translation</td>
</tr>
<tr>
<td>WA</td>
<td>1.00</td>
<td>0.851</td>
<td>0.211</td>
<td>0.108</td>
<td>7.47 m</td>
</tr>
<tr>
<td>CMCA</td>
<td>1.00</td>
<td>1.00</td>
<td>1.54 × 10⁻³</td>
<td>4.02 × 10⁻³</td>
<td>9.15 m</td>
</tr>
<tr>
<td>TBMCA</td>
<td>1.00</td>
<td>1.00</td>
<td>4.77 × 10⁻⁴</td>
<td>2.82 × 10⁻⁴</td>
<td>7.64 m</td>
</tr>
</tbody>
</table>
3.2. Performance According to Quality Metrics

The MCAs were then compared regarding quantitative quality metrics. As quality metrics, the correlation coefficient (CC, Equation (3)), the absolute difference (AD, Equation (4)) [15] and the root mean square error (RMSE, Equation (5)) were calculated:

\[
CC = \frac{\max R(a_{ref}, a_{MCA})}{\max R(a_{ref}, a_{ref})} \tag{3}
\]

\[
AD = \frac{\int |a_{ref} - a_{MCA}| \, dt}{\int |a_{ref}| \, dt} \tag{4}
\]

\[
RMSE = \sqrt{\frac{1}{n} \sum (a_{ref} - a_{MCA})^2} \tag{5}
\]

The cross-correlation coefficient CC is defined as the normalized cross-correlation of the reference signal \(a_{ref}\) and the output signal \(a_{MCA}\). It lies in the range between 0 and 1 and indicates a better result if CC is close to 1. The absolute difference AD describes “the ratio of the area of the difference between the two signals divided by the area of the reference signal” [15]. The RMSE is commonly used to compare data [16]. For AD and RMSE, a small value is desired.

Figure 6 shows the results for the individual quality metrics plotted against the APP. It can be seen that the proposed motion cueing algorithm TBMCA outperforms the CMCA and the CWA at all applied metrics. Furthermore, it can be seen that the performance of the CWA decreases with increasing APP. The CWA can reproduce these more dynamic maneuvers with higher maximum accelerations and jerk only with a loss of accuracy. For the CMCA, relatively small errors occur during high dynamic acceleration changes. The TBMCA can also reproduce these dynamic components. It shows even better accuracy than the CMCA, which has an acceptable performance. Thus, values for AD and RMSE in the range of \(10^{-4}\) can be achieved.
subjective evaluation of the TBMCA. The next step was a study on the

regarding the tilt, the TBMCA has the widest range, since it was developed to map most
of the reference acceleration via tilt coordination.

3.3. Limitations of the TBMCA

Regardless of the almost perfect simulation results, there are also limitations resulting
from the closed-loop implementation.

First, if the scaling factor is set too high, the tilt rotation can exceed its limit. Higher
values are filtered by the saturation function. However, this results in a high translational
acceleration component that cannot be represented within the limited linear motion space.

Second, if the tilt rotation is relatively high or low at a constant level (i.e., at high
and low lasting accelerations), and the reference acceleration changes suddenly, the tilt
coordination will follow the reference signal only with a time delay due to the rotation
rate limit. This also results in a high translational acceleration component that cannot be
represented within the limited linear motion space. Thus, for the TBMCA a slightly higher
translational workspace demand or a lower scaling factor is necessary if acceleration and
braking change suddenly.

Considering this, the study design has an important influence on the parametrization
of the TBMCA.

4. Study

The proposed motion cueing algorithm outperforms the CWA and the CMCA in a
simulation environment for the given test scenarios. The next step was a study on the
subjective evaluation of the TBMCA.

4.1. Study Design

The driving profile in this study consisted of an acceleration phase, a coasting phase
and a braking phase. It was calculated by using the Speed4E driveline model and scaled
by 50%. In the first maneuver, the test subjects were asked to accelerate up to a speed of
120 km/h by pushing the APP by 50%. As an orientation, the APP and BPP (brake pedal
position) were displayed in virtual reality (VR). The APP was limited to 50%, and the BPP
was limited to 30%, on the software side, in order to ensure that all the test subjects experienced
the same drive profile. A maximum acceleration of 2.80 m/s² (scaled 1.40 m/s²) was reached,
which lies in the range of accelerations in typical traffic situations of 1.0 to 3.3 m/s² [17]
(p. 102). After the acceleration phase, a coasting phase to 100 km/h followed. Finally, the
test subjects braked into standstill. In addition, the negative acceleration was downscaled
with a factor of 0.6, which leads to a more realistic feeling in braking situations [6] (p. 105).
This whole maneuver was repeated once to obtain more reliable results.
During the whole study, the test subjects wore an Oculus Rift VR Headset. Wind and tire noises were presented via noise-cancelling headphones. After the maneuvers, the test subjects answered the following four questions:

1. How do you rate the quality of the acceleration presentation on a scale from 1 (very bad) to 7 (very good)?
2. How strong was the feeling of being rotated on a scale from 1 (very weak) to 7 (very strong)?
3. How often did you feel that improper accelerations occurred on a scale from 1 (not at all) to 7 (very often)?
4. How do you rate the correspondence between the visual and vestibular sensory impression on a scale from 1 (very bad) to 7 (very good)?

The first question relates to the overall evaluation of the presented acceleration. The second question concerns the perception of the tilt rate and tilt acceleration. The third question refers to the washout, and the fourth question refers to the impact of scaling on the evaluation of the visual and vestibular impression. For every question, the test subjects had the possibility to explain their rating.

4.2. Results

The participant group consisted of 13 male and 4 female test subjects between the ages of 22 and 35 (M = 26.7; SD = 4.0). Eight of them were scientific employees, and nine of them were students at Technical University Darmstadt. Eight test subjects already had experience in a dynamic driving simulator. Figure 7 shows the results of the subjective evaluation.

![Figure 7. Results of the subjective evaluation of the TBMCA.](image)

For all four questions, Wilcoxon signed-rank tests were applied. The test statistics indicate that the median values (6, 2, 1, 6) deviate significantly from the scale median value of 4 at the 0.1% significance level (p < 0.001).

The results show that the overall impression was good (Question 1). Most of the negative impressions referred to the transition from the acceleration phase to the coasting phase, which results in a sharp change in acceleration. However, this criticism concerns the vehicle model and the motion cueing algorithm as such. The turning rates and accelerations were rated as not noticeable or slightly noticeable by most of the test subjects (Question 2). Nevertheless, one test subject felt the tilt. The washout was hardly noticed at all (Question 3). This is relevant insofar as the relatively high washout rate was fully compensated by the motion cueing algorithm. Last but not least, the scaling of 50% was not perceived negatively by most test subjects (Question 4). The evaluation shows that a high correspondence between visual and vestibular perception was achieved.
5. Conclusions

In this paper, a threshold-based motion cueing algorithm was developed and evaluated throughout a test subject study in the IMS driving simulator. In the simulation environment, it was compared to the classical washout algorithm and the compensation algorithm. The translational workspace demand can be reduced by over 20% for specific driving scenarios whilst enhancing the tilt angle activity. By means of the selected objective criteria of cross-correlation, absolute difference and RMSE, it showed nearly ideal results. Subjective evaluation demonstrated that even high washout rates can be realized without the test subjects noticing. Overall, the motion cueing was rated as very good.

Further research will focus on exploiting the given workspace through prepositioning strategies. This could further decrease the overall workspace demand and thus allow higher scaling factors for dynamic acceleration motion cueing.

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**References**
