



Article Research on the dq-Axis Current Reaction Time of an Interior Permanent Magnet Synchronous Motor for Electric Vehicle

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Abstract: An interior permanent magnet synchronous motor (IPMSM) is a kind of drive motor with high power density that is suitable for electric vehicles. In this paper, the dq-axis current reaction time of IPMSM was investigated in order to improve the reaction time of the electric vehicle. Firstly, the mathematical model of the current-loop decoupling of IPMSM was presented. Secondly, the controller design of dq-axis current-loop decoupling of IPMSM was investigated by the methods of proportional integral (PI) and internal model control PI (IMC-PI). Thirdly, based on the methods of PI and IMC-PI, the influence of the inverter switching frequency on the dq-axis current reaction time of IPMSM was analyzed and simulated, and it was found that the inverter switching frequency only had a significant influence on the parameters set of the PI controller. Lastly, compared with the PI method, the results of the simulation and hardware experiment demonstrate that the dq-axis current reaction time of IPMSM was improved by the IMC-PI method, and the IMC-PI method had the advantage of simple parameters setting and was not influenced by the inverter switching frequency.

Keywords: start-up response; synchronous motor; current-loop decoupling; electric vehicle; dq-axis current



Citation: Huang, A.; Chen, Z.; Wang, J. Research on the dq-Axis Current Reaction Time of an Interior Permanent Magnet Synchronous Motor for Electric Vehicle. *World Electr. Veh. J.* 2023, *14*, 196. https:// doi.org/10.3390/wevj14070196

Academic Editors: Zhongze Wu and Ziqiang Zhu

Received: 15 June 2023 Revised: 14 July 2023 Accepted: 20 July 2023 Published: 23 July 2023



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1. Introduction

IPMSM is a rotor permanent magnet motor with permanent magnets embedded in the rotor [1–3]. With the advantages of high power density and high torque/inertia ratio, IPMSM is widely used in high-performance drive systems such as industrial robots, equipment manufacture, and electric vehicles. In order to improve the driving performance of IPMSM, the current-loop control of IPMSM were investigated in some literatures. The current-loop control of IPMSM is an output torque control strategy, which aims to improve the dynamic response capability of IPMSM, including the reaction time of the starting operation state and constant speed performance of the stable operation state [4,5].

Usually, the theoretical modeling and hardware experiment of current loop control of IPMSM are based on the dq synchronous rotating coordinate system [6,7]. In this coordinate system, the amplitudes of coupling voltages of IPMSM are determined by the torque (dq-axis current) and speed of IPMSM [8,9]. The reason is that the high torque or high speed will increase the amplitude of coupling voltages, which will seriously affect the performance of current-loop control of IPMSM. For the traditional controller design of the current loop of the motor, the common practice is to ignore the coupling voltages of dq synchronous rotating coordinate system [10–12]. In this condition, if the q-axis current changes, an error will occur in the d-axis current, which will lead to the distortion of the motor's output torque and dynamic response performance.

With the certain electrical parameters, the dq-axis coupling voltages of IPMSM can be eliminated by voltage feedforward decoupling control (VFDC). However, the electrical parameters of IPMSM depend on its operating conditions and control modes [13,14]. Therefore, the constant values setting of electrical parameters of IPMSM is not beneficial for the voltage decoupling of IPMSM thoroughly.

Based on the Popov hyperstability theory, Qiu T. et al. proposed an adaptive observer to monitor the permanent magnet flux linkage of PMSM, and the experimental results showed that the sensitivity of q-axis inductance of PMSM was decreased by the adaptive observer and adaptation proportional-integral (PI) controller [15,16]. However, with the increase in the PMSM speed, the q-axis inductance errors of the adaptive observer increased. Saleh M. and Hassan M. et al. proposed a comprehensive control method including the fusion of the sliding-mode method and type-2 neuro-fuzzy systems to control the speed of the induction motor (or the doubly fed induction generator). The analysis and comparison results indicated that the adaptive sliding-mode type-2 neuro-fuzzy controller can control the induction motor (or the doubly fed induction generator) with higher performance (compared with type-1 neuro-fuzzy systems) [17,18]. However, the speed fluctuation of the induction motor still existed, and the reaction time of the motor was not analyzed in detail. Xu W. et al. proposed a novel sliding-mode-based extended state observer (SMESO) to improve the dynamic response capability of the permanent magnet synchronous motor (PMSM). After the signal was input into the feed-forward compensation controller, the comprehensive simulation and experiment's results show that the dynamic response capability of PMSM can be improved [19]. Furthermore, some improved methods based on the field-oriented control (FOC), direct torque control (DTC), and sliding-mode observer (SMO) were proposed to investigate the dynamic response of PMSM [20–24]. Nevertheless, it is necessary to explore a simple method to improve the reaction time of PMSM on the basis of traditional PI control technology.

