Overview of Position-Sensorless Technology for Permanent Magnet Synchronous Motor Systems

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Abstract: In recent years, permanent magnet synchronous motors (PMSMs) have been widely used in industry. Position-sensorless control has the advantages of reducing costs and improving reliability, and is becoming one of the most promising technologies for permanent magnet synchronous motors. This article reviews the main position-sensorless technologies. The advantages and disadvantages of model-based and saliency-based techniques were summarized and compared. Finally, the developmental trends and research directions of position-sensorless technology were discussed.

Keywords: permanent magnet synchronous motor (PMSM); sensorless control; model-based method; saliency-based method

1. Introduction

Due to global warming and the energy crisis, new energy vehicles with fewer emissions, less pollution, and higher energy conversion efficiency are increasingly favored by governments and enterprises worldwide [1–4]. Permanent magnet synchronous motors (PMSMs) have been widely used in the industry due to the advantages of high power density, high efficiency, and a rapid control response [5–11].

A PMSM drive system is a typical nonlinear control system. To obtain good control performance, field-oriented control (FOC) [12–17], direct torque control (DTC) [18–25], sliding mode control (SMO) [26–33], and model predictive control (MPC) [34–44] have been used to improve the control performance of PMSMs. In [21], a novel DTC control strategy was proposed, which used the torque error square minimization technique to determine the duty cycle, thereby reducing the ripple size of the PMSM. As for the design of the observer, the work of [29] studied the main problems and developmental trends of the observer. As an efficient control strategy, MPC is used more and more widely. The authors of [35] proposed a sensorless control MPCC control scheme which enhanced the robustness of the system and improved the accuracy of estimating the rotor’s position.

However, these control methods need accurate information on the rotor’s position and speed, and the acquisition of the rotor’s position signals relies on mechanical sensors. Installing mechanical sensors not only increase the manufacturing costs and complexity of the system but also reduce the operating reliability of the system under extreme conditions. To solve this issue, sensorless control schemes have been invented. Sensorless control technology uses specific algorithms to estimate the rotor’s position and speed by detecting relevant signals in the motor’s windings. This control scheme has gradually become a trend in the development of PMSM control systems.

Over the past few decades, researchers have developed sensorless control techniques for a wide range of speeds from zero to high speed. Figure 1 shows the classification of sensorless technology approaches. Depending on the operating speed, sensorless control schemes can be divided into two categories: model-based methods [45–111] and saliency-based methods [112–167]. When the motor operates in the medium- to high-speed range, a
model-based approach is used. These mainly include two schemes: back-EMF estimation and flux linkage estimation. However, when the motor is running at low or zero speeds, due to factors such as modeling uncertainty and the nonlinearity of the inverter, the signal-to-noise ratio of the useful signal is very low and it is difficult to extract, so the model-based method does not work well at low speeds. People usually use the method of high frequency signal injection to obtain information on the rotor’s position. High-frequency signals mainly include rotating high-frequency voltage signals and pulsating high-frequency voltage signals.

**Figure 1.** Classification of position-sensorless control methods.

Due to the increasing application of position-sensorless control, this article introduces the most advanced position-sensorless control technologies of permanent magnet synchronous motors from the perspective of technological development. The main contribution is that it summarizes the research status of different methods, as well as the problems and plans for improvement of each method. Essentially, we explored and researched position-sensorless control methods. The feasibility, versatility, and effectiveness of these methods were analyzed and summarized. We also explored the future development and research directions of position-sensorless sensing.

The rest of this article is organized as follows. The Section 2 introduces the drive system of permanent magnet synchronous motors and the basic principles of sensorless control. In the Section 3, various sensorless control methods are introduced. The Section 4 discusses the developmental trends and research direction of position-sensorless sensing. The fifth section is the conclusion of this article.

2. The Composition of PMSM Drive Systems Based on Sensorless Control

2.1. Structure and Mathematical Model of PMSM Systems

Figure 2 shows the structure of a typical PMSM drive system, which mainly includes the current loop and hardware facilities. The hardware facilities include inverter, permanent magnet synchronous motor, power supply and various sensors, while the current loop
is composed of two PI controllers. The operation of the permanent magnet synchronous motor requires an accurate position of the rotor and usually requires position sensors (such as photoelectric encoders and Hall sensors) to obtain accurate information on the rotor’s position, and then accurately control the motion state of the motor. The position-sensorless method can eliminate the position sensor, estimate the rotor’s position and speed through a specific algorithm, and enhance the stability of the system.