In order to improve the dq-axis current reaction time of IPMSM with a simplified voltage-decoupling controller, PI and IMC-PI methods were used to investigate the current-loop control of IPMSM in this paper. The main contributions of this paper are as follows. Firstly, the theoretical model of current-loop decoupling of IPMSM was analyzed and presented. Secondly, the controller design of current-loop decoupling of IPMSM was investigated, including the methods of PI and IMC-PI. Thirdly, based on the methods of PI and IMC-PI, the influence of inverter switching frequency on the dq-axis current reaction time of IPMSM was simulated and analyzed. The analysis results showed that the inverter switching frequency had a significant influence on the parameters set of the PI controller. Lastly, the results of the simulation calculation and hardware experiment demonstrated that compared with the PI method, the dq-axis current reaction time of IPMSM was improved by the IMC-PI method, and the IMC-PI method had the advantage of the easy setting of the control parameters.

2. Mathematical Model of the Current Loop of IPMSM

In the dq synchronous rotating coordinate system, if the magnetic saturation, eddy current loss, and copper loss are ignored, then the voltage equation of *d*-axis and *q*-axis of IPMSM can be described as

$$\begin{cases} u_d = Ri_d + L_d \frac{d}{dt} i_d - \omega_e \psi_q \\ u_q = Ri_q + L_q \frac{d}{dt} i_q + \omega_e \psi_d \end{cases}$$
(1)

where the subscript symbols *d* and *q* are the d-axis and q-axis, respectively, u_d and u_q are the voltages, i_d and i_q are the currents, L_d and L_q are the inductances, ψ_d and ψ_q are the flux linkages, *R* is the resistance of stator phase winding, and ω_e is the electric angular velocity of rotor of IPMSM [25–27]. In addition, the d-axis flux linkage ψ_d and q-axis flux linkage ψ_q can be written as

$$\begin{cases} \psi_d = L_d i_d + \psi_f \\ \psi_q = L_q i_q \end{cases}$$
(2)

where ψ_f is the excitation flux linkage of permanent magnets of IPMSM.

Substitute Equation (2) into Equation (1), then the voltage equation of IPMSM can be rewritten as

$$\begin{cases} u_d = Ri_d + L_d \frac{a}{dt} i_d - \omega_e L_q i_q \\ u_q = Ri_q + L_q \frac{d}{dt} i_q + \omega_e \left(L_d i_d + \psi_f \right) \end{cases}$$
(3)

Equation (3) indicates that the q-axis coupling term $\omega_e L_q i_q$ exists in the d-axis voltage u_d , and the d-axis coupling term $\omega_e L_d i_d$ exists in the q-axis voltage u_q , and thus the couple voltages occurred in the dq synchronous rotating coordinate system of IPMSM. Furthermore, the amplitude of dynamic term $\omega_e \psi_f$ is decided by the electric angular velocity ω_e (namely the speed of rotor of IPMSM).

In order to design the controller of the current loop of IPMSM, the decoupling of coupling terms $\omega_e L_q i_q$ and $\omega_e L_d i_d$ should be completed. Therefore, by adopting the decoupling method that ignores the coupling terms $\omega_e L_q i_q$ and $\omega_e L_d i_d$, and also ignores the dynamic term $\omega_e \psi_f$, Equation (3) can be simplified as

$$\begin{cases} u_d = Ri_d + L_d \frac{d}{dt} i_d \\ u_q = Ri_q + L_q \frac{d}{dt} i_q \end{cases}$$
(4)