Figure 2. Block diagram of a typical vector control system of a PMSM.

In a typical control block diagram, information on the rotor’s position and speed are obtained by sensors, information on the angle is used for transformation of the coordinates, and information on the speed is used for the speed loop PI controller. The precise operation of the motor is inseparable from accurate information on the rotor’s position and speed.

To better control the operation of the motor, the mathematical model of the permanent magnet synchronous motor can be written as

\[
\begin{bmatrix}
    u_d \\
    u_q
\end{bmatrix} = R \begin{bmatrix}
    i_d \\
    i_q
\end{bmatrix} + \frac{d}{dt} \begin{bmatrix}
    \psi_d \\
    \psi_q
\end{bmatrix} + \omega_e \begin{bmatrix}
    -\psi_q \\
    \psi_d
\end{bmatrix}
\] (1)

where \( u_d, i_d \) and \( \psi_d \) represent the voltage, current, and magnetic flux on the d-axis, respectively; \( i_q, u_q \) and \( \psi_q \) represent the current, voltage, and magnetic flux on the q-axis, respectively; \( \omega_e \) is the electrical angular velocity; and \( R \) is the stator resistance. \( \psi_q \) and \( \psi_d \) can be expressed as

\[
\begin{bmatrix}
    \psi_d \\
    \psi_q
\end{bmatrix} = \begin{bmatrix}
    L_d & 0 \\
    0 & L_q
\end{bmatrix} \begin{bmatrix}
    i_d \\
    i_q
\end{bmatrix} + \begin{bmatrix}
    \psi_f \\
    0
\end{bmatrix}
\] (2)

where \( L_d \) and \( L_q \) are the stator inductance of the \( dq \) axis, and \( \psi_f \) is the permanent magnet flux linkage.

The electromagnetic torque equation of the motor is expressed as shown in Equation (3), and the mechanical equation can be expressed as Equation (4).

\[
T_e = \frac{3}{2} p_n i_q \left( (L_d - L_q) i_d + \psi_f \right)
\] (3)

\[
\begin{bmatrix}
    u_d \\
    u_q
\end{bmatrix} = \begin{bmatrix}
    i_d \\
    i_q
\end{bmatrix} + \frac{d}{dt} \begin{bmatrix}
    \psi_d \\
    \psi_q
\end{bmatrix} + \omega_e \begin{bmatrix}
    -\psi_q \\
    \psi_d
\end{bmatrix}
\] (1)
\[ \int \frac{d\omega_m}{dt} = T_e - T_L - B\omega_m \]  

where \( p_n \) is the number of pole pairs, \( J \) is the rotational inertia, \( B \) is the damping coefficient, \( \omega_m \) is the mechanical angular velocity, and \( T_e \) and \( T_L \) are the electromagnetic torque and the load torque, respectively.

It is worth noting that these equations and parameters are significant for sensorless control because information on the rotor’s position is included in some parameters.

2.2. Analysis of the Sensorless Control Principle

To achieve a high-performance PMSM control system, it is generally necessary to obtain accurate information on the rotor’s position and speed from the position sensor, but when the working conditions of the motor are harsh, the mechanical sensor may cause errors or even damage, and the sensorless control method can avoid the shortcomings of the mechanical sensor. Sensorless control technology detects the electrical signal in the motor’s winding and uses the corresponding algorithm to extract the rotor’s position and speed.

In the model-based sensorless control methods, the back-EMF or flux linkage contains information on the rotor’s position and speed. The following analysis extracts the rotor’s position from the back-EMF.

If we rewrite the voltage equation of the PMSM, the voltage equation of the motor in the stationary coordinate system is

\[
\begin{bmatrix}
    u_a \\
    u_\beta
\end{bmatrix} = \begin{bmatrix}
    R + pL_d & \omega_e(L_d - L_q) \\
    -\omega_e(L_d - L_q) & R + pL_q
\end{bmatrix} \begin{bmatrix}
    i_a \\
    i_\beta
\end{bmatrix} + \begin{bmatrix}
    E_\alpha \\
    E_\beta
\end{bmatrix}
\]

where \( u_a \) and \( i_a \) represent the voltage and current on the \( a \)-axis, respectively; \( u_\beta \) and \( i_\beta \) represent the voltage and current on the \( \beta \)-axis, respectively; \( L_d \) and \( L_q \) are the inductance components of the \( dq \) axis; \( p \) is the differential operator; and \( E_\alpha \) and \( E_\beta \) are the extended back-EMF. \( E_\alpha \) and \( E_\beta \) can be expressed as

\[
\begin{bmatrix}
    E_\alpha \\
    E_\beta
\end{bmatrix} = \begin{bmatrix}
    (L_d - L_q)(\omega_e i_d - pi_q) + \omega_e \psi_f \\
    -\sin \theta_e \\
    \cos \theta_e
\end{bmatrix}
\]

where \( \theta_e \) is the electrical angle.