After the Laplace transform [28], the transfer function between IPMSM's dq-axis current and dq-axis voltage can be described as

$$\begin{cases} G_d(s) = \frac{i_d(s)}{u_d(s)} = \frac{1}{L_d s + R} \\ G_q(s) = \frac{i_q(s)}{u_q(s)} = \frac{1}{L_q s + R} \end{cases}$$
(5)

Based on Equation (5) and automatic control theory, the traditional PI controller of the current loop of IPMSM can be obtained as

$$\begin{pmatrix}
u_d^* = \left(k_{pd} + \frac{k_{id}}{s}\right) \left(i_{dref} - i_d\right) - \omega_e L_q i_q \\
u_q^* = \left(k_{pq} + \frac{k_{iq}}{s}\right) \left(i_{qref} - i_q\right) + \omega_e \left(L_d i_d + \psi_f\right)
\end{cases}$$
(6)

where k_{pd} and k_{id} are the proportional coefficient and integral coefficient of the d-axis current loop, and i_{dref} and i_d are the set value and feedback value of the d-axis current. In the same way, k_{pq} and k_{iq} are the proportional coefficient and integral coefficient of the q-axis current loop, and i_{qref} and i_q are the set value and feedback value of q-axis current.

3. Controller Design of Current-Loop Decoupling of IPMSM

3.1. PI Controller Design

Considering the transfer function of d-axis voltage $G_d(s)$ and inverter $K_{pwm}/(T_{pwm}s+1)$ [29], the d-axis PI current-loop structure of IPMSM is shown in Figure 1a. In this paper, the transfer function of d-axis voltage $G_d(s)$ is derived from the mathematical model of the current loop of IPMSM (see Section 2 of this paper), and the transfer function of inverter $K_{pwm}/(T_{pwm}s+1)$ can be assumed as a pure lag amplification link with delay. Additionally, the transfer function of q-axis voltage $G_q(s)$ is same with the transfer function of d-axis voltage $G_d(s)$ (see Equation (5)), and thus the q-axis PI current-loop structure of IPMSM is the same as Figure 1a, as shown in Figure 1b.



Figure 1. The PI current-loop structure of IPMSM: (**a**) d-axis PI current-loop structure; (**b**) q-axis PI current-loop structure.

In Figure 1, K_{pwm} and T_{pwm} are the magnification factor and switching cycle of the inverter, respectively. Taking the d-axis PI current-loop structure of IPMSM as an example, the loop transfer function of Figure 1a can be written as

$$G_{d}(s) = \frac{k_{pd}(\tau_{i}s+1)}{\tau_{i}s} \frac{K_{pwm}}{T_{pwm}s+1} \frac{1/R}{\frac{L_{d}}{R}s+1} \bigg|_{\tau_{i}=k_{wd}/k_{id}}$$
(7)

It is assumed that $\tau_i = k_{pd}/k_{id} = L_d/R$, where $\tau_i = k_{pd}/k_{id}$ is the structure transformation of the PI controller and $\tau_i = L_d/R$ is the structure transformation of the transfer function of IPMSM; then, the extreme points of the d-axis transfer function $G_d(s)$ of Equation (7) can be eliminated. In this condition, Equation (7) can be regarded as the typical I type system, as shown in Equation (8).

$$G_d(s) = \frac{k_{pd}K_{pwm}}{L_d(T_{pwm}s+1)s} = \frac{K_I}{(T_{pwm}s+1)s}$$
(8)

In Equation (8), the parameter K_I is described as $K_I = k_{pd}K_{pwm}/L_d$. According to the motion control theory of typical I type system [29,30], if the desired overshoot of the d-axis current of IPMSM is less than 5%, then the parameter K_I should be selected as

$$K_I = \frac{1}{2T_{pwm}} \tag{9}$$

Under situation of $K_I = k_{pd}K_{pwm}/L_d = 1/(2T_{pwm})$, the proportional coefficient k_{pd} and integral coefficient k_{id} of the d-axis current loop of IPMSM can be calculated as

$$k_{pd} = \frac{L_d}{2T_{pwm}K_{pwm}} \tag{10}$$

$$K_{id} = \frac{K_{pd}}{\tau_i} = \frac{R}{2T_{pwm}K_{pwm}} \tag{11}$$

In the same way, the proportional coefficient k_{pq} and integral coefficient k_{iq} of the q-axis current loop of IPMSM can be inferred as

$$K_{pq} = \frac{L_q}{2T_{pwm}K_{pwm}} \tag{12}$$

$$K_{iq} = \frac{K_{pq}}{\tau_i} = \frac{R}{2T_{pwm}K_{pwm}}$$
(13)

In addition, the above PI parameters (k_{pd} , k_{iq} , k_{pq} , and k_{iq}) of the dq-axis current loop of IPMSM also can be inferred and obtained by the classical automatic control theory. Taking the d-axis PI current-loop structure of IPMSM as an example, based on Equation (8), the d-axis closed-loop transfer function of Figure 1a can be written as

$$\Phi_d(s) = \frac{k_{pd}k_{pwm}}{L_d T_{pwm} s^2 + L_d s + k_{pd}K_{pwm}} = \frac{K_g}{s^2 + \frac{1}{T_{pwm}}s + K_g} \bigg|_{K_g = \frac{k_{pd}K_{pwm}}{L_d T_{pwm}}}$$
(14)

In the classic control theory of some references [31,32], the transfer function of the second-order system can be written as

$$\Phi(s) = \frac{\omega_n^2}{s^2 + 2\xi\omega_n s + \omega_n^2} \tag{15}$$

Therefore, the relationship between the transfer function of the second-order system and typical type I system can be obtained by the comparison of Equations (14) and (15)

$$\omega_n = \sqrt{K_g} = \frac{1}{2\xi T_{pwm}} \tag{16}$$

After combining Equations (14) and (16), the proportional coefficient k_{pd} and integral coefficient k_{id} of Equation (14) can be obtained as

$$K_{pd} = \frac{L_d}{4\xi^2 T_{pwm} K_{pwm}} \tag{17}$$

$$K_{id} = \frac{K_{pd}}{\tau_i} = K_{pd} \frac{R}{L_d} = \frac{R}{4\xi^2 T_{pwm} K_{pwm}}$$
(18)

If the damping coefficient is $\zeta = 0.707$ (ideal value), then the proportional coefficient k_{pd} and integral coefficient k_{id} of the d-axis current loop of IPMSM can be further refined as

$$\begin{cases} K_{pd} = \frac{L_d}{2T_{pwm}K_{pwm}} \\ K_{id} = \frac{R}{2T_{pwm}K_{pwm}} \end{cases}$$
(19)

Similarly, the proportional coefficient k_{pq} and integral coefficient k_{iq} of the q-axis current loop of IPMSM can be inferred as

$$\begin{cases} K_{pq} = \frac{L_q}{2T_{pwm}K_{pwm}} \\ K_{iq} = \frac{R}{2T_{pwm}K_{pwm}} \end{cases}$$
(20)

The comparison of Equations (10)–(13), (19) and (20) indicates that the above two PI parameter tuning results of IPMSM are the same. Actually, the above two PI parameter tuning results of IPMSM all originated from the dynamic performance indicators and empirical formulas of the typical type I system.

3.2. IMC-PI Controller Design

In Section 3.1, the PI parameter tuning result of IPMSM is under the condition of full dq-axis current-loop decoupling. Actually, the existence of salient pole characteristics in IPMSM determines that the dq-axis current loop cannot be fully decoupled. This phenomenon of non-fully decoupled dq-axis current loop is not beneficial to the high-precision and low-sensitivity parameters setting of the controller. In order to ensure the high precision and low sensitivity of the parameters setting of the controller, the IMC method

was adopted in this paper to improve traditional PI controller design of the current loop of IPMSM, which is named as the IMC-PI method. Furthermore, it should be noted that the aim of the low-sensitivity parameters setting of the controller is to improve the operational stability (anti-interference ability) of IPMSM. Therefore, there is no contradiction between the high precision and low sensitivity of the parameters setting of the controller.

Figure 2 shows the structure of IMC, where the parameters of Figure 2 are described in Table 1.



Figure 2. The structure of IMC.

Table 1. The parameters of IMC.