It can be seen from Equation (6) that the information on the rotor’s position \( \theta_e \) is included in the extended back-EMF. Therefore, only by obtaining the back-EMF accurately can the information on the speed and position of the motor be calculated. In general, to obtain an accurate back-EMF, the sliding mode observer method or the model reference adaptive method can be used. Taking the sliding mode observer as an example, by designing the control law of the sliding mode observer, the error can be zero. At this time, the state variable of the observer reaches the sliding mode’s surface. According to the equivalent control principle of sliding mode control, the level of control at this time can be regarded as an equivalent level of control, that is, the estimated back-EMF is equal to the actual back-EMF.

After obtaining the accurate counter electromotive force, the information on the rotor’s position, angle, and speed can be obtained after some technical processing. Among these technologies, the arctangent method and the phase-locked loop method are the most mature. Among them, the arctangent method usually requires angle compensation, because the use of a low-pass filter will cause a phase delay, which will directly affect the accuracy of the estimated position of the rotor. Compared with the arctangent method, the phase-locked loop method has no phase delay problem. These two methods can obtain the estimated position angle, and by differentiating the position angle \( \theta_e \), the rotor’s speed can be obtained. At this time, the information on the rotor’s position and the rotational speed of the motor are known quantities, and the motor can realize high-performance control.
However, when the motor is running at zero speed or low speed, the model-based method is not available. To obtain accurate information on the rotor’s position at zero speed and low speed, the high-frequency signal injection method is an effective method.

A transformation of Equation (1) into the stationary coordinate system can be expressed as

\[
\begin{bmatrix}
  u_a \\
  u_\beta
\end{bmatrix} = R
\begin{bmatrix}
  i_a \\
  i_\beta
\end{bmatrix} + \frac{d}{dt}
\begin{bmatrix}
  \psi_a \\
  \psi_\beta
\end{bmatrix}
\] (7)

\[
\begin{bmatrix}
  \psi_a \\
  \psi_\beta
\end{bmatrix} = \begin{bmatrix}
  L + \Delta L \cos 2\theta_e & -\Delta L \sin 2\theta_e \\
  -\Delta L \sin 2\theta_e & L - \Delta L \cos 2\theta_e
\end{bmatrix}
\begin{bmatrix}
  i_a \\
  i_\beta
\end{bmatrix} + \psi_f \begin{bmatrix}
  \cos \theta_e \\
  \sin \theta_e
\end{bmatrix}
\] (8)

where \( L = (L_d + L_q)/2 \) is the average inductance and \( \Delta L = (L_q - L_d)/2 \) is half the differential inductance.

We define the inductance matrix \( L_{a\beta} \) in the static coordinate system as

\[
L_{a\beta} = \begin{bmatrix}
  L + \Delta L \cos 2\theta_e & -\Delta L \sin 2\theta_e \\
  -\Delta L \sin 2\theta_e & L - \Delta L \cos 2\theta_e
\end{bmatrix}
\] (9)

It can be seen from Equation (9) that the inductance matrix contains the information on the rotor’s position \( \theta_e \).

According to the different injection reference frames, the current main high-frequency signal injection is divided into the rotation signal and the pulse vibration signal.

The high-frequency signal injection method is very suitable for controlling a low-speed motor because of its simple implementation and does not depend on the internal parameters of the motor. However, in the process of signal processing, the use of LPF will reduce the response bandwidth of the whole system, so that the dynamic performance of the system is insufficient, and the precision of control is not high. In addition, because the signal injection needs to consume part of the DC bus voltage, as the motor’s speed increases, its performance will also decrease.

Through a brief introduction and analysis of sensorless technologies, it was found that they have many problems. Through in-depth studies of sensorless technologies, more and more researchers have made contributions to improving the performance of motor drive systems. The latest sensorless control methods are described in detail in the next section.