Parameters	Descriptions	
R(s)	System's input signal	
C(s)	Feedback controller	
$\hat{D}(s)$	Feedback signal	
$G_{IMC}(s)$	IMC controller	
$G_p(s)$	System's model	
$\hat{G}_{p}(s)$	Internal model	
D(s)	Interference signal	
Y(s)	System's output signal	

In Figure 2, the node signal U(s) can be described as

$$U(s) = \frac{(R(s) - D(s))G_{IMC}(s)}{1 + (G_p(s) - \hat{G}_p(s))G_{IMC}(s)}$$
(21)

and the system's output signal Y(s) is

$$Y(s) = G_p(s)U(s) + D(s)$$
⁽²²⁾

According to Equations (21) and (22), the relationship among the system's output signal Y(s), system's input signal R(s), and interference signal D(s) can be expressed as

$$Y(s) = \frac{G_p(s)G_{IMC}(s)}{1 + (G_p(s) - \hat{G}_p(s))G_{IMC}(s)}R(s) + \frac{1 - G_{IMC}(s)\hat{G}_p(s)}{1 + (G_p(s) - \hat{G}_p(s))G_{IMC}(s)}D(s)$$
(23)

Based on Equation (23), the structure of IMC (see Figure 2) can be simplified, as shown in Figure 3. In Figure 3, the feedback controller C(s) can be described as

$$C(s) = \frac{G_{IMC}(s)}{1 - G_{IMC}(s)\hat{G}_p(s)}$$
(24)



Figure 3. Equivalent structure simplification of IMC.

If there is no interference signal D(s), and $G_{IMC}(s) = \hat{G}_p(s)^{-1}$, then the relationship between the system's input signal R(s) and system's output signal Y(s) can be expressed as

$$Y(s) = G_{IMC}(s)G_p(s)R(s) = G_p(s)^{-1}G_p(s)R(s) = R(s)$$
(25)

From Equation (25), it can be concluded that the IMC method is beneficial to ensure the consistence between the system's input signal R(s) and system's output signal Y(s).

Regardless of the interference signal D(s), the d-axis IMC-PI current-loop structure of IPMSM is shown in Figure 4.



Figure 4. The *d*-axis IMC-PI current-loop structure of IPMSM.

It is assumed that $G_p(s) = \hat{G}_p(s)$, and

$$G_{IMC}(s) = \hat{G}_p^{-1}(s)L(s) = G_p^{-1}(s)L(s)$$
(26)

where $L(s) = \varepsilon/(s + \varepsilon)$, and ε is the modulation parameter of the d-axis IMC-PI currentloop structure of IPMSM. On this basis, substitute Equation (26) into Equation (24), then the feedback controller C(s) and the parameter tuning results of the d-axis IMC-PI current-loop structure of IPMSM can be obtained as

$$C(s) = \varepsilon \left(L_d + \frac{R}{s} \right) \tag{27}$$

$$\begin{cases} K_{pd(IMC)} = \varepsilon L_d \\ K_{id(IMC)} = \varepsilon R \end{cases}$$
(28)

The comparison results between Equations (19) and (28) indicates that the number of parameter tuning is decreased from two (T_{pwm} and K_{pwm} of PI current-loop structure) to one (ε of IMC-PI current-loop structure), and thus the difficulty of parameter tuning is also decreased by the IMC-PI current-loop structure of IPMSM.

Similarly, the parameter tuning results of the q-axis IMC-PI current-loop structure of IPMSM can be inferred as

$$\begin{cases} K_{pq(IMC)} = \varepsilon L_q \\ K_{iq(IMC)} = \varepsilon R \end{cases}$$
(29)

From Equations (28) and (29), it can be concluded that responsiveness of the dq-axis current of IPMSM can be improved by the larger modulation parameter ε of the IMC-PI current-loop structure. However, the larger modulation parameter ε will also increase the overshoot and stability time of the dq-axis current. Therefore, the selection of modulation parameter ε of the IMC-PI current-loop structure should be solved reasonably.

3.3. The Modulation Parameter Selection of IMC-PI

In the practical engineering application, the current loop of IPMSM can be transformed and approximated to one order system. If the inverter transfer function $K_{pwm}/(T_{pwm}s+1)$ is ignored, then the d-axis open-loop transfer function $G_{d1}(s)$ and d-axis closed-loop transfer function $\Phi_{d1}(s)$ of IPMSM can be described as

$$G_{d1}(s) = \left(K_{pd} + \frac{K_{id}}{s}\right) \frac{1}{L_d s + R}$$
(30)

$$\Phi_{d1}(s) = \frac{K_{pd}s + K_{id}}{L_d s^2 + K_{pd}s + Rs + K_{id}}$$
(31)

Substitute the proportional coefficient $K_{pd(IMC)}$ and integral coefficient $K_{id(IMC)}$ of Equation (28) into Equation (31), then the Equation (31) can be simplified as

$$\Phi_{d1}(s) = \frac{\varepsilon}{s+\varepsilon} = \frac{1}{Ts+1} = \frac{1}{\frac{1}{\varepsilon}s+1}\Big|_{T=\frac{1}{\varepsilon}}$$
(32)

where Equation (32) is a closed-loop transfer function with one order system, and its open-loop system is a typical I type system.

According to the definition of bandwidth frequency ω_b of typical Type I systems

$$20lg|\Phi(j\omega_b)| = 20lg\frac{1}{\sqrt{1+T^2\omega_b^2}} = 20lg\frac{1}{\sqrt{2}} \Rightarrow \omega_b = \frac{1}{T} = \varepsilon$$
(33)

the modulation parameter ε of the IMC-PI current-loop structure is also the bandwidth frequency of the closed-loop transfer function of IPMSM. Moreover, the transfer function $1/(L_ds + R)$ of the d-axis current loop of IPMSM can be regarded as a *RL* system, which is composed of d-axis inductance L_d and resistance *R*. If it is assumed that the parameter $T = L_d/R$, then the modulation parameter ε of the IMC-PI current-loop structure can be further described as

$$=2\pi \frac{R}{L_d} \tag{34}$$

where the coefficient 2π converts the unit of modulation parameter ε of the IMC-PI currentloop structure from frequency H_z to radians per second rad/s.

ε

Considering that IPMSM has both the d-axis current loop and q-axis current loop, the modulation parameter ε of the IMC-PI controller is calculated as

$$\varepsilon = 2\pi \min\left(\frac{R}{L_d}, \frac{R}{L_q}\right) \tag{35}$$

4. Simulation Analysis and Experimental Verification

4.1. Simulation Analysis

In order to analyze the difference between the PI method and IMC-PI method, and verify the advantage of the IMC-PI method in improving the dq-axis current reaction time of IPMSM, some simulation analysis is carried out in this section. The electrical parameters of IPMSM are shown in Table 2, and the dq-axis current-loop structure of IPMSM is shown in Figure 5.

Table 2. Electrical parameters of IPMSM.

Item	Value	Unit
Number of phases	3	-
Power	1.5	kW
Rated line voltage	220	V
Rated line current	4.5	А
Rated speed	2000	r/min
Number of stator slots	18	-
Number of rotor poles	8	-
Air-gap length	0.5	mm
Phase resistance	2.92	Ω
D-axis inductance	8.96	mH
Q-axis inductance	12.29	mH
Excitation flux linkage	0.955	Wb



Figure 5. The dq-axis current-loop structure of IPMSM.

Based on the Equations (19), (20), (28) and (29), and the electrical parameters of IPMSM (see Table 2), the parameter tuning results of the PI method and IMC-PI method are shown in Table 3, and the relevant simulation analysis results of the dq-axis current reaction time of IPMSM are shown in Figures 6–8. In the process of simulation analysis, the magnification factor of the inverter is $K_{pwm} = 1$, and the IPMSM's speed is zero (namely, the IPMSM's rotor is in the locked condition).

Table 3. Parameter tuning results of the PI method and IMC-PI method.

	Item	$T_{pwm} = 0.001s$	$T_{pwm} = 0.01s$	$T_{pwm} = 0.1s$
PI method	K_{pq}	6.145	0.6145	0.06145
	K _{iq}	1460	146	14.6
	K_{pd}	4.48	0.448	0.0448
	Κ _{id}	1460	146	14.6
IMC-PI method	$K_{pq(IMC)}$	18.3	18.3	18.3
	$K_{ia(IMC)}$	4356	4356	4356
	$K_{pd(IMC)}$	13.3	13.3	13.3
	$K_{id(IMC)}$	4356	4356	4356



Figure 6. The simulation analysis results of the dq-axis current reaction time of IPMSM $(T_{pwm} = 0.001s)$: (a) PI method; (b) IMC-PI method.