3. An Overview of the Recent Developments in Sensorless Methods of PMSM

The current sensorless control technologies of PMSM are mainly divided into two categories, namely, model-based methods and salience-based methods. The former are mainly used in the high-speed range of the motor, while the latter are mainly used in the zero-speed and low-speed ranges. This section presents the latest research results regarding these two methods in detail.

3.1. Model-Based Sensorless Methods

Most of the model-based sensorless control techniques can generally be divided into two steps. The first step is estimating the back-EMF or flux linkage, and the second step is observing the position or velocity. The techniques used for estimating the back electromotive force and flux linkage in the first step are relatively mature and can be divided into open-loop methods and closed-loop methods. In the second step, the law needs to be constructed so that the error is zero. When the estimated error of back-EMF and flux linkage tends to zero, the estimated values of back-EMF and flux linkage are equal to their actual values, and then the position and speed of the motor’s rotor can be calculated. To improve the performance of estimation, researchers have invented techniques such as the sliding mode observer (SMO) [26–33,45–52], the model reference adaptive system (MRAS) [53–66], the extended Kalman filter (EKF) [67–85], and the state observer (SO) [100–111]. These techniques are described in detail below.
3.1.1. Sliding Mode Observer

Sliding mode control is a control strategy of variable-structure control systems. The difference between this control strategy and the conventional control strategy is the discontinuity of control, that is, the discrete switch control of the sliding mode observer will cause chattering. To reduce chattering, different improvement schemes have been proposed.

The traditional SMO uses the sign function as the switch function, and some researchers have made modifications to the switch function. For example, the sign function can be replaced by the sigmoid function [48], or the super-twisting function [27,45], and the hyperbolic tangent function [30] can be used instead of the sign function. Experiments have shown that these functions can effectively reduce chattering as the switching functions.

In addition to their contribution to reducing the chattering problem, researchers have also improved the performance of the SMO in other ways. For example, when the motor has been running for a long time, the motor’s parameters (the stator’s resistance, the stator’s inductance, etc.) may change, which will cause a mismatch between the set value and the actual value, affecting the accuracy of the estimation and even affecting the stability of the system. To solve this kind of problem, in [45], a second-order sliding mode observer for estimating the online stator’s resistance was proposed. Through estimating the online stator’s resistance, the change in resistance due to a change in temperature can be considered, which improves the robustness of the system.

In terms of improving the robustness of the system [27–29,47–50], some have proposed an adaptive algorithm for online adjustment of the sliding mode’s coefficients [27]. The proposed adaptive algorithm can reduce the error in estimating the position and improve the estimated accuracy of sensorless technologies. In [29], a novel compound discrete-time sliding mode observer based on the stator’s flux state was designed, which could simultaneously estimate the disturbance of the flux parameter, the error in the rotor’s position, and the load torque. The influence of the disturbance of the flux linkage parameter on the estimation error was eliminated, and the robustness of the system was greatly improved. In addition, some people have studied the parameter uncertainty of PI control [50] and proposed a model-free speed controller based on a hyperlocal model, which has strong control over the uncertainty of the motor’s parameters. A new method was developed in [47] to linearize the nonlinear model of a PMSM near the operating point using DO to estimate the load torque and back-EMF. The operating point was updated using DO, and a state feedback controller (SFC) was designed, similar to the gain-scheduled method. Experiments showed that this method enhanced the robustness and dynamic performance of the system. Figure 3 shows a control block diagram of the method.

![Block diagram of a sensorless control system based on a disturbance observer](image-url)
3.1.2. Model Reference Adaptive Systems

Model reference adaptive systems (MRAS) are types of adaptive systems. They include three parts, namely, the adjustable model, the reference model, and the adaptive rate. A block diagram of the structure of a MRAS is shown in Figure 4.

![Control block diagram of a model reference adaptive system](image)

Figure 4. Control block diagram of a model reference adaptive system.

In addition to being used in sensorless control, the model reference adaptive system can also be applied to the identification of parameters to enhance the robustness of the system. In [54], a sensorless control strategy using an MRAS observer was proposed. The proposed MRAS observer could automatically adjust the PI according to the magnitude of the current error variable, and the accuracy of the estimated resistance was greatly improved, which enhanced the robustness of the system. Moreover, the author proposed a voltage compensation method based on a disturbance observer that was, in turn, based on the voltage distortion problem of the voltage source inverter, which improved the performance of the system. The disadvantage was that the system includes two observers, the design is relatively complicated, and the required computing power of the hardware is relatively high. Other researchers have used the MRAS observer to estimate the stator’s resistance [55,56]. Regarding the voltage distortion problem of the voltage source inverter [60,62,64,77], ref. [60] proposed a MRAS-based adaptive second-order active flux linkage observer (ASO-AFO) and a MRAS-based VSI nonlinear compensation method. The nonlinearity of the voltage source inverter will lead to harmonic components of the current, which will cause noise, power loss, and additional heating problems. In the study by [60], the root mean square (RMS) value of the cross-product was selected as the objective function, and the voltage was compensated by minimizing the objective function.