Figure 7. Cont.



Figure 7. The simulation analysis results of the dq-axis current reaction time of IPMSM ($T_{pwm} = 0.01s$): (a) PI method; (b) IMC-PI method.



Figure 8. The simulation analysis results of the dq-axis current reaction time of IPMSM ($T_{pwm} = 0.1s$): (a) PI method; (b) IMC-PI method.

In Figures 6–8, the step pulse amplitude of the q-axis target current is $i_{qref} = 5A$, and the d-axis target current is $i_{dref} = 0A$. From Figures 6–8, it can be concluded that with the IMC-PI method, the switching cycle T_{pwm} of the inverter almost has no impact on the dq-axis current reaction time of IPMSM ($T_{pwm} = 0.001s$, $T_{pwm} = 0.01s$, and $T_{pwm} = 0.1s$, respectively). However, when the switching cycle T_{pwm} of the inverter varies from 0.001 s to 0.1 s, the dq-axis current reaction time of IPMSM is decreased by the PI method. For example, based on the PI method and switching cycle $T_{pwm} = 0.01s$, the delay time of the dq-axis current reaction time of IPMSM is approximately 0.1 s, as shown in Figure 7a. What is more important is that when the switching cycle is $T_{pwm} = 0.1s$, the delay time of the dq-axis current reaction time of IPMSM is increased to 1 s (see Figure 8a).

In addition, as the switching cycle T_{pwm} increases, the stability of the dq-axis current of IPMSM decreases. For example, the mutual influence between the q-axis feedback current i_q and d-axis feedback current i_d occurs (see Figures 7a and 8a), and even the distortion of the q-axis feedback current i_q and d-axis feedback current i_d occurs (see Figures 7a and 8a).

The comparison results among Figures 6–8 indicate that by the PI method, the switching cycle T_{pwm} of the inverter plays an important role in the dq-axis current reaction time of IPMSM. However, the IMC-PI method can ensure a fine dq-axis current reaction time of IPMSM with a different switching cycle T_{pwm} of the inverter. These conclusions are consistent with the above analysis results (the comparison among Equations (19), (20), (28) and (29)).

4.2. Hardware Experimentation

Figure 9 shows the IPMSM's structure and test platform, where the electrical parameters of IPMSM are the same as Table 2. In Figure 9b, the rotor position of IPMSM is measured by the rotary encoder (2500 lines of resolution ratio), where the rotary encoder is coaxial with the rotor of IPMSM and installated in the back-end department of the rotor. The 2500 lines mean that if the rotor of IPMSM rotates one revolution (360 degrees), the rotary encoder will generate 2500 pulse signals. The more lines of rotary encoder, the more precise the position of the rotor.



Figure 9. Cont.



Figure 9. Experimental test of the dq-axis current reaction time of IPMSM: (**a**) IPMSM's structure; (**b**) test platform.

In order to keep the same operating conditions as the simulation model of Section 4.1, a magnetic particle brake is installed in the test platform of Figure 9b, and the magnetic particle brake is coaxial with the front-end department of the rotor.

During the experimental process, the experimental data were measured by a current sensor and processed by the software of the controller. If the three-phase currents of IPMSM were measured by an oscilloscope, the measured data looks more like the experimental data, but some calculation processes of Park transformation (from three-phase currents to dq-axis currents) should be achieved. Therefore, this paper adopts the current sensor and controller's software to measure and process the experimental data.

Figures 10 and 11 show the hardware test results of the dq-axis current reaction time of IPMSM by the PI method and IMC-PI method, where the inverter's switching cycle T_{pwm} are 0.001 s and 0.1 s, respectively. With the increase in the inverter's switching cycle T_{pwm} , Figures 10a and 11a indicate that the response time of the q-axis current of IPMSM is 25 ms $(T_{pwm} = 0.001s)$ and 50 ms $(T_{pwm} = 0.01s)$, respectively. However, if the IMC-PI method is adopted, the response time of the q-axis current of IPMSM is nearly stable regardless of whether the inverter's switching cycle is $T_{pwm} = 0.001s$ or $T_{pwm} = 0.01s$, which are shown in Figures 10b and 11b.



Figure 10. Cont.



Figure 10. The hardware test results of the dq-axis current reaction time of IPMSM ($T_{pwm} = 0.001s$): (a) PI method; (b) IMC-PI method.



Figure 11. The hardware test results of the dq-axis current reaction time of IPMSM ($T_{pwm} = 0.01s$): (a) PI method; (b) IMC-PI method.

The comparison between Figures 6 and 10 shows that, in the condition of the inverter's switching cycle $T_{pwm} = 0.001s$, there is no significant difference in the hardware test result and simulation result. For example, by the PI method, the q-axis current reaction time of the hardware test and simulation are 25 ms and 28 ms, respectively. In another example, the q-axis current reaction time of the hardware test and simulation are 12 ms and 13 ms by adopting the IMC-PI method.

However, with the increasing of the inverter's switching cycle T_{pwm} , a difference in the q-axis current reaction time between the hardware test result and simulation result occurs. Take the inverter's switching cycle $T_{pwm} = 0.01s$ and PI method as an example, the q-axis current reaction time of the hardware test and simulation are 95 ms and 135 ms, respectively. Compared with the PI method, the IMC-PI method still has a good performance, in that the hardware test result (13 ms) agrees with the simulation result (13 ms).

Therefore, the above comparison of the hardware test result and simulation result vividly demonstrates that the dq-axis current reaction time of IPMSM is improved by the IMC-PI method.

Furthermore, because the larger inverter's switching cycle T_{pwm} was not beneficial to the operation of the inverter (such as in the condition of $T_{pwm} = 0.1s$), the relevant hardware experimental test was not conducted in this paper.

5. Discussion

In Sections 4.1 and 4.2, the simulation results (see Figures 6 and 7) are compared and verified by hardware experiments (see Figures 10 and 11), and the hardware experiment results indicate that, based on the IMC-PI method, the stability time of the q-axis current start-up response of IPMSM was approximately 12 ms~13 ms, which was better than that of the PI method (25 ms~95 ms). However, the limitations of the proposed IMC-PI method and PI method should be discussed.

Firstly, the dq-axis current start-up response of IPMSM is only an intermediate quantity, and the final dq-axis control effect will be reflected in the speed and torque output of IPMSM.

Secondly, it is not that the shorter the stability time of dq-axis current start-up response of IPMSM the better, because the high overshoot of dq-axis current will cause the severe speed and torque output fluctuation of IPMSM, which is not beneficial to the safe operation and speed change of electric vehicles.

Thirdly, the results of the simulation and hardware experiment also demonstrate that the inverter's switching frequency has a significant influence on the parameter variation of the PI controller, thus affecting the control performance of the dq-axis current of IPMSM.

Therefore, in the next research work, inverter non-linearities (switching frequency), speed, and torque output of IPMSM should be fully considered, and the parameter variation of the PI method and IMC-PI method should be further researched.

6. Conclusions

Two methods were used in this paper to investigate the dq-axis current reaction time of IPMSM. After the theoretical model and controller design, the current-loop decoupling of IPMSM was presented, and the dq-axis current reaction time of IPMSM was simulated and analyzed. Then, the simulation results were verified by the hardware experiments, and the results of the simulation and hardware experiment indicated that the switching frequency of the inverter had a significant influence on the parameters setting of the PI controller. Lastly, the results of the simulation and hardware experiment demonstrated that, compared with the PI method, the dq-axis current reaction time of IPMSM was improved by the IMC-PI method. In addition, the results of the simulation and hardware experiment also showed that the IMC-PI method had the advantage of the easy setting of the control parameters and was not influenced by the inverter's switching frequency. **Author Contributions:** Conceptualization, A.H. and Z.C.; methodology, A.H. and Z.C.; software, A.H. and J.W.; validation, Z.C.; writing—original draft preparation, Z.C.; writing—review and editing, A.H. All authors have read and agreed to the published version of the manuscript.

Funding: This work was financially supported by the Scientific and Technological Project in Henan Province under Grant No. 232102241024.

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: Some or all data and models generated or used during the study are available in a repository or online.

Conflicts of Interest: The authors declare no conflict of interest.

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