In addition to using the MRAS observer alone for estimation of the motor’s parameters, some researchers have developed a new method combining artificial intelligence algorithms and MRAS observers [58]. They used the gray wolf algorithm (GWO) to adapt the speed obtained by the MRAS. The proportional–integral (PI) controller parameters of the law were optimized, which enhanced the robustness of the system and improved the accuracy of estimating the rotor’s position and speed.

3.1.3. Extended Kalman Filter

The extended Kalman filter is an adaptive system and is also a nonlinear random observer. The parameters or disturbance of the permanent magnet synchronous motor can be estimated online, so the observer’s parameters can be adjusted in real time, and the system can be controlled in real time, which improves the performance of the control system.

The EKF can be used for online estimation of the parameters of permanent magnet synchronous motors. The design of the EKF is divided into two steps. The first step is to predict the state vector, and the second step is to correct the predicted state vector. It is worth noting that near zero speed, as the stator’s voltage becomes smaller, the state vector’s
estimation error will increase, and the system will lose its controlling ability, so the EKF is not available at low speeds.

In addition to using the EKF to estimate the information on the rotor’s position and speed, most people have used the EKF for online parameter estimation \[74,75,77,82\]. In [77], two EKF-based online parameter identification schemes were proposed, and a general formulation for online parameter estimation was proposed, which can be applied to any electrical parameter. There was an obvious improvement in identifying the stator’s resistance, and it took the influence of noise on the system into account, improving the robustness of the system. Figure 5 shows a structural block diagram of a double extended Kalman filter. In addition to online estimation of the stator’s resistance and inductance, the estimation of the rotor’s flux linkage has also been studied \[78\]. In addition, some have combined the EKF and adaptive linear active disturbance rejection control \[75\] to form a degree-of-freedom control strategy, which performed well in terms of dynamic response and antidisturbance performance. However, the shortcomings are also obvious, such as the complex structure, the large amount of calculation, and the relatively expensive cost.

![Figure 5. Control block diagram of double extended Kalman filter.](image)

From the content above, we can see that many researchers have used the extended Kalman filter and model reference adaptive systems for online parameter estimation. Table 1 shows a comparison of the online parameter identification methods.

<table>
<thead>
<tr>
<th>Methods</th>
<th>Accuracy</th>
<th>Complexity</th>
<th>Advantage</th>
<th>Disadvantage</th>
</tr>
</thead>
<tbody>
<tr>
<td>MRAS</td>
<td>Medium</td>
<td>Medium</td>
<td>Wide speed range, Easy to implement, the small amount of calculation</td>
<td>Sensitive to noise</td>
</tr>
<tr>
<td>RLS</td>
<td>Medium</td>
<td>Medium</td>
<td>Low accuracy</td>
<td>Complex computation</td>
</tr>
<tr>
<td>EKF Neural network</td>
<td>High</td>
<td>High</td>
<td>Less impact of measurement noise</td>
<td>Complex computation</td>
</tr>
</tbody>
</table>

3.1.4. State Observer

Many scholars have used the state observer (SO) for the sensorless control of the PMSM drive system, mainly to enhance the robustness of the system. The most widely used state observer is the extended state observer (ESO) \[102–111\]. The ESO is an important part of active disturbance rejection control. It has high precision and is independent of the controlled object model.
The ESO is usually used to estimate the total disturbance \([105,108]\), which generally includes the rotor’s flux, load torque, and unmodeled nonlinear disturbances. In \([105]\), the ESO was combined with sliding mode speed control (SMSC), and the control law of SMSC was updated in real time by the estimated total disturbance, which greatly improved the accuracy and robustness to disturbance of the system.

### 3.2. Saliency-Based Sensorless Methods

The model-based methods above are only suitable for motors running at medium and high speeds. When the motor is running at low speeds, the model-based methods are not available due to the low signal-to-noise ratio. Therefore, in the low-speed range, the sensorless control method should use a significance-based method. The saliency-based methods mainly utilize the position-dependent inductance signal in the stator’s winding to realize this, e.g., Equation (9).

The saliency-based methods mainly include two categories. One includes the high-frequency signal (HF) injection methods, and the other includes the fundamental pulsewidth modulation (PWM) excitation (FPE)-based methods. Among them, the high-frequency signal injection method is divided into rotation signal injection and pulse vibration signal injection. These methods are described in detail below.

#### 3.2.1. Rotating Signal Injection

The injected high-frequency voltage signal can be expressed as

\[
U_{\text{in}} = \begin{bmatrix} u_{\alpha h} \\ u_{\beta h} \end{bmatrix} = U_{\text{in}} \begin{bmatrix} \cos(\omega_h t) \\ \sin(\omega_h t) \end{bmatrix}
\]

where \(\omega_h\) is the frequency of the injected high-frequency signal and \(U_{\text{in}}\) is the amplitude of the high-frequency signal.

After injecting a high-frequency voltage signal, the corresponding equation of the current is

\[
\begin{bmatrix} i_{\alpha h} \\ i_{\beta h} \end{bmatrix} = \begin{bmatrix} I_{sp} \sin(\omega_h t) + I_{sn} \sin(-\omega_h t + 2\theta_e) \\ -I_{sp} \cos(\omega_h t) - I_{sn} \cos(-\omega_h t + 2\theta_e) \end{bmatrix}
\]

where \(I_{sp}\) and \(I_{sn}\) are the positive and negative terms of the high-frequency response current, respectively.

Formula (11) can be transformed to the stationary coordinate system as follows:

\[
\begin{bmatrix} i_{dh} \\ i_{qh} \end{bmatrix} = \begin{bmatrix} I_{sp} \sin(2\omega_h t) + I_{sn} \sin(2\theta_e) \\ -I_{sp} \cos(2\omega_h t) - I_{sn} \cos(2\theta_e) \end{bmatrix}
\]

After obtaining Formula (12), only a low-pass filter is needed to extract the information on the rotor’s position.

Figure 6 is a basic block diagram of the rotating high-frequency signal injection method. There are two typical methods based on rotating high-frequency signal injection, namely, the negative-sequence current method \([118–124]\) and the zero-sequence voltage method \([125–127]\). Both methods are described below.

The phase of the negative-phase-sequence’s high-frequency current component contains information on the rotor’s position, but to obtain accurate information on the rotor’s position, signals such as low-order harmonic currents and the positive-phase-sequence’s high-frequency currents must be filtered out. The band-pass filter can remove harmonic currents, and the synchronous shafting high-pass filter can remove the positive-phase-sequence’s high-frequency current. A new method of extracting the rotor’s position was proposed in \([118]\), which extracts the information on the rotor’s position from the relationship between the injected voltage and the induced current, and can also be calculated by using the induced current envelope using an all-pass filter. In this method, there is no time delay and the dynamic performance is improved.
3.2.2. Pulsating Signal Injection

The pulsating signal injection method is another effective saliency-based sensorless control scheme. According to the different injected signals, these methods can be divided into two categories: pulsating sinusoidal injection [128–135] and pulsating square wave injection [143–156].

Unlike the rotating HF voltage injection method, the pulsating HF voltage injection method can only inject HF signals on the d-axis of the estimated synchronous rotating coordinate system. To estimate the rotor’s position accurately, an estimated synchronous rotation coordinate system of the rotor is established.

Similar to the rotation signal, the injected pulsating high-frequency signal can be expressed as
\[
U_{in} = \begin{bmatrix} u_{ih} \\ u_{qh} \end{bmatrix} = U_{in} \begin{bmatrix} \sin(\omega_c t) \\ 0 \end{bmatrix}
\] (13)

where \( U_{in} \) is the amplitude of the HF signal, and the symbol “\( \cdot \)” indicates the components of the estimated rotor’s frame of reference.

The response current equation is
\[
\begin{bmatrix} i_{sh} \\ i_{qh} \end{bmatrix} = \begin{bmatrix} \cos(\theta_i) \cos(\Delta \theta_e) \\ \sin(\theta_i) \cos(\Delta \theta_e) \end{bmatrix} \int U_{in} dt + \begin{bmatrix} \sin(\theta_i) \sin(\Delta \theta_e) \\ -\cos(\theta_i) \sin(\Delta \theta_e) \end{bmatrix} \int U_{in} dt
\] (14)

where \( \Delta \theta_e = \theta_i - \hat{\theta}_e \) is the position’s error. When the position’s error tends to zero, Equation (14) can be written as
\[
\begin{bmatrix} i_{sh} \\ i_{qh} \end{bmatrix} = \frac{1}{L_d} \begin{bmatrix} \cos(\theta_i) \\ \sin(\theta_i) \end{bmatrix} \cdot \int U_{in} dt.
\] (15)

After obtaining Formula (15), the information on the position can be obtained after demodulation of the signal.
Figure 7 is a block diagram of heartbeat signal injection.

Figure 7. Block diagram of pulsating signal injection.

To improve the accuracy, some researchers injected two kinds of HF pulsation signals with different frequencies [135]. In [131], the author proposed a new pulsating sinusoidal signal injection method, using three HF pulsation signals with different frequencies and amplitudes. The voltage is injected into the ABC frame. This method demodulates the three frequency components in the response current signal and then combines them together to directly calculate the rotor’s position, which reduces the influence of the system’s delay and improves the accuracy of the estimation.

Compared with the pulsating sinusoidal signal, the pulsating square wave signal has a high injection frequency, which is beneficial for the separation and extraction of high-frequency signals. The square-wave injection voltage at different frequencies was evaluated in [93], and the results showed that designing an appropriate frequency of the injection voltage could significantly improve the performance of the system. Some researchers also proposed an improved HF square wave voltage injection method, which is more robust to voltage errors [156].

In practical applications, researchers have also considered the inverter’s dead zone [145], cross-saturation [131,132,147,152], the second harmonic [134,138], and variations in the machine’s parameters [135–137,140,146] to improve the accuracy of estimation.

3.2.3. FPE-Based Methods

In addition to injecting high-frequency signals, the abovementioned high-frequency signal injection methods also require an observer to process the signals to obtain the accurate position of the rotor, which increases the complexity and cost of the system. To solve this problem, a control method based on FPE has been proposed.

FPE-based methods can be mainly divided into three categories, namely indirect flux detection by in-line reactance measurement (INFORM) [158–160], the zero-sequence current derivative (ZSCD) measurement method [161–163], and the zero-voltage vector injection method (ZVVI) [164–167].

INFORM works by applying a voltage vector in different directions and then measuring the resulting of response the current. The authors of [159] improved INFORM to reduce the current’s harmonics and switching losses. The working principle of ZVVI is as follows. The test signal is injected into the system, the zero-sequence current derivative of the inductor can be obtained, and the information on the rotor’s position and speed
can be obtained. The ZSCD method is simple and has excellent performance, but it needs to be connected to the neutral point, which limits the development of the ZSCD. ZVVI combines the derived calculations of the current and zero-voltage vector injection, which is effective for sensorless control of a PMSM during zero-speed and low-speed operation. These control methods are worthy of further study.

To compare the differences of several methods more intuitively, Table 2 gives the advantages and disadvantages of various methods.

### Table 2. Comparison of Saliency-Based Methods.

<table>
<thead>
<tr>
<th>Method</th>
<th>Advantages</th>
<th>Disadvantages</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rotating signal injection</td>
<td>Does not require information on the initial location, good robustness</td>
<td>Only applicable to salient pole motors</td>
</tr>
<tr>
<td>Pulsating sinusoidal injection</td>
<td>Low injection frequency. The influence of the inverter’s nonlinearity is small. High injection frequency.</td>
<td>LPF affects the system’s bandwidth and has insufficient dynamic performance.</td>
</tr>
<tr>
<td>Pulsating square wave injection</td>
<td>High-frequency signal extraction is simple, and the influence of the inverter’s nonlinearity is small. No external signal injection required, no high-frequency noise.</td>
<td>LPF affects the system’s bandwidth and has insufficient dynamic performance. Information on the initial location.</td>
</tr>
<tr>
<td>FPE-based methods</td>
<td></td>
<td>High requirements of the current signal sampling circuit.</td>
</tr>
</tbody>
</table>

In this section, the high-speed sensorless control methods and the low-speed sensorless control methods are summarized. They all have their own advantages and disadvantages, and some shortcomings still need to be overcome. Table 3 [123,168–189] presents the characteristics of various methods.

### Table 3. Comparison of various sensorless methods.

<table>
<thead>
<tr>
<th>Categories</th>
<th>Speed Range</th>
<th>Advantages</th>
<th>Disadvantages</th>
</tr>
</thead>
<tbody>
<tr>
<td>SMO</td>
<td>Medium and high speed</td>
<td>Good robustness</td>
<td>Chattering exists. Heavy calculation demands Depends on the motor’s parameters</td>
</tr>
<tr>
<td>MRAS</td>
<td>Medium and high speed</td>
<td>Simple structure, easy to implement quick response</td>
<td></td>
</tr>
<tr>
<td>EKF</td>
<td>Medium and high speed</td>
<td>Strong anti-interference resistance to noise</td>
<td>Heavy calculation</td>
</tr>
<tr>
<td>SO</td>
<td>Medium and high speed</td>
<td>Good robustness</td>
<td>Complex structure</td>
</tr>
<tr>
<td>Rotating signal injection</td>
<td>Startup and low speed</td>
<td>Easy to implement, good robustness</td>
<td>High-frequency noise, torque ripple</td>
</tr>
<tr>
<td>Pulsating signal injection</td>
<td>Startup and low speed</td>
<td>Suitable for salient pole and hidden pole motors</td>
<td>LPF affects the system’s bandwidth</td>
</tr>
<tr>
<td>FPE-based methods</td>
<td>Startup and low-speed</td>
<td>No need to inject a signal</td>
<td>High requirements for the hardware detection circuit</td>
</tr>
</tbody>
</table>

### 4. Future Directions

According to the summary and review of the existing methods, sensorless control methods have been developed rapidly. However, with the increasing application of sensorless control systems and the increasingly complex working environment, sensorless control must adapt to more scenarios. Some development trends mainly focus on the following aspects.

#### 4.1. High Dynamic Performance throughout the Full Speed Range

The dynamic performance of a PMSM directly affects the quality of the motor. A good motor drive system must have good dynamic performance. In the future, dy-
namic performance will attract more and more attention to adapt to high-performance application scenarios.

4.2. Smooth Switching between Low Speed and High Speed

At present, there is no mature and reliable solution that can efficiently and stably realize the position-sensorless control of permanent magnet synchronous motors across the full speed range. Traditional position-sensorless control techniques are mainly divided into two categories, namely high-speed model-based methods and low-speed saliency-based methods, which lead to changes in the control methods when transitioning from low speeds to medium and high speeds. A combination of these two methods constitutes a hybrid control strategy [190–192], but the difficulty of the hybrid control strategy is how to switch between the two methods without large fluctuations in speed. Therefore, how to smoothly switch from low speeds to high speeds is a direction worth studying.

4.3. Sensorless Control of Ultra-High-Speed PMSMs

In some specific occasions, permanent magnet synchronous motors may require ultra-high speed, such as centrifugal compressors, turbo generators, etc. When the motor is running at ultra-high speed (e.g., 15,000 rpm), the mechanical position sensor is not reliable; to solve this problem, sensorless control of the motor is required [193–195]. Moreover, the stability of the PMSM is an important challenge when the motor operates at ultra-high speeds. Therefore, it is necessary to study the stable control methods of permanent magnet synchronous motors at ultra-high speed.

4.4. High Robustness under Heavy and Changing Loads

As we all know, drastic changes in the load will cause fluctuations in speed, so how to reduce such fluctuations is the focus of research. Strong robustness to load disturbance is an important indicator for evaluating the performance of sensorless control, and how to maintain accurate information on the rotor’s position when the load changes drastically is an important research direction.

4.5. High Robustness to Changes in the Motor’s Parameters

As the operation or working conditions of the motor change, the mechanical parameters of the motor (such as the stator’s resistance, inductance, and flux linkage, etc.) will change, which will lead to a decrease in the performance of control and an increase in the error of estimation. Therefore, to improve the performance of sensorless control, high robustness to variation in the motor’s parameters is essential.

5. Conclusions

This article summarized the research status of sensorless control technology used for permanent magnet synchronous motors, and introduces the basic principles of sensorless control. In the high-speed range, the methods of the sliding mode observer, model reference adaptive system, and the Kalman filter have been introduced and compared. In the low-speed range, the methods of rotating high frequency signal injection and pulsating high frequency signal injection have been introduced. However, the methods above still have some limitations, such as sensorless control methods for the full speed domain, etc. To solve these problems, some advanced control theories have been proposed, such as particle swarm optimization algorithms and neural networks. With the development of science and technology, ultra-high-speed sensorless control and high robustness to disturbance will become the focus of research.

